## punto14

## April 8, 2022

```
[]: GPA<-c(2.8,3.4,3,3.5,3.6,3,2.7,3.7)
ACT<-c(21,24,26,27,29,25,25,30)
df<-data.frame(ACT,GPA)
df
```

```
ACT
                               GPA
                      <dbl>
                               <dbl>
                      21
                               2.8
                      24
                               3.4
                      26
                               3.0
A data.frame: 8 \times 2
                      27
                               3.5
                      29
                               3.6
                      25
                               3.0
                      25
                               2.7
                      30
                               3.7
```

```
[]: X<-data.frame(1.0,df$ACT)
Y<-data.frame(df$GPA)
Y<-data.matrix(Y)
X<-data.matrix(X)
X_t<-t(X)
X_tX<-X_t %*% X
X_tX_inv<-solve(X_tX)
X_tY<-X_t %*% Y</pre>
BETA<-X_tX_inv %*% X_tY
```

```
[]: cat('if ACT up in 7.0, GPA will be up in ',BETA[2,1]*7,'\n')
```

if ACT up in 7.0, GPA will be up in 0.7153846

```
[]: df$GPA_pred<-X %*% BETA df$ERRORS<-df$GPA-df$GPA_pred df
```

```
ACT
                              GPA
                                       GPA_pred
                                                    ERRORS
                                       <dbl[,1]>
                     <dbl>
                              <dbl>
                                                    <dbl[,1]>
                     21
                              2.8
                                       2.714286
                                                    0.08571429
                     24
                              3.4
                                       3.020879
                                                    0.37912088
                     26
                              3.0
                                       3.225275
                                                    -0.22527473
A data.frame: 8 \times 4
                     27
                              3.5
                                       3.327473
                                                    0.17252747
                     29
                              3.6
                                       3.531868
                                                    0.06813187
                     25
                              3.0
                                       3.123077
                                                    -0.12307692
                     25
                              2.7
                                       3.123077
                                                    -0.42307692
                     30
                              3.7
                                       3.634066
                                                    0.06593407
```

```
[]: cat('the sum of errors is ',sum(round(df$ERRORS,0)))
```

the sum of errors is 0

```
[]: cat('if ACT is 20, GPA will be ',BETA[1,1]+BETA[2,1]*20)
```

if ACT is 20, GPA will be 2.612088

```
[]: var_gpa<-var(df$GPA)
  var_gpa_prec<-var(df$GPA_pred)
  var_gpa_prec<-var_gpa_prec[1,1]

cat('the variance of GPA is ',var_gpa,'\n')
  cat('the variance of GPA_pred is ',var_gpa_prec,'\n')

cat('R^2 is ',var_gpa_prec/var_gpa,'\n')</pre>
```

the variance of GPA is 0.1469643 the variance of GPA\_pred is 0.08486068  $R^2$  is 0.5774238

una gran proporcion de la varianza de GPA esta explicada por ACT, por lo que se puede concluir que ACT esta siendo un buen predictor de GPA