Paper Number(s): E2.4

**ISE2.4** 

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2002** 

EEE/ISE PART II: M.Eng., B.Eng. and ACGI

#### **COMMUNICATIONS II**

Wednesday, 22 May 2:00 pm

There are FIVE questions on this paper.

Answer THREE questions.

Corrected Copy

Time allowed: 2:00 hours

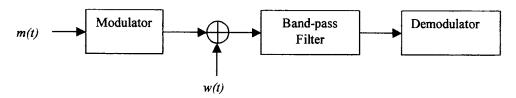
#### **Examiners responsible:**

First Marker(s):

Ward, D.B.

Second Marker(s): Barria, J.A.

1. (a) Consider the communications system shown in the following diagram



where m(t) is the base-band message signal, w(t) is additive zero-mean Gaussian noise with a flat power spectral density of height  $N_o/2$ , and the band-pass filter has a pass band (of appropriate width) centered on the carrier frequency  $\omega_c$ .

Show that the noise component of the signal at the output of the band-pass filter can be represented as:  $n(t) = \sum_{k} a_k \cos(\omega_k t + \theta_k)$ .

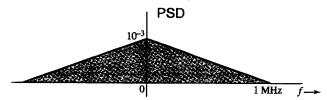
Also show that this noise can be written as:  $n(t) = n_c(t) \cos \omega_c t - n_s(t) \sin \omega_c t$ 

[10]

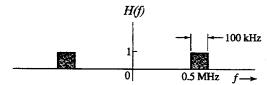
- (b) With reference to the system in part (a), if the message signal has a bandwidth of 15 kHz, and the noise has  $N_o = 2 \times 10^{-6}$ , calculate the average power in n(t) for each of the following modulation schemes:
  - (i) DSB-SC
  - (ii) FM with a modulation index of  $\beta = 3$ .

[5]

(c) A noise signal with the power spectral density shown here:



is passed through the band-pass filter shown here:



Draw the power spectral densities of the base-band components  $n_c(t)$  and  $n_s(t)$  at the output of the filter. Also calculate the average power in each base-band component.

Assume that the center frequency in the band-pass representation is  $f_c = 0.5$  MHz.

[5]

2. (a) Consider an AM receiver consisting of an ideal band-pass filter followed by an envelope detector. Assume the input to the band-pass filter consists of the AM signal:

$$s_{\rm AM}(t) = \left[A_c + m(t)\right] \cos \omega_c t$$

plus zero-mean Gaussian noise with a flat power spectral density. If the noise power is much greater than the power of the carrier and the message, show that the output of the receiver is:

$$y(t) = R(t) + [A_c + m(t)] \cos \phi(t),$$

where 
$$R(t) = \sqrt{n_c^2(t) + n_s^2(t)}$$
, and  $\tan \phi(t) = n_s(t)/n_c(t)$ .

You may find the following relationship useful:  $\sqrt{1+x} \approx 1 + \frac{x}{2}$  for x << 1.

[8]

(b) With the reference to the output expression y(t) of the system in part (a), explain why an AM receiver using an envelope detector exhibits a threshold effect.

[4]

(c) Consider an FM receiver consisting of an ideal band-pass filter followed by an FM demodulator. If the carrier power is much greater than the noise power at the output of the band-pass filter, then the signal-to-noise ratio at the output of the receiver is given by:

$$SNR_o = 3\beta^2 \frac{P}{\left|\max m(t)\right|^2} SNR_{\text{base}}$$

where P is the average power of the message signal m(t), and we assume that the noise is zero-mean Gaussian with a flat power spectral density.

Explain why  $SNR_o$  cannot be increased arbitrarily simply by increasing  $\beta$ .

HINT: The transmission bandwidth of FM is given by Carson's rule:  $B_T = 2(\beta + 1)W$ 

[4]

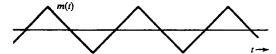
(d) Explain pre-emphasis and de-emphasis and why it is used in FM systems.

[4]

3.	(a) Using the Huffman coding procedure, construct a coding scheme for an alphabet whose symbols occur independently with probabilities 0.15, 0.08, 0.25, 0.10, 0.30, 0.12. Calculate t average codeword length of the resulting coding scheme, and compare it with the source entropy.	
	(b) What is the major practical disadvantage of Huffman coding?	[2]
	(c) State the channel capacity theorem. Also give the Hartley-Shannon expression for channe capacity, explaining and giving units for all terms used.	[6]
	(d) Explain the difference between source coding and channel coding.	[2]

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- 4. (a) A signal m(t) that is band-limited to 3 kHz is sampled at a rate  $33 \frac{1}{3}$  % higher than the Nyquist rate. The maximum acceptable error in the sample amplitude (i.e., the maximum quantization error) is 0.5% of the peak amplitude of m(t). The quantized samples are binary coded. Find the minimum bandwidth of a channel required to transmit the encoded binary signal. Assume that a channel of bandwidth B Hz can transmit B bits of information per second.
  - (b) The input to a uniform *n*-bit quantizer is the periodic triangular waveform shown below, which has a period of T = 4 seconds, and an amplitude that varies between +1 volt and -1 volt.

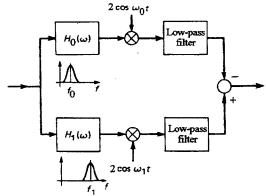


Derive an expression for the signal-to-noise ratio (in decibels) at the output of the quantizer. Assume that the dynamic range of the quantizer matches that of the input signal. Note that the mean-square error of a uniform quantizer is  $\Delta^2/12$ , where  $\Delta$  is the quantizer step size.

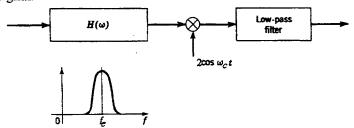
[4]

[8]

(c) Consider the synchronous FSK detector shown in the figure below, where the input to the detector is an FSK signal.



Also consider the synchronous PSK detector shown in the figure below, where the input to the detector is a PSK signal.



Show that the average power of the noise at the FSK detector output is twice that of the noise at the PSK detector output.

Assume in each case that the noise at the receiver input is additive zero-mean Gaussian noise with a flat power spectral density.

[8]

	each:
	(i) twisted pair (ii) coaxial cable
	(iii) microwave
	(iv) optical fiber
	(v) broadcast wireless
	(b) Briefly describe and contrast the following switching techniques:
	(i) circuit switching
	(ii) message switching
	(iii) packet switching

protocol reference model to elaborate your answer.

[10]

(01)

SOLUTIONS - COMMUNICATIONS I

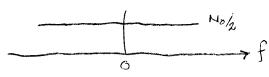
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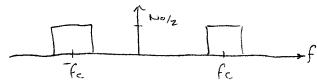
(a)

white Garesian woise has the PSD:

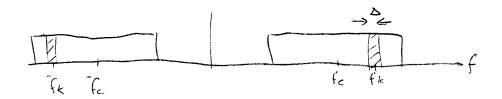
13



After the BPF this is:



Consider a small range of frequencies in this signal, about a frequency fk, is:



For Af small, the shaded components can be represented as the cos wave:

nk(+) = ak (os wkt + 0k

where ak is random amplitude of Ok is random phase.

Senning up over all such fx in the board, we have:

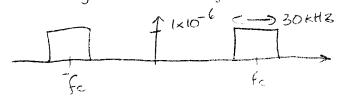
(5) n(t) = & nkt) = & ak los/wk++0k)

Let  $w_k = w_k - w_{c} + w_{c}$ , of use Cos(At8) = CosACosB - SiASinB  $\therefore n_k(t) = a_k Cos((w_k - w_{c})t + \theta_k) Cosw_{c}t$   $-a_k Bin((w_k - w_{c})t + \theta_k) Sinw_{c}t$ three,  $n(t) = n_{c}(t) Cosw_{c}t - n_{s}(t) Sinw_{c}t$ where  $n_{c}(t) = \sum_{k} a_k Cos((w_k - w_{c})t + \theta_k)$ 

(5) ns(t) = & ak Sin((w) + + Ok)

 $W = 15 \times 10^{3}$ ,  $N_0 = 2 \times 10^{-6}$   $\omega N_0/2 = 1 \times 10^{-6}$ 

(i) for DSB-SC, the transmission 6/w is  $B_7 = 2W$ , so two PSD of the moise after the BPF is:



Turb, the average power is:

$$P = \int_{\omega}^{\infty} P = 0$$
 of  $= 2 \times \text{area under each above}$   
 $= 2 \times 1 \times 10^{-6} \times 30 \times 10^{3}$   
 $= 0.06 \text{ Watts}.$ 

(2)

(its for FM, trasurssion b/w by Carson's rule is BT = 2(BTI)W = 120 KHZ.

Alg power of notice of the BPF is therefre:

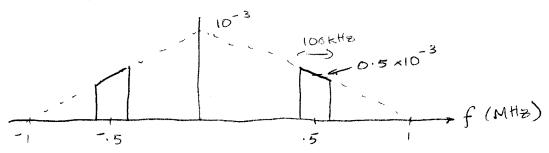
$$P = 2 \times 1 \times 10^{-6} \times 120 \text{ kHz}$$
  
= 0.24 Watts

(

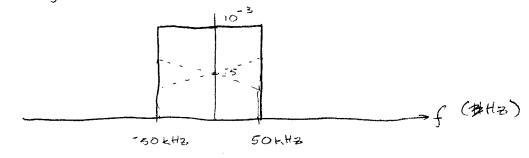
(3)

岁(c)

PSD of n(t) is:



: PSD of nelt) 4 ns(1) are both:



Dug pover is:

(D) P= 100 ×103 × 1×10-3 = 100 Watts.

4

After BPF, signal is:

Phasor diagram is:

Output of en. det. will be:

$$y(t) = \sqrt{(A_{c} + m(t))^{2} + n_{c}^{2}(t)}$$

$$= \sqrt{(A_{c} + m(t))^{2} + 2(A_{c} + m(t))n_{c}(t) + n_{c}^{2}(t) + n_{c}^{2}(t)}$$

But n(t) >> Actm(t), so no(t) 4 no(t) >> Actm(t)

But, 
$$R^{2} = n_c^2 + n_s^2$$

$$n_c = R \cos \phi$$

... y(x) = 
$$\sqrt{R^2 + 2 R \cos \phi (A_{ct}m(t))}$$
  
=  $\sqrt{R^2 \left[1 + 2 \cos \phi (A_{ct}m(t))\right]}$   
=  $R \sqrt{1 + 2/R \cos \phi (A_{ct}m(t))}$   
=  $R \left[1 + \frac{1}{R} \cos \phi (A_{ct}m(t))\right]$  using given expression  
=  $R + \cos \phi \left[A_{ct}m(t)\right]$ 

(8)

- (b) The o/p of the env. Out. consists of vi(t)

  multiplied by a time-varying moise team GsG(t).

  Here, it is of no use in recovering the message m(t).

  Because the noise is multiplicative when the noise

  neverses above a certain level, the env. olet. has

  a threshold effect.
- (c) Because the bootsond noise poner at the ofp of the BPF is related to the transmission b/w, if B is neversed the moise poner also viereases.

  At some stage the requirement that the camer poner is much greated than noise poner is what there is not greated than noise poner is

rois PSD of moise at o/p of FM detectors is of the

uhoueous PD of most message signals is of the

bour.

The, at high freqs the SNR is very poot.

Pre-euph is used to boost high freq components of message prior to FM modulation, thereby majoring SNR.

De-euph performs inverse operation by de-euphasizing

a) high free components, thereby leaving message industrated.

BLESTION 3

(25)

Aug length: 
$$C = \mathcal{E}_{Pk}lk$$
  
= .3x2+.25x2+.15x3+.12x3+.1x3+.08x3  
= a.45 bits

- (10) Endogry: W=-& Pk log\_2 Pk = 2.418 bits
- (b) Mayor disad, of Hifmon is that it a priori requires

  source, statistics. In many practical causes thuse one

  symbol not know.
  - then there exists a cooling scheme such that source can be transmitted over a noisy charel into an arbitrarily small prob. of ever.

Horoley Shower: C= Blogz (1+ 3/N)

where C is charel capitally in cits/see

B is charel 6/w n Hz

S is any sig power at receiver upit in Walts

N is any noise power at receiver upit in Walts

(d) Source cooling: concerned until assiging binary coolewords to source symbols.

Chanel cooling: concerned until introducing reducatant bits to enable received to detect/correct

errors introduced by chanel

OUESTION 4

(a) Nygnist saping rate is 6000 saples/sec. So actual rapping rate is:

fs = 6000 x 13 = 8000 Hz.

Quant. step size is 0, so max error is 0/2. If there are L levels, then the step size is:

D= L more peak is max sig auphilials

We require 0/2 < 0.5 peak.

Suce L must be a power of Z for a binary coole, we choose L=256, requiring log\_256 = 8 bit quantizer. Here, each scaple requires 8 bits, so soupling at 8 k.113 requires 64000 bit/s.

Hence, we require a b/w of  $\frac{64000}{2} = 32 \text{ kHz}$ .

8

(A)

Signal paver,  $P = \frac{1}{T} \int_{c}^{T} m^{2}(t) dt$   $= \frac{4}{T} \int_{0}^{1} m^{2}(t) dt \text{ because of symptry}$   $= \int_{0}^{1} t^{2} dt$   $= \frac{1}{3}$ 

Moix power, N= D2/12

where  $\Delta = 2/2^n$ 

 $||N| = \frac{4 \times 3^{-20}}{12} = \frac{1}{3} 2^{-20}$ 

 $1.5NR = \frac{1}{3} 2^{2n} ...5NR_{olb} = 10 log_{10}(2^{2n})$   $= 20 n log_{10} 2 = 6.02 n.$ 

(Q4)

(0)

Consider the FSK system.

If the upit is AWGN, then;

(Dupper-branch:

-after BPF, no(t) = no(t) (os wot - no(t) Sin wot)

-after multiplier, signal is:

2no(t) (os wot = no(t) (1+ (os 2wot)) - no(t) Sin 2wot)

-after LPF, noise = no(t)

(ii) lower-branch,

If Holus a Holus do not arenap, then no (+) a ro (+) are incorrelated, a moise at output, is no (+) - no (+) has various that is twice the various of each.

For PSK, noise at o/p will have some various as

- afto LPF, worse = no (+)

Here, FSK voise has ture various of PSK voise. For zero-mean Garsaiai signal, ang power = varione. Here, FSK voise has turce the power of PSK voise. (4)

### is Trusted par:

- -consists of two insulated copper wines
- application is to connect individual residential telephones to local exchange

### in Goax!

- -consists of hollow outer cylindrical conductor that summed a single inner nine conductor
- application are TU, long-distant phones, LANS

### (近) MICROUARE:

- uses parabolic desh for directoral transmission over the our - primary application is long-haul telecommunications

## ( optical fibre:

- consists of 3 concentric sextimos; core (one or more fibers), chadoling (gloss/plastic coating until different optical props) V jacket (protective covering)
- -application are long-boul trucks, LANS

### (3) westers broadcast radio:

- omnidurational ares air, so no med for directional
- application is conversial radio, UHFYVHF TU.

(b)

arcuito scutching:

- deducated comms path is established between two stations through modes of the network

- phoises one!

(i) establishment - an end-to-end circuit is established by fire data can be transmitted

3 port

(# data trasfer -> data can only be transmitted from the originating station to destination station; usually fill duple (#) disconnect -> after some period of time, connection is terminated

- appropriate unen there is a relatively continuous flow of olds, ig voice - disadiantages!

- both stations must be abulable at some time

- resources between stations i network unet be available V deducated

Message surtaing:

- station wishing to send message appends a destination address of message is than passed through network from nade to made - at each wode, message is received, stored briefly, of their

trainitied to next mode

Aport - advantages over cercuit custoing:

- greater the effuerce

- no requirement by sender of receiver to be avoilable antitaveachy

- inder heavy trafic rather than blocked ealls (as in circuit), inescages still delicendibit with greater debuy

- single message con be sent to many distinations

- can establish unersays presented

- ever recovery covered built into network

11.

Packet Swacing:

- attempts to combine advantages of both circuit of message suitching

- mai diference from necessor sudching is that length of data inits is limited in packet sudching

- returns can handle stream of paciets entires by:

3 port

ti datagram

- each packet treated independently

- packets ca be delivered out of order, I its up to destination node to figure out reordering

# (#) virtual cercuit :

- logical connection is established before pachets sent

- orig. sends call request to dest. node, union sends accept packet back to arig.

the logical connection

- eventually, one station termiales connection

(Sport)

#### (c) MANS:

- cores large geographical region, relying en circuits provided by a common carrer
- trovennssion from station is routed through internal suitering nodes to destination
- traditionally uplemented using circuit suitching or parket suitching

#### LAWS:

- confined to small area
- -traditionally makes use of broadcast network, whereby transmission from a station is broadcast to & received by all other stations
- distinctions from walls:
  - smaller geographical ecopoe
  - ownexty save organization
  - internal dates rates with greater
- topologies used are ring, bus, tree of star
- -sure only one device can successfully trasmit at a time, important requirement is be media access control
  - centralized scheme uses single controller to grant acres to returne; station unst usit intil permission is
  - to received from controller
  - elecentralized scheme: crations collectively perform MAC
    function to dynamically determine order in which
    stations havening

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(5 post)