IMPERIAL COLLEGE LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2018**

EIE PART II: MEng, BEng and ACGI

FEEDBACK SYSTEMS

Corrected copy

Wednesday, 6 June 10:00 am

Time allowed: 1:30 hours

There are THREE questions on this paper.

Answer ALL questions. Question 1 carries 40% of the marks. Questions 2 and 3 carry equal marks (30% each).

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible

First Marker(s): I.M. Jaimoukha

Second Marker(s): S.A. Evangelou

1. a) Consider the system illustrated in Figure 1.1 where all the symbols have the standard interpretation. The input is the applied force f(t) and the output is the displacement of the box z(t). Take $M = K_2 = D = 1$ in appropriate units.

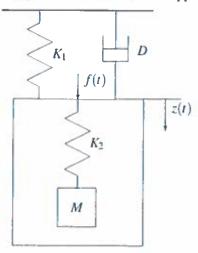


Figure 1.1

i) Show that the transfer function relating z to f is given by

$$G(s) = \frac{n(s)}{s^3 + (1 + K_1)s^2 + s + K_1}$$

where n(s) is a polynomial in s. What is n(s)?

- ii) Use the Routh array to find the range of values of K_1 for stability. [5]
- iii) Find the value of K_1 for which G(s) is marginally stable. For this value of K_1 , what are the poles of G(s)? [5]
- iv) Let f(t) be a unit step applied at t = 0. Use the final value theorem, which should be stated, to find the steady-state value z_{ss} , of z(t) in terms of K_1 . What is the value of K_1 for which $z_{ss} = 2$? [5]
- b) In Figure 1.2 below, $G(s) = 2/(s^2 1)$ and K(s) is a compensator.
 - Use the Routh-Hurwitz stability criterion to determine if the closedloop can be stabilised using:

ii) Design a PD so that the closed-loop is critically damped and has a pole at s = -1. [5]



Figure 1.2

[5]

Consider the feedback control system in Figure 2.1 below. Here, K(s) is the transfer function of a compensator while G(s) is a stable transfer function with no finite zeros whose frequency response is shown in Figure 2.2.

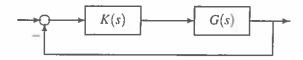


Figure 2.1

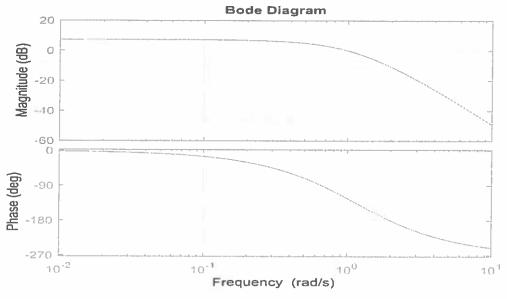


Figure 2.2

- a) Use the frequency response to sketch a rough Nyquist diagram of $G(s)_*$ indicating the low and high frequency portions and the real-axis intercepts. [5]
- b) Give approximate values for the crossover frequency and the gain and phase margins. Comment on the adequacy of the stability margins. [5]
- c) i) State the Nyquist stability criterion. [5]
 - ii) Use the Nyquist stability criterion to determine the number of unstable closed-loop poles when:

I.
$$K(s) = 1$$
, [5]

II.
$$K(s) = 10$$
. [5]

d) Let K(s) have the frequency response shown in Figure 2.3 overleaf. Describe K(s) briefly and indicate its effects on the performance and stability of the feedback loop. [5]

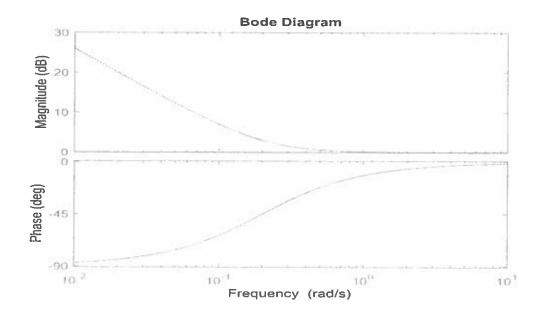


Figure 2.3

3. Consider the feedback loop shown in Figure 3.1 below. Here

$$G(s) = \frac{1}{s-1}.$$

It is required to design a compensator K(s) such that the closed-loop has a double pole at s = -2.

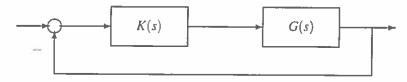


Figure 3.1

- a) Let $K(s) = K_P$, a proportional compensator. By writing down the closed–loop characteristic equation (CE), find the closed–loop poles as a function of K_P . [6]
- b) Design a PI compensator $K(s) = K_P + K_I s^{-1}$, where $K_P > 0$ and $K_I > 0$, that achieves the design specification as follows:
 - i) Write K(s) as $K(s) = K_P(s+z)/s$ where $z = K_I/K_P$. Write down the closed-loop CE in terms of K_P and z. [6]
 - Demonstrate using the CE that the design specifications can be achieved in principle for some value of z and K_P . [6]
 - iii) Find the value of K_P that achieves the design specification. [6]
 - iv) Find the value of z. Hence, deduce the value of K_I . [6]

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