



DEPARTMENT of ELECTRICAL and ELECTRONIC ENGINEERING  
EXAMINATIONS 2001  
M.Sc in Communications and Signal Processing  
M.Eng. Part IV

## ADVANCED COMMUNICATION THEORY

- *There are FOUR questions (Q1 to Q4)*
- *Answer question Q1 plus 2 other questions.*

*Comments for Question Q1:*

- *Question Q1 has 20 multiple choice questions numbered 1 to 20.*
- *Circle the answers you think are correct on the answer sheet provided.*
- *There is only one correct answer per question.*

*The following are provided:*

- *A table of Fourier Transforms*
- *A "Gaussian Tail Function" graph*

**Examiners responsible: Dr. A. Manikas**

## Question-2

- a) Consider a binary communication model in which one of two known signals  $s_0(t)$  or  $s_1(t)$  is received in the time interval  $(0, T)$  in the presence of bandlimited additive white Gaussian noise of power-spectral-density  $PSD_n(f) = \frac{N_0}{2} \text{rect}\left\{\frac{f}{2B}\right\}$ .

If a correlation receiver is used, estimate the probability of error,  $p_e$ , as a function of  $\lambda_0$ , EUE, and  $\rho$  and the a priori probabilities  $\Pr(H_0)$ ,  $\Pr(H_1)$  **(40%)**

where  $\begin{cases} \lambda_0 & \text{is the likelihood ratio threshold defined by the chosen decision criterion,} \\ \text{EUE} & \text{is the Energy-Utilization-Efficiency of the system, and} \\ \rho & \text{is the time cross-correlation between signals.} \end{cases}$

N.B.:

A correlation receiver is based on the **Decision Rule**:

$$\text{choose } H_1 \text{ if } G > r_{\text{threshold}} \text{ where } \begin{cases} G = \int_0^{T_{cs}} r(t) s_1(t) dt - \int_0^{T_{cs}} r(t) s_0(t) dt \\ r_{\text{threshold}} \equiv \frac{N_0}{2} \ln(\lambda_0) + \frac{1}{2} \int_0^{T_{cs}} (s_1(t)^2 - s_0(t)^2) dt \end{cases}$$

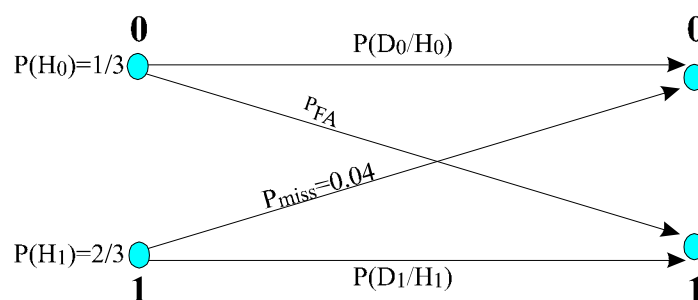
otherwise, choose  $H_0$

where  $r(t)$  represents the received signal.

- b) Consider a binary communication system in which the channel noise is additive Gaussian of zero mean and variance 1, that is  $N(0,1)$ . The system employs two correlated signals with cross-correlation coefficient  $\rho$ , and a correlation receiver which operates on the Bayes-decision criterion with the following costs:

$$C_{00}=C_{11}=0; C_{10}=1.858; C_{01}=0.5.$$

If the communication system has an energy utilisation efficiency  $\text{EUE} = 5.25 \times 10^{-2}$  and is modelled as follows:



estimate the cross correlation coefficient  $\rho$ . **(40%)**

What is the False Alarm Probability,  $P_{FA}$ , and the bit error probability,  $P_e$ , for the above system? **(20%)**

### Question-3

- a) Consider an  $m$ -sequence waveform  $b(t)$  of period  $NT_c$  with  $R_{b,M}(\tau)$  denoting its partial autorrelation function over  $MT_c$  with  $M < N$ ,

$$\text{i.e. } R_{b,M}(\tau) = \frac{1}{MT_c} \int_0^{MT_c} b(t) \cdot b(t - \tau) \cdot dt$$

Plot the mean and the variance of  $R_{b,M}(\tau)$  for  $-NT_c < \tau < NT_c$ . **(20%)**

- b) A BPSK direct sequence spread spectrum system (BPSK/DS-SSS) has a PN-code rate of 10 Mcips per second and a binary message rate of 1000 bits per second. The EUE at the receiver's input is 100 and the double-sided power spectral density of the received noise is  $0.5 \times 10^{-8}$  Watts per Hz. For this system, in which the correlation time is exactly one message bit, what would be the receiver's synchronization errors  $(\tau, \theta)$  which would provide code noise power equal to  $3.75 \times 10^{-8}$  W, knowing that if  $\tau > T_c$  then the code noise is constant and equal to  $1.5 \times 10^{-7}$  W. **(80%)**

N.B.:  $\tau$  represents the PN-code time error and  $\theta$  denotes the carrier's phase error.

### Question-4

Consider an  $M$ -ary Communication System with its signal set described as follows:

$$s_i(t) = A_i \mathbf{\Lambda} \left\{ \frac{2t}{T_{cs}} \right\}, i = 1, 2, \dots, M.$$

$$\text{with } \begin{cases} M = 4 \\ A_i = (2i - 1 - M) \times 10^{-3} \text{ Volts} \\ T_{cs} = 12 \text{ sec} \\ \Pr(H_1) = \Pr(H_4) = 1/8 \text{ and } \Pr(H_2) = \Pr(H_3) = 3/8 \end{cases}$$

The signals are transmitted over a communication channel which adds white Gaussian noise having a double-sided power spectral density of  $10^{-6}$  W/Hz.

- Find and plot the power spectral density of the transmitted signal  $s(t)$ . **(20%)**
- Calculate the values of the signal-vectors  $\underline{w}_{s_i}$ ,  $i = 1, 2, 3, 4$  for the above signal-set. **(20%)**
- Draw a labelled block diagram of the MAP correlation receiver, based on the signals vectors  $\underline{w}_{s_i}$ ,  $i = 1, 2, 3, 4$ . **(20%)**
- plot the constellation diagram and label the decision regions. **(25%)**
- Find the symbol error probability  $p_{e,cs}$  at the output of MAP receiver. **(15%)**

**[END]**