## UNIVERSITY OF LONDON IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE

## **EXAMINATIONS 2004**

MSci Honours Degree in Mathematics and Computer Science Part IV

MEng Honours Degrees in Computing Part IV

for Internal Students of the Imperial College of Science, Technology and Medicine

This paper is also taken for the relevant examinations for the Associateship of the City and Guilds of London Institute This paper is also taken for the relevant examinations for the Associateship of the Royal College of Science

## PAPER C437

## **DISTRIBUTED ALGORITHMS**

Tuesday 11 May 2004, 14:30 Duration: 120 minutes

Answer THREE questions

Paper contains 4 questions Calculators not required

- 1a What are the three assumptions that characterise a synchronous network model?
- b The *SyncBFS* algorithm computes a breadth-first spanning tree in a general synchronous network.
  - i) Give an informal description of the algorithm stating what assumptions are made about the network.
  - ii) Using the state machine notation, give a formal specification of SyncBFS.
  - iii) Give the communication and time complexity of the algorithm.
- c The initiating process of a *SyncBFS* does not know when the spanning tree construction is complete. Describe informally an extension to *SyncBFS* which detects *termination*.
- d Describe informally an algorithm that uses terminating *SyncBFS* to elect a leader in a general synchronous network. Give precise measures of the time and communication complexity of this algorithm in a network which is in fact a ring with *N* nodes. Give a brief explanation of how you arrived at these measures.

The four parts carry, respectively, 15%, 30%, 20%, 35% of the marks.

- 2a Give the specification for Atomic Commitment and include the conditions for both Strong and Weak Atomic Commitment.
- b Sketch an informal proof that Strong Atomic Commitment is impossible in a synchronous connected network with no process failures but in which link failures may occur.
- c Give an informal description of the Three-Phase Commit termination protocol which is invoked when the coordinator crashes.
- d Consider a synchronous system where communication link failures may occur. In such a system, describe an execution (scenario) of the Three-Phase Commit Algorithm where the *Agreement* property is violated.
- e Assume that a maximum of 2 processes fail while Three-Phase Commit is executed in a group of 7 processes. What is the worst possible *number of messages* (upper bound) required for the termination of 3PC in this environment? Describe the scenario in which this worst case occurs.

The five parts carry, respectively, 20%, 20%, 20%, 20%, 20% of the marks.

- 3 An asynchronous system consists of a fixed number of distributed processes P<sub>i</sub> each of which needs exclusive access to a particular resource at various times.
- Lamport's algorithm for mutual exclusion uses three types of message with logical timestamps: request req, release rel and acknowledgement ack. Each process Pi maintains a local request queue Q<sub>i</sub>. Assuming that the queues are initially empty, outline the following:
  - i) the actions of  $P_i$  on receipt of a timestamped message m from  $P_i$ ,
  - the conditions required for granting of the resource at P<sub>i</sub>,

What is the communications overhead in order for a process to gain exclusive access?

- b Lamport's algorithm (part (a)) requires that there be no overtaking of messages between sites. Show a scenario where, if two processes  $P_0$  and  $P_1$  both send request messages, and overtaking of an acknowledgement message is possible, it can lead to a violation of mutual exclusion. Indicate the state of the local queues  $Q_0$  and  $Q_1$  in each process at each stage.
- Ricart and Agrawala's algorithm does not require that there be no overtaking of messages between sites. Give an outline description for this algorithm, including the types of message used and the information that is stored at each site. Briefly justify why this algorithm is not sensitive to message overtaking.

What is the communications overhead in order for a process to gain exclusive access?

The three parts carry, respectively, 30%, 30%, 40% of the marks.

- Define the Validity, Agreement and Integrity properties required of a reliable 4a broadcast algorithm in an asynchronous distributed system. Define the additional property that must be satisfied by a reliable broadcast algorithm that provides FIFO delivery order.
- b Explain the difference between Causal and FIFO broadcast. Outline a simple algorithm which uses FIFO broadcast to implement Causal Broadcast.
- С Describe briefly how the ISIS CBCAST protocol is implemented and comment on why it is more efficient than the protocol you described in part b.
- d Andrew, Bob and Cameron (A, B & C) all subscribe to an Internet mailing list on interesting car registration plates. Andrew broadcasts a request for plates beginning with m and Bob responds with his latest sightings s. However, when Cameron reads his email, he sees Bob's response (s) before Andrew's request (m) arrives. Using message diagrams, explain the operation of the protocols you described in each of parts b & c in resolving this situation.

The four parts carry respectively 20%, 30%, 30%, 20% of the marks.