## $\label{eq:Graph Consistency Rule Mining with LLMs: an Exploratory Study} Rules Generated by LLMs on the property graphs$

Cybersecurity	Zero-shot prompt	Supp-Cover (%)-Conf (%)
LLaMA-3	(1) Each person node should have a unique id property	2020 - 100 - 100
	(2) Each person node should have a name and dob property	1678 - 82.69 - 83
	(3) Each match node should have a unique id property	284 - 100 - 100
	(4) Each match node should have a date and stage property	284 - 100 - 100
	(5) Each squad node should have a unique id property	136 - 100 - 100
	(6) Each squad node should have an id property	136 - 100 - 100
	(7) Each team node should have a unique id property	36 - 100 - 100
	(8) Each team node should have a name property	36 - 100 - 100
	(9) A person node can only be connected to a match node through a 'PLAYED_IN' or 'SCORED_GOAL' relationship	1576 - 100 - 100
	(10) A squad node can only be connected to a tournament node through a 'FOR' relationship	136 - 100 - 100
	(11) A team node can only be connected to a squad node through a 'NAMED' relationship	36 - 100 - 100
	(11) A team node can only be connected to a tournament node through a 'PARTICIPATED_IN' relationship	36 - 100 - 100
	(12) A match node can only be connected to a tournament node through an 'IN_TOURNAMENT' relationship	284 - 100 - 100
Mixtral	(1) Each tournament should have a unique identifier	8 - 100 - 100
	(2) Each match should have a unique identifier within its respective tournament	8 - 100 - 100
	(3) Each squad should have a unique identifier within its respective tournament	136 - 100 - 100
	(4) For any given tournament, every team should be associated with a squad	136 - 100 - 100
	(5) A team should be involved in at least one match for each tournament they participate in	136 - 100 - 100
	(6) A match should have a score for both teams (no NULL values) if their match has a score defined	284 - 100 - 100
	(7) Each player should have a unique identifier	2020 - 100 - 100
	(8) A player should be associated with a squad, and that squad should belong to the tournament for which the player has played a match	7684 - 81.1 - 81.1
	(9) A player should score a goal in a match only if they played in that match	903 - 99.2 - 24.5 5
Twitter	Few shot learning	
LLaMA-3	(1) Ensures that the id_str in Tweet nodes is unique. Each Tweet should have a unique id_str	2020 - 100 - 100
	(2) Validates that the date values in Match nodes fall within a valid range (e.g., from 1900 to 2030)	284 - 100 - 100
	(3) Ensures that the stage values in Match nodes are consistent and contain no invalid values or errors	284 - 100 - 100
	(4) Ensures that Team nodes have valid and non-null name attributes	36 - 100 - 100
	(5) Ensures that each Match node is associated with exactly two Team nodes	284 - 100 - 100
	(6) Ensures that squad names are unique within a tournament, meaning no duplicate squad names for a given tournament	136 - 100 - 100
	(7) Ensures each Person node is associated with at most one Team node	1928 - 95.3 - 100
	(8) Ensures that only Person nodes associated with a Team participating in a Match can score a goal	756 - 42.5 - 100
Mixtral	(1) Each Match node must have a unique ID	2020 - 100 - 100
	(2) Each Match node must have a unique date and phase in a specific tournament	39 - 100 - 100
	(3) Each Team node must have a unique name in a specific tournament	36 - 100 - 100
	(4) Each Tournament node must have a unique name	8 - 100 - 100
	(5) Each Squad node must have a unique ID	136 - 100 - 100
	(s) Eastri Squar note inter a unique ID	1268 - 100 - 66
	(0) Ensure that each Match-Team relationship has exactly one squau representing the relation (7) Ensure that each Match-Team relationship within a specific tournament is valid	568 - 100 - 100
	(8) Ensure no duplicate SCORED_GOAL relationships exist with the same scoring minute	907 - 42.5 - 100
	(o) Ensure no auphicate SCOKED_GOAL relationships exist with the same scoring minute	907 - 42.5 - 100

Table 1: Rules Generated by LLMs on the WWC-2019 graph with Sliding Window Attention

Cybersecurity	Zero-shot prompt	Supp-Cover (%)-Conf (%)
LLaMA-3	(1) Each node should have a unique ID within its respective category (e.g., player, team, coach)	2468 - 100 - 100
	(2) Each node should have a consistent label corresponding to its category (e.g., player, team, coach)	2468 - 100 - 100
	(3) A coach can coach only one team at a time	77 - 100 - 75
	(4) A player can only belong to one squad at a time	1268 - 100 - 66
	(5) The IN_SQUAD relationship should only exist between a player and a team	2880 - 100 - 100
	(6) The COACH_FOR relationship should only exist between a coach and a team	140 - 100 - 100
	(7) The REPRESENTS relationship should only exist between a player/coach and a team	1929 - 100 - 100
Mixtral	(1) Each player should be uniquely represented in the graph. There should not be two nodes with the same id under	
	the REPRESENTS relationship	2020 - 100 - 100
	(2) A player cannot be in two different squads at the same time. There should not be two IN_SQUAD relationships for the same	
	player and different squads	1268 - 100 - 66
	(3) A player cannot be in the same squad more than once. There should not be multiple IN_SQUAD relationships between the same	
	player and the same squad	1268 - 100 - 66
	(4) If a player is substituted in a game, the minuteOn value in the PLAYED_IN relationship should be less than the minute value in the	
	SCORED_GOAL relationship (if it exists)	0 - 0 - 0
	(5) A player cannot score two goals in the same minute of the same game. There should not be two SCORED_GOAL relationships for the	
	same player, same game, and same minute	907 - 42.5 - 100
	(6) A coach cannot coach two different teams at the same time. There should not be two COACH_FOR relationships for the same coach	
	and different teams	77 - 100 - 75
Twitter	Few shot learning	
LLaMA-3	(1) Each REPRESENTS relationship should have a unique id	2468 - 100 - 100
	(2) A player can only be part of one squad at a time	1268 - 100 - 66
	(3) A player can only play in one match at a time	1565 - 100 - 100
	(4) A coach can only coach one team at a time	77 - 100 - 75
	(5) A player can only score one goal per match	636 - 42.5 - 100
	(6) A player can only be subbed on or off once per match	0 - 0 0
Mixtral	(1) Each relationship should have unique nodes at its ends. This means that a relationship cannot connect the same two nodes more than once,	
	regardless of the relationship type	14528 - 100 - 100
	(2) The relationship types should match the node types they are connecting. For example, a 'PLAYED_IN' relationship	
	should only connect a Person node	
	to a Match node	7684 - 100 - 100
	(3) Each Player node should have only one 'REPRESENTS' relationship to a Person node. This ensures that each player is represented	
	by only one person	1928 - 95.3 - 100
	(4) For 'PLAYED_IN' relationships with a 'minuteOn' property, the sum of 'minuteOn' for a player	
	in a match should not exceed	
	the total match minutes	0 - 0 - 0
	(5) For 'PLAYED_IN' relationships, if a 'type' property is present, it should be consistent for all relationships of a player in a match	7684 - 20.3 - 100

Table 2: Rules Generated by LLMs on the WWC-2019 graph with RAG

Cybersecurity	Zero-shot prompt	Supp-Cover (%)-Conf (%)
LLaMA-3	(1) Each node should have a unique neo4jImportId (2) All nodes with a domain property should have a valid domain name (3) The owned property should only be True or False (4) The enabled property should only be True or False (5) User nodes should have a valid displayname and username (7) Computer nodes should have a valid operatingsystem and domain (7) Group nodes should have a valid displayname and domain (8) OU nodes should have a valid displayname and domain (9) GPO nodes should have a valid displayname and domain (10) Relationships should only connect nodes of compatible types (e.g., User-Computer, Group-User, etc.)	953 - 1.0 - 1.0 953 - 100 - 100 603 - 63 - 100 600 - 63 - 100 300 - 100 - 100 301 - 100 - 100 308 - 100 - 100 21 - 100 - 100 22 - 100 - 100 0 - 0 - 0
Mixtral	(1) If a node has the label Computer, it must have the properties operatingsystem, name, objectid, and enabled (2) If a node has the label User, it must have the properties displayname, pwdlastset, domain, lastlogon, name, objectid, and enabled (3) If a relationship has the type HAS_SESSION, it must involve a Computer node and a User node (4) If a relationship has the type MEMBER_OF, it must connect a User node to a Group or Domain node (5) If a relationship has the type ADMIN_TO, it must connect a User or Group node to a Domain or Computer node (6) For each Domain node, there must be at most one Domain node connected via the PARENT_OF relationship (7) For each Domain node, there must be at least one Domain node connected via the SUB_DOMAINS relationship (8) For each Group node, there must be at least one User node connected via the MEMBER_OF relationship (9) For each Domain node, there must be at least one OU node connected via the CONTAINS relationship (10) For each GPO node, there must be exactly one OU node connected via the AFFECTS relationship	300 - 97.2 - 99.67 299 - 99.67 - 99.76 264 - 100 - 100 1043 - 76.7 - 76.6 Support: 1347 - 100 - 100 0 - 0 - 0 0 - 0 - 0 262 - 100 - 100 1 - 0 0
Twitter	Few shot learning	
LLaMA-3	(1) Each node should have a unique neo4jImportId property (2) Each node should have a unique objectid property (3) Only allowed labels: User, Group, Domain, OU, GPO, and Computer (4) The owned property should be a boolean value (5) The domain property should be a string value matching domain format (6) The operatingsystem property should match valid OS names (7) The name property should match username or computer name format (8) The enabled property should be a boolean value (9) Only allowed relationship types: HAS_SESSION, MEMBER_OF, CONTAINS, GP_LINK, etc	953 - 100 - 100 948 - 99.5 - 99.8 953 - 100 - 100 603 - 63 - 100 - 100 300 - 100 - 100 953 - 100 - 100 953 - 100 - 100 600 - 63 - 100 3762 - 80 - 81
Mixtral	(1) Each node in the database should have a unique neo4jImportId value (2) Each node in the database should have a unique objectid value (3) Only the allowed node labels (User, Group, Domain, OU, GPO, and Computer) should be present (4) A Computer node should not have a MEMBER_OF relationship with a Domain node (5) A GPO node should be linked to either a Domain node or an OU node through a GP_LINK relationship	953 - 100 - 100 948 - 99.5 - 99.8 953 - 100 - 100 301 - 100- 100 21 - 60 - 60

Table 3: Rules Generated by LLMs on the Cybersecurity graph with Sliding window attention

Cybersecurity	Zero-shot prompt	Supp-Cov (%)-Conf (%)
LLaMA-3	(1) Each node should have at most one unique neo4jImportId	953 - 100 - 100
	(2) If node A has a MEMBER_OF relationship with node B, then node B should also have a MEMBER_OF relationship with node A (3) If node A has an ADMIN_TO relationship with node B, and B has an ADMIN_TO relationship with node C, then node A should	2 - 2/1361 - 2/1361
	also have an ADMIN_TO relationship with node C	0 - 0 - 0
	(4) Each node should have at most one HAS_SESSION relationship with another node	114 - 43 - 100
	(5) Each node should have at most one CAN_RDP relationship with another node	12 - 12/60 - 12/60
	(6) Each node should have at most one EXECUTE_DCOM relationship with another node	19 - 19/60 - 19/60
	(7) Each node should have at most one ALLOWED_TO_DELEGATE relationship with another node	14 - 30 - 0.67
Mixtral	(1) Each node should have only one neo4jImportId property	953 - 100 - 100
	(2) A MEMBER_OF node should not have more than one outgoing relationship. This ensures that a node is not a member of multiple entities (3) A node connected to the GENERIC_ALL node should not have any other relationships, ensuring that it only inherits properties from the	340 - 100 - 59
	GENERIC_ALL node	1 - 50 - 50
	(4) The enabled property should only be True or False	600 - 63 - 100
	(5) A node with the CONTAINS label should not have any incoming relationships, ensuring it does not inherit properties from other nodes	0 - 0 - 0
	(6) A node with the MEMBER_OF label should not have any incoming relationships, ensuring it does not inherit properties from other nodes	0 - 0 - 0
Twitter	Few shot learning	
LLaMA-3	(1) Ensure that each node has a unique id property, which helps in distinguishing nodes in the graph	953 - 100 - 100
	(2) Ensure that each node has a label from the allowed set: User, Group, Domain, OU, GPO, or Computer, ensuring proper classification of nodes	953 - 100 - 100
	(3) Ensure that MEMBER_OF relationships point from a User or Group node to a Group node	1043 - 77 - 98
	(4) Ensure that ADMIN_TO relationships point from a Group node to a Computer node, indicating correct access delegation	1347 - 100 - 100
	(5) Ensure that HAS_SESSION relationships point from a User node to a Computer node, indicating user sessions on computers	264 - 100 - 100
	(6) Ensure that CAN_RDP relationships point from a User node to a Computer node, indicating remote desktop permissions (7) Ensure that ALLOWED_TO_DELEGATE relationships point from a User node to a Computer node, indicating delegation rights for	30 - 50 - 100
	remote desktop access	30 - 100 - 100
Mixtral	(1) Ensure that each relationship has a unique relationship Type property. This helps distinguish and identify each relationship	4698 - 100 - 100
MIAHAI	(2) Ensure that the isacl property for GENERIC ALL nodes is consistently set to True, indicating they are ACL entries	901 - 100 - 100
	(2) Ensure that the label property for all nodes is one of User, Group, Domain, OU, GPO, Computer, or GENERIC ALL	953 - 100 - 100
	(4) Ensure that no nodes are isolated and all nodes are connected within the graph structure	952 - 99.8 - 100
	(s) The highvalue property should be consistent across nodes of the same type	1 - 100 - 100

Table 4: Rules Generated by LLMs on the Cybersecurity graph with RAG

Twitter	Zero-shot prompt	Support-Coverage (%)-Confidence (%)
LLaMA-3	(1) Each tweet node should have a unique <i>id</i> property (2) All URL properties in Link nodes should be valid URLs (starting with 'http://' or 'https://') (3) All User nodes should have a non-empty name property (screen_name) (4) All Hashtag nodes should have a non-empty name property (5) Each Tweet node should have at most one Source node connected to it through the USING relationship (6) Ensure that the relationships between nodes are valid and consistent (e.g., Tweet node connected to User node through POSTS) (7) Each User node should have a unique id property (8) Ensure that FOLLOWS relationships between User nodes are valid and consistent (i.e., no cycles, only User to User)	2407 - 100 - 100 1561 - 100 - 100 38986 - 100 - 100 344 - 100 - 100 2146 - 89.15 - 100 2146 - 89 - 100 0 - 0 - 0 44630 - 100 - 100
Mixtral	(1) A User node must have a unique screen_name property (2) A Tweet node should not have more than one created_at property (3) A User node should not be connected to a Tweet node by both MENTIONS and MENTIONS, Me relationships (4) A User node linked with the FOLLOWS relationship should have a name property (5) A Hashtag node should not be connected to a Tweet node by both TAGS and TAGS, Me relationships (6) A A Tweet node should have a text property with a maximum length of 280 characters. (7) A Tweet node should have a unique id property (8) A Link node should have zero or more RETWEETS relationships (10) A Tweet node should have zero or one created_by relationship	38986 - 100 - 100 2407 - 100 - 100 3459 - 100 - 100 34597 - 100 - 100 1439 - 100 - 100 2146 - 100 - 100 2407 - 100 - 100 1561 - 100 - 100 286 - 11.89 - 11.89 2407 - 100 - 100
Twitter	Few shot learning	
LLaMA-3	(1) Each user node should have a unique screen_name property to ensure that no duplicate users exist (2) The followers property should be a non-negative integer (3) The following property should be a non-negative integer (4) The profile_image_url property should be a valid URL (5) The location property should follow a consistent format (e.g., city, state, country) (6) The url property should be a valid URL (7) The statuses property should be a non-negative integer	38986 - 100 - 100 38690 - 100 - 100 38690 - 100 - 100 38960 - 100 - 100 32 - 0.082 - 0.082 16997 - 100 - 100 4052 - 100 - 100
Mixtral	(1) Ensure that every tweet has a unique id_str property (2) Ensure that no two users have the same name and screen_name combination (3) Ensure that Hashtag nodes are only connected to Tweet nodes (4) Ensure that relationships going out from User nodes have the label "FOLLOWS" and connect to a User node (5) Ensure that a user does not have multiple nodes with the same location as their home_location (6) Ensure that User, Me nodes only have Tweet and Follows relationships (7) Ensure that a tweet does not have multiple nodes with different labels and urls	2146 - 100 - 100 38986 - 100 - 100 1493 - 100 - 100 44630 - 100 - 100 7808 - 79.33 - 79.33 2146 - 4.59 - 4.59 129 - 67.64 - 79.24

Table 5: Rules Generated by LLMs on the Twitter graph with Sliding window attention

Twitter	Zero-shot prompt	Support-Coverage (%)-Confidence (%)
LLaMA-3	(1) A Tweet node can only be connected to one User node with the POSTS relationship type (2) A Tweet node can only be connected to the same User node (Me) with the MENTIONS relationship type once (3) A Tweet node can only be connected to one other Tweet node with the REPLY_TO relationship type (4) A Tweet node can only be connected to one other Tweet node with the RETWEETS relationship type (5) A User node can only be connected to the same User node (Me) with the FOLLOWS relationship type once (6) A Tweet node can only be connected to one Link node with the CONTAINS relationship type (7)A Tweet node can only be connected to one Hashtag node with the TAGS relationship type (8) A Tweet node can only be connected to one Source node with the USING relationship type	2147 - 89 - 100 899 - 37 - 30 504 - 100 - 100 268 - 100 - 100 0 - 0 - 0 1499 - 89 - 100 389 - 47 - 100 2146 - 100 - 100
Mixtral	(1) In the graph, a Tweet can only have a REPLY_TO or RETWEETS relationship with another Tweet. It cannot have both or neither (2) n the graph, a User can only have a FOLLOWS relationship with another User. It cannot follow a Tweet directly (3) In the graph, a User or User, Me can only have a POSTS relationship with a Tweet. It cannot post to another User directly (4) In the graph, a Tweet can only have a TAGS relationship with a Hashtag. It cannot be tagged with a User or any other node (5) In the graph, a Tweet can only have a CONTAINS relationship with a Link. It cannot contain a User or any other node (6) In the graph, a Tweet can only have a USING relationship with a Source. It cannot use a User or any other node (7) In the graph, a User, Me can only have a FOLLOWS relationship with a User. It cannot follow a Tweet directly	722 - 32 - 32 44630 - 100 - 100 2146 - 100 - 100 389 - 47 - 100 1499 - 92 - 100 2146 - 100 - 100 0 - 0 - 0
Twitter	Few shot learning	
LLaMA-3	(1) Each user node should have a unique screen_name property to ensure that no duplicate users exist (2) Each Tweet node should have a valid created_at timestamp in the format yyyy-MM-dd'T'HH:mm:ss'Z' to ensure consistent date formatting (3) Every Tweet node should have a valid text property to ensure that tweet content is not empty (4) Each Hashtag node should have a unique name property to prevent duplicate hashtags (5) Each Link node should have a valid url property to ensure that links are property formatted (6) Every User node should have a valid id property to ensure that user IDs are consistent (7) Each Tweet node should have at most one RETWEETS relationship to another Tweet node to prevent multiple retweet relationships (8) Each User node should have at most one FOLLOWS relationship to another User node to prevent multiple follow relationships (9) Each Tweet node should have at most one MENTIONS relationship to another User node to prevent multiple mention relationships	38986 - 100 - 100 2407 - 100 - 100 2416 - 89.16 - 100 344 - 100 - 100 1561 - 100 - 100 0 - 0 - 0 286 - 100 - 100 34506 - 88.51 - 100 718 - 66.40 - 100
Mixtral	(1) Each User node should have a unique screen_name property to ensure no duplicate user accounts exist (2) Nodes labeled Tweet should have a created_at property to ensure the timeline of tweets is correct (3) Nodes labeled Hashtag should have a unique name property to ensure no duplicate hashtags exist (4) The MENTIONS relationship should only exist between User and Tweet nodes to maintain the integrity of the graph (5) The REPLY_TO relationship should only exist between Tweet nodes to maintain the integrity of the graph (6) The RETWEETS relationship should only exist between Tweet nodes to maintain the integrity of the graph (7) The USING relationship should only exist between Tweet nodes to maintain the integrity of the graph (8) The FOLLOWS relationship should only exist between User nodes to maintain the integrity of the graph	38986 2407 - 100 - 100 344 - 100 - 100 3459 - 100 - 100 504 - 100 - 100 268 - 100 - 100 2146 - 100 - 100 44630 - 100 - 100

Table 6: Rules Generated by LLMs on the Twitter graph with RAG