

MA 26100
EXAM 2 Green
April 3, 2018

NAME leaderboard YOUR TA'S NAME bla bla bla
STUDENT ID # 1097 RECITATION TIME some time

Be sure the paper you are looking at right now is GREEN! Write the following in the TEST/QUIZ NUMBER boxes (and blacken in the appropriate spaces below the boxes): 00

You must use a #2 pencil on the mark-sense sheet (answer sheet). On the mark-sense sheet, fill in your TA's name and the COURSE number. Fill in your NAME and STUDENT IDENTIFICATION NUMBER and blacken in the appropriate spaces. Fill in your four-digit SECTION NUMBER. If you do not know your section number, ask your TA. Sign the mark-sense sheet.

There are 11 questions, each worth 9 points (you will automatically earn 1 point for taking the exam). Blacken in your choice of the correct answer in the spaces provided for questions 1–11. Do all your work in this exam booklet. Use the back of the test pages for scrap paper. Turn in both the mark-sense sheet and the exam booklet when you are finished.

If you finish the exam before 7:20, you may leave the room after turning in the scantron sheet and the exam booklet. You may not leave the room before 6:50. If you don't finish before 7:20, you MUST REMAIN SEATED until your TA comes and collects your scantron sheet and your exam booklet.

EXAM POLICIES

1. Students may not open the exam until instructed to do so.
2. Students must obey the orders and requests by all proctors, TAs, and lecturers.
3. No student may leave in the first 20 min or in the last 10 min of the exam.
4. Books, notes, calculators, or any electronic devices are not allowed on the exam, and they should not even be in sight in the exam room. Students may not look at anybody else's test, and may not communicate with anybody else except, if they have a question, with their TA or lecturer.
5. After time is called, the students have to put down all writing instruments and remain in their seats, while the TAs will collect the scantrons and the exams.
6. Any violation of these rules and any act of academic dishonesty may result in severe penalties. Additionally, all violators will be reported to the Office of the Dean of Students.

I have read and understand the exam rules stated above:

STUDENT NAME: leaderboard

STUDENT SIGNATURE: Why should I put it?

1. Find the maximum of $3x + y$ on the circle $x^2 + y^2 = 10$.

A. 12

B. 8

C. 10

D. 6

E. $3\sqrt{10}$

Calc 1

$$3x + \sqrt{10 - x^2}$$

$$3 = \frac{x}{\sqrt{10 - x^2}}$$

$$\frac{dy}{dx} = 3 \cdot \frac{1 - 2x}{\sqrt{10 - x^2}}$$

$$9 = \frac{x^2}{10 - x^2}$$

$$90 - 9x^2 = x^2$$

2. Compute $\int_0^4 \int_{x/2}^2 \cos(2y^2) dy dx$ by reversing the order of integration.

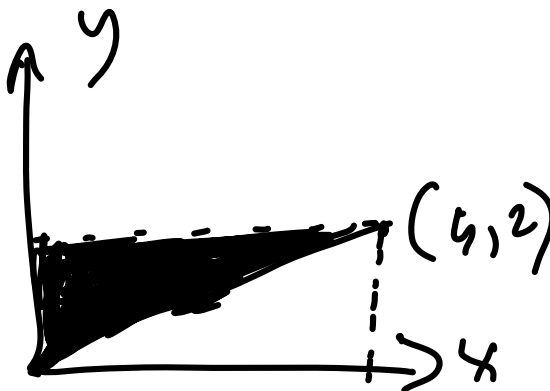
A. $\frac{1}{2} \sin 8$

B. $\frac{1}{2} \cos 8$

C. $\sin 2$

D. $\sin 8 - \sin 4$

E. $\cos 8$



$$90 = 10x^2$$

$$x = \pm 3$$

$$y = \pm 1$$

$$max = 3 + 1$$

$$= \underline{\underline{10}}$$

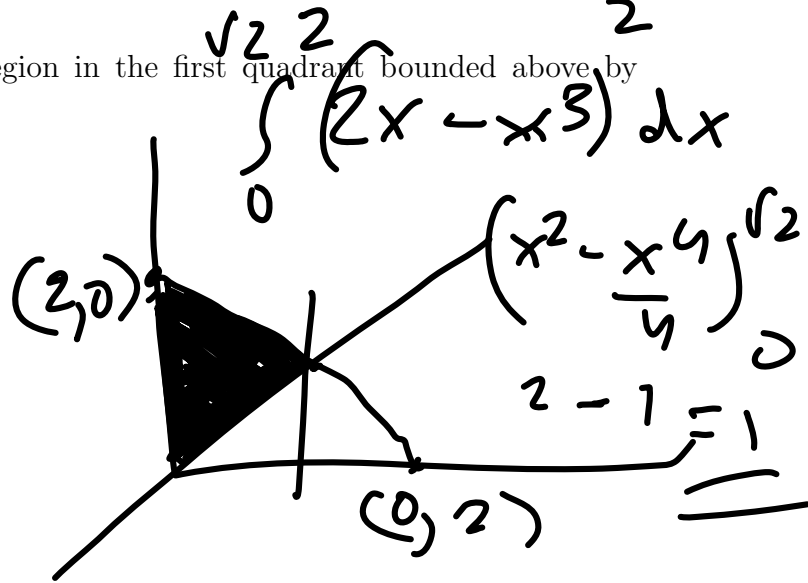
$$\int_0^2 \int_0^{2y} \cos(2y^2) dx dy$$

$$= \int_0^2 2y \cos(2y^2) dy = \left[\frac{1}{2} \sin(2y^2) \right]_0^2 = \frac{\sin 8}{2}$$

$$= \left(\frac{xy^2}{2} \right) \sqrt{4-x^2} = \frac{x(4-x^2)}{2} - \frac{x^3}{2}$$

3. Evaluate $\iint_D xy \, dA$ where D is the region in the first quadrant bounded above by $y = \sqrt{4-x^2}$ and below by $y = x$

- A. $\frac{2}{3}$
 B. $\frac{\pi}{2}$
 C. $\frac{1}{2}$
 D. 1
 E. $\frac{3\pi}{8}$

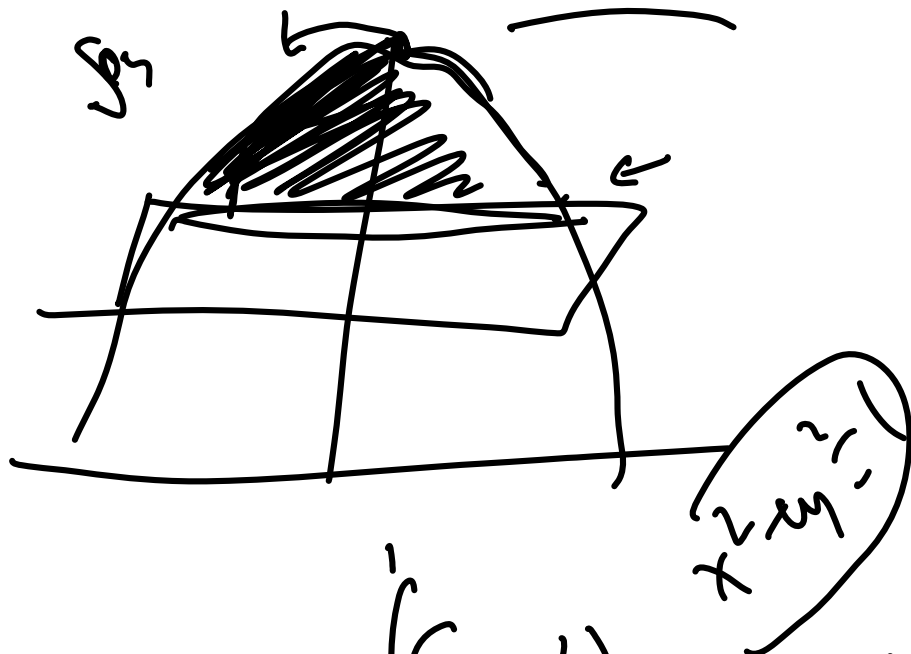


$$\int_0^{\sqrt{2}} \int_x^{\sqrt{4-x^2}} xy \, dy \, dx$$

$$\begin{aligned} x &= \sqrt{4-x^2} \\ x^2 &= 4-x^2 \\ 2x^2 &= 4 \quad x = \sqrt{2} \end{aligned}$$

4. Find the volume of the solid region bounded by the paraboloid $z = 3 - x^2 - y^2$ and the plane $z = 2$.

- A. $5\pi/2$
 B. $4\pi/3$
 C. $16\pi/3$
 D. $\pi/2$
 E. π



$$\int_0^{2\pi} \int_0^1 \int_2^{3-r^2} r \, dz \, dr \, d\theta = 2\pi \int_0^1 (1-r^2) r \, dr \, d\theta = 2\pi \left[\frac{r^2}{2} - \frac{r^4}{4} \right]_0^1 = 2\pi \left(\frac{1}{2} - \frac{1}{4} \right) = \frac{2\pi}{4} = \frac{\pi}{2}$$

5. Find the surface area of the part of the plane $z = \sqrt{13}x + \sqrt{2}y$ that lies between the cylinders $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$.

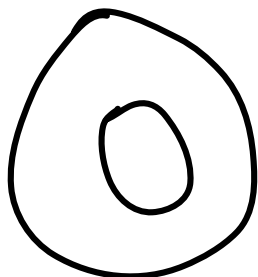
A. 12π

B. 6π

~~C. 8π~~

D. 60π

E. 24π



on length

$$\int_0^2 \int_1^2 \sqrt{1+13+2} \, d\sigma \, d\theta$$

~~2r~~

6. Let T be the solid tetrahedron bounded by the planes $x + y + z = 1$, $z = 0$, $y = x$, and $x = 0$. If for all continuous functions $f(x, y, z)$ on T we have

$$\iiint_T f(x, y, z) \, dV = \int_0^{1/2} \int_{a(x)}^{b(x)} \int_0^{1-x-y} f(x, y, z) \, dz \, dy \, dx,$$

then $a(x) + 2b(x)$ is equal to

A. 2

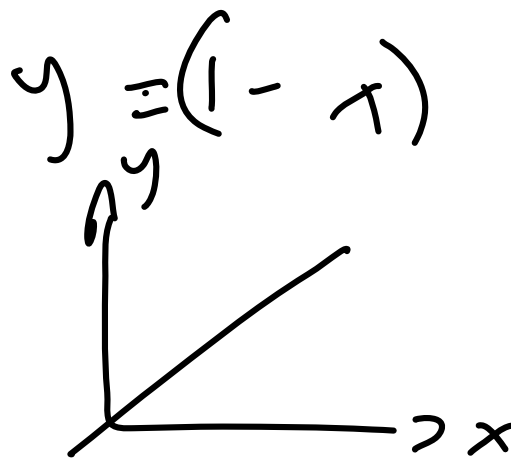
B. $x + 2$

~~C. $2 - 2x$~~

D. $2 - x$

E. $2x$

~~$x + 2(1-x)$~~



7. Evaluate the integral

$$\iiint_E (x^2 + y^2 + z^2)^{3/2} dV$$

where E is the region that lies inside the sphere $x^2 + y^2 + z^2 = 1$.

- A. $\pi/3$
- B. $\pi/2$
- C. π
- D. $4\pi/5$
- ☒ E. $2\pi/3$

$$x^2 + y^2 + z^2 = r^2$$

$$\int_0^{2\pi} \int_0^{\pi} \int_0^1 r^3 \cdot r^2 \sin \phi \, dr \, d\phi \, d\theta$$

$$\int_0^{2\pi} \int_0^{\pi} \frac{1}{6} \sin \phi \, d\phi \, d\theta$$

8. Let C be the line segment joining the points $(1, 2, 1)$ and $(3, 2, 1)$. The line integral $\int_C x \, ds$ is equal to

- A. 8
- ☒ B. 4
- C. 3
- D. 2
- E. 1

$$= \left(\frac{1}{6} \cos \phi \right)_0^{\pi}$$

$$= -\frac{1}{6} (-1 - 1) = \frac{1}{3} \times 2\pi$$

$$\vec{r}(t) = a + t(b-a)$$

$$\langle 1, 2, 1 \rangle + t \langle 2, 0, 0 \rangle$$

$$\langle 1+2t, 2, 1 \rangle$$

$$|\vec{r}'(t)| = 2$$

$$\int_0^1 (1+2t) \, dt$$

$$= \left(t + t^2 \right)_0^1$$

$$= 2(2) = 4$$

9. The vector field $\vec{F}(x, y, z) = yz^2\vec{i} + (xz^2 + 4y)\vec{j} + 2xyz\vec{k}$ is the gradient vector field of a function $f(x, y, z)$ such that $f(0, 0, 0) = 0$. Find $f(1, 1, 1)$.

- A. 2
B. 3
C. 4
D. 5
E. 8

think this is illegal
but I am not fully
sure yet.

10. Evaluate the line integral $\int_C \vec{F} \cdot d\vec{r}$ where $\vec{F}(x, y, z) = (x - y)\vec{i} + y\vec{j} + z\vec{k}$ and C is the line segment from the point $(1, 1, 2)$ to the point $(2, 3, 5)$.

- A. 15
B. 5
C. 16
D. 22
E. 14


illegal

11. Evaluate $\int_C \vec{\mathbf{F}} \cdot d\vec{\mathbf{r}}$, where $\vec{\mathbf{F}}(x, y, z) = yz\vec{\mathbf{i}} + xz\vec{\mathbf{j}} + xy\vec{\mathbf{k}}$ and C is the piecewise smooth

curve which consists of the conic spiral $x(t) = t \cos \frac{\pi t}{2}$, $y(t) = 3t \sin \frac{\pi t}{2}$ and $z(t) = 2t$, $0 \leq t \leq 1$, followed by the line segment $x = t$, $y = t + 3$ and $z = t + 2$, $0 \leq t \leq 2$.

Hint: Ask yourself if $\vec{\mathbf{F}}$ is the gradient vector field of some function.

A. 16

B. 24

C. 40

D. 34

E. 12

X
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