

IMPERIAL COLLEGE LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING
EXAMINATIONS 2005

MSc and EEE/ISE PART III/IV: MEng, BEng and ACGI

COMMUNICATION NETWORKS

Wednesday, 27 April 10:00 am

Time allowed: 3:00 hours

Corrected Copy

There are FIVE questions on this paper.

Answer FOUR questions.

All questions carry equal marks

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible	First Marker(s) :	J.A. Barria
	Second Marker(s) :	P.J. Beevor

a)

In ARQ protocol utilisation is defined as:

$$U = \frac{T_f}{N_r T_t}$$

Where N_r is the expected number of re-transmissions, T_f is the transmission time and T_t is the time line is engaged.

- i) Derive N_r for stop and wait protocol.
- ii) Derive N_r for the selective repeat protocol.
- iii) Derive N_r for go back N protocol.
- iv) Discuss the effect of propagation time and transmission time in the derivations of i), ii) and iii).

[8]

b)

- i) Discuss a price based flow control scheme for a delay sensitive service known to you.
- ii) Derive and describe a congestion price that would assign rates amongst i users taking into account users utility functions.
- iii) If the delay faced by each byte that is being transmitted is given by

$$d = \frac{\Lambda}{M(M - \Lambda)}$$

where Λ is the total arrival rate to the system and M is the total capacity of the system.

Derive the optimal congestion price p_c .

[12]

2

a)

Derive the channel efficiency of a 1-persistent CSMA/CD. Clearly state all assumptions made in your derivations.

[10]

b) For the network of Figure 2.1 assume the following data:

Link	$C(i)$ [Kbit/s]	$x(i)$ [Kbit/s]
1	10	5
2	10	5
3	10	1
4	10	4
5	30	6
6	20	6
7	10	4
8	10	4

- Solve the shortest path problem with the Dijkstra algorithm using link cost $l_0(i) = 1$.
- Solve the shortest path problem with the Belman Ford using link cost $l_1(i) = \frac{x(i)}{C(i)}$.
- Solve the shortest path problem with the Dijkstra algorithm and using link cost $l_2(i) = \frac{C(i)}{[C(i) - x(i)]^2}$.

[10]

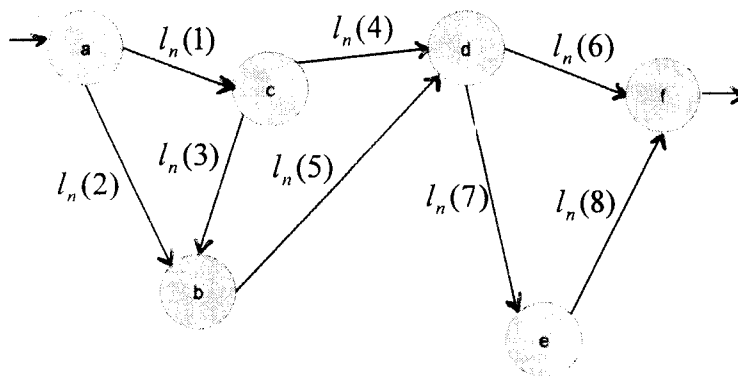


Figure 2.1:

3.

- a) A proposed formulation of a combined optimal routing problem and flow control problem has been suggested as follows:

$$\text{Minimise: } D(x) + \sum_{w \in PW_w} e_w(r_w)$$

- i) Describe and discuss a suitable function $D(x)$. State clearly the meaning of x and associated constraints.
- ii) Suggest, describe and discuss the meaning of a suitable function $e_w(r_w)$.

[10]

b)

- i) For the network of Figure 3.1 formulate a combined optimal routing and flow control problem. State clearly the optimality condition.
- ii) Assume $C(1) = C(2) = 100$ kbit/s. Suggest a suitable function $e_w(r_w)$ and the value of its parameters if it is required that the flow carried by the network should be kept below 10 kbit/s (i.e. $r \leq 10$).

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$$r \leq 10$$

[10]

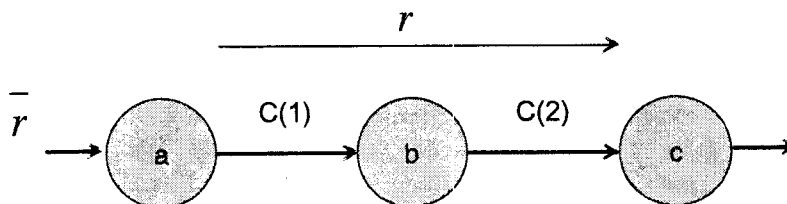


Figure 3.1:

4.

- a) Network survivability is an issue of great importance to the telecommunication industry. Describe and discuss briefly three class of survivability network architecture known to you.

[10]

b)

- i) Explain and discuss the notion of equivalent capacity and its relevance in the context of traffic management in ATM networks.
- ii) Explain and discuss traffic policing in ATM networks. Give examples of possible algorithms that could implement a traffic policing mechanism.

[10]

5.

- a) Describe and discuss three gate protocols which may be Interior or Exterior gate protocols.

[7]

- b) Describe and compare DiffServ and IntServ models.

[6]

- c) Classify and discuss routing protocols in ad hoc networks known to you.

[7]

Examinations : 2004-5 Session		Confidential
MODEL ANSWER and MARKING SCHEME		
First Examiner	Paper Code	3.17
Second Examiner	Question	Page 1 out of 5
Question labels in left margin		Marks allocations in right margin
1(a)	<p>i) $\mu_R = \sum_{i=1}^{\infty} i p^{i-1} (1-p) = \frac{1}{1-p}$</p> <p>ii) $\mu_R = \frac{1}{1-p}$</p> <p>iii) $\mu_R = \sum_{i=1}^{\infty} f(i) p^{i-1} (1-p)$</p> <p>$f(i) = 1 + (i-1)K = (1-K) + Ki$</p> <p>$\mu_R = (1-K) \sum_{i=1}^{\infty} p^{i-1} (1-p) + K \sum_{i=1}^{\infty} i p^{i-1} (1-p)$</p> <p>$= 1-K + \frac{K}{1-p}$</p> <p>$= \frac{1-p+Kp}{1-p}$</p> <p>$K \sim 2a+1$ if $N > 2a+1$ $K \sim N$ if $N \leq 2a+1$</p> <p>iv) $a = \frac{\text{propagation time}}{\text{transmission time}}$</p> <p>$\text{propagation time} = \frac{\text{distance}}{\text{velocity}} = \frac{d}{v}$</p> <p>$\text{transmission time} = \frac{\text{length of frame}}{\text{data rate}} = \frac{L}{R}$</p>	<p>2</p> <p>2</p> <p>2</p> <p>2</p>

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(b) The benefit of user i :

$$u^i(\lambda^i) - \gamma^i d \lambda^i$$

 $u^i(\lambda^i)$ - value of transmitting λ^i bytes/s

 d - delay faced by each byte

 γ^i - converts delay into user i 's cost
User is charged a congestion price of P_c Then the user will choose to transmit λ^i :

$$\max_{\lambda^i} u^i(\lambda^i) - \gamma^i d \lambda^i - P_c \lambda^i$$

Optimal rate is obtained by solving

$$\frac{\partial u^i}{\partial \lambda^i} = \gamma^i d + P_c$$

$$\Lambda = \sum \lambda^i$$

Planner will try to max $\sum_i [u^i(\lambda^i) - \gamma^i d \lambda^i]$

$$d = f(\Lambda, M)$$

$$\frac{\partial u^i}{\partial \lambda^i} = \gamma^i f(\Lambda, M) + \underbrace{\frac{\partial f}{\partial \Lambda}(\Lambda, M) \sum_j \gamma^j \lambda^j}_{\text{congestion price}}$$

$$f(\Lambda, M) = \frac{1}{M} \frac{\Lambda}{M - \Lambda}$$

$$P_c = \frac{\partial f}{\partial \Lambda} \sum_i \gamma^i \lambda^i = \frac{\sum_i \gamma^i \lambda^i}{M^2} \left[\frac{p}{1-p} + \frac{p^2}{(1-p)^2} \right]$$

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2(a)

1-persistent CSMA/CD

$$A = \binom{N}{1} p^1 (1-p)^{N-1} = NP (1-p)^{N-1}$$

N = no of stations

P = probability that a station transmit during an available slot

Slot = twice the end to end propagation

A = probability that exactly one station attempts transmission in a slot

• probability that a successful transmission will take j attempts

$$A (1-A)^{j-1}$$

• Mean number of slots per contention

$$\sum_{j=0}^{\infty} j A (1-A)^{j-1} = \frac{1}{A}$$

• Mean contention interval $2t/A$

• channel efficiency (L = frame size)

$$C_{eff} = \frac{L}{L + 2t/A}$$

2

2

2

2

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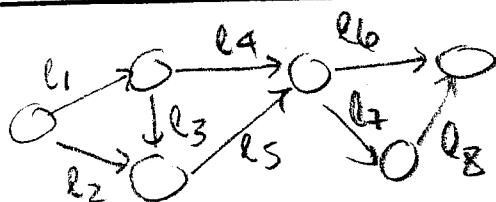
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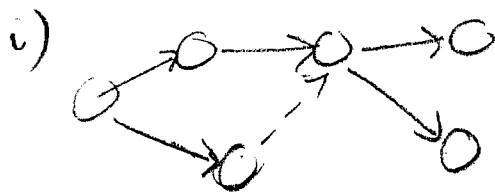
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2b

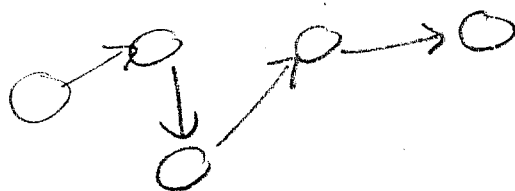


(Explanation)

	$(x_i - \bar{x})^2$
1	25
2	25
3	81
4	36
5	576
6	196
7	36
8	36

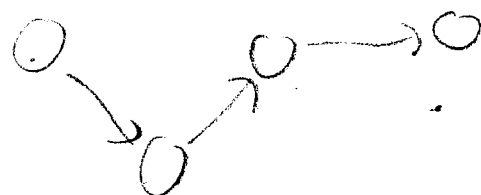


ii)



	$L_1(x)$
1	.5
2	.5
3	.1
4	.4
5	.2
6	.3
7	.4
8	.4

iii)



	$L_2(x)$
1	0.4
2	0.4
3	0.123
4	0.277
5	0.052
6	0.102
7	0.277
8	0.277

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3a

$$i) D(x) = \sum_{(i,j)} D_{ij} (F_{ij}(x_p))$$

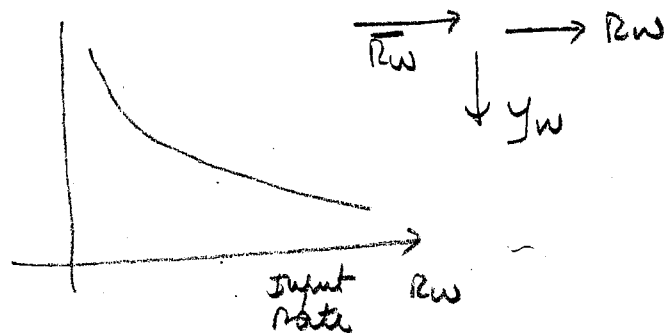
$$\sum_{p \in P_w} x_p = R_w \quad \forall w \in W$$

$$x_p \geq 0 \quad \forall w \in W$$

$$F_{ij} = \sum_{\substack{\text{all paths} \\ \text{containing link } (i,j)}} x_p$$

$$0 \leq R_w \leq \bar{R}_w \quad \forall w \in W$$

$$ii) R_w(R_w) = \frac{a_w}{R_w}$$



$$\text{If } \min D = \sum_{(i,j)} D_{ij} (F_{ij}) \quad \text{wrt } \{x_p\} \text{ and } \{R_w\}$$

the optimal solution is $x_p = 0$ and $R_w = 0$

therefore the need to include a penalty for inputs $\{R_w\}$ becoming too small

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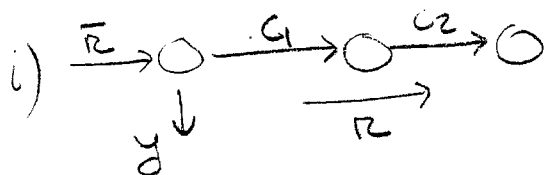
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3(b)



$$D = \frac{R}{C_1 - R} + \frac{R}{C_2 - R} + \frac{a}{R}$$

optimality condition

$$\frac{C_1}{(C_1 - R)^2} + \frac{C_2}{(C_2 - R)^2} = \frac{a}{(\bar{R} - y)^2}$$

ii) if $C_1 = C_2 = 100$

$$y = 0, R = \bar{R}$$

$$\frac{2 \cdot 100}{(100 - R)^2} = \frac{a}{R^2}$$

$$200R^2 = a(100 - R)^2$$

$$\sqrt{2}10R = \sqrt{a}(100 - R)$$

$$\sqrt{a} \geq \frac{\sqrt{2}10R}{100 - R} \Big|_{R=10} = \frac{\sqrt{2}100}{90}$$

5

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4(a)

Survivable fibre network architecture

- Protection switching: established pre-assigned replacement connection (no network management function)
- Re-Routing: establishment or replacement of connection (by a network management control connection)
- Self-healing: establishment of a replacement connection by network (no network management function)

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4(b)

Equivalent capacity is relevant to call admission control (CAC) schemes

- Two entirely different time scale issues (virtual cell and cell level)
- Lack of traffic descriptors may compromise potential effectiveness

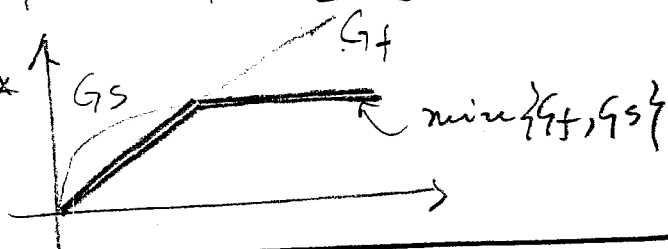
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$$G_x(m) = f(R_p, b, m, u, x)$$

R_p = peak rate, b = mean burst length,

u = utilisation, x = capacity of buffer

m = no. of vc

Two approximations C^* Fluid flow approx (G_f)Stationary approx (G_s)

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5(a) Routing Protocols in Internet
 IGP: relies on IP addresses to construct paths
 Examples:
 - Routing Information Protocol (RIP)
 - Open Shortest Path First (OSPF)
 EGP: relies on Autonomous System numbers to construct AS paths
 Examples
 - Border Gate Protocol (BGP v4)
 Discussion on above protocols

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(5) Intserv : discussion on
 - packet classifier
 - Packet Schedulers
 - Admission Control
 - Explicit Resource Reservation (RSVP)
 DiffServ : discussion on
 - Simpler model and more scalable than Intserv
 - per flow → aggregate service
 - complex processing from core to edge
 - Service level Agreement (SLA)
 - Per Hop Behaviour (PHB)
 - Traffic classification
 - Traffic conditioner

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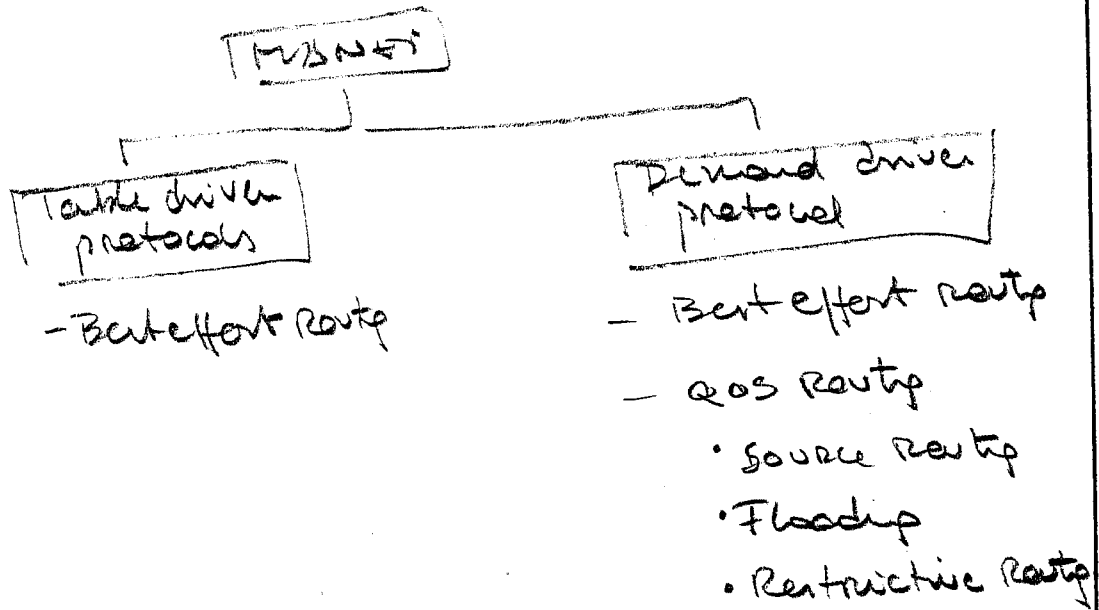
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Q.1) Routing protocols in Mobile Ad hoc network



Discussion on the above

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