MA 261 PRACTICE PROBLEMS

1. If the line ℓ has symmetric equations

$$\frac{x-1}{2} = \frac{y}{-3} = \frac{z+2}{7}$$

 $\frac{x-1}{2} = \frac{y}{-3} = \frac{z+2}{7},$ find a vector equation for the line ℓ' that contains the point (2,1,-3) and is parallel to ℓ .

- A. $\vec{r} = (1+2t)\vec{i} 3t\vec{j} + (-2+7t)\vec{k}$ B. $\vec{r} = (2+t)\vec{i} 3\vec{j} + (7-2t)\vec{k}$ C. $\vec{r} = (2+2t)\vec{i} + (1-3t)\vec{j} + (-3+7t)\vec{k}$ D. $\vec{r} = (2+2t)\vec{i} + (-3+t)\vec{j} + (7-3t)\vec{k}$ E. $\vec{r} = (2+t)\vec{i} + \vec{j} + (7-3t)\vec{k}$
- 2. Find parametric equations of the line containing the points (1, -1, 0) and (-2, 3, 5).
 - A. x = 1 3t, y = -1 + 4t, z = 5t
- C. x = 1 2t, y = -1 + 3t, z = 5t
- B. x = t, y = -t, z = 0D. x = -2t, y = 3t, z = 5t
- E. x = -1 + t, y = 2 t, z = 5
- 3. Find an equation of the plane that contains the point (1, -1, -1) and has normal vector $\frac{1}{2}\vec{i} + 2\vec{j} + 3\vec{k}$.
- A. $x y z + \frac{9}{2} = 0$ B. x + 4y + 6z + 9 = 0 C. $\frac{x-1}{\frac{1}{2}} = \frac{y+1}{2} = \frac{z+1}{3}$ D. x y z = 0 E. $\frac{1}{2}x + 2y + 3z = 1$

- 4. Find an equation of the plane that contains the points (1,0,-1), (-5,3,2), and (2,-1,4).
 - A. 6x 11y + z = 5D. $\vec{r} = 18\vec{i} 33\vec{j} + 3\vec{k}$ B. 6x + 11y + z = 5E. x 6y 11z = 12C. 11x 6y + z = 0

- 5. Find parametric equations of the line tangent to the curve $\vec{r}(t) = t\vec{i} + t^2\vec{j} + t^3\vec{k}$ at the point (2,4,8)
 - A. x = 2 + t, y = 4 + 4t, z = 8 + 12t B. x = 1 + 2t, y = 4 + 4t, z = 12 + 8t

- C. x = 2t, y = 4t, z = 8t D. x = t, y = 4t, z = 12t E. x = 2 + t, y = 4 + 2t, z = 8 + 3t
- 6. The position function of an object is

$$\vec{r}(t) = \cos t\vec{i} + 3\sin t\vec{j} - t^2\vec{k}$$

Find the velocity, acceleration, and speed of the object when $t = \pi$.

- Velocity Acceleration Speed A. $-\vec{i} \pi^2 \vec{k}$ $-3\vec{j} 2\pi \vec{k}$ $\sqrt{1 + \pi^4}$ B. $\vec{i} 3\vec{j} + 2\pi \vec{k}$ $-\vec{i} 2\vec{k}$ $\sqrt{10 + 4\pi^2}$ C. $3\vec{j} 2\pi \vec{k}$ $-\vec{i} 2\vec{k}$ $\sqrt{9 + 4\pi^2}$ D. $-3\vec{j} 2\pi \vec{k}$ $\vec{i} 2\vec{k}$ $\sqrt{9 + 4\pi^2}$ E. $\vec{i} 2\vec{k}$ $\sqrt{5}$

- 7. A smooth parametrization of the semicircle which passes through the points (1,0,5), (0,1,5) and (-1,0,5) is

 - A. $\vec{r}(t) = \sin t \vec{i} + \cos t \vec{j} + 5 \vec{k}, 0 \le t \le \pi$ C. $\vec{r}(t) = \cos t \vec{i} + \sin t \vec{j} + 5 \vec{k}, \frac{\pi}{2} \le t \le \frac{3\pi}{2}$ E. $\vec{r}(t) = \sin t + \cos t \vec{j} + 5 \vec{k}, \frac{\pi}{2} \le t \le \frac{3\pi}{2}$ B. $\vec{r}(t) = \cos t \vec{i} + \sin t \vec{j} + 5 \vec{k}, 0 \le t \le \pi$ D. $\vec{r}(t) = \cos t \vec{i} + \sin t \vec{j} + 5 \vec{k}, 0 \le t \le \frac{\pi}{2}$
- 8. The length of the curve $\vec{r}(t) = \frac{2}{3}(1+t)^{\frac{3}{2}}\vec{i} + \frac{2}{3}(1-t)^{\frac{3}{2}}\vec{j} + t\vec{k}$, $-1 \le t \le 1$ is
 - A. $\sqrt{3}$
- B. $\sqrt{2}$
- C. $\frac{1}{2}\sqrt{3}$ D. $2\sqrt{3}$
- E. $\sqrt{2}$

- 9. The level curves of the function $f(x,y) = \sqrt{1-x^2-2y^2}$ are
 - A. circles
- B. lines
- C. parabolas
- D. hyperbolas
- E. ellipses
- 10. The level surface of the function $f(x, y, z) = z x^2 y^2$ that passes through the point (1, 2, -3) intersects the (x, z)-plane (y = 0) along the curve
 - A. $z = x^2 + 8$
- B. $z = x^2 8$ C. $z = x^2 + 5$ D. $z = -x^2 8$

- E. does not intersect the (x, z)-plane
- 11. Match the graphs of the equations with their names:
 - $(1) x^2 + y^2 + z^2 = 4$
- (a) paraboloid
- (2) $x^2 + z^2 = 4$
- (b) sphere
- (c) cylinder
- (2) $x^2 + y^2 = z^2$ (3) $x^2 + y^2 = z^2$ (4) $x^2 + y^2 = z$ (5) $x^2 + 2y^2 + 3z^2 = 1$
- (d) double cone (e) ellipsoid
- A. 1b, 2c, 3d, 4a, 5e
- B. 1b, 2c, 3a, 4d, 5e

C. 1e, 2c, 3d, 4a, 5b

- D. 1b, 2d, 3a, 4c, 5e
- E. 1d, 2a, 3b, 4e, 5c
- 12. Suppose that $w = u^2/v$ where $u = g_1(t)$ and $v = g_2(t)$ are differentiable functions of t. If $g_1(1) = 3$, $g_2(1) = 2$, $g'_1(1) = 5$ and $g'_2(1) = -4$, find $\frac{dw}{dt}$ when t = 1.
 - A. 6
- B. 33/2
- D. 33
- E. 24

- 13. If $w = e^{uv}$ and u = r + s, v = rs, find $\frac{\partial w}{\partial r}$.
 - A. $e^{(r+s)rs}(2rs+r^2)$ B. $e^{(r+s)rs}(2rs+s^2)$ D. $e^{(r+s)rs}(1+s)$ E. $e^{(r+s)rs}(r+s^2)$.

C. $e^{(r+s)rs}(2rs + r^2)$

- 14. If $f(x,y) = \cos(xy)$, $\frac{\partial^2 f}{\partial x \partial y} =$
 - B. $-xy\cos(xy) \sin(xy)$ A. $-xy\cos(xy)$

C. $-\sin(xy)$

- D. $xy\cos(xy) + \sin(xy)$
- E. $-\cos(xy)$
- 15. Assuming that the equation $xy^2 + 3z = \cos(z^2)$ defines z implicitly as a function of x and y, find $\frac{\partial z}{\partial x}$.
- A. $\frac{y^2}{3-\sin(z^2)}$ B. $\frac{-y^2}{3+\sin(z^2)}$ C. $\frac{y^2}{3+2z\sin(z^2)}$ D. $\frac{-y^2}{3+2z\sin(z^2)}$ E. $\frac{-y^2}{3-2z\sin(z^2)}$

- 16. If $f(x,y) = xy^2$, then $\nabla f(2,3) =$

 - A. $12\vec{i} + 9\vec{j}$ B. $18\vec{i} + 18\vec{j}$
- C. $9\vec{i} + 12\vec{i}$
- D. 21
- E. $\sqrt{2}$.
- 17. Find the directional derivative of $f(x,y) = 5 4x^2 3y$ at (x,y) towards the origin
 - A. -8x 3
- B. $\frac{-8x^2 3y}{\sqrt{x^2 + y^2}}$ C. $\frac{-8x 3}{\sqrt{64x^2 + 9}}$ D. $8x^2 + 3y$
- E. $\frac{8x^2+3y}{\sqrt{x^2+y^2}}$.
- 18. For the function $f(x,y) = x^2y$, find a unit vector \vec{u} for which the directional derivative $D_{\vec{u}}f(2,3)$ is
 - A. $\vec{i} + 3\vec{j}$ B. $\frac{i+3\vec{j}}{\sqrt{10}}$ C. $\vec{i} 3\vec{j}$ D. $\frac{i-3\vec{j}}{\sqrt{10}}$

- E. $\frac{3\vec{i}-\vec{j}}{\sqrt{10}}$.
- 19. Find a vector pointing in the direction in which $f(x, y, z) = 3xy 9xz^2 + y$ increases most rapidly at the point (1, 1, 0).

- A. $3\vec{i}+4\vec{j}$ B. $\vec{i}+\vec{j}$ C. $4\vec{i}-3\vec{j}$ D. $2\vec{i}+\vec{k}$ E. $-\vec{i}+\vec{j}$.
- 20. Find a vector that is normal to the graph of the equation $2\cos(\pi xy) = 1$ at the point $(\frac{1}{6}, 2)$.
 - A. $6\vec{i} + \vec{j}$

B. $-\sqrt{3}\vec{i}-\vec{i}$

- C. $12\vec{i} + \vec{j}$ D. \vec{i} E. $12\vec{i} \vec{j}$.
- 21. Find an equation of the tangent plane to the surface $x^2 + 2y^2 + 3z^2 = 6$ at the point (1, 1, -1).
 - A. -x + 2y + 3z = 2
- B. 2x + 4y 6z = 6E. x + 2y 3z = 6.

C. x - 2y + 3z = -4

- D. 2x + 4y 6z = 0
- 22. Find an equation of the plane tangent to the graph of $f(x,y) = \pi + \sin(\pi x^2 + 2y)$ when $(x,y) = (2,\pi)$.
 - $A. 4\pi x + 2y z = 9\pi$
- B. $4x + 2\pi y z = 10\pi$
- C. $4\pi x + 2\pi y + z = 10\pi$
- A. $4\pi x + 2y z = 9\pi$ B. $4x + 2\pi y$ D. $4x + 2\pi y z = 9\pi$ E. $4\pi x + 2y + z = 9\pi$.

23.	The differential a	f of the function	f(x, y, z) =	$xe^{y^2-z^2}$	is
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A.
$$df = xe^{y^2 - z^2}dx + xe^{y^2 - z^2}dy + xe^{y^2 - z^2}dz$$

$$B. df = xe^{y^2 - z^2} dx dy dz$$

C.
$$df = e^{y^2 - z^2} dx - 2xye^{y^2 - z^2} dy + 2xze^{y^2 - z^2} dz$$

A.
$$df = xe^{y^2 - z^2} dx + xe^{y^2 - z^2} dy + xe^{y^2 - z^2} dz$$

B. $df = xe^{y^2 - z^2} dx dy dz$
C. $df = e^{y^2 - z^2} dx - 2xye^{y^2 - z^2} dy + 2xze^{y^2 - z^2} dz$
D. $df = e^{y^2 - z^2} dx + 2xye^{y^2 - z^2} dy - 2xze^{y^2 - z^2} dz$
E. $df = e^{y^2 - z^2} (1 + 2xy - 2xz)$

E.
$$df = e^{y^2 - z^2} (1 + 2xy - 2xz)$$

24. The function
$$f(x,y) = 2x^3 - 6xy - 3y^2$$
 has

A. a relative minimum and a saddle point

B. a relative maximum and a saddle point

C. a relative minimum and a relative maximum D. two saddle points

E. two relative minima.

25. Consider the problem of finding the minimum value of the function $f(x,y) = 4x^2 + y^2$ on the curve xy=1. In using the method of Lagrange multipliers, the value of λ (even though it is not needed) will be

B.
$$-2$$

C.
$$\sqrt{2}$$

D.
$$\frac{1}{\sqrt{2}}$$

E. 4.

26. Evaluate the iterated integral $\int_{1}^{3} \int_{0}^{x} \frac{1}{x} dy dx$.

A.
$$-\frac{8}{9}$$

$$C. \ln 3$$

E. ln 2.

27. Consider the double integral, $\iint_R f(x,y)dA$, where R is the portion of the disk $x^2 + y^2 \le 1$, in the upper half-plane, $y \ge 0$. Express the integral as an iterated integral.

A.
$$\int_{-1}^{1} \int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}} f(x,y) dy dx$$

B.
$$\int_{-1}^{0} \int_{0}^{\sqrt{1-x^2}} f(x,y) dy dx$$

C.
$$\int_{-1}^{1} \int_{0}^{\sqrt{1-x^2}} f(x,y) dy dx$$

D.
$$\int_0^1 \int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}} f(x,y) dy dx$$

E.
$$\int_0^1 \int_0^{\sqrt{1-x^2}} f(x,y) dy dx$$
.

28. Find a and b for the correct interchange of order of integration:

$$\int_0^2 \int_{x^2}^{2x} f(x, y) dy dx = \int_0^4 \int_a^b f(x, y) dx dy.$$

A.
$$a = y^2, b = 2y$$

D. $a = \sqrt{y}, b = \frac{y}{2}$

B.
$$a = \frac{y}{2}, b = \sqrt{y}$$

C.
$$a = \frac{y}{2}, b = y$$

D.
$$a = \sqrt{y}, b = \frac{y}{2}$$

B. $a=\frac{y}{2}, b=\sqrt{y}$ C. $a=\frac{y}{2}, b=y$ E. cannot be done without explicit knowledge of f(x,y).

29. Evaluate the double integral $\iint_R y dA$, where R is the region of the (x, y)-plane inside the triangle with vertices (0,0), (2,0) and (2,1).

B.
$$\frac{8}{2}$$

C.
$$\frac{2}{3}$$

E. $\frac{1}{3}$.

30. The volume of the solid region in the first octant bounded above by the parabolic sheet $z = 1 - x^2$, below by the xy plane, and on the sides by the planes y = 0 and y = x is given by the double integral

A.
$$\int_0^1 \int_0^x (1-x^2) dy dx$$

B.
$$\int_0^1 \int_0^{1-x^2} x \, dy \, dx$$

C.
$$\int_{-1}^{1} \int_{-x}^{x} (1-x^2) dy dx$$

A.
$$\int_0^1 \int_0^x (1-x^2) dy dx$$
 B. $\int_0^1 \int_0^{1-x^2} x \, dy dx$ D. $\int_0^1 \int_x^0 (1-x^2) dy dx$ E. $\int_0^1 \int_x^{1-x^2} dy dx$.

E.
$$\int_0^1 \int_x^{1-x^2} dy dx$$

- 31. The area of one leaf of the three-leaved rose bounded by the graph of $r = 5 \sin 3\theta$ is
 - A. $\frac{5\pi}{6}$
- C. $\frac{25\pi}{6}$
- E. $\frac{25\pi}{3}$.
- 32. Find the area of the portion of the plane x + 3y + 2z = 6 that lies in the first octant.
 - A. $3\sqrt{11}$
- B. $6\sqrt{7}$
- C. $6\sqrt{14}$
- E. $6\sqrt{11}$.
- 33. A solid region in the first octant is bounded by the surfaces $z = y^2$, y = x, y = 0, z = 0 and x = 4. The volume of the region is
 - A. 64
- B. $\frac{64}{3}$
- C. $\frac{32}{3}$
- D. 32
- 34. An object occupies the region bounded above by the sphere $x^2 + y^2 + z^2 = 32$ and below by the upper nappe of the cone $z^2 = x^2 + y^2$. The mass density at any point of the object is equal to its distance from the xy plane. Set up a triple integral in rectangular coordinates for the total mass m of the object.
 - A. $\int_{-4}^{4} \int_{-\sqrt{16-x^2}}^{\sqrt{16-x^2}} \int_{-\sqrt{x^2+y^2}}^{\sqrt{32-x^2-y^2}} z \, dz \, dy \, dx$

B. $\int_{-4}^{4} \int_{-\sqrt{16-x^2}}^{\sqrt{16-x^2}} \int_{\sqrt{x^2+y^2}}^{\sqrt{32-x^2-y^2}} z \, dz \, dy \, dx$

- C. $\int_{-2}^{2} \int_{-\sqrt{4-x^{2}}}^{\sqrt{4-x^{2}}} \int_{-\sqrt{x^{2}+y^{2}}}^{\sqrt{32-x^{2}-y^{2}}} z \, dz \, dy \, dx$ E. $\int_{-4}^{4} \int_{-\sqrt{16-x^{2}}}^{\sqrt{16-x^{2}}} \int_{\sqrt{x^{2}+y^{2}}}^{\sqrt{32-x^{2}-y^{2}}} xy \, dz \, dy \, dx.$

D. $\int_0^4 \int_0^{\sqrt{16-x^2}} \int_{\sqrt{x^2+y^2}}^{\sqrt{32-x^2-y^2}} z \, dz \, dy \, dx$

- 35. Do problem 34 in spherical coordinates.
 - A. $\int_0^{2\pi} \int_0^{\frac{\pi}{4}} \int_0^{\sqrt{32}} \rho^3 \cos \varphi \sin \varphi \, d\rho \, d\varphi \, d\theta$

B. $\int_0^{2\pi} \int_0^{\frac{\pi}{4}} \int_0^{\sqrt{32}} \rho \cos \varphi \sin \varphi \, d\rho \, d\varphi \, d\theta$

C. $\int_0^{2\pi} \int_0^{\frac{\pi}{4}} \int_0^{\sqrt{32}} \rho^3 \sin^2 \varphi \, d\rho \, d\varphi \, d\theta$

D. $\int_0^{2\pi} \int_0^{\frac{\pi}{2}} \int_0^{\sqrt{32}} \rho^3 \cos \varphi \sin \varphi \, d\rho \, d\varphi \, d\theta$

- E. $\int_0^{2\pi} \int_0^{\frac{\pi}{4}} \int_0^{\sqrt{32}} \rho \cos \varphi \, d\rho \, d\varphi \, d\theta$.
- 36. The double integral $\int_0^1 \int_0^{\sqrt{1-x^2}} y^2 (x^2+y^2)^3 dy dx$ when converted to polar coordinates becomes
 - A. $\int_0^{\pi} \int_0^1 r^9 \sin^2 \theta \, dr \, d\theta$
- B. $\int_0^{\frac{\pi}{2}} \int_0^1 r^8 \sin^2 \theta \, dr \, d\theta$
- C. $\int_0^{\pi} \int_0^1 r^8 \sin \theta \, dr \, d\theta$

- D. $\int_0^{\frac{\pi}{2}} \int_0^1 r^8 \sin \theta \, dr \, d\theta$ E. $\int_0^{\frac{\pi}{2}} \int_0^1 r^9 \sin^2 \theta \, dr \, d\theta$.

37. Which of the triple integrals converts
$$\int_{-2}^2 \int_{-\sqrt{4-x^2}}^{\sqrt{4-x^2}} \int_{\sqrt{x^2+y^2}}^2 dz \, dy \, dx$$
 from rectangular to cylindrical coordinates?

- A. $\int_0^{\pi} \int_0^2 \int_r^2 r \, dz \, dr \, d\theta$ B. $\int_0^{2\pi} \int_0^2 \int_r^2 r \, dz \, dr \, d\theta$
- C. $\int_{0}^{2\pi} \int_{-2}^{2} \int_{r}^{2} r \, dz \, dr \, d\theta$

- D. $\int_0^{\pi} \int_0^2 \int_0^2 r \, dz \, dr \, d\theta$ E. $\int_0^{\frac{2\pi}{2}} \int_0^2 \int_0^2 r \, dz \, dr \, d\theta$.
- 38. If D is the solid region above the xy-plane that is between $z=\sqrt{4-x^2-y^2}$ and $z=\sqrt{1-x^2-y^2}$, then $\iiint_D \sqrt{x^2+y^2+z^2}\ dV=$
 - A. $\frac{14\pi}{3}$
- B. $\frac{16\pi}{3}$
- D. 8π
- E. 15π .

	1. $\vec{F}(x,y) = (xy^2 + 2)$ 2. $\vec{F}(x,y) = \frac{x}{y}\vec{i} + \frac{3}{x}\vec{j}$						
	3. $\vec{F}(x,y,z) = ye^z \vec{i} + (xe^z + e^y)\vec{j} + (xy+1)e^z \vec{k}$.						
	A. 1 and 2	B. 1 and 3	C. 2 and 3	D. 1 only	E. all three		
40.	40. Let \vec{F} be any vector field whose components have continuous partial derivatives up to second order, let f be any real valued function with continuous partial derivatives up to second order, and let $\nabla = \vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z}$. Find the incorrect statement.						
	A. $\operatorname{curl}(\operatorname{grad} f) = \vec{0}$		B. $\operatorname{div}(\operatorname{curl} \vec{F}) = 0$	С.	$\operatorname{grad}(\operatorname{div}\vec{F})=0$		
	D. curl $\vec{F} = \nabla \times \vec{F}$	E. div $\vec{F} =$	$\nabla \cdot ec{F}$				
41.	41. A wire lies on the xy-plane along the curve $y = x^2$, $0 \le x \le 2$. The mass density (per unit length) at any point (x, y) of the wire is equal to x. The mass of the wire is						
	A. $(17\sqrt{17} - 1)/12$		B. $(17\sqrt{17} - 1)/8$		C. $17\sqrt{17} - 1$		
	D. $(\sqrt{17} - 1)/3$	E. $(\sqrt{17} - 1)/2$	12				
42.	Evaluate $\int_C \vec{F} \cdot d\vec{r}$ whand from $(1,0)$ to $(1,$	here $\vec{F}(x,y) = y\vec{i} + i$ 2).	$x^2\vec{j}$ and C is composed of	of the line segments fro	om $(0,0)$ to $(1,0)$		
	A. 0	B. $\frac{2}{3}$	C. $\frac{5}{6}$	D. 2	E. 3		
43.	43. Evaluate the line integral $\int_C x dx + y dy + xy dz$						
	where C is parametri	zed by $\vec{r}(t) = \cos t\vec{i}$	$+\sin t\vec{j} + \cos t\vec{k} \text{ for } -\frac{\pi}{2}$	$\leq t \leq 0.$			
	A. 1	В. –1	C. $\frac{1}{3}$	D. $-\frac{1}{3}$	E. 0		
44.	 Are the following statements true or false? The line integral ∫_C (x³ + 2xy)dx + (x² - y²)dy is independent of path in the xy-plane. ∫_C(x³ + 2xy)dx + (x² - y²)dy = 0 for every closed oriented curve C in the xy-plane. There is a function f(x, y) defined in the xy-plane, such that grad f(x, y) = (x³ + 2xy)i + (x² - y²)j. 						
	A. all three are false D. 1 is true, 2 and 3		d 2 are false, 3 is true 2. all three are true	C. 1 and 2 a	re true, 3 is false		
45.	Evaluate $\int_C y^2 dx + 6x$ x = 4, in the counterest	axy dy where C is the clockwise direction.	ne boundary curve of the	e region bounded by y	$=\sqrt{x}, y=0 \text{ and }$		

39. Determine which of the vector fields below are conservative, i. e. $\vec{F} = \text{grad } f$ for some function f.

C. 8

A. 0

B. 4

D. 16

E. 32

	A. $8\sqrt{6}$	B. $\frac{8}{3}\sqrt{6}$	C. $\frac{8}{3}\sqrt{14}$	D. $\frac{\sqrt{14}}{3}$	E. $\frac{\sqrt{10}}{3}$		
50.	If Σ is the part of the paraboloid $z=x^2+y^2$ with $z\leq 4$, \vec{n} is the unit normal vector on Σ directed upward, and $\vec{F}(x,y,z)=x\vec{i}+y\vec{j}+z\vec{k}$, then $\iint_{\Sigma} \vec{F}\cdot\vec{n}dS=$						
	A. 0	B. 8π	C. 4π	D. -4π	E. -8π		
51.	51. If $\vec{F}(x,y,z) = \cos z\vec{i} + \sin z\vec{j} + xy\vec{k}$, Σ is the complete boundary of the rectangular solid region bounded by the planes $x=0,\ x=1,\ y=0,\ y=1,\ z=0$ and $z=\frac{\pi}{2}$, and \vec{n} is the outward unit normal on Σ , then $\iint_{\Sigma} \vec{F} \cdot \vec{n} dS =$						
	A. 0	B. $\frac{1}{2}$	C. 1	D. $\frac{\pi}{2}$	E. 2		
52.	52. If $\vec{F}(x,y,z) = x\vec{i} + y\vec{j} + z\vec{k}$, Σ is the unit sphere $x^2 + y^2 + z^2 = 1$ and \vec{n} is the outward unit normal on Σ , then $\iint_{\Sigma} \vec{F} \cdot \vec{n} dS =$						
	A. -4π	B. $\frac{2\pi}{3}$	C. 0	D. $\frac{4\pi}{3}$	E. 4π		
53. Use Stoke's theorem to evaluate $\iint_S \text{curl} \vec{F} \cdot d\vec{S}$, where $\vec{F}(x,y,z) = x^2 e^{yz} \vec{i} + y^2 e^{xz} \vec{j} + z^2 e^{xy} \vec{k},$							
and S is the hemisphere $x^2 + y^2 + z^2 = 4$, $z \ge 0$, oriented upward.							
	A. $-\pi/3$	B. 2π	C. 0	D. $\frac{4}{3}$	E. 2π		
54.	54. Use Stoke's theorem to evaluate $\int_C \vec{F} \cdot d\vec{r}$, where $\vec{F}(x,y,z) = x^2 z \vec{i} + x y^2 \vec{j} + z^2 \vec{k}.$						
	and C is the curve of intersection of the plane $x + y + z = 1$ and the cylinder $x^2 + y^2 = 9$ oriented counterclockwise as viewed from above.						
	A. $\frac{81\pi}{2}$	B. $\frac{\pi}{2}$	C. 1	D. $\frac{3\pi}{8}$	E. 9π		
			_				

46. If C goes along the x-axis from (0,0) to (1,0), then along $y=\sqrt{1-x^2}$ to (0,1), and then back to (0,0)

A. $-\int_0^1 \int_0^{\sqrt{1-x^2}} y \, dy \, dx$ B. $\int_0^1 \int_0^{\sqrt{1-x^2}} y \, dy \, dx$ C. $-\int_0^1 \int_0^{\sqrt{1-x^2}} x \, dy \, dx$ E. 0

47. Evaluate $\int_C \vec{F} \cdot d\vec{r}$, if $\vec{F}(x,y) = (xy^2 - 1)\vec{i} + (x^2y - x)\vec{j}$ and C is the circle of radius 1 centered at (1,2) and oriented counterclockwise.

C. 0

48. Green's theorem yields the following formula for the area of a simple region R in terms of a line integral

49. Evaluate the surface integral $\iint_{\Sigma} x \, dS$ where Σ is the part of the plane 2x + y + z = 4 in the first octant.

B. $\int_C y \, dx$ C. $\int_C x \, dx$ D. $\frac{1}{2} \int_C y \, dx - x \, dy$ E. $-\int x \, dy$

over the boundary C of R, oriented counterclockwise. Area of $R = \iint_R dA =$

E. -2

along the y-axis, then $\int_C xy dy =$

A. $-\int_C y \, dx$

ANSWERS

1-C, 2-A, 3-B, 4-B, 5-A, 6-D, 7-B, 8-D, 9-E, 10-B, 11-A, 12-E, 13-B, 14-B, 15-D, 16-C, 17-E 18-D, 19-A, 20-C, 21-E, 22-A, 23-D, 24-B, 25-E, 26-B, 27-C, 28-B, 29-E, 30-A, 31-B, 32-D, 33-B, 34-B, 35-A, 36-E, 37-B, 38-C, 39-B, 40-C, 41-A, 42-D, 43-D, 44-E, 45-D, 46-B, 47-D, 48-A, 49-B, 50-E, 51-A, 52-E, 53-C, 54-A