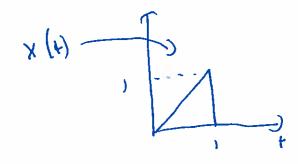
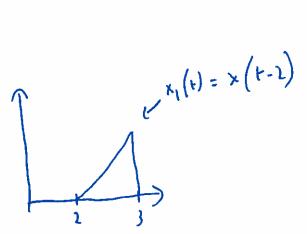
QUESTION 1

(6)



i.



ic.

$$y_{2}(t) = x(-2(t-2))$$
 $1 = x(-2(t-2))$
 $x_{2}(t)$
 $x_{2}(t)$

iii.

$$\frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) = \frac{1}$$

12

LET US CHECK LINEARITY

$$Y_{1}(t) \longrightarrow Y_{1}(t) = Y_{1}(t-2) + Y_{1}(2-t)$$

 $Y_{2}(t) \longrightarrow Y_{2}(t) = Y_{2}(t-2) + Y_{2}(2-t)$

HENCE UNFAR

LET US CHECK TIME-INVARIANCE

$$x_{1}(t) \rightarrow y_{1}(t) = x_{1}(t-2) + x_{1}(2-t)$$
 $x_{1}(t-t_{0}) = x_{2}(t) \rightarrow y_{2}(t) = x_{2}(t-2) + x_{2}(2-t)$
 $= x_{1}(t-t_{0}-2) + x_{2}(1-t-t_{0})$
 $\neq y_{1}(t-t_{0})$
 $\neq y_{1}(t-t_{0})$

NOTE THAT Y, (+-to) = 4, (+-to-2) +4, (2-++to)

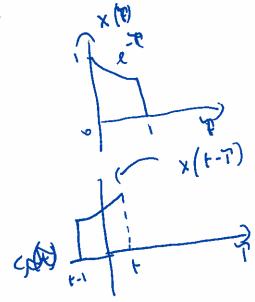
HENCE TIME-VARIANT

THE SYSTEM IS LIVEAR

LET US CHECK FOR TIME-INVANIANCE

HEHGE TIME -VARIANT

(c)



(1) + x(4) = (2) x(4) x(4-4) 1 (4 = 5) x(4) x(4-4) 0 < 4 = 1

(4) + x(4) = (50) (4) x(4-4) 0 < 4 = 1

(5) x(4) x(4-4) 0 < 4 = 1

(6) x(4) x(4-4) 0 < 4 = 1

(7) x(4) x(4-4) 0 < 4 = 1

(8) x(4) x(4-4) 0 < 4 = 1

(9) x(4) x(4) = (10) x(4) = 1

(10) x(4) x(4) x(4) = (10) x(4) = 1

(10) x(4) x(4) x(4) = (10) x(4) = 1

(10) x(4) x(4) x(4) = (10) x(4) = 1

(10) x(4) x(4) x(4) = (10) x(4) = 1

(10) x(4) x(4) x

$$\int_{0}^{t} x(\tau) x(t-\tau) d\tau = \int_{0}^{t} e^{-(\tau-\tau)} d\tau = f e^{-t} \cdot (t+2)$$

$$\int_{0}^{t} x(\tau) x(t-\tau) d\tau = \int_{0}^{t} e^{-(\tau-\tau)} d\tau = (t-\tau) \cdot (t+2)$$

$$\int_{0}^{t} x(\tau) x(\tau-\tau) d\tau = \int_{0}^{t} e^{-\tau} e^{-(\tau-\tau)} d\tau = (2-t)e^{-\tau} \cdot (t+2)$$

OF THE FT YEARDS:

$$Y(w) = X(w) e^{-jw} + X(-w) e^{-jw}$$

$$= \frac{1}{w^{2}} \left(1 - jw - e^{-jw} + (+jw - e^{-jw})\right)$$

$$= \frac{1}{w^{2}} \left(1 - e^{-jw} - e^{-jw}\right) e^{-jw}$$

$$= \frac{1}{w^{2}} \left(1 - e^{-jw}\right) e^{-jw}$$

CHARACTERISTIC POLYHONIAL

5244543

CHARA CTERISTIC ROOTS -1

S1,2 = -2 + \(\frac{4-3}{4-3} = \)

CHARACTERISTIC MODES

-t -3t

$$y(0) = c_1 + c_2 = 0$$

 $y(0) = -c_1 - 3c_2 = 2$
 $=0$
 $c_1 = 1$

HEW CE

iii.

$$(s^2 + 4s + 5)y(s) = y(s)$$

 $since y(s) = \frac{1}{s}$

WE HAVE THAT

USING COVENING METHON WE FIND THAT

$$y(6) = \frac{1}{35} - \frac{1}{2(541)} + \frac{1}{6(5+3)}$$

$$y(4) = (\frac{1}{3} - \frac{1}{2}x^{2} + \frac{1}{6}x^{2})u(4)$$

BELAUSE OF LINFAMITY

THE FOTAL ANSWER IS THE

SUN OF THE RESPONSES IN

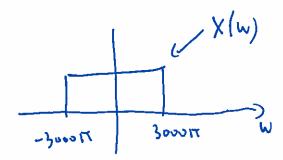
MART Ci. AND ICI. THAT IS

$$y_{\text{TOT}}(t) = (x^{-1} + y^{-1}) u(t) + (\frac{1}{3} - \frac{1}{2} + \frac{1}{6} + \frac{3}{6} + \frac{1}{6} + \frac{$$

$$=\left(\frac{1}{3}+\frac{1}{2}-\frac{5}{6}-\frac{3}{6}+\frac{1}{2}\right)u(t)$$

USING FOURIER TABLES

Ĺ



(;;)

(3)

$$\chi(1) = \frac{1}{2^{1}-5+1} = \frac{1}{2^{1}-5+1} = \frac{A}{1-1} + \frac{B}{1-1}$$

$$=\frac{5}{3}\frac{1}{1-4}-\frac{1}{3}\frac{1}{1-1}$$

HENCE

USING 1-TRAMSFORM TABLE WE GET

$$\times [-] = \left(\frac{2}{5}\right)(1)^{m} - \frac{2}{5}$$
 $u[m]$

IN STEADY STOTE THE INDUCTOR

IS A SHORT CIRCUIT AND THE (APACITOR

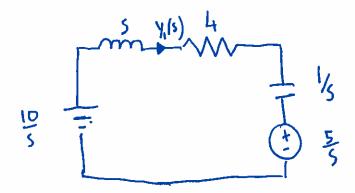
IS AN OPEN CIRCUIT

THEREFORE

$$V_{c}(o^{-}) = 0$$

$$V_{c}(o^{-}) = 5V$$

(b) THE EQUIVALENT CIRCUIT IN THE



THUS THE LOOP EQUATION IN THE LAVIDCE

$$1\frac{1}{5} = 5\frac{1}{5}$$
 $(5^{2} + 45 + 1) = 5$
 $(5^{2} + 45 + 1) = 5$

(c)
$$Y_1(s) = \frac{5}{5^2+45+1} = \frac{5}{(5+2-V_3)(5+2+V_3)} = \frac{5}{2V_3} \left(\frac{1}{5+2-V_3} - \frac{1}{5+2+V_3}\right)$$

USING THE FACT TAAT

$$e^{-\lambda t}$$
 $u(t)$ $=$ $\frac{1}{5+\lambda}$

$$y_1(t) = \frac{5}{2\sqrt{3}} \left(2 - (2-\sqrt{3})^{\frac{1}{2}} - 2 - (2+\sqrt{3})^{\frac{1}{2}} \right) u(t)$$

IF WE DENOTE WITH F(s) THE OUTPUT OF THE FEEDBACK SYSTEM WE HAVE THAT

$$Y(s) = (S+2) F(s)$$

$$F(s) = IL(X(s) - (S+a)^{2}F(s))$$

THE RE FORE

AND

THE TRANSFER FUNCTION IS:

$$H(s) = \frac{Y(s)}{Y(s)} = \frac{I((s+1))^2}{(1+I((s+a))^2)}$$

(b) USING FINAL VALUE THEOMEN
WE HAVE THAT

WE HAVE THAT

$$y(0) = lin \frac{5+2}{1+(5+0)^2} = \frac{2}{1+a^2}$$

(v) (.

$$= \frac{C}{5} + \frac{A54B}{5^2 + 25 + 2}$$

MULTIPLY BOTH SIDES BY S AND SET S=0

1:6

THEN MULTI PLY BOTH SIDES BY S AND LET 5-DOD

WE HAVE

$$\gamma(s) = \frac{1}{5} - \frac{5+1}{(5+1)^2+1}$$

USING LAPLACE TABLES WE OBTAIN

U.

THE GIVEN POINT ARE EITHEN LOCAL

HITINA ON LOCAL MAXIMATISCAVSF OF

THE TERM Let IN THE EXPRESSION

OF y(t).