

EEE PART I: MEng, BEng and ACGL

Corrected copy

Time allowed: 2:00 hours

Answer ALL questions.

Question One carries 40% of the marks. Questions Two and Three each carry 30%.

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible

First Marker(s) :	K. Fobelets
Second Marker(s) :	S. Lucyszyn

Constants

permittivity of free space:	$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$
permeability of free space:	$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$
intrinsic carrier concentration in Si:	$n_i = 1.45 \times 10^{10} \text{ cm}^{-3} \text{ at } T = 300 \text{ K}$
dielectric constant of Si:	$\epsilon_{\text{Si}} = 11$
dielectric constant of SiO ₂ :	$\epsilon_{\text{ox}} = 4$
thermal voltage:	$V_T = kT/e = 0.026 \text{ V at } T = 300 \text{ K}$
charge of an electron:	$e = 1.6 \times 10^{-19} \text{ C}$
Planck's constant:	$h = 6.63 \times 10^{-34} \text{ Js}$
Bandgap of Si:	$E_G = 1.12 \text{ eV at } T = 300 \text{ K}$
Effective density of states of Si:	$N_C = 3.2 \times 10^{19} \text{ cm}^{-3} \text{ at } T = 300 \text{ K}$ $N_V = 1.8 \times 10^{19} \text{ cm}^{-3} \text{ at } T = 300 \text{ K}$

Formulae

$$f(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{kT}\right)}$$

Fermi distribution

$$n_i = \sqrt{N_V N_C} \exp\left(\frac{-E_G}{2kT}\right)$$

Intrinsic carrier concentration

$$n = N_C e^{\frac{(E_F - E_C)}{kT}}$$

Concentration of electrons

$$p = N_V e^{\frac{(E_V - E_F)}{kT}}$$

Concentration of holes

$$\frac{dE}{dx} = \frac{\rho(x)}{\epsilon}$$

Poisson equation in 1 dimension

$$\left. \begin{aligned} J_n(x) &= e\mu_n n(x)E(x) + eD_n \frac{dn(x)}{dx} \\ J_p(x) &= e\mu_p p(x)E(x) - eD_p \frac{dp(x)}{dx} \end{aligned} \right\}$$

Drift and diffusion current densities in a semiconductor

$$I_{DS} = \frac{\mu C_{ox} W}{L} \left((V_{GS} - V_{th}) V_{DS} - \frac{V_{DS}^2}{2} \right)$$

Current in a MOSFET

$$\left. \begin{aligned} J_n &= \frac{eD_n n_{p0}}{L_n} \left(e^{\frac{eV}{kT}} - 1 \right) \\ J_p &= \frac{eD_p p_{n0}}{L_p} \left(e^{\frac{eV}{kT}} - 1 \right) \end{aligned} \right\}$$

Current densities for a pn-junction with lengths L_n & L_p

$$V_{bi} = \frac{kT}{e} \ln\left(\frac{N_A N_D}{n_i^2}\right)$$

Built-in voltage

$$c = c_0 \exp\left(\frac{eV}{kT}\right) \text{ with } \begin{cases} c = p_n \text{ or } n_p \\ c_0 \text{ bulk minority carrier concentration} \end{cases}$$

Minority carrier injection under bias V

$$D = \frac{kT}{e} \mu$$

Einstein relation

$$w_n(V) = \left[\frac{2\epsilon(V_{bi} - V)N_A}{e(N_A + N_D)N_D} \right]^{1/2} \quad \& \quad w_p(V) = \left[\frac{2\epsilon(V_{bi} - V)N_D}{e(N_A + N_D)N_A} \right]^{1/2}$$

Depletion widths under bias V

$$W_{depl}^{\max} = 2 \left[\frac{\epsilon kT \ln\left(\frac{N_{\text{substrate}}}{n_i}\right)}{e^2 N_{\text{substrate}}} \right]^{1/2}$$

Maximum depletion width

The Questions

1.

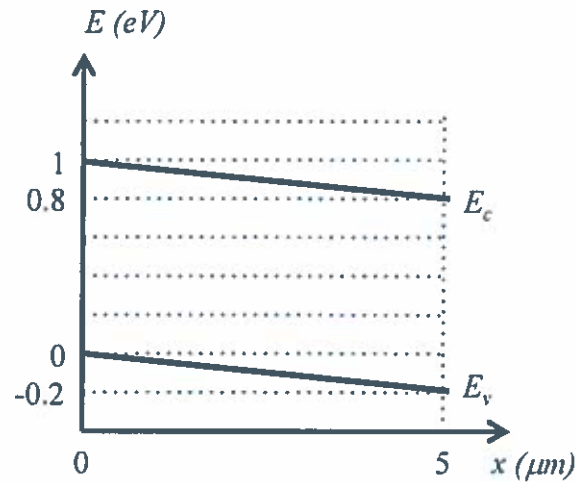


Figure 1.1: Energy band diagram of a semiconductor with $N_v = N_c$.

- a) Redraw the energy band diagram of the semiconductor of fig. 1.1 and add:
- i) The bandgap E_G and its value. [2]
 - ii) The intrinsic level E_i . [2]
 - iii) The electrostatic potential difference ΔV between $x = 0$ and $5 \mu\text{m}$ and give its amplitude. [4]
 - iv) The electric field vector \mathcal{E} and give its amplitude. [4]
 - v) Draw the material cross section of this semiconductor and add a battery with a value and polarity consistent with the energy band diagram in fig. 1.1. Assume no voltage drop at the contacts. [4]
 - vi) Assuming the semiconductor of fig. 1.1 is doped with acceptor atoms N_A , draw the electron and hole flow (flux) through the material as appropriate for the doping type. [4]
- b)
- i) Give the relationship between the workfunction of a metal contact and workfunction of p-type Si to obtain a Schottky contact. [2]
 - ii) The doping density of the p-type Si in b) i) is 10^{16} cm^{-3} . The Schottky barrier height $\phi_B = 0.395 \text{ eV}$ ($\phi_B = |E_F - E_{vs}|$ with E_{vs} the top of the valence band at the metal-semiconductor junction). Give the absolute value of the workfunction difference between the metal and p-type Si. [4]
 - iii) Give the relationship between the on-voltage, V_{ON} of the Schottky diode based on the material combination in b) ii) and that of a n^+p diode with the same doping in the p-region and an n-type doping a factor 100 larger. Justify your answer. [4]

QUESTION CONTINUES ON NEXT PAGE

- c) Answer the following questions on semiconductors and semiconductor devices with “yes” or “no”.
- i) At room temperature, the valence band is almost completely filled with electrons covalently bound to the atoms. [1]
 - ii) If the mass of holes is smaller than the mass of electrons then the hole mobility will be larger than the electron mobility. [1]
 - iii) Current through the depletion region of a pn diode is mainly determined by drift. [1]
 - iv) The reverse bias current through a pn diode is limited by the electric field across the diode. [1]
 - v) The substrate doping in an n-channel enhancement mode MOSFET is n-type. [1]
 - vi) Increasing the substrate doping of a MOSFET will decrease the threshold voltage. [1]
 - vii) The transconductance, g_m of a MOSFET in the triode region (low V_{DS}) will increase when the doping density in the substrate increases. [1]
 - viii) The equivalent gate-drain capacitance C_{GD} of a MOSFET can be neglected for the MOSFET in saturation. [1]
 - ix) The current gain in an n^+pn bipolar junction transistor is larger than that of an npn BJT. [1]
 - x) The output current I_C of a BJT in saturation and in common-emitter configuration increases quasi linearly with increasing bias across the emitter-collector junction, $|V_{CE}|$. [1]

2.

- a) Give the general charge neutrality expression for a semiconductor. Define all parameters in your expression. [4]
- b) Prove the law of mass action $n \times p = n_i^2$ for a semiconductor in equilibrium. [4]
- c) A p-type Si substrate is doped with a density of 10^{17} cm^{-3} boron atoms. To make a pn junction, arsenic atoms are implanted into this substrate creating a final homogeneous doping density of 10^{18} cm^{-3} . Calculate the exact electron and hole densities both in the p-type substrate and the implanted region. [10]
- d) The excess carrier concentration of a pn diode under bias is given in fig. 2.1.

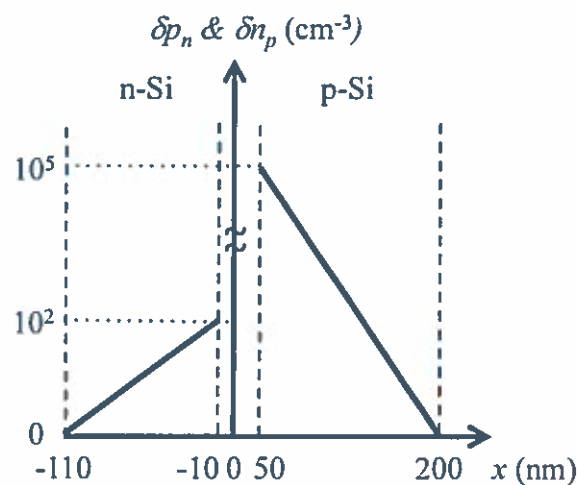


Figure 2.1: The excess minority carrier concentrations of a pn diode under bias.

- i) Is the diode in fig. 2.1 in forward or reverse bias? [2]
- ii) Which region in fig. 2.1 has the highest majority carrier concentration? Give two features in fig. 2.1 that support your answer. [4]
- iii) Calculate the total current density through the pn diode of fig. 2.1. The diffusion constants for the minority carriers are: $D_n = 50 \text{ cm}^2 \text{ s}^{-1}$ and $D_p = 20 \text{ cm}^2 \text{ s}^{-1}$, for electrons and holes respectively. Take the depletion regions into account. [6]

3.

- a) Draw the energy band diagram (E_c , E_F , E_v) from emitter through base into the collector of an n^+pn bipolar junction transistor in forward active mode. Indicate the amplitude of the voltage drops $|V_{EB}|$ and $|V_{CB}|$ on the drawing and include the depletion regions.

[10]

- b) Give the main carrier transport process (drift or diffusion) through the different regions of the “short” BJT in forward active mode.

- i) the emitter region. [1]
- ii) the emitter-base depletion region. [1]
- iii) the base region. [1]
- iv) the base-collector depletion region. [1]
- v) the collector region. [1]

- c) The equivalent circuit of a BJT is given in fig. 3.1.

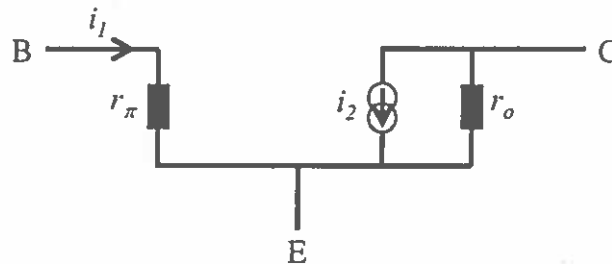


Figure 3.1: Equivalent circuit of a BJT in forward active mode.

- i) What is the condition on the emitter-base AC voltage to allow use of the equivalent circuit in fig. 3.1? [4]
- ii) Give the expression for i_1 in fig. 3.1 in terms of the BJT material parameters. Use X_E , X_B and X_C as the undepleted lengths of the emitter, base and collector, respectively. Identify clearly the doping type and region in the expression of i_1 . [5]
- iii) Give the expression of i_2 in fig. 3.1 in terms of transconductance, g_m . [2]
- iv) Why is the output conductance of the BJT $g_o = r_o^{-1}$ larger than zero? Give a physical reason for this effect and illustrate with an equation or a sketch. [4]

