DATA 621 HW 1

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2024-02-22

Introduction

In this assignment, we are given a baseball training and evaluation dataset, which contains approximately 2200 records. The data spans from 1871 to 2006, with each row representing a baseball team's performance from that year. The statistics were all adjusted to reflect a 162 game season. Our objective is to construct a multiple linear regression model of the training data to predict the number of wins for a team.

1. Data Exploration

Glimpse of the data

There are 2,276 rows and 17 columns in the dataset. The response variable is TARGET_WINS and the remaining 15 variables, with the exception of the INDEX column, are predictor variables.

```
## Rows: 2,276
## Columns: 17
## $ INDEX
                     <dbl> 1, 2, 3, 4, 5, 6, 7, 8, 11, 12, 13, 15, 16, 17, 18, 1~
## $ TARGET_WINS
                     <dbl> 39, 70, 86, 70, 82, 75, 80, 85, 86, 76, 78, 68, 72, 7~
## $ TEAM_BATTING_H
                     <dbl> 1445, 1339, 1377, 1387, 1297, 1279, 1244, 1273, 1391,~
                    <dbl> 194, 219, 232, 209, 186, 200, 179, 171, 197, 213, 179~
## $ TEAM_BATTING_2B
## $ TEAM_BATTING_3B
                    <dbl> 39, 22, 35, 38, 27, 36, 54, 37, 40, 18, 27, 31, 41, 2~
## $ TEAM_BATTING_HR
                    <dbl> 13, 190, 137, 96, 102, 92, 122, 115, 114, 96, 82, 95,~
## $ TEAM_BATTING_BB
                    <dbl> 143, 685, 602, 451, 472, 443, 525, 456, 447, 441, 374~
                    <dbl> 842, 1075, 917, 922, 920, 973, 1062, 1027, 922, 827, ~
## $ TEAM_BATTING_SO
                    <dbl> NA, 37, 46, 43, 49, 107, 80, 40, 69, 72, 60, 119, 221~
## $ TEAM_BASERUN_SB
## $ TEAM BASERUN CS
                    <dbl> NA, 28, 27, 30, 39, 59, 54, 36, 27, 34, 39, 79, 109, ~
## $ TEAM PITCHING H <dbl> 9364, 1347, 1377, 1396, 1297, 1279, 1244, 1281, 1391,~
## $ TEAM_PITCHING_HR <dbl> 84, 191, 137, 97, 102, 92, 122, 116, 114, 96, 86, 95,~
## $ TEAM PITCHING BB <dbl> 927, 689, 602, 454, 472, 443, 525, 459, 447, 441, 391~
## $ TEAM PITCHING SO <dbl> 5456, 1082, 917, 928, 920, 973, 1062, 1033, 922, 827,~
## $ TEAM_FIELDING_E <dbl> 1011, 193, 175, 164, 138, 123, 136, 112, 127, 131, 11~
## $ TEAM_FIELDING_DP <dbl> NA, 155, 153, 156, 168, 149, 186, 136, 169, 159, 141,~
```

Summary table

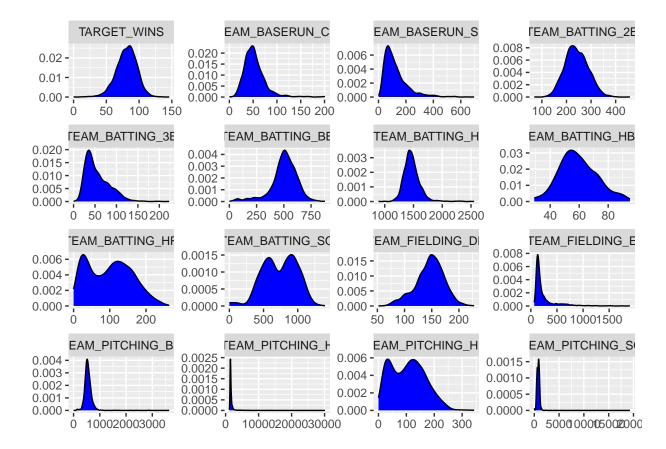
We can see from the summary, that the mean of TARGET_WINS is 80.79, which is about half the games in a baseball season. For the most part, most variables have 2276 values but there are some, TEAM_BATTING_HBP in particular, have less, suggesting that there is missing data.

```
sd median trimmed
                             n
                                   mean
                                                                    mad
                                                                         min
                                                                                max
## TARGET_WINS
                        1 2276
                                  80.79
                                           15.75
                                                   82.0
                                                          81.31
                                                                  14.83
                                                                            0
                                                                                146
## TEAM_BATTING_H
                        2 2276 1469.27
                                         144.59 1454.0 1459.04 114.16
                                                                               2554
```

```
## TEAM BATTING 2B
                        3 2276
                                241.25
                                         46.80
                                                 238.0
                                                        240.40 47.44
                                                                         69
                                                                              458
                        4 2276
                                 55.25
                                         27.94
                                                  47.0
                                                         52.18
                                                                23.72
                                                                          0
                                                                              223
## TEAM_BATTING_3B
                                                102.0
## TEAM BATTING HR
                        5 2276
                                 99.61
                                         60.55
                                                         97.39
                                                                78.58
                                                                              264
## TEAM_BATTING_BB
                        6 2276
                                501.56
                                        122.67
                                                512.0
                                                        512.18
                                                                94.89
                                                                              878
                                                                          0
## TEAM BATTING SO
                        7 2174
                                735.61
                                        248.53
                                                750.0
                                                        742.31 284.66
                                                                          0
                                                                             1399
## TEAM BASERUN SB
                        8 2145
                                124.76
                                         87.79
                                                101.0
                                                        110.81
                                                                60.79
                                                                          0
                                                                              697
## TEAM BASERUN CS
                        9 1504
                                 52.80
                                         22.96
                                                  49.0
                                                         50.36
                                                                17.79
                                                                          0
                                                                              201
## TEAM BATTING HBP
                       10
                          191
                                 59.36
                                         12.97
                                                  58.0
                                                         58.86
                                                                11.86
                                                                         29
                                                                               95
## TEAM PITCHING H
                       11 2276 1779.21 1406.84 1518.0 1555.90 174.95 1137 30132
## TEAM_PITCHING_HR
                       12 2276
                               105.70
                                         61.30
                                                107.0
                                                       103.16
                                                                74.13
                                                                          0
                                                                              343
## TEAM_PITCHING_BB
                       13 2276
                                553.01
                                        166.36
                                                536.5
                                                        542.62
                                                                98.59
                                                                          0
                                                                             3645
## TEAM_PITCHING_SO
                       14 2174
                                        553.09
                                                813.5
                                                        796.93 257.23
                                                                          0 19278
                                817.73
## TEAM FIELDING E
                       15 2276
                                246.48
                                        227.77
                                                 159.0
                                                        193.44
                                                                62.27
                                                                         65
                                                                             1898
## TEAM_FIELDING_DP
                               146.39
                                         26.23
                       16 1990
                                                 149.0
                                                       147.58
                                                                23.72
                                                                         52
                                                                              228
##
                    range
                            skew kurtosis
                                              se
## TARGET_WINS
                       146 -0.40
                                     1.03
                                           0.33
## TEAM_BATTING_H
                           1.57
                      1663
                                     7.28
                                           3.03
## TEAM BATTING 2B
                      389
                            0.22
                                     0.01
                                           0.98
## TEAM_BATTING_3B
                      223
                           1.11
                                     1.50
                                           0.59
## TEAM BATTING HR
                      264
                           0.19
                                    -0.96
                                           1.27
## TEAM_BATTING_BB
                      878 -1.03
                                     2.18
                                           2.57
## TEAM BATTING SO
                      1399 -0.30
                                    -0.32
                                           5.33
## TEAM_BASERUN_SB
                                     5.49
                      697
                           1.97
                                           1.90
## TEAM BASERUN CS
                       201
                           1.98
                                     7.62
                                           0.59
## TEAM BATTING HBP
                                           0.94
                        66
                           0.32
                                    -0.11
## TEAM PITCHING H
                    28995 10.33
                                   141.84 29.49
## TEAM_PITCHING_HR
                      343
                           0.29
                                    -0.60
                                           1.28
## TEAM_PITCHING_BB
                     3645
                           6.74
                                    96.97
                                           3.49
## TEAM_PITCHING_SO 19278 22.17
                                   671.19 11.86
## TEAM FIELDING E
                      1833 2.99
                                    10.97 4.77
## TEAM_FIELDING_DP
                      176 -0.39
                                     0.18 0.59
```

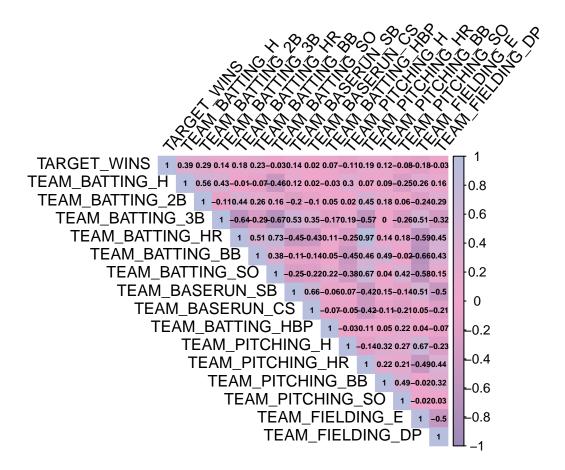
Distribution of variables

The TARGET_WINS, TEAM_BATTING_2B, TEAM_BATTING_HBP, and TEAM_FIELDING_DP variables show a normal distribution. The TEAM_BATTING_HR, TEAM_BATTING_SO, and TEAM_PITCHING_HR variables show a bimodal distribution.



Correlation of variables

From this visual, wins seem to be most linearly correlated with TEAM_BATTING_H (0.39), TEAM_BATTING_2B (0.29), TEAM BATTING BB (0.23), TEAM PITCHING HR (0.19), and TEAM BATTING HR (0.18).



2. Data Preparation

Checking for missing values within the dataset by creating flags for every column

```
## [1] "TARGET_WINS missing values? FALSE"
## [1] "TEAM BATTING H missing values? FALSE"
## [1] "TEAM_BATTING_2B missing values? FALSE"
## [1] "TEAM_BATTING_3B missing values? FALSE"
## [1] "TEAM_BATTING_HR missing values? FALSE"
## [1] "TEAM_BATTING_BB missing values? FALSE"
  [1] "TEAM_BATTING_SO missing values? TRUE"
## [1] "TEAM_BASERUN_SB missing values? TRUE"
## [1] "TEAM_BASERUN_CS missing values? TRUE"
## [1] "TEAM_BATTING_HBP missing values? TRUE"
## [1] "TEAM_PITCHING_H missing values? FALSE"
## [1] "TEAM_PITCHING_HR missing values? FALSE"
  [1] "TEAM_PITCHING_BB missing values? FALSE"
  [1] "TEAM_PITCHING_SO missing values? TRUE"
   [1] "TEAM_FIELDING_E missing values? FALSE"
   [1] "TEAM_FIELDING_DP missing values? TRUE"
##
##
        TARGET WINS
                      TEAM BATTING H
                                      TEAM_BATTING_2B
                                                        TEAM BATTING 3B
##
##
   TEAM_BATTING_HR
                     TEAM_BATTING_BB
                                      TEAM_BATTING_SO
                                                        TEAM_BASERUN_SB
##
                  0
                                                   102
   TEAM_BASERUN_CS TEAM_BATTING_HBP
                                      TEAM_PITCHING_H TEAM_PITCHING_HR
```

```
## 772 2085 0 0
## TEAM_PITCHING_BB TEAM_PITCHING_SO TEAM_FIELDING_DP
## 0 102 0 286
```

Since the TEAM_BATTING_HBP variable was missing 2000 values, we will just remove this column from the dataset. The other columns that had missing values (TEAM_BATTING_SO, TEAM_BASERUN_SB, TEAM_BASERUN_CS, TEAM_PITCHING_SO, and TEAM_FIELDING_DP) will be replaced with the median value of that variable.

```
TEAM_BATTING_H TEAM_BATTING_2B TEAM_BATTING_3B
##
     TARGET_WINS
##
    Min.
          : 0.00
                             : 891
                                      Min.
                                             : 69.0
                                                       Min.
                                                               : 0.00
    1st Qu.: 71.00
                      1st Qu.:1383
                                      1st Qu.:208.0
                                                       1st Qu.: 34.00
    Median: 82.00
                                      Median :238.0
##
                      Median:1454
                                                       Median: 47.00
           : 80.79
##
    Mean
                             :1469
                                                               : 55.25
                      Mean
                                      Mean
                                              :241.2
                                                       Mean
##
    3rd Qu.: 92.00
                      3rd Qu.:1537
                                      3rd Qu.:273.0
                                                       3rd Qu.: 72.00
##
    Max.
           :146.00
                      Max.
                              :2554
                                      Max.
                                              :458.0
                                                       Max.
                                                               :223.00
##
    TEAM_BATTING_HR
                      TEAM_BATTING_BB TEAM_BATTING_SO
                                                         TEAM_BASERUN_SB
##
    Min.
           : 0.00
                             : 0.0
                                              :
                                                   0.0
                                                         Min.
                                                                : 0.0
                      Min.
                                       Min.
    1st Qu.: 42.00
                      1st Qu.:451.0
                                       1st Qu.: 556.8
                                                         1st Qu.: 67.0
    Median :102.00
##
                      Median :512.0
                                       Median: 750.0
                                                         Median :101.0
##
    Mean
           : 99.61
                      Mean
                             :501.6
                                       Mean
                                              : 736.3
                                                         Mean
                                                                 :123.4
##
    3rd Qu.:147.00
                      3rd Qu.:580.0
                                       3rd Qu.: 925.0
                                                         3rd Qu.:151.0
                             :878.0
                                              :1399.0
##
    Max.
           :264.00
                      Max.
                                       Max.
                                                         Max.
                                                                 :697.0
    TEAM_BASERUN_CS
                      TEAM_PITCHING_H TEAM_PITCHING_HR TEAM_PITCHING_BB
##
##
    Min.
           : 0.00
                      Min.
                             : 1137
                                       Min.
                                              : 0.0
                                                         Min.
                                                                     0.0
##
    1st Qu.: 44.00
                      1st Qu.: 1419
                                       1st Qu.: 50.0
                                                         1st Qu.: 476.0
    Median : 49.00
                      Median: 1518
                                       Median :107.0
                                                         Median : 536.5
           : 51.51
                                                                 : 553.0
##
    Mean
                      Mean
                             : 1779
                                       Mean
                                               :105.7
                                                         Mean
    3rd Qu.: 54.25
##
                      3rd Qu.: 1682
                                       3rd Qu.:150.0
                                                         3rd Qu.: 611.0
##
                                                                 :3645.0
   {\tt Max.}
           :201.00
                      Max.
                              :30132
                                       Max.
                                               :343.0
                                                         Max.
    TEAM_PITCHING_SO
                       TEAM_FIELDING_E
                                         TEAM_FIELDING_DP
##
    Min.
           :
                 0.0
                       Min.
                               :
                                 65.0
                                         Min.
                                                 : 52.0
##
    1st Qu.:
              626.0
                       1st Qu.: 127.0
                                         1st Qu.:134.0
   Median:
              813.5
                       Median: 159.0
                                         Median :149.0
##
              817.5
                               : 246.5
                                                 :146.7
    Mean
                       Mean
                                         Mean
    3rd Qu.:
              957.0
                       3rd Qu.: 249.2
                                         3rd Qu.:161.2
           :19278.0
    Max.
                       Max.
                               :1898.0
                                         Max.
                                                 :228.0
```

Checking for any missing values within the dataset.

```
## [1] "Count of total missing values "
## [1] 0
```

Now there is no more missing values within the dataset.

3. Build Models

Model 1

For this model, we are going to use the three variables that were most linearly correlated to target wins: TEAM_BATTING_H (0.39), TEAM_BATTING_2B (0.29), TEAM_BATTING_BB (0.23).

```
##
## Call:
## lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_2B +
## TEAM_BATTING_BB, data = df)
```

```
##
## Residuals:
##
       Min
                1Q
                    Median
                                 30
                                        Max
   -59.753
                      0.529
                              9.176
                                     48.847
##
            -8.719
##
##
  Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   -1.753191
                                3.384614
                                          -0.518
                                                     0.605
  TEAM BATTING H
                    0.045218
                                0.002538
                                          17.819
                                                    <2e-16 ***
  TEAM_BATTING_2B -0.004206
                                0.008088
                                          -0.520
                                                     0.603
  TEAM_BATTING_BB
                    0.034136
                                0.002557
                                          13.348
                                                    <2e-16 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 13.92 on 2272 degrees of freedom
## Multiple R-squared: 0.2196, Adjusted R-squared: 0.2185
## F-statistic: 213.1 on 3 and 2272 DF, p-value: < 2.2e-16
```

The coefficient estimate for TEAM_BATTING_H is 0.045218, which means that each hit by a batter will increase the TARGET_WINS by 0.045. In addition, the coefficient estimate for TEAM_BATTING_BB is 0.034136, which indicates that every walk by a batter increases the TARGET_WINS by 0.034. Both TEAM_BATTING_H and TEAM_BATTING_BB have a p-value less than 0.05 so they are statistically significant in predicting the number of wins. On the other hand, TEAM_BATTING_2B has a coefficient of -0.04206 with a p-value of 0.603. The negative coefficient suggests that the more doubles a team has, the lower amount of wins. However, since the p-value is so high, we cannot say there is a relationship between the number of doubles and the number of wins.

The residual standard error of 13.92 indicates that the typical difference between the observed and predicted number of wins is 14 wins. This error is relatively large considering the average wins is 80.79. Also, the Multiple R-squared value of 0.2196 indicates that about 22% of the variability in wins can be explained by this multiple linear regression model. Lastly, the p-value of the model is <2.2e-16, signifies that this model is statistically significant in predicting the number of wins.

In summary, while this model is statistically significant in predicting the number of wins, we would not use it as the R-squared is low at 0.22 and the standard error is relatively high. Although it makes sense that the increasing the number of hits (TEAM_BATTING_H) and walks(TEAM_BATTING_BB) increases the amount of wins, it is odd that increasing the amount of doubles decreases the total wins.

Model 2

This multiple linear regression model omits the intercept within the model because if the intercept in a regression model predicting baseball team wins is negative, it suggests that even when all independent variables are set to zero, the model predicts a negative number of wins. This negative prediction essentially indicates that the team is expected to have more losses than wins, which is not realistic or meaningful in the context of baseball.

```
##
## Call:
  lm(formula = TARGET WINS ~ TEAM BATTING H + TEAM BATTING BB +
##
       TEAM_BATTING_2B + 0, data = df)
##
##
  Residuals:
                                  3Q
##
       Min
                 1Q
                     Median
                                         Max
##
   -59.621
            -8.766
                      0.515
                               9.242
                                      48.825
## Coefficients:
```

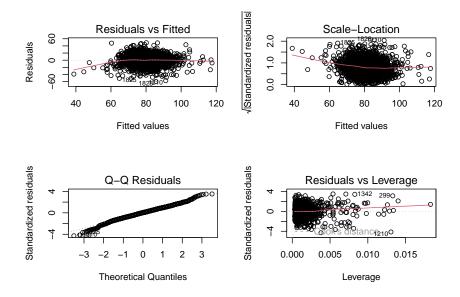
```
##
                    Estimate Std. Error t value Pr(>|t|)
                    0.044092
                                0.001309
## TEAM BATTING H
                                          33.680
                                                   <2e-16
  TEAM BATTING BB
                    0.033513
                                0.002257
                                          14.848
                                                   <2e-16
  TEAM BATTING 2B
                   -0.003267
                                0.007881
                                          -0.415
                                                    0.679
##
  Signif. codes:
                           0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
## Residual standard error: 13.92 on 2273 degrees of freedom
## Multiple R-squared: 0.9714, Adjusted R-squared:
## F-statistic: 2.576e+04 on 3 and 2273 DF, p-value: < 2.2e-16
```

The coefficients obtained from our multiple linear regression model shed light on the relationship between specific baseball metrics and the number of wins. For instance, the coefficient for "TEAM_BATTING_H" (Base Hits by batters) is approximately 0.044, indicating that for each additional base hit, we expect around 0.044 more wins, holding other variables constant. Similarly, the coefficient for "TEAM_BATTING_BB" (Walks allowed) is approximately 0.034, suggesting that each additional walk allowed by the pitching team is associated with around 0.034 more wins.

However, the coefficient for "TEAM_BATTING_2B" (Doubles by batters) is approximately -0.003, which is statistically insignificant (p-value = 0.679). This suggests that the number of doubles by batters may not have a significant effect on wins. This finding may appear counterintuitive, as one might expect teams with more doubles to win more games. The residual standard error of 13.92 indicates that the typical difference between the observed and predicted number of wins is 14 wins. This error is relatively large considering the average wins is 80.79.

Despite this inconsistency, the overall model demonstrates a strong ability to explain win variance, with an adjusted R-squared value of 0.9714. This indicates that the model accounts for a significant portion of the variability in wins based on the included variables. Therefore, it may be advisable to retain the model for further analysis and refinement.

Residual Analysis - Model 2



Residuals vs Fitted: The residuals are clustered around 60-100, suggesting that the assumption of linearity is not met. Scale-location: The data is not randomly dispersed around the horizontal line so the assumption of homoscedasticity is not met. *Normal Q-Q: For the most part, the plot follows the normal line but there are some deviations at the tail.

Judging from the residual plots, this model might not be the best fit for predicting the response variable.

Model 3

Let's construct a multiple linear regression model with the response variable as TARGET_WINS and additional explanatory variables as TEAM_PITCHING_H, TEAM_PITCHING_HR, and TEAM_PITCHING_BB. This selection is based on their correlation coefficients with TARGET_WINS: TEAM_PITCHING_H (-0.10993705), TEAM_PITCHING_HR (0.18901373), and TEAM_PITCHING_BB (0.124174536). Despite TEAM_PITCHING_H having a negative correlation coefficient, indicating a potentially negative impact on wins, it's essential to consider its significance in the model along with the positive coefficients of TEAM_PITCHING_HR and TEAM_PITCHING_BB. By including these variables, we aim to capture the collective influence of pitching-related statistics on the number of wins in our dataset.

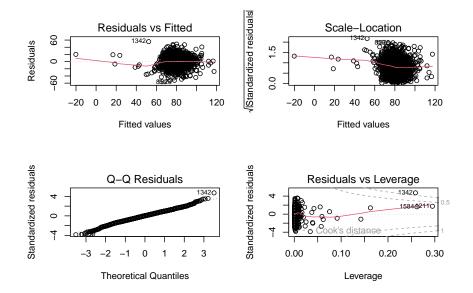
```
## Call:
  lm(formula = TARGET_WINS ~ TEAM_BATTING_H + TEAM_BATTING_BB +
##
       TEAM_BATTING_2B + TEAM_PITCHING_H + TEAM_PITCHING_HR + TEAM_PITCHING_BB +
##
##
       0, data = df)
##
##
  Residuals:
##
       Min
                    Median
                                3Q
                                       Max
                1Q
   -52.370
           -8.915
                     0.355
                             9.095
                                    55.659
##
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                     0.0522497
## TEAM_BATTING_H
                                0.0015908
                                           32.844
                                                   < 2e-16 ***
## TEAM BATTING BB
                     0.0107415
                                0.0040568
                                            2.648 0.008158 **
## TEAM BATTING 2B
                    -0.0180974
                                0.0085538
                                           -2.116 0.034476 *
## TEAM PITCHING H
                    -0.0026699
                                0.0003321
                                           -8.040 1.43e-15 ***
## TEAM PITCHING HR
                    0.0212424
                                0.0058310
                                            3.643 0.000276 ***
## TEAM PITCHING BB
                    0.0099604
                                0.0027667
                                            3.600 0.000325 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 13.69 on 2270 degrees of freedom
## Multiple R-squared: 0.9724, Adjusted R-squared: 0.9723
## F-statistic: 1.333e+04 on 6 and 2270 DF, p-value: < 2.2e-16
```

The coefficients obtained from our multiple linear regression model shed light on the relationship between specific baseball metrics and the number of wins. For instance, the coefficient for "TEAM_BATTING_H" (Base Hits by batters) suggests that each additional base hit is associated with around 0.044 more wins, holding other variables constant. Similarly, the coefficient for "TEAM_BATTING_BB" (Walks allowed) indicates that each additional walk allowed by the pitching team correlates with around 0.034 more wins.

However, the coefficient for "TEAM_BATTING_2B" (Doubles by batters) is statistically insignificant (p-value = 0.679), suggesting that the number of doubles by batters may not significantly impact wins. This finding may seem counterintuitive, as one might expect teams with more doubles to win more games.

Despite this inconsistency, the overall model demonstrates a strong ability to explain win variance, with an adjusted R-squared value of 0.9714. Therefore, it may be advisable to retain the model for further analysis and refinement.

Residual Analysis - Model 3



Residuals vs Fitted: The residuals are clustered around 60-100, suggesting that the assumption of linearity is not met. Scale-location: The previous plot showed a more uniform distribution of residuals across fitted values, while the current plot exhibits a dip in residuals around the range of 60 to 100 fitted values, indicating potential heteroscedasticity or a distinct pattern of variability in that range. Normal Q-Q: For the most part, the plot follows the normal line but there are some deviations at the tail. Residuals vs Leverage: We see a concentration of points toward the left end of the x-axis in the plot which suggests the presence of influential data points with high leverage, indicating they have a significant impact on the regression model's coefficients.

Model 4

For this model, we are going to create an interaction term by taking the product of TEAM_BATTING_H, TEAM_BATTING_HR, and TEAM_BATTING_BB. These were most linearly correlated with TARGET_WINS and all of these variables have a positive impact on the number of wins. An interaction term will show that the multiplicative effects of these variables on predicting the TARGET_WINS might be better than the sum of them individually. Doubles hit by batters was not included as it had a high p-value in the first model, suggesting it might not be a significant predictor, and it is slightly correlated with hits by batter.

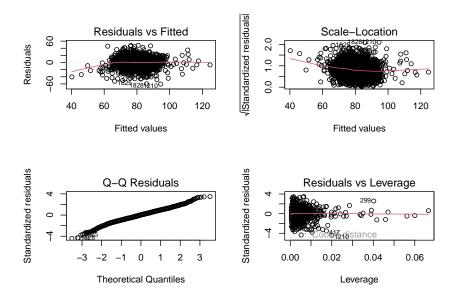
```
##
##
  Call:
   lm(formula = TARGET_WINS ~ (TEAM_BATTING_H * TEAM_BATTING_BB *
##
       TEAM_BATTING_HR) + 0, data = df)
##
##
   Residuals:
##
                                 3Q
       Min
                 1Q
                                         Max
                     Median
##
    -60.510
            -8.755
                      0.406
                              9.190
                                      48.240
##
##
   Coefficients:
##
                                                       Estimate Std. Error t value
  TEAM BATTING H
                                                      4.516e-02
                                                                 1.117e-03
##
                                                                             40.423
  TEAM BATTING BB
##
                                                      5.706e-02
                                                                 1.324e-02
                                                                              4.310
  TEAM BATTING HR
                                                     -5.191e-01
                                                                 1.956e-01
                                                                             -2.654
  TEAM_BATTING_H:TEAM_BATTING_BB
                                                     -2.142e-05
                                                                 9.034e-06
                                                                             -2.371
  TEAM_BATTING_H: TEAM_BATTING_HR
                                                      3.305e-04
                                                                 1.332e-04
                                                                              2.481
  TEAM_BATTING_BB:TEAM_BATTING_HR
                                                      8.261e-04
                                                                 3.401e-04
                                                                              2.429
## TEAM_BATTING_H:TEAM_BATTING_BB:TEAM_BATTING_HR -4.995e-07
                                                                 2.304e-07
                                                                             -2.169
```

```
##
                                                   Pr(>|t|)
## TEAM BATTING H
                                                    < 2e-16 ***
  TEAM BATTING BB
                                                    1.7e-05
  TEAM_BATTING_HR
                                                    0.00802 **
  TEAM_BATTING_H:TEAM_BATTING_BB
                                                    0.01782
  TEAM BATTING H: TEAM BATTING HR
                                                    0.01316 *
  TEAM BATTING BB: TEAM BATTING HR
                                                    0.01523 *
  TEAM BATTING H:TEAM BATTING BB:TEAM BATTING HR
                                                   0.03021 *
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
  Signif. codes:
## Residual standard error: 13.86 on 2269 degrees of freedom
## Multiple R-squared: 0.9717, Adjusted R-squared:
## F-statistic: 1.114e+04 on 7 and 2269 DF, p-value: < 2.2e-16
```

These results of the coefficient estimates are a bit surprising as I was expecting all of them to be positive since they all have a positive impact on wins. The coefficients for TEAM_BATTING_H and TEAM_BATTING_BB are positive, indicating that an increase in these variables is associated with an increase in TARGET_WINS. However, the main effect of TEAM_BATTING_HR is negative, suggesting that an increase in home runs is associated with a decrease in wins. This is counterintuitive as one would expect the more home runs a team hit, the more wins they have. Also, the coefficient for the interaction term TEAM_BATTING_H:TEAM_BATTING_BB:TEAM_BATTING_HR is -4.995e-07, indicating that for each combined base hit, walk, and home run, th model predicts a decrease in the amount of wins by 4.995e-07. Again, this does not seem to align with the fact that these individually have a positive impact on wins. All of the p-values are low indicating statistical significance. However, coefficients themselves are small so it debatable how relative this model is in predicting wins.

Like the previous models, the R-squared is high at 0.9717 so 97% of the variance in the response model can be attributed to this model. In addition, all of the p-values for these variables are low, indicating that they are statistically significant predictors in this model. But, the magnitude of these coefficients is quite small, which suggests the practical significance of these predictors in this model. Overall, while this model has strong statistical significance, the coefficients do not match with our conception of baseball so it will need further refinement.

Residual Analysis - Model 4



These residual plots are similar to the previous models. The plots suggest some issues with the assumptions

of homoscedasticity and linearity. Therefore a linear regression model may not be the best fit for the data.

4. Select Models

To evaluate the performance of the models, let's look at the R-squared, Mean Squared Error, and Root Mean Squared Error.

```
##
##
   Model 1
## Adjusted R-squared:
                        0.218542337673064
        193.562551032368
## RMSE:
         13.9126759120008
##
   Model 2
## Adjusted R-squared: 0.97138957456795
## MSE:
        193.58540982541
## RMSE: 13.9134973973264
##
##
   Model 3
## Adjusted R-squared:
                        0.972330323973487
## MSE:
         186.972959428232
## RMSE: 13.6738055942094
##
   Model 4
##
## Adjusted R-squared:
                        0.971633024820375
## MSE:
         191.600392909153
## RMSE:
          13.8419793710709
```

Based on all of our multiple linear regression models, model 3 seems to have performed best. In comparison to the other models, model 3 has the highest R-squared value at 0.9724, the lowest MSE at 186.97, and the lowest RMSE at 13.67. In addition, the p-value for the coefficient estimates and for the f-statistic were all statistically significant. Also, we did take into account whether the models made practical sense. We concluded that all the models seem to have one or more variables that seem counterinituitive and they all have residual plots that suggest a linear model might not be the best fit for the data. Thus, we decided to go with the model that the highest R-squared and lowest RMSE, which was model 3.

Predicting the evaluation data set We will use our trained model to predict the number of wins in the evaluation dataset. Here is a summary of the evaluation dataset:

```
TEAM BATTING H TEAM BATTING 2B TEAM BATTING 3B
                                                       TEAM BATTING HR
##
    Min.
           : 819
                    Min.
                           : 44.0
                                     Min.
                                            : 14.00
                                                       Min.
                                                              : 0.00
##
    1st Qu.:1387
                    1st Qu.:210.0
                                     1st Qu.: 35.00
                                                       1st Qu.: 44.50
##
   Median:1455
                    Median :239.0
                                     Median : 52.00
                                                       Median: 101.00
##
    Mean
           :1469
                    Mean
                           :241.3
                                     Mean
                                             : 55.91
                                                       Mean
                                                               : 95.63
##
    3rd Qu.:1548
                    3rd Qu.:278.5
                                     3rd Qu.: 72.00
                                                       3rd Qu.:135.50
##
                           :376.0
                                     Max.
                                             :155.00
    Max.
           :2170
                    Max.
                                                       Max.
                                                               :242.00
##
    TEAM_BATTING_BB TEAM_BATTING_SO
                                       TEAM_BASERUN_SB TEAM_BASERUN_CS
##
    Min.
           : 15.0
                                 0.0
                                       Min.
                                               : 0.0
                                                                : 0.00
                     Min.
                                                        Min.
##
    1st Qu.:436.5
                     1st Qu.: 565.0
                                       1st Qu.: 60.5
                                                        1st Qu.: 44.00
##
    Median :509.0
                     Median: 686.0
                                       Median: 92.0
                                                        Median: 49.50
           :499.0
                            : 707.7
                                               :122.1
                                                                : 51.37
##
    Mean
                     Mean
                                       Mean
                                                        Mean
   3rd Qu.:565.5
##
                     3rd Qu.: 904.5
                                       3rd Qu.:149.0
                                                        3rd Qu.: 56.00
                             :1268.0
                                               :580.0
##
    Max.
           :792.0
                     Max.
                                       Max.
                                                        Max.
                                                                :154.00
##
    TEAM_PITCHING_H TEAM_PITCHING_HR TEAM_PITCHING_BB TEAM_PITCHING_SO
    Min.
           : 1155
                     Min.
                            : 0.0
                                       Min.
                                               : 136.0
                                                         Min.
```

```
1st Qu.: 1426
                     1st Qu.: 52.0
                                       1st Qu.: 471.0
                                                         1st Qu.: 622.5
##
    Median: 1515
                     Median :104.0
                                       Median: 526.0
##
                                                         Median: 745.0
                     Mean
##
    Mean
           : 1813
                            :102.1
                                       Mean
                                              : 552.4
                                                         Mean
                                                                : 795.9
    3rd Qu.: 1681
                     3rd Qu.:142.5
                                       3rd Qu.: 606.5
                                                         3rd Qu.: 927.5
##
           :22768
##
    Max.
                     Max.
                            :336.0
                                       Max.
                                              :2008.0
                                                         Max.
                                                                :9963.0
    TEAM FIELDING E
                      TEAM_FIELDING_DP
##
           : 73.0
##
    Min.
                      Min.
                             : 69.0
    1st Qu.: 131.0
##
                      1st Qu.:134.5
##
    Median : 163.0
                      Median :148.0
           : 249.7
##
    Mean
                      Mean
                             :146.3
##
    3rd Qu.: 252.0
                      3rd Qu.:160.5
           :1568.0
                             :204.0
##
    Max.
                      Max.
   [1] "Model 3: Evaluation data"
   [1] "Mean Squared Error:
                              330.38129718844"
## [1] "Root Mean Squared Error:
                                   18.1763939544795"
```

When model 3 was applied to the evaluation data, the RSME increased from 13.67 to 18.17, which suggests that the model's predictions are not as accurate on the evaluation data as they were on the training data. The high R-squared value of the model on the training data is an indication that there is possible overfitting. This means that the model is good at predicting data from the training dataset but not unseen data in the evaluation set. In conclusion, more work needs to be done so that the model performs well on both seen and unseen data.

Appendix: Code for this assignment