Department of Electrical and Electronic Engineering Examinations Confidential Model Answers and Mark Schemes J. TBARRIA 1/6 First Examiner: Paper Code: EE4-05 Paper Code: EL4-05 Second Examiner: D Mandic Traffic Theory Z avereing systems Question Number etc. in left margin Mark allocation in right margin Total cells per hour 280 colls/n -> 4.66 cells/m i) bunge dunation of call 3 m. in) affered treffic = 4.66 × 3 = 13.98 Enloys N = 21 from treffir aparity Enlarg chart Loss probability = Bc = 0.002 (arried happi = 13.98 [1-0.002] = 13.95 Falgo Q1  $\lambda = 173$  colls  $\ln 1/\mu = 203 = E(5)$ i)  $\lambda = 2.88333$  colls  $\ln 1/\mu = 0.333$  m p = 0.96 ill  $E[Q_{\pm}] = \frac{\Lambda^2}{1-\rho} =$ 3 ii) = [w] = P E(s) = ini) = [Q=] = Zip(1-p)pi = p Zi2(1-p)pi  $= \rho \left(\rho \left(\frac{z}{(1-\rho)^2} - \frac{1}{1-\rho}\right)\right) = \rho^2 \left(\frac{z}{(1-\rho)^2} - \frac{1}{1-\rho}\right)$  $Van \left[Ged\right] = \rho^2 \left(\frac{2}{(17)^2} - \frac{1}{1-\rho}\right) - \left(\frac{\rho^2}{1-\rho}\right)^2$  $=\frac{\rho^2}{(1-\rho)^2}\left(\Lambda+\rho-\rho^2\right)=$ 

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Question Number etc. in left margin

First Examiner:

Paper Code:

Second Examiner:

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2

6

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2

@z ~) A TX HIMIK >0 ->
5%

Total annual nate y = 2+5x -> y = 1-5

If p is the service nate per dannel:

for a stable system:  $\frac{1}{K_{\mu}(1-5)} < 1 \Rightarrow \frac{1}{K_{\mu}} < 1-5$ 

P = d (offered fregtive > p < 1-5 => 5 < 1-p system)

K = 1 a) without feedback E(H) = f-p = d

a) with jeed bach  $= (\mu_{\xi}) = \frac{\rho'}{(-\rho')}$   $\rho' = \frac{\lambda}{M} = \frac{\lambda}{M(\lambda-5)}$ 

Link yeard cotoro hits/s = (1-5-P)

mensage service note  $\mu = \frac{64000}{700}$   $S^{-1}$ mensage service note  $\mu = \frac{64000}{700}$   $S^{-1}$   $\rho = \frac{\lambda}{4} = 0.875 = \rho_2$ mensage norce note  $\lambda = 80.5^{-1}$ 

Acknowledgement service tre = 2×32 5 = 1 ms

for a non- pre-entire priority system: PA = 80 x 8.001

rea merrage wouting the = R (1-P1)(1-P1-P2)

 $2 = \frac{1}{2} \left[ \lambda_1 \, \text{Hs}_1^2 \right] + \lambda_2 \, \text{E}(s_2^2) \right] = \frac{4.83}{0.92 \times 0.045} = \frac{1}{2} \left[ \frac{\lambda_1}{\mu_1^2} + \frac{\lambda_2}{Hz^2} \right] = 4.83 \, \text{ms} = 0.1166 \, \text{s}$ 

02

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Model Answers and Mark Schemes

Paper Code:

Second Examiner:

3

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Mean value analysis of HIGH system define R: = residuel service time = time with finished

E[W] = E[R] + E[Q; E[S]] = E[Ri] +E[Ri] E[s]

suice Poisson arnivals see an unmassed sample of queue between E[N] = ATE] + ETG] E[G] but also E[G] = A E[N]

E[W] = E[R]

P=ZETS]

E[Pt] = him - | Total+ = him 1 \frac{1}{25i^2} = him \frac{1}{T} \left(\frac{1}{T}) \left(\frac{1}{T} \sum\_{i=1}^{H\_T} \

(MT is the when of confleted services in [0,7])

E[Er] = = JAE[SZ]

E[W] = JE[SZ] 2(1-1)

for an MIDII system 5 = constant=h => E[52] = h2 (Van(5) =c)

 $E[N] = \frac{\rho}{2(1-\rho)} h = \frac{\rho}{2(1-\rho)} E[S]$ 

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Model Answers and Mark Schemes

First Examiner:

Paper Code:

Second Examiner:

4/

Question Number etc. in left margin

Mark allocation in right margin

(Q3

$$\frac{1}{7}(t+\Delta t,x) = \left[N-(i-1)\right] \wedge \Delta t + \left[t-(t+x)\right] + \left(i+1\right) \times \Delta t + \left[t-(t+x)\right] + \left(t-(t+x)\right) +$$

$$Ti(t+\Delta t_{1}\times)-Ti(t_{1}\times) = h_{1}\Delta t Tin(t_{1}\times) + h_{2}\Delta t Tin(t_{1}x) + h_{3}\Delta t Ti(t_{1}x-\Delta x) + Ti(t_{1}x-\Delta x) - Ti(t_{1}x)$$

$$Ti(t+\Delta t_{1}x)-Ti(t_{1}x)$$

$$= h_{1}Tin(t_{1}x) + h_{2}Tin(t_{1}x) + h_{3}Ti(t_{1}x-\Delta x)$$

$$+Ti(t_{1}x-\Delta x)-Ti(t_{1}x) \Delta x$$

$$\Delta t$$

At ME - 0

ii) In statestical equilibrium: DF:(k,t) =0 and Fi(t,k) -> Fi(x)

$$\frac{(i-c)_{x} d + i_{x}}{d x} = [\nu - (i-1)]_{x} + (i-1)_{x} - [(\nu - i)_{x} + i_{x}] + (i+1)_{x} + (i+1$$

in matrix form:

m

This expression represents a set of first-order lineau differentials equations for which the postion is well-known to be a sur of exponentials

4

6

2

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Model Answers and Mark Schemes

First Examiner:

Paper Code:

Second Examiner:

5

Question Number etc. in left margin

Mark allocation in right margin

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OH-OFF Source trettie source  $R_p = peach Rate$   $P_p = aucaque burst leigth$   $P = \frac{\alpha}{\alpha+p}$   $P = \frac{\alpha}{\alpha+p}$ 

Equivalent copacity = CL = mRp + KURP m Rp = mean =) m = NP for NON-OFF SOURCE TRP = Standard duration=> ( = m(1-p) for N ON OF SOURIS

k = k (Qcs)

C = CL = M+KJ = Np + k \ Np (1-p) and k ~ PL on E  $E = \frac{R}{2} \pi;$ PL = Z (i-C)Tic

in) For a longe unher of sources multiplexed, for N>>1, P <<1:

 $\pi_i = \left(\frac{N}{i}\right) p^i (1-p)^{N-i} \quad (\text{binomial})$ 

can be appreximated quite closely by the normal distribution (m = Np , 02 = Np(1-p))

 $E = \int_{0}^{\infty} \frac{e^{-(x-m)^2}}{2\sigma^2} dx$ 

if (c-m)>3/25

 $\overline{E} = Ge \frac{-(c-m)^2}{ZGZ}$ 1/20 ( C-m)

5

5

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-(xp+yn) yp yn

52p -2p (1-5)2p

2n P -2n 3