

3.1 \rightarrow Breath-first-search, we will start at the root node then explore each of its neighbors before going to its child node. We can't use recursive here for BFS but we should use queue. BFS is generally good for finding shortest path. Time complexity is $O(V+E)$ if we use adjacency list and $O(V^2)$ if we use adjacency matrix.

The order is a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q

+ Depth-first-search, we start at root then explore each branch completely before going to a different child node or next branch. DFS is ^{preferred} ~~used~~ if we want to visit each node in the graph (simpler than BFS). We use stack data structure to implement and recursive is also used. Time complexity is $O(V+E)$ if using adjacency list and $O(V^2)$ if we use adjacency matrix.

Order: a, b, d, e, c, f, h, l, m, q, i, g, j, n, o, k, p

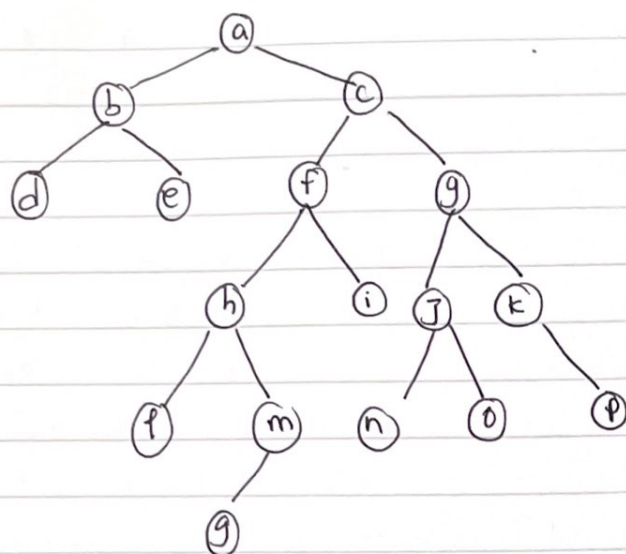
3.2 Clearly explain why algo work:

We are going to implement DFS in the problem. We will pick a vertex or node then we will go to ~~it node~~ explore that node in depth. If there are more than one node, we will pick the first node in an ascending order then alternate between the two child nodes until we get to the leaf vertex. At the leaf vertex, we will backtrack to get to the vertex that has ~~that other child~~ more than one child and pick the other child to go down (explore that child's node). We will continue until we reach the root node or starting node.

This ~~exec~~ will exactly crossing the tree twice because we will go depth on the child node until we reach the leaf node. From that leaf node, ~~from that~~ we backtrack all the way up to the node that has more than 1 child then choose that other child vertex. Continue this process, we will ensure that we cross each edge of tree exactly 5.

The runtime is $O(n)$ where n is # of nodes.

3.3



Clearly explain why diameters of above tree is 7 :

from root node a to b , we know the $\text{dist}(a, b) = 1$; hence, in the left branch of the tree the max dist is $\text{dist}(d, a) = \text{dist}(e, a) = 2$.

from the right branch, we could connect left and right branch of the tree through node a , from node a to h , $\text{dist}(a, h) = 3$ and from h , we could go down to g ; therefore, we would get max distance from the right node of $\max(a, g) = 5$ if we ~~put~~ get the distance from left to right node which is $\max \text{dist}(d, g)$ or $\max \text{dist}(e, g) = 5 + 2 = 7$

\therefore The maximum distance of x and y chosen all over is 7