Paper Number(s): ISE2.4

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL ELECTRONIC ENGINEERING EXAMINATIONS 2000

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COMMUNICATIONS 2

Tuesday, May 2 2000, 2:00 pm

There are 4 questions on this paper. Answer 3 questions.

Time allowed: 2:00 hours.

Examiner(s):Prof L.F. Turner

(1) A speech signal is to be sampled in preparation for analogue-to-digital conversion. The probability density function associated with the sampled process is as shown in Figure 1 and a 4-bit uniform quantizer is to be used. The quantizer has a step-size △ and the boundries of the quantization levels are as indicated in the figure. Derive from first principle an expression in terms of a, b and △ for the minimum quantization noise associated with the level bounded by the sample values -△ and 0. Use your expression to evaluate the numerical value of the quantization noise for the level. Also, use your derived expression to deduce the quantization noise in the situation in which the probability density function is constant within a level. Give your answer in terms of the quantization step size, △, and the probability that the sampled value will fall within the level.

[20]

(2) A speech signal S(t), can be represented in the short term by $S(t) = \sum_{i=1}^{N} a_i cos(w_i t + \phi_i)$. The signal is to be used to amplitude modulate a carrier and envelope detection is to be used at the receiver.

If ϕ_i , i=1,...,N, has a probability density function that is uniform over the range 0 to 2π and is zero elsewhere, determine as a function of the a_i 's the maximum percentage of the total transmitted power that can be placed in the side-frequencies (the sidebands) if distortion is to be avoided.

In a radio communication system a signal Q(t) is used to amplitude modulate a carrier and envelope detection is to be used.

If the signal reaches the receiver by two paths, a direct path and one which introduces an attenuation k and delay τ relative to the direct path, derive an expression for the output of the envelope detector.

[20]

- (3) Derive an expression for the signal-to-noise power ratio at the output of a detector in terms of the corresponding signal-to-noise power ratio at the input to detector for
 - (i) Double-Sideband Suppressed Carrier Amplitude Modulation (DSB-SC), and
 - (ii) Single-Sideband Suppressed Carrier Amplitude Modulation (SSB-SC).

If there are differences between your two results explain why you think this occurs.

From the point of view of signal-to-noise ratios, compare the overall performance of the DS SSB-SC and SSB-SC systems.

[20]

- (4) (i) Describe and compare the circuit, message and packet switched methods of communication.
 - Describe and compare three methods by which a number of individuals can access and use a communication channel simultaneously.
 - (iii) It is proposed to store data in groups of 4 information digits in computer memory and to protect each group of digits by using a Hamming (7,4) code.

The code is to be used for the purpose of DETECTING errors.

Derive an expression for the overall probability of undetected codeword error as a function of the digit error probability, P.

[20]

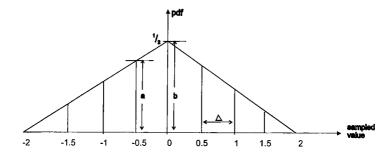


Figure 1

Solutions

mento

Q1. Consider the pdf within the quantization level as included in Fig 1 to question

noticalist in Fig. 1 the greshin.

1 a Lassigned quantiford level palue.

We have to determine the artimum position for V the assigned quantized value

Inse = $\int_{(x-v)^{2}P(x)}^{\Delta} dx$, where P(x) is the pof

of the sampled value

Now the odf has an agration P(x) = a + (b-a). X

hence the use due to quantization is

$$\int_{0}^{\Delta} (x-V)^{2} Rx/dx = \int_{0}^{\Delta} (x-V)^{2} \left[a + \left(\frac{b-a}{a} \right) x \right] dx$$

 $= \iint_{0}^{\sqrt{a}} x^{2} - 2aV_{x} + aV^{2} + (6-a)x^{3} - 2(6-a)V_{x}^{2} + (6-a)V_{x}^{2} + \sqrt{a}V_{x}^{2} = \sqrt{a}V_{x}^{2} + \sqrt{a}V_{x}^{2} + \sqrt{a}V_{x}^{2} = \sqrt{a}V_{x}^{2} + \sqrt{$

 $MSG = \frac{a \Delta^{3}}{3} - 2aV \frac{\Delta^{2}}{2} + aV^{2} + \left(\frac{b-a}{\Delta}\right) \frac{\Delta^{4}}{4} - 2\left(\frac{b-a}{\Delta}\right) \frac{\lambda^{3}}{3} + \left(\frac{5-a}{\Delta}\right) V^{2} \frac{\lambda^{2}}{2}$ This has the minimized by choice of position for V d(mse) = 0 yelds minim which is $-a\Delta^{2} + 2a\Delta \cdot v + (b-a)\Delta \cdot v - 2(b-a)\Delta^{2} = 0$ 3 - ad + 2a V + (6-a) V - 2 (6-a) 0 = 0 Som which we get-NA. This is an essential part of the question and the assumption, board on a uniform/constant part that V = B12 will not be accepted. Now the quantisation noise power No = me for the bevel is Blamed by substituing for V in equation 1, using the result given in 25 2. If we do this we then Blais

Now () which can be re-author as Ng = (a+36).13- (a+26) 12. V + (a+6) 1 12 m substituting for V = (9+26).A hermes Ng = (9+36) 13-(9+26) 253+(9+6) (9+26) 203 9(9+6) 18(9+6)2 6 Ng = 5 (9+36) (3 + (9+36) 2 3 / - (3) Numeral value 1Ng: D=1/2; a=3/2, b=1/2 which are to / Now if the post is constant without a level a=6 and hence Ng 45me smylpen to $\left(\frac{a}{3} - \frac{9a^2}{36a}\right) 1^3 = \frac{a}{12} \cdot 1^3 = \left(\frac{a4}{12}\right) \cdot 1^2 = \frac{a \cdot 4}{12}$ So the grantzation note in this case become P. 5 Where R = a D is the publish of the Saughed Value falling in level L. muck out ? 22

Since encelipe delection is to be und the transmitted signis has to be of the four Mt)= A/1+ m sto)/65w/-, when An the amplitude of the corner and me is the modulation under. In order to avoid distatus in sity must never be made day negative than -1. Now said the dis are random, in well to ensure that the above condition is satisfied it follows that Since it is possible for SIE to have a maximum negative value (-(q+-+an) and hence we have to select in so that Now the carrier power is A2 and the anything of the side fragmen at \$(w + wi) and mai

and the amplitude of the count (No-Wi) and main and want

It follows that the ponen in sidefrequenty at we two in magin p and at w-w is man AZ To the What power in the side proguence is Em2 q2/4 A2 is Sideband Power M2 (92+-+9N2) A and the total hanculat power is 12 + m2 Sq2+ To pomen in the side progression m 2 912. A2 M 2 (5 q 2)

1+ m 2 m 2

2 4 121 $\frac{A^{2}+\frac{m^{2}A^{2}}{4}}{\frac{2}{4}} = \frac{n^{2}A^{2}}{\frac{2}{4}} = \frac{n^{2}A^{2}}{\frac{2}{4}}$ But m= 1 So we have to knew

912 The transmilled signist is · A[Hma(t)] asuct and the received signal is R(t)= A[I+ malt] wsw.l-HA/1+m a(6-0)]4500(6-0) = Ali+m Q(+)] GS W. + + + A [i+m Q(+-r)] Gos W. Cont + KASI+mall--C/]sin arsinul-= { A[1+ an a(+)] + kA[1+ an a(-)] wsw.t } (65 a) (-+ { KA [HM Q (6-2)]sin yz.}sin we and the organ from the envelope delecter will be have heavy, por-linear distriture introduced

(hunh out / 20

Expression for (S/N) out as function of (S/N) in DSB-50 The received signal and more is Sty GSW + + MH = SIT GSW+ + X(t) / LOW - - XSty singl-The recover signis power is (SIE) 65 4 = 1/2 SET and the received mice power = N (S/N) N = 1/2 Sity/N After danished and Inopus filtering we get at the Styles wet + XIHONET - XIH Sin at + Howel is hich is los pur filter have only = \$ 25 25. こもらけ ナセメント - (5/N) on t = 1/4 sits/14 xxt) = Have (S/N) out = 2 (S/N) /N 55B-56

Received signil = 5(5) 60 mg 6 - 5(175 in mg (-+ n)ty

- 7-15 kin mg 6 + x1+16 mg (-= Ithank-govsnigt + xltumil-

•

hept Signil Ponen = (SITIGNEE-SET)SINGE) = 1/2 50) + 1/2 566 But suit Stoy is suity Sty Hilbert Transford 5(4) = 5(4) " hapt signil power = Sity Name pour = N : (5/N) N = Sit// After Demodulater and filtery we obtain at autput \$517 + 2 Xelty Hence (S/N) out = 1/4 str/14 xxx) 1. (5/N) out = (5/N) M. Part 2 The reason for the 3dB gain with DS13-SC is that signit side fragme symmetral an a tur site of cames at on a Maye basis, but the noise Component, bring of random phose, add on a pome bain is 3dB gain 12

It a pears that DSB-SC is beller. This is in fact, so in so far as perference of detection is concerned but

If we send the same power (signil more) in

the two caas then 5/4/ =

the right to the delector

Homener, With SSIS only half the bandwallh is involved as compared in the DSB and homes

we have that

(5/N),N = 1/2 (5/N)/N/SSB

" after demodulate /delection the 6/h) out 35B

= 2 (5/N)/M = 2 x 1/2 (5/N)/M = (5/N)/M = (5/N)/M = (5583.

S/X wie the two systems areall, are the

Mark art 8 20

lant-1. This is lace of lost known and lectime notes. l'ergel points such as the following to be made Civaint- Switching (CS) Dedicated link for duration of section (ii) below in setting up session (iii) Small delay's once session established (iv) Inefficient nee of channel capacity sind link held even when 'sitence' cexists chang session (not good for burst-ligne date) Medage Sustituy (MS) (1) Long message are passed from strage / sonting cashed to strage / sonting centre. (ii) Link only held during period when data acting - here high capacity allegation (iii) Delays can be long due to quewing and recent to recent complete message before hunding (iv) Small To overhead (address into sto) Parkt Smithy (PS) (i) Message bother down into smaller pulls (11) again link my med when puchet to be sent (ii) analoush greater than MS
(iv) Halays loss than MS, but greater ham (5) Part 2

I erget a description and discussion of

(i) FDMA

(ii) TDMA

(41) CDMA - coole division multiple access.

The Hamming (7,4) coole has three check digit Gara which are computed from the four informations digits using the following parity theck equalion

I,+I2+I3 FC, E1+F2+ I4=62 I,+ I3+I4= C3

The complete set of works wants are I, I, I, I, I, C, C, C3

> 0000 1000 0100 11

11 0 0 00 00 1 0 \$.0

1010 0 / 011 0

1110 10

000 1 1001

0101 10

1101 01

00 11 00

00

Now the only even 1 terms that will not be delected are those that are in put equal to will work.

Sx amination the cet f who would show that 6 we have 7 wight 3 who would,

7 weight 4 when and \$1 (me) wight 7 will would.

So Pe = 7 P(1-p) + 7 P4(1-p) 3 + P7

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