

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2007** 

MSc and EEE PART IV: MEng and ACGI

Corrected Copy

#### RADIO FREQUENCY ELECTRONICS

Wednesday, 25 April 10:00 am

Time allowed: 3:00 hours

There are SIX questions on this paper.

Answer FOUR questions.

All questions carry equal marks

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible

First Marker(s):

S. Lucyszyn

Second Marker(s): E. Rodriguez-Villegas

Special instructions for invigilators: This is a Closed Book examination. A Smith Chart is to be distributed.

Information for candidates:

This is a Closed Book examination.

A Smith Chart is provided and, if used, you must attach this to your answer book.

1.

a) The Michelson interferometer, shown in Figure 1.1, can be analysed as a general two-port network. By inspection of Figure 1.1, write down equations for the effective forward voltage wave transmission coefficient ( $S_{21}$ ) and input voltage wave reflection coefficient ( $S_{11}$ ) for this passive and reciprocal network. Clearly define all variables used. Hints, the electrical path lengths can be represented by ( $k_o dx$ ), where  $k_o = 2\pi/\lambda$ ,  $\lambda$  is the wavelength for a monochromatic input source, x is the designation of a particular path and the beam splitter is both symmetrical and reciprocal.

[6]

b) Given that the optical path difference is given by  $\delta = 2(d3 - d4)$ , if  $d1 = d2 = \lambda$  and both mirrors are made from perfectly conducting metals, simplify the equations obtained in 1(a).

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- c) For this interferometer to function properly, an ideal beam splitter must reflect 50% of any incident power and allow the rest of the power to be transmitted through without attenuation.
  - Write down the effective forward voltage wave transmission and forward voltage wave reflection coefficients for an ideal beam splitter, given that they must be in phase quadrature with one another. Hint, there are a number of possible solutions, so only choose one.

[4]

ii) From the solution obtained in 1(c)(i), show that the beam splitter obeys the conservation of energy principle.

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iii) Using the solution obtained in 1(c)(i), simplify the equations obtained in 1(b).

[2]

iv) From the solution obtained in 1(c)(iii), show that this Michelson interferometer obeys the conservation of energy principle for  $\delta = n\lambda$  and  $(n+1/2)\lambda$ , where n is any positive integer.

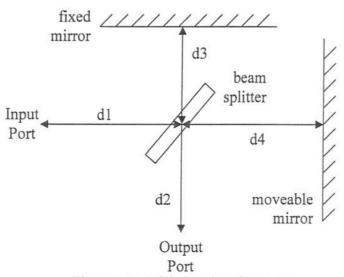


Figure 1.1A Michelson interferometer

- 2.
- a) Draw the circuit diagram of a simple class-A amplifier, having ideal components and describe clearly the function of each component. Describe the performance characteristics of a class-A RF power amplifier and state its applications.

[6]

b) Consider a 4 x 75 μm FET with the following specifications:

$$V_{gd|BD}$$
 = 12 V  
 $V_p$  = -1.5 V  
 $V_k$  = 0.5 V  
 $I_{dss}$  = 60 mA  
Small-Signal Power Gain = 4 dB

All variables have their usual meaning

Calculate the following for delivering the maximum linear output power:

i) Optimal bias voltages. [2] ii) Optimal load impedance. [2] iii) Values of maximum linear output power and peak output power. [2] iv) DC power and power dissipated per unit gate width. [3] v) Drain efficiency and power-added efficiency. [2] c) Explain the Cripps technique for impedance matching of power amplifiers. [3]

- 3.
- a) Using a signal flow graph or otherwise, derive an expression for the input voltage wave reflection coefficient for a 2-port network that is terminated with a load impedance  $Z_L$ .

[5]

b) From the expression derived in 3(a), describe how stability circles can be created on the Smith chart. What does this stability circle represent when it encompasses the impedance matched, z<sub>o</sub>, point on the Smith chart and when it does not encompass this point?

[5]

c) Given a 2-port network with the following S-parameters:

$$[S] = \begin{bmatrix} 0.5 & 0.5 \\ 10 & 0.5 \end{bmatrix} \tag{3.1}$$

What is the input voltage wave reflection coefficient if the output port is terminated with a load impedance  $Z_L = -5 \Omega$  and a reference impedance  $Z_0 = 50 \Omega$ ?

[5]

d) For the 2-port network given in 3(c) the Rollett's stability factor is 2.3. Comment on the apparent contradiction between the Rollett's stability factor and the input voltage wave reflection coefficient found in 3(c). What is the maximum gain that can be achieved with a passive load impedance termination?

[5]

- 4.
- a) What are the levels of insertion loss and return loss at the -3 dB cut-off frequency for a lossless filter? You are asked to design a filter with a maximum pass band return loss level of -6.868 dB. What will be the worst-case pass band insertion loss ripple for a lossless filter?

[5]

b) Using the worst-case pass band insertion loss level calculated in 3(a), design a lumpedelement L-C band stop filter to meet the following specifications:

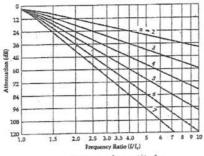
Lower pass band -3 dB cut-off frequency:	540 MHz
Upper pass band -3 dB cut-off frequency:	660 MHz
Stop band bandwidth:	60 MHz
Band stop attenuation:	> 45 dB
Source impedance, Zs:	50 Ω
Load impedance, $Z_L$ :	$100 \Omega$

[10]

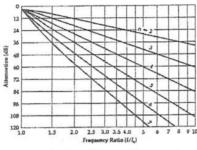
c) Define group delay and explain the general relationship between its frequency response and that of sharp cut-off insertion loss characteristics.

[5]

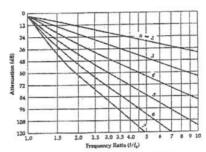
## Filter tables



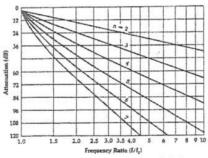
Attenuation characteristics for Butterworth filters.



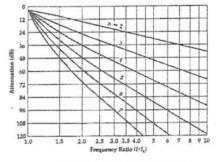
Attenuation characteristics for a Chebyshev filter with 0.01-dB ripple.



Attenuation characteristics for a Chebyshev filter with 0.1-dB ripple.

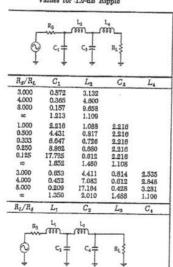


Attenuation characteristics for a Chebyshev filter with 0.5-dB ripple.



Attenuation characteristics for a Chebyshev filter with 1-dB ripple.

Chebyshev Low-Pass Prototype Element Values for 1.0-dB Ripple



		6	) C <sub>1</sub>	C; + C;	C, _	RL		
n	$R_8/R_L$	C <sub>1</sub>	L <sub>2</sub>	C <sub>3</sub>	L <sub>4</sub>	<b>↓</b> C <sub>5</sub>	Lq	C,
5	1.000 0.500 0.333 0.250 0.125	2.207 4.414 5.622 8.829 17.657 1.721	1.128 0.565 0.376 0.282 0.141 1.845	3.103 4.653 6.205 7.756 13.961 2.061	1.128 1.128 1.128 1.128 1.128 1.128 1.493	2.207 2.207 2.207 2.207 2.207 1.103		
6	3,000 4,000 8,000 &	0.679 0.481 0.227 1.378	3.873 5.644 12.310 2.097	0.771 0.476 0.198 1.890	4.711 7.351 16.740 2.074	0.969 0.849 0.726 1,494	2.406 2.582 2.800 1.102	
7	1.000 0.500 0.333 0.250 0.125	2.204 4.408 6.612 8.815 17.631 1.741	1.131 0.568 0.377 0.283 0.141 1.677	3.147 5.293 9.441 12.588 25.175 2.155	1.194 0.895 0.798 0.747 0.671 1.703	3.147 3.147 3.147 3.147 3.147 2.079	1.131 1.131 1.131 1.131 1.131 1.494	2.204 2.204 2.204 2.204 2.204 1.102
n	$R_L/R_s$	$L_1$	C <sub>2</sub>	L <sub>3</sub>	C <sub>4</sub>	L <sub>8</sub>	C <sub>8</sub>	L <sub>7</sub>
	10/4		R <sub>5</sub> L <sub>1</sub>		r m	78	U <sub>8</sub>	Lī

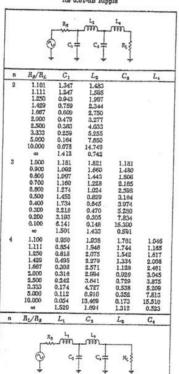
Butterworth Low-Pass Prototype Element Values

		€ c'	[ c, ]	R	
n	$R_g/R_L$	C,	Lo	C <sub>2</sub>	L,
2	1.111 1.250 1.429 1.667 2.000 2.500 3.333 5.000 10.000	1.035 0.846 0.697 0.566 0.448 0.342 0.245 0.156 0.074 1.414	1.835 2.121 2.439 2.828 3.346 4.095 5.313 7.707 14.814 0.707		
3	0.900 0.600 0.700 0.600 0.500 0.400 0.300 0.200 0.100	0.808 0.844 0.915 1.023 1.181 1.425 1.838 2.669 5.167 1.500	1.833 1.384 1.165 0.985 0.779 0.604 0.440 0.284 0.138 1.333	1.599 1.928 2.277 2.702 3.261 4.004 5.363 7.910 15.455 0.500	
4	1.111 1.250 1.429 1.867 2.000 2.500 3.333 5.000 10.000	0.466 0.388 0.325 0.269 0.218 0.169 0.124 0.080 0.039 1.531	1,592 1,695 1,862 2,103 2,452 2,986 3,883 5,684 11,094 1,577	1.744 1.511 1.291 1.062 0.363 0.691 0.507 0.331 0.162 1.082	1.489 1.811 2.175 2.013 3.187 4.000 5.336 7.940 15.642 0.383
л	$R_L/R_S$	L <sub>1</sub>	C <sub>2</sub>	La	C,
	₽. R.S	c' - 	- c+	R <sub>L</sub> §	

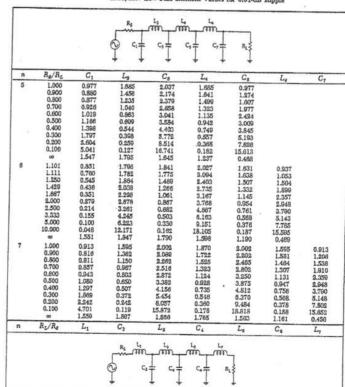
Butterworth Low-Pass Prototype Element Values

73	$R_R/R_L$	C <sub>1</sub>	La	C <sub>a</sub>	L,	C <sub>s</sub>	Lo	C <sub>7</sub>
5	0.900 0.800 0.700 0.500 0.500 0.400 0.300 0.200 0.100	0.442 0.470 0.517 0.586 0.886 0.838 1.094 1.608 3.512 1.545	1.027 0.886 0.731 0.609 0.496 0.388 0.285 0.186 0.091	1.910 2.061 2.285 2.600 3.051 3.736 4.884 7.185 14.095 1.382	1.756 1.544 1.333 1.126 0.924 0.727 0.537 0.352 0.173 0.894	1.389 1.738 2.108 2.552 3.133 3.965 5.307 7.935 18.710 0.309		
Ð	1.111 1.250 1.429 1.667 2.000 5.500 3.333 5.000 10.000	0.289 0.245 0.207 0.173 0.141 0.111 0.082 0.054 0.028 1.553	1.040 1.116 1.236 1.407 1.653 2.028 2.656 3.917 7.705 1.759	1.392 1.128 0.957 0.801 0.654 0.514 0.379 0.248 0.132 1.553	2.054 2.239 2.499 2.858 3.369 4.141 5.423 8.020 15.786 1.202	1,744 1,550 1,348 1,143 0,942 0,745 0,552 0,363 0,179 0,758	1.335 1.688 2.062 2.509 3.094 3.931 5.280 7.922 15.738 0.259	
'	0.800 0.700 0.700 0.600 0.500 0.400 0.300 0.200 0.100	0.299 0.322 0.357 0.408 0.480 0.590 0.775 1.145 2.257 1.558	0.711 0.606 0.515 0.432 0.354 0.278 0.206 0.135 0.067 1.799	1.404 1.517 1.688 1.928 2.273 2.795 3.671 5.427 10.700 1.659	1.489 1.278 1.091 0.917 0.751 0.592 0.437 0.287 0.142 1.397	2.125 2.334 2.618 3.005 3.553 4.380 5.761 8.526 16.822 1.055	1.727 1.546 1.350 1.150 0.951 0.754 0.500 0.369 0.182 0.656	1.296 1.652 2.028 2.477 3.064 3.904 5.258 7.298 15.748 0.223
	$R_L/R_g$	$L_1$	Ca	L <sub>3</sub>	C,	L	C.	L

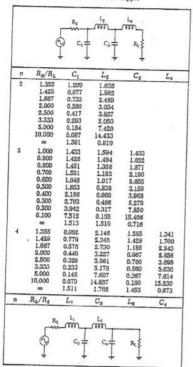
Chebyshev Low-Pass Element Values for 0.01-dB Ripple



Chebyshev Low-Pass Element Values for 0.01-dB Ripple



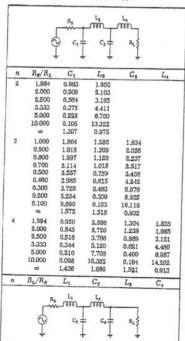
Chebyshev Low-Pass Prototype Element Values for 0.1-dB Ripple



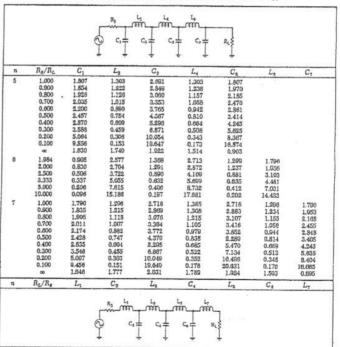
Chebyshev Low-Pass Prototype Element Values for 0.1-dB Ripple

n	$R_s/R_z$	C,	L <sub>2</sub>	C <sub>3</sub>	L <sub>4</sub>	C <sub>5</sub>	La	C <sub>1</sub>
5	1.000	1.301	1.556 1.433	2.241 2.360	1.556 1.488	1.301		07
	0.800	1.300	1.282	2.582	1.382	1.488		
	0.700	1.358	1.117	2.868	1.244	2.062		
	0.800	1.470	0.947	3,269	1.085	2.484		
	0.500	1.654	0.778	3.845	0.913	3,055		
	0.300	1.954 2.477	0.612	4.720 6.196	0.733	3,886		
	0.200	3,546	0.295	9.127	0.550	5.237 7.889		
	0.100	6.787	0.115	17,957	0.182	15.745		
	00	1.561	1.807	1.706	1.417	0.651		
	1.355	0.942	2.080	1.659	2.247	1.534	1.277	
	1.429	0.735	2.249	1.454	2.544	1.405	1.629	
	1.687 2.000	0.542	2.600	1.183	3.064	1.185	2.174	
	2.500	0.310	3.068	0.958	3.712	0.979	2.794	
	3.333	0.220	4.927	0.749	4.651 6.195	0.778	3.645	
	5,000	0.139	7.250	0.361	9.261	0.384	4.996 7.618	
	10.000	0.067	14,220	0.178	18.427	0.190	15,350	
	00	1.534	1,884	1.831	1.749	1.394	0.838	
	0.900	1.282	1.520	2.239	1.680	2.239	1.520	1.262
	0.800	1.242 1.255	1.395	2.361	1.578	2.397	1.459	1,447
	0.700	1.310	1.083	2.548	1.443	2.624	1.362	1.697
	0.600	1.417	0.917	3.205	1.209	3.384	1.233	2.021
	0.500	1.595	0.753	3.764	0.928	4.015	0.914	3.018
	0.400	1,885	0.593	4.618	0.742	4.970	0.738	3.855
	0.300	2.392	0.437	6.054	0.556	8.569	0.557	5.217
	0.100	8.570	0.141	8.937 17.603	0.360	9.770 19.376	0.372	7.890
	00	1.575	1.858	1.921	1.827	1.734	0.188	0.631
	$H_L/R_0$	L <sub>1</sub>	C <sub>2</sub>	L <sub>3</sub>	C,	L <sub>5</sub>	C.	L <sub>7</sub>

Chebyshev Low-Pass Prototype Element Values for 0.5-dB Ripple



Chebyshev Low-Pass Prototype Element Values for 0.5-dB Ripple



5.

a) Draw the topology of a double-balanced amplifier: If 3 dB quadrature couplers are used in conjunction with identical non-ideal single-ended amplifiers, use S-parameter analysis to determine expressions for the overall insertion gain and input return loss. Assume the couplers are perfectly matched to the reference impedance, Zo, and the interconnections between the main components are ideal.

[10]

b) For the topology in 5(a), if the working single-ended amplifiers have a forward voltage wave transmission coefficient of  $S_{2l} = |10| \angle 35^{\circ}$ , determine the overall insertion gain and input return loss if one of the amplifiers fails, such that  $S_{2l} = 0$ . Assume that there is no change in the input or output impedances of the failed transistor. What is the main application of this topology and what are its advantages and disadvantages when compared to a single-ended amplifier?

[10]

- 6. A 500 MHz small-signal amplifier has an output impedance of 20 j 15  $\Omega$ . Using the Smith charts provided, design suitable impedance matching networks to transform this impedance to 50  $\Omega$ .
  - a) using a quarter-wavelength transformer

[3]

b) using a short-circuit stub

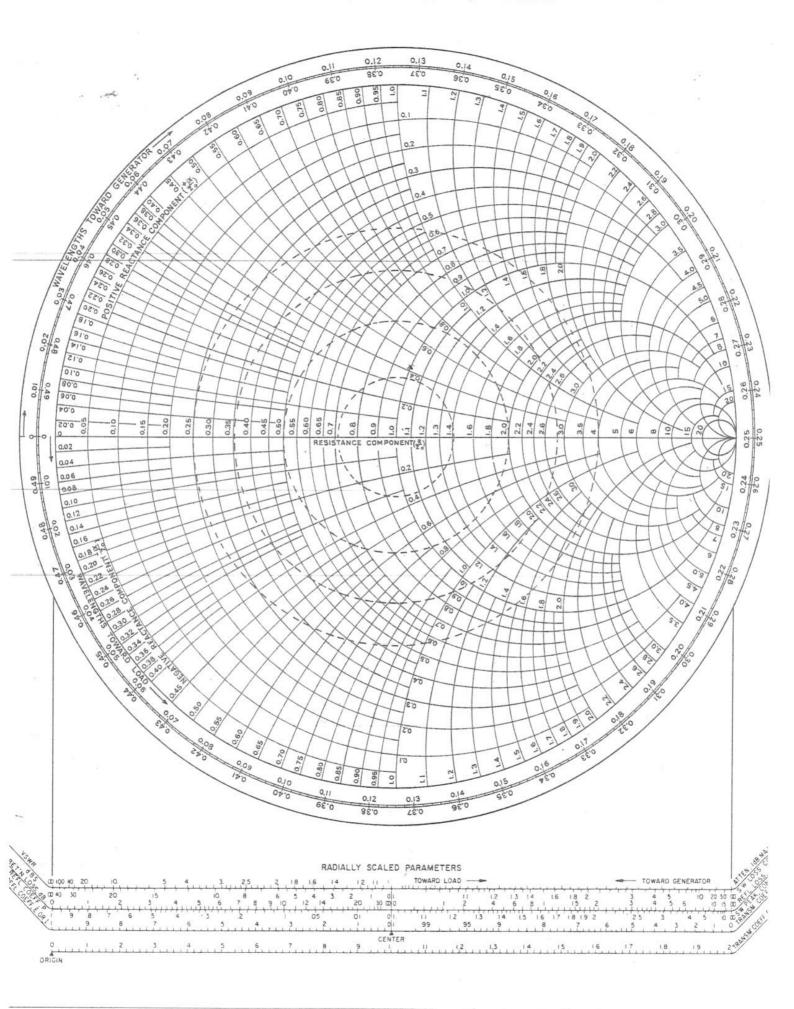
[8]

c) using a discrete inductor and capacitor

[6]

d) make general comments about the loaded-Q factor of the matching networks in 6(a),

(b) and (c) and how this relates to the resulting bandwidth of the networks.



# The Solutions for E4.18 (2007)

A06

# Model answer to Q 1(a): New Application of Theory

The effective input voltage wave transmission coefficient is given by:

$$S_{21} = \exp(-jk_o d1)\rho_s \exp(-jk_o d3)\rho_m \exp(-jk_o d3)\tau_s \exp(-jk_o d2)$$
$$+ \exp(-jk_o d1)\tau_s \exp(-jk_o d4)\rho_m \exp(-jk_o d4)\rho_s \exp(-jk_o d2)$$

 $\rho_s$  = voltage wave reflection coefficient of the beam splitter

 $\tau_s$  = voltage wave transmission coefficient of the beam splitter

 $\rho_m$  = voltage wave reflection coefficient of a mirror

$$S_{11} = \exp(-jk_o d1)\rho_s \exp(-jk_o d3)\rho_m \exp(-jk_o d3)\rho_s$$
  
+ \exp(-jk\_o d1)\tau\_s \exp(-jk\_o d4)\rho\_m \exp(-jk\_o d4)\tau\_s

# Model answer to Q 1(b): New Application of Theory

Given:

$$d1 = d2 = \lambda$$
 :  $\exp(-jk_ad1) = \exp(-jk_ad2) = \exp(-j2\pi) = 1$ 

And the mirrors are made from perfectly conducting metal,  $\therefore \rho_m = -1$ 

$$S_{21} = -\rho_s \tau_s [\exp(-j2k_o d3) + \exp(-j2k_o d4)]$$

$$S_{11} = -\rho_s^2 \exp(-j2k_o d3) - \tau_s^2 \exp(-j2k_o d4)$$
[3]

## Model answer to Q 1(c): New Application of Theory

(i) Since 50% of the power is reflected and 50% is transmitted through the ideal beam splitter then it must have the following solutions for its forward voltage wave transmission coefficient and input voltage wave reflection coefficient:

$$\tau_s = \rho_s \exp(\pm j\pi/2) = \frac{\exp[j(\angle \rho_s \pm \pi/2)]}{\sqrt{2}}$$
 e.g.  $\tau_s = \pm \frac{j}{\sqrt{2}}$ 

$$\rho_s = \tau_s \exp(\pm j\pi/2) = \frac{\exp[j(\angle \tau_s \pm \pi/2)]}{\sqrt{2}} \quad e.g. \ \rho_s = \pm \frac{1}{\sqrt{2}}$$

(ii) For a lossless 2-port network, the beam splitter must satisfy the following in order to obey the conservation of energy principle:

$$\left|\tau_{s}\right|^{2}+\left|\rho_{s}\right|^{2}=1$$
 and this is confirmed!

[2]

[4]

[6]

$$S_{21} = \pm \frac{j}{2} \exp(-j2k_o d3)[1 + \exp(+jk_o \delta)]$$

$$S_{11} = \pm \frac{1}{2} \exp(-j2k_o d3)[1 - \exp(+jk_o \delta)]$$

[2]

(iv) For a lossless 2-port network, the interferometer must satisfy the following in order to obey the conservation of energy principle:

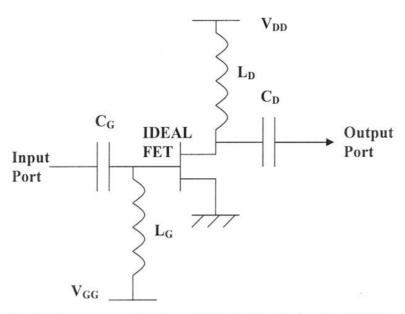
 $|S_{21}|^2 + |S_{11}|^2 = 1$  and this is confirmed, since:

$$|S_{21}| = 1$$
 and  $|S_{11}| = 0$  when  $\delta = n\lambda$ 

$$|S_{21}| = 0$$
 and  $|S_{11}| = 1$  when  $\delta = (n+1/2)\lambda$ 

#### Model answer to Q 2(a): Bookwork

The topology for a class-A amplifier is given below:



 $L_{\text{D}}$  and  $L_{\text{G}}$  are Radio Frequency Chokes (RFCs), ideally having infinite inductance.  $C_{\text{D}}$  and  $C_{\text{G}}$  are DC blocking capacitors, ideally having infinite capacitance. Since the field-effect transistor is also ideal, there is no need for any impedance matching networks. In practice, all these inductors and capacitors will be finite in value and lossy. They may also be absorbed into any impedance matching networks.

The class-A amplifiers have the following characteristics, when compared to other classes:

- Output current flows for the full period of the input voltage cycle.
- No high order harmonics are generated and, therefore, minimum output signal distortion (in the time-domain) is found.
- This gives the best Pout to Pin linearity.
- Maximum dynamic range.
- Ideal for non-CW applications (e.g. AM, multi-carrier and band-filtered CW modulated signals).
- Continuously dissipates power (as heat), even when there is no input signal.
- Low theoretical efficiency (<50%) and, therefore, it can get hot without cooling.

[6]

Model answer to Q 2(b): Computed Example

(i)

$$Vds \mid_{\text{max}} = Vgd \mid_{BD} - |Vp| = 10.5V$$
$$\therefore Vdd = \frac{Vds \mid_{\text{max}} - Vk}{2} = 5.5V$$

[2]

(ii)
$$R_L = \frac{Vds \mid_{\text{max}} -Vk}{Idss} = 167\Omega$$

[2]

$$P_{OUT|MAXLIN} = \frac{\left(\frac{Vds \mid_{\max} - Vk}{2\sqrt{2}}\right)^2}{R_L} = 75mW = +19dBm$$

$$P_{OUT|PEAK} = 2P_{OUT|MAXLIN} = 150mW = +22dBm$$

[2]

(iv)

$$\begin{split} P_{DC} &= Ids \mid_{Q} Vds \mid_{Q} = \frac{Idss}{2} Vdd = 165mW \\ Pin &= \frac{Pout}{G} = \frac{75mW}{2.51} = 30mW = +14.75dBm \end{split}$$

$$\therefore P_{DISS} = (Pin + P_{DC}) - Pout = 120mW$$

but, 
$$Wg = 4 \times 75 \mu m = 300 \mu m$$

$$\therefore \frac{P_{DISS}}{Wg} = 0.4W / mm$$

[3]

(v)

$$\eta_{DRAIN} = \frac{Pout}{P_{DC}} = 45\%$$

$$\eta_{ADD} = \frac{Pout}{P_{DC}} \left( 1 - \frac{1}{G} \right) = 27\%$$

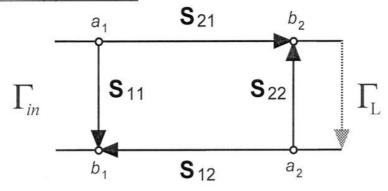
[2]

#### Model answer to Q 2(c): Bookwork

Cripps Technique assumes that the optimal load resistance is identical to that calculated using the I-V characteristics of the transistor and that the optimal load reactance is the conjugate of the FET's small- or large-signal output reactance (since Cds is not a strong function of the input power level).

The input stage is then matched to the complex conjugate of the resulting input impedance of the FET (having the optimal load impedance at its output), using the resulting linear S-parameters at the  $P_{OUT|MAXLIN}$  point.

#### Model answer to Q 3(a): Bookwork



Flow graph representation of a device with output load termination

Using Mason's non-touching loop rule it can easily be shown that:

$$\Gamma_{in} = S_{11} + \frac{S_{21}S_{12}\Gamma_L}{1 - S_{22}\Gamma_L}$$

where, 
$$\Gamma_L = \frac{Z_L - Z_O}{Z_L + Z_O}$$

[5]

#### Model answer to Q 3(b): Bookwork

Conditional stability occurs when the magnitude of the input voltage wave reflection coefficient is equal to or greater than unity. Therefore, the stability circle for the terminating impedance can be determined by equating the expression in 3(a) to unity. When the circle encompasses the matched impedance, zo, point then when the terminating impedance's voltage wave reflection coefficient is inside the circle this corresponds to conditional stability and instability outside the circle. Conversely, the opposite is true when the stability circle does not encompass the zo point.

[5]

# Model answer to Q 3(c): Computed Example

$$\Gamma_{\rm I}$$
 = -1.222 and therefore  $\Gamma_{\rm IN}$  = -3.3

[5]

#### Model answer to Q 3(d): Computed Example

A Rollett's stability factor of K = 2.3 is greater than unity and, therefore, it would normally represent an unconditionally stable circuit. However, since the magnitude of the reflection coefficient of the load is greater than unity then the circuit is now unstable.

When K is greater than unity (and the magnitudes of  $S_{11}$  and  $S_{22}$  are both less than unity), the device is unconditionally stable and the maximum gain that can be achieved is called the maximum available gain (MAG), given by:

MAG = 
$$\left| \frac{S_{21}}{S_{12}} \right| \left( K - \sqrt{K^2 - 1} \right) = 4.575 = 6.6 \text{ dB}$$

[5]

# Model answer to Q 4(a): Lecture Discussions

From the conservation of energy, for a lossless tow-port network:  $|S21|^2 = 1 - |S11|^2$ 

At the -3 dB cut-off frequency,  $|S21|^2 = 0.5$  and, therefore,  $|S11|^2 = 0.5$  In other words both the insertion loss and return loss levels are -3 dB.

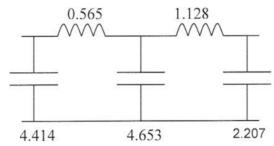
For a maximum return loss level or –6.868 dB, the worst-case insertion loss level is 1 dB.

[5]

## Model answer to Q 4(b): New Application of Theory

-3 dB cut-off frequencies are at  $f_{P1}$  = 540 MHz and  $f_{P2}$  = 660 MHz centre frequency, fo =  $\sqrt{(f_{P1} f_{P2})}$  pass band bandwidth, Bp =  $f_{P1}$ -  $f_{P2}$  = 120 MHz stop band bandwidth, Bs = 60 MHz f/fc = Bp/Bs = 2

From the attenuation curves, the  $5^{th}$  order 1 dB ripple Chebyshev filter with Rs/R<sub>L</sub> = 0.5 meets the specification with a stop band attenuation margin of 3 dB. The normalised values for the low-pass prototype is given below:

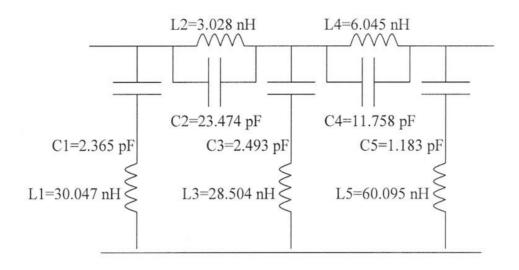


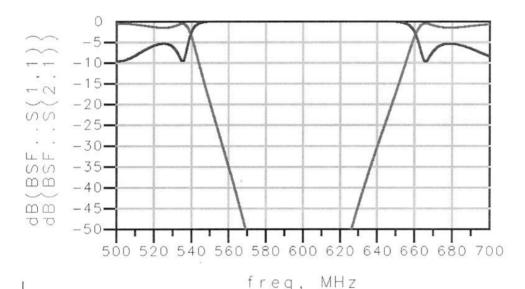
For a band stop filter, the capacitors are replaced by a series L-C resonators and the inductors are replaced by parallel L-C resonators. The un-normalized shunt connected series tuned circuit element values are:

$$Cs = \frac{BpCn}{2\pi f_0^2 R_L}$$
 and  $Ls = \frac{R_L}{2\pi BpL_n}$ 

The un-normalized series connected parallel tuned circuit element values are:

$$Cp = \frac{1}{2\pi BpCnR_L}$$
 and  $Lp = \frac{BpLnR_L}{2\pi f_o^2}$ 





The slight deviations in pass band levels are due to rounding errors in the component values (3 decimal places).

## Model answer to Q 4(c): Lecture Discussions

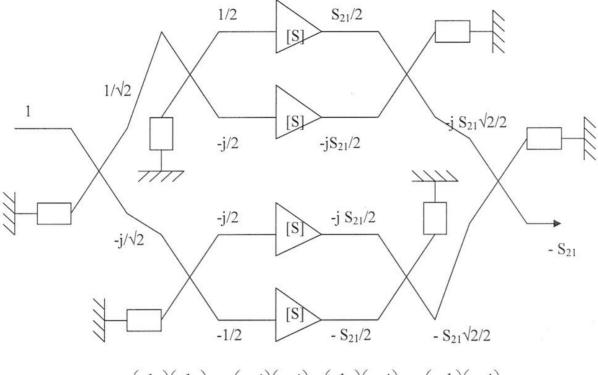
Group delay is defined as  $\tau = -\partial \angle S21/\partial \omega$ 

With sharp cut-off frequencies, high order filters are needed. This means that there are large numbers of passive filter components, where electromagnetic energy is exchanged between them. As a result the signal stays within the filter longer than for filters with a less sharp insertion loss cut off and, thus, the group delay is higher. Also, more energy is dissipated in the components and, therefore, insertion loss is higher unless larger components are employed.

[5]

[10]

# Model answer to Q 5(a): New Application of Theory



$$\begin{split} S_{21} \mid_{overall} &= \left(\frac{1}{\sqrt{2}}\right) \left(\frac{1}{\sqrt{2}}\right) S_{21} \left(\frac{-j}{\sqrt{2}}\right) \left(\frac{-j}{\sqrt{2}}\right) + \left(\frac{1}{\sqrt{2}}\right) \left(\frac{-j}{\sqrt{2}}\right) S_{21} \left(\frac{-1}{\sqrt{2}}\right) \left(\frac{-j}{\sqrt{2}}\right) + \left(\frac{-j}{\sqrt{2}}\right) \left(\frac{1}{\sqrt{2}}\right) S_{21} \left(\frac{-j}{\sqrt{2}}\right) \left(\frac{1}{\sqrt{2}}\right) \left(\frac{-j}{\sqrt{2}}\right) \left(\frac{-j}{\sqrt{2}}\right) S_{21} \left(\frac{1}{\sqrt{2}}\right) \left(\frac{1}{\sqrt{2}}\right) = S_{21} \end{split}$$

$$\begin{split} &Insertion\ Loss = 10\log\left\{S_{21}\mid^2\right\} \\ &S_{11}\mid_{overall} = \left(\frac{1}{\sqrt{2}}\right)\left(\frac{1}{\sqrt{2}}\right)S_{11}\left(\frac{1}{\sqrt{2}}\right)\left(\frac{1}{\sqrt{2}}\right) + \left(\frac{1}{\sqrt{2}}\right)\left(\frac{-j}{\sqrt{2}}\right)S_{11}\left(\frac{-j}{\sqrt{2}}\right)\left(\frac{1}{\sqrt{2}}\right) + \left(\frac{-j}{\sqrt{2}}\right)\left(\frac{1}{\sqrt{2}}\right)S_{11}\left(\frac{1}{\sqrt{2}}\right)\left(\frac{-j}{\sqrt{2}}\right) + \left(\frac{-j}{\sqrt{2}}\right)\left(\frac{-j}{\sqrt{2}}\right)S_{11}\left(\frac{-j}{\sqrt{2}}\right)\left(\frac{-j}{\sqrt{2}}\right) = 0 \end{split}$$

Return Loss = 
$$10\log\{0|^2\} \rightarrow -\infty$$

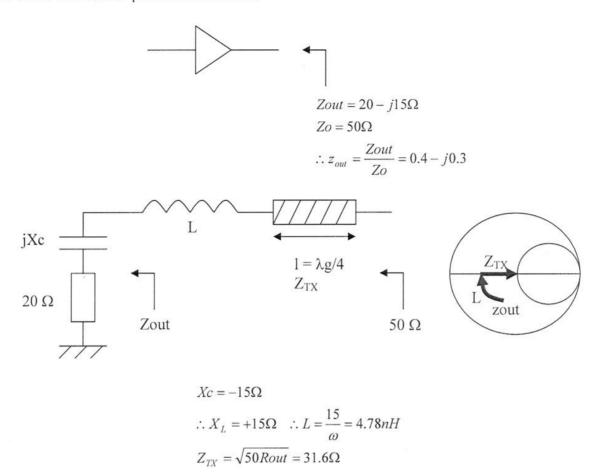
[5]

## Model answer to Q 5(b): Lecture Discussion

The main application of this amplifier is power combining, since the output power is ideally a factor of 4 greater than that of the single-ended amplifier. If one of the single-ended amplifiers fails then  $S_{21|\text{overall}} = 3S_{21}/4$  and Insertion loss is  $10\log\{(3|S_{21}|/4)^2\} = 17.5$  dB, i.e. a drop of 2.5 dB from a fully working amplifier. The input return loss should not change if the impedance of the failed amplifier doesn't change and is, therefore, still minus infinity. Therefore, this type of power combining amplifier is useful because it provides redundancy in the case of failure and also ideal port impedance matching. The disadvantages of this topology is that it requires 4 identical single-ended amplifiers. Also, practical losses in the couplers result in a direct loss in power gain and output efficiency will be significantly reduced.

# Model answer to Q 6(a): Computed Example

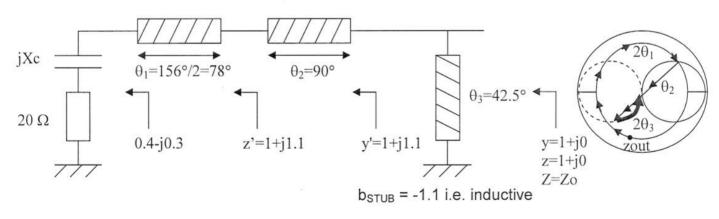
There are a number of possible solutions.



[3]

# Model answer to Q 6(b): Computed Example

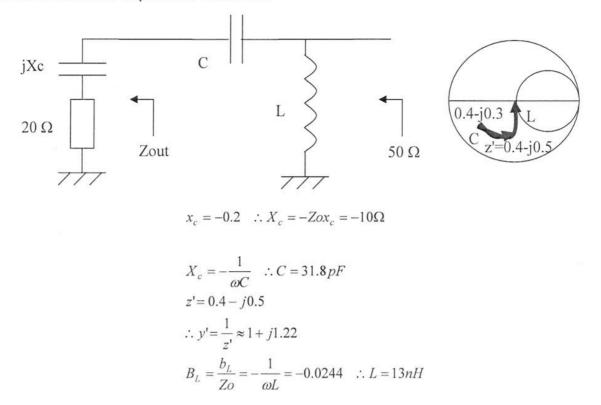
There are a number of possible solutions.



[8]

## Model answer to Q 6(c): Computed Example

There are a number of possible solutions.



## Model answer to Q 6(d): Textbook

On the Smith chart, loaded Q-factor is zero at the centre and infinite on the unit circle. This means that the L-C network has a point closer to the unit circle, when compared with that using the quarter-wave transformer or single stub solutions. Also, the bandwidth will be less, since loaded Q-factor is inversely proportional to bandwidth. Since the stub solution has more length of transmission line, it will operate over a narrower bandwidth, when compared to the quarter-wave transformer solution.

[3]

[6]