Algorithms & complexity 
$$l_0 14 = EE10-C$$
 ]

a)  $T(n) = 4 T(n/2) + n^3$ 
 $a = 4$ ;  $b = 2$   $d = 3$ .

 $log_b a = log_2 4 = 2 < d = 3$ .

Hence  $T(n) = 0(n^3)$ 

b)  $T(n) = 17 T(n/4) + n^2$ 
 $a = 17 b = 4 d = b$ 
 $log_b a = log_b 17 7 log_b 16 = 27 d$ 

Hence  $T(n) = 0(n^3)$ 

c) 
$$T(n|= 9 + (n/3) + n^2$$
  
 $a = 9 + 3 + 3 + 2$   
 $\log_5 a = \log_3 9 = 2 = 3 = 2$   
=D  $T(n) = O(n^2 \log_3 n)$ .  
d)  $T(n|= + (\sqrt{n}) + 1$   
 $= O(k|= O(\log_3 n)$ .

2

a) For each ai the for loop or j bounts the number of times ai appears in the list.

For each ai it then check whether it appears note than -/2 times.

The algorithm then either neturns

i there is no mejority elevent ist more
of the eis appears more than h/2

this or returns the Unitable
olerent that appears more than h/2

this.

The of sorithm, our, two for Logs an e'd') from 1 to a Doits comprexity is  $O(n^2)$ .

nejoritz / [No] [75 & m, nn) [No) / ys & mz Ini, ni major to for E; & ni=# of + it both Prijority 1 & 2 return no then there is no majority number sink no say, thit all ai, olur tever then 1/4

1

ties in each at the lists End Ez ( de por fewer then m/2 tins in total. + if This ority 2 returns (m1, mn) d nojoritje returs no. Here we new the number of occurrent of Mn in £ 2, 12, if nn + n2 7 n/2 then you mais a regarity element Atervie no.

\* Similarly if Dajon't 2 return, ("2, n2) KNG-on't 1 return, m-

+ Bookly if Nejority 1 de nejority

2 return (n, m) de (u, n2) Hens

Clearly n i) the nejority element.

# finally if Majorty 1 returns (M1, Mn) (6

& Najority 2 returns (M1, M2) M1 # M2

We need to be at the occurrence

of M1 in \( \tau = M21

then see whether M1+M12 \)

Net M21 is larger than M/2.

Vive a list and a number let

Num (Ē, u)= # appenent st u in Ē.

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Majority (an -- an)
                        ; Rajn = Majority (E.
   Let En=an.on12
                        ; ng2 = nojox + LEZ
       EL= 0/2+1 -- 00.
If Moj = (+,0) and Ping=(+,0)
       (*,0)
   ng,= (2,, m) & ng.(+,=).
     then if men + Non (n1, Ez) > n/2
          the (n, n)
    else (+,0).
    Naj2 = (M2, N2) & ngn=(+,0)
    then if n2 = n2+ Non (42, E1) 7 "2
           then ( nz, nz)
       el1 (*,-)
e/10
    ng,-(m,m) & ng2 (m2, n2)
    then if nn=nz then
               ( nn, nn + n2).
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if nem1 + Num(x1/E2) 7 n/2 Hen (\*1/ n1) elx it n2 cn2 + N/n ("2, En) >n/2 then ( N2, NZ) elic (+,-). RENARK: Strater, con either provide text st a prevalouale TBand) (+2), if this provide Complexity. Co-plexity. e(n/= 2[c(n/z) + n/z] neci, to CIIFO bot the number En Ez of time on Men. the publish In DES Ch: 2 C(r/2) + n c(n= dolos). Poster theoren ->

(5) We have to look at all polhible subword) in both un(d) 2.2h. i) aitsi this means that aidst Const belong to the some subward. Hence either ai belong, to the comm sub word & p(ij) = p(n',j-1) 82 big & plijo) = p(i-1/0) ii) ait by=x thre either x below) to the corner published in which (a) c p(ij)= p(i-1,j-1)+1

8 nt & p(i,j)= (i-1,j-1)-

Putting all the iii) pied together we have p(ij) = max (p(ij-1), p(i-1,j), p(i-1,j-1)+ fails). either i of sleercess of each ptep we have at most un steps longlexity of of MM).

Hence bodab