Search for Heavy Neutral Leptons with IceCube DeepCore

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Colophon

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The source code of this thesis is available at:

https://github.com/LeanderFischer/phd_thesis

	Zusammenfassung
Zusammenfassung	

Abstract

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Add comparions of SM cross sections between NuXSSplMkr and genie	3
add information about the matter profile used	9
add information about the oscillation probability calculation and the software used for it	9
get correct final level rates from my pipeline(s)	9
add rate and poisson error for HNL samples	9
maybe just pick one mixing?	9
add 3D expectation and/or S/sqrt(B) plots	10
Do I want/need to include the description of the KDE muon estimation?	10
Add table with all systematic uncertainties used in this analysis (in the analysis chapter)	12
add final level effects of varying the axial mass parameters (or example of one)	12
add final level effects of varying the DIS parameter (or example of one)	12
put in asimov inject/recover plots for other masses in the appendix	13

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1.1 Model Independent Simulation

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- 1.1.3 Realistic Set
- 1.2 Model Specific Simulation

1.2 Wiodel Specific Simulation

1.2.1 Custom LeptonInjector

Signal events are simulated using a custom LeptonInjector (LI) tool [1], modified from its standard version to include the HNL particle and the description of the HNL decays needed to produce the double cascade signature (currently only ν_{τ} related). In its SM work mode, LI injects a lepton and a cascade (under the general name *Hadrons*) at the interaction vertex of the neutrino. Both objects have the same (x,y,z,t) coordinates. In the modified version, the lepton at the interaction vertex is replaced by the HNL. After a chosen distance the HNL is forced to decay. The decay is sampled from the kinematically accessible decay modes shown in Figure 1.2.

A big addition to the standard LI is that the decay products of the HNL are added to the list of particles in the I3MCTree with a displaced position and delayed time from the interaction vertex. These daughter particles form a second cascade, not in the form of a *Hadrons* object, but as the explicit particles forming the shower. The kinematics of the two-body decays are computed analytically, while the three-body decays are dealt with using MadGraph5. To do so, we randomly pick an event from a list that we generated for each three-body decay mode. Independent of the number of particles in the final state of the HNL decay, the kinematics are calculated/simulated at rest and then boosted along the HNL momentum. The decay mode is randomly chosen based on the mass dependent branching ratios shown in Figure 1.2.

Each file is produced by running the generation level processing script using the filenumber as random seed and the above settings for the sampling distributions. The main part is calling the *MultiLeptonInjector* module in *volume mode* adding two generators (for ν_{τ} and $\bar{\nu}_{\tau}$) with 50% of the events. The generators are provided with the custom double-differential/total cross section splines described in Section 1.2.1 and the parameters defining the sampling distributions. For each frame *OneWeight* and a reference weight are also calculated and stored using the weighting functions and a baseline atmospheric ν_{τ} flux + oscillation spline. The weight will later be calculated inside of the analysis framework

Re-write/re-formulate this section (copied from HNL technote).

[1]: Abbasi et al. (2021), "LeptonInjector and LeptonWeighter: A neutrino event generator and weighter for neutrino observatories"

Figure 1.1: Custom HNL total cross sections for the four target masses compared to the total $(\nu_{\tau}/\bar{\nu}_{\tau}$ neutral current) cross section used for SM neutrino simulation production with GENIE.

PISA, based on the input OneWeight. In addition to the i3 file itself, a LeptonInjector configuration file is written which stores the needed information to produce event weights using LeptonWeighter. Optionally the script can also produce an hdf5 file with the same name in the same location. This will store a fixed set of keys, extracted from the i3 file.

We are using *volume mode*, for the injection of the primary particle on a cylindrical volume. The main generation/sampling happens in VolumeLeptonInjector::DAQ inside

LeptonInjector.cxx. After writing the config (s) frame (currently not kept), the energy is sampled from a power law distribution, then the cosine(zenith) and azimuth angles are sampled from uniform distributions. The (x,y) position is sampled uniform in r, ϕ (for position on disk) and the z position is sampled from a uniform distribution. After the primary properties have been sampled the EventProperties is created and handed over to the FillTree functions which is where the custom HNL simulation happens:

add varied total cross-section for a few background HNL events

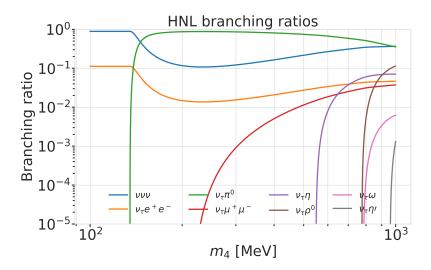
Cross Sections

The cross sections are calculated using a modified version of Carlos Argüelles' NuXSSplMkr, which is a tool to calculate neutrino cross sections from parton distribution functions (PDFs) and then produce splines that can be read and used with IceCube software. The main modification to calculate the cross sections for the ν_{τ} neutral current interaction into the new heavy mass state is the addition of a kinematic condition to ensure that there is sufficent energy to produce the heavy mass state. It is the same confition that needs to be fulfilled for the charged current case, where the outgoing lepton mass is non-zero. Following [2] (equation 7), the condition

$$(1 + x\delta_N)h^2 - (x + \delta_4)h + x\delta_4 \le 0, (1.1)$$

is implemented for the neutral current case. Here $\delta_4 = \frac{m_4^2}{s-M^2}$, $\delta_N = \frac{M^2}{s-M^2}$, and $h \stackrel{def}{=} xy + \delta_4$, with x,y being the Bjorken variables, m_4 and M the mass of the heavy state and the target nucleon, respectively, and s the center of mass energy squared. Since the (SM) neutrino background simulation used for this analysis was created using GENIE (version 2.12.8), interfaced through the IceCube software package *genie-icetray*, with the GRV98LO PDFs, those were added as $GRV98lo_patched$ to the

[2]: Levy (2009), "Cross-section and polarization of neutrino-produced tau's made simple"



Channel	Opens [MeV]	Max BR [%]
$v_4 \rightarrow v_\tau v_\alpha \bar{v_\alpha}$	0	100.0
$\nu_4 \rightarrow \nu_\tau e^+ e^-$	1	?
$\nu_4 \rightarrow \nu_\tau \pi^0$	135	?
$\nu_4 \rightarrow \nu_\tau \mu^+ \mu^-$	211	?
$\nu_4 \rightarrow \nu_{\tau} \eta$	548	?
$\nu_4 \rightarrow \nu_\tau \rho^0$	770	?
$\nu_4 \rightarrow \nu_\tau \omega$	783	?
$\nu_4 \to \nu_\tau \eta'$	958	?

Figure 1.2: Branching ratios of the HNL within the mass range considered, calculated based on the results from [3]. Given the existing constraints on $|U_{e4}|^2$ and $|U_{\mu4}|^2$, we consider that the corresponding decay modes are negligible.

Table 1.1: xx

cross section spline maker, to ensure the best possibe agreement. Double-differential (dsdxdy) and total (σ) cross sections were produced for the four target HNL masses and then splined. The produced cross section splines are stored in the resources of the custom LeptonInjector module. Figure 1.1 shows the total cross sections that were produced compared to the cross section used for the production of the SM $\nu_\tau/\bar{\nu}_\tau$ neutral current background simulation .

Add comparions of SM cross sections between NuXSS-plMkr and genie

Decay Channels

The accessible decay channels are dependent on the mass of the HNL and the allowed mixing. For this analysis, where only $|U_{\tau 4}|^2 \neq 0$, the considered decay channels are listed in Table 1.1 and the corresponding branching ratios are shown in Figure 1.2. The individual branching ratio for a specific mass is calculated as $\mathrm{BR}_i(m_4) = \Gamma_i(m_4)/\Gamma_{\mathrm{total}}(m_4)$, where $\Gamma_{\mathrm{total}}(m_4) = \sum \Gamma_i(m_4)$. The formulas to calculate the decay width show up in multiple references, but we chose to match them to [3], which also discusses the discrepencies in previous literature.

[3]: Coloma et al. (2021), "GeV-scale neutrinos: interactions with mesons and DUNE sensitivity"

2-Body Decay Widths The decay to a neutral pseudoscalar mesons is

$$\Gamma_{\nu_4 \to \nu_\tau P} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^3}{32\pi} f_P^2 (1 - x_p^2)^2, \tag{1.2}$$

with $x_P = m_P/m_4$ and

$$f_{\pi^0} = 0.130 \,\text{GeV}, \qquad f_{\eta} = 0.0816 \,\text{GeV}, \qquad C_2 = f_{\eta'} = -0.0946 \,\text{GeV},$$
(1.3)

while the decay to a neutral vector meson is given by

$$\Gamma_{\nu_4 \to \nu_\tau V} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^3}{32\pi} \left(\frac{f_V}{m_V}\right)^2 g_V^2 (1 + 2x_V^2) (1 - x_V^2)^2, \tag{1.4}$$

with $x_V = m_V/m_4$,

$$f_{\rho^0} = 0.171 \,\text{GeV}^2, \qquad f_{\omega} = 0.155 \,\text{GeV}^2,$$
 (1.5)

and

$$g_{\rho^0} = 1 - 2\sin^2\theta_w, \qquad g_{\omega} = \frac{-2\sin^2\theta_w}{3}, \qquad \sin^2\theta_w = 0.2229$$
 (1.6)

[4].

[4]: Tiesinga et al. (2021), "CODATA recommended values of the fundamental physical constants: 2018"

3-Body Decay Widths The (invisible) decay to three neutrinos is

$$\Gamma_{\nu_4 \to \nu_\tau \nu_\alpha \bar{\nu_\alpha}} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^5}{192\pi^3},\tag{1.7}$$

while the decay to two charged leptons (using $x_{\alpha} = (m_{\alpha}/m_4)^2$) of the same flavor reads

$$\Gamma_{\nu_4 \to \nu_\tau I_\alpha^+ I_\alpha^-} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^5}{192\pi^3} \left[C_1 f_1(x_\alpha) + C_2 f_2(x_\alpha) \right], \tag{1.8}$$

with the constants defined as

$$C_1 = \frac{1}{4}(1 - 4s_w^2 + 8s_w^4), \qquad C_2 = \frac{1}{2}(-s_w^2 + 2s_w^4),$$
 (1.9)

the functions as

$$f_1(x_\alpha) = (1 - 14x_\alpha - 2x_\alpha^2 - 12x_\alpha^3)\sqrt{1 - 4x_\alpha} + 12x_\alpha^2(x_\alpha^2 - 1)L(x_\alpha),$$
 (1.10)

$$f_2(x_\alpha) = 4[x_\alpha(2+10x_\alpha-12x_\alpha^2)\sqrt{1-4x_\alpha} + 6x_\alpha^2(1-2x_\alpha+2x_\alpha^2)L(x_\alpha)], \ (1.11)$$

and

$$L(x) = \ln\left(\frac{1 - 3x_{\alpha} - (1 - x_{\alpha})\sqrt{1 - 4x_{\alpha}}}{x_{\alpha}(1 + \sqrt{1 - 4x_{\alpha}})}\right). \tag{1.12}$$

1.2.2 MadGraph5 3-Body Decays

The code to produce the 3-body decay kinematics is MadGraph4 v3.4.0 based on the decay diagrams calculated with FeynRules 2.0 using the Lagrangians derived in [3]. The Universal FeynRules Outpur (UFO) from effective_HeavyN_Majorana_v103 were used for our calculation. For each meass and corresponding decay channel, we produce 1e06 decay kinematic variations (rest frame) and store those in a text file.

[3]: Coloma et al. (2021), "GeV-scale neutrinos: interactions with mesons and DUNE sensitivity"

variable distribution range $[2, 10^4]$ GeV energy [180°, 80°] zenith uniform (in $cos(\theta)$) azimuth [0°, 360°] uniform vertex (x, y)uniform $r = 600 \, \text{m}$ vertex z uniform [-600, 0] m [0.3, 0.6, 1.0] GeV fixed m_{HNL} L^{-1} $[0.0004, 1000.0] \,\mathrm{m} / [1.0, 1000.0] \,\mathrm{m}$ $L_{\rm decay}$

Table 1.2: Sampling distributions of HNL simulation generation.

1.2.3 Sampling Distributions

This is the description of the signal simulation generator used to (re-)start simulation production in December 2023. The underlying sampling distributions are listed in Table 1.2. Judging from how the generation/processing efficiency was for the 190607 set, we target 1e04 files per set with 5e05 events per file at generation, resulting in a maximum of 5e09 events per set at generation level. Note here that the actual number of events per set at generation might be a little lower since some events won't be allowed if they don't have enough energy to produce the HNL.

1.2.4 Weighting Scheme

The weighting for the HNL signal simulation happens in a custom stage of PISA. The only input is the stored OneWeight and the variable physics parameter $|U_{\tau 4}|^2$, which is the mixing strength of the new heavy mass state and the tau sector. The custom re-weighting is needed to go from the used sampling PDF (1/L with fixed range in lab frame decay length) to the target PDF (exponential defined by proper lifetime of the HNL). For each event the re-weighting factor is calculated using the gamma factor

$$\gamma = \frac{\sqrt{E_{\rm kin}^2 + m_{\rm HNL}^2}}{m_{\rm HNL}},\tag{1.13}$$

with the HNL mass $m_{\rm HNL}$ and it's kinetic energy $E_{\rm kin}$. The speed of the HNL is calculated as

$$v = c \cdot \sqrt{1 - \frac{1}{\gamma^2}},\tag{1.14}$$

where c is the speed of light. With these the lab frame decay length range can be converted into the rest frame lifetime range for each event

$$\tau_{\min/\max} = \frac{s_{\min/\max}}{v \cdot \gamma}.$$
 (1.15)

The proper lifetime of each HNL event can be calculated using the total decay width Γ_{total} shown in Figure ?? and the chosen mixing strength $|U_{\tau 4}|^2$ as

$$\tau_{\text{proper}} = \frac{\hbar}{\Gamma_{\text{total}}(m_{\text{HNL}}) \cdot |U_{\tau 4}|^2},$$
(1.16)

where \hbar is the reduced Planck constant. Since the decay length/lifetime of the events is sampled from an inverse distribution instead of an exponential as it would be expected from a particle decay we have to re-weight accordingly to achieve the correct decay length/lifetime

distribution. This is done by using the wanted exponential distribution

$$PDF_{exp} = \frac{1}{\tau_{proper}} \cdot e^{\frac{-\tau}{\tau_{proper}}}, \qquad (1.17)$$

and the inverse distribution that was sampled from

$$PDF_{inv} = \frac{1}{\tau \cdot (\ln(\tau_{max}) - \ln(\tau_{min}))}.$$
 (1.18)

The lifetime re-weighting factor is calculated as

$$w_{\text{lifetime}} = \frac{\text{PDF}_{\text{exp}}}{\text{PDF}_{\text{inv}}} = \frac{\Gamma_{\text{total}}(m_{\text{HNL}}) \cdot |U_{\tau 4}|^2}{\hbar} \cdot \tau \cdot (\ln(\tau_{\text{max}}) - \ln(\tau_{\text{min}})) \cdot e^{\frac{-\tau}{\tau_{\text{proper}}}}.$$
(1.19)

Adding another factor of $|U_{\tau 4}|^2$ to account for the mixing at the interaction vertex the total re-weighting factor becomes

$$w_{\text{total}} = |U_{\tau 4}|^2 \cdot w_{\text{lifetime}}, \tag{1.20}$$

which can be applied on top of flux and oscillation weight to get the final HNL weight for a given mixing (and mass).

1.3 Model Dependent Simulation Distributions

1.3.1 Generation Level

1.3.2 Final Level

Detecting Low Energetic Double Cascades 2

2.1 Reconstruction	Reconstruction
2.1.1 Table-Based Minimum Likelihood Algorithms	
2.1.2 Double Cascade Hypothesis	
2.1.3 Modification to Low Energy Events	
2.2 Performance	
2.2.1 Energy/Decay Length Resolution	
2.2.2 Double Cascade Classification	

The measurement performed in this thesis is the search for an excess of
HNL events in the 10 years of IceCube DeepCore data. In principle the
two physics parameters to be probed are the mass of the HNL, m_4 , and the
mixing between the fourth heavy mass state and the SM $ au$ sector, $ U_{ au 4} ^2$
Since the mass itself influences the production and decay kinematics
of the event and the accessible decay modes, individual mass sets were
produced as described in Section 1.2. The mass slightly influences the
energy distribution, while the mixing both changes the overall scale of the
HNL events and the shape in energy and PID. IceCube DeepCore is suited
to measure the excess which appears around and below 20 GeV, due to
its production from the atmospheric tau neutrinos, although a reduced
lower energy threshold could improve the analysis. The measurement
will be performed for the three mass sets individually, while the mixing
is the parameter that can be varied continuously and will be measured
in the fit.

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3.4	Results

3.1 Final Level Sample

The final level sample of this analysis always consists of the neutrino and muon MC introduced in Section ?? and one of the three HNL samples explained in Section 1.2. All of those simulation sets and the 10 years of IceCube DeepCore data are processed through the full processing and event selection chain described in Section ?? leading to the final level sample. Since applying the last cuts from Section ?? leaves an insignificant amount of pure noise events in the sample, the noise simulation is not included in the analysis and won't be listed here.

3.1.1 Expected Rates/Events

The rates and the expected events in 10 years are shown in Table 3.1. For the HNL the expectation depends on the mass and the mixing. Shown here are two example mixings for all the three masses. A mixing of 0.0 would result in a rate of 0.0 and therefore no HNL events.

Type	Rate [mHz]	Events (in 10 years)		
v_{μ}^{CC}	0.3522	103063 ± 113		
ν ^μ ν ^{CC} ν ^{CC}	0.1411	41299 <u>+</u> 69		
v_{τ}^{CC}	0.0348	10187 ± 22		
$\nu_{ m NC}$	0.0667	968 ± 57		
μ	0.0033	19522 ± 47		
HNL		$ U_{\tau 4} ^2 = 10^{-3}$	$ U_{\tau 4} ^2 = 10^{-1}$	
m_4 =0.3 GeV	x.xxx	2.5	1342.5	
$m_4 = 0.6 \text{GeV}$	X.XXX	9.0	1207.0	
m_4 =1.0 GeV	x.xxx	9.6	966.5	

add information about the matter profile used

add information about the oscillation probability calculation and the software used for it

get correct final level rates from my pipeline(s)

add rate and poisson error for HNL samples

maybe just pick one mixing?

Table 3.1: Final level rates and event expectation of the SM background particle types and the HNL signal for all three masses and two example mixing values.

Table 3.2: Three dimensional binning used in the analysis. All variables are from the FLERCNN reconstruction explained in Section ??.

Variable	$N_{ m bins}$	Edges	Step
P_{ν}	3	[0.00, 0.25, 0.55, 1.00]	linear
E	12	[5.00, 100.00]	logarithmic
$\cos(\theta)$	8	[-1.00, 0.04]	linear

3.1.2 Analysis Binning

[5]: Yu et al. (2023), "Recent neutrino oscillation result with the IceCube experiment"

The identical binning to the analysis performed in [5] is used. It was chosen such that the track-like bin has the largest ν_{μ} -CC fraction. Extend the binning towards lower energies or increasing the number of bins did not improve the HNL sensitivities significantly. It also has to be considered that sufficient data events need to end up in the individual bins to result in a good fit, which was already investigated in the previous analysis. To mitigate the low data statistics, a few bins were not taken into account in the analysis. There are three bins in PID (cascade-like, mixed and track-like), 12 bins in reconstructed energy, and 8 bins in cosine of the reconstructed zenith angle as specified in Table 3.2. Originally, there were two more bins in $\cos(\theta)$, which were removed to reduce muons coming from the horizon and some low energy bins in the cascade-like bin are removed due to the low event expectation.

add 3D expectation and/or S/sqrt(B) plots

3.2 Statistical Analysis

3.2.1 Test Statistic

The measurements are performed by comparing the weighted MC to the data. Through variation of the nuisance and physics parameters that govern the weights, the best matching set of parameters can be found. The comparison is done using a modified χ^2 defined as

$$\chi^{2}_{\text{mod}} = \sum_{i \in \text{bins}} \frac{(N_{i}^{\nu} + N_{i}^{\mu} + N_{i}^{\text{HNL}} - N_{i}^{\text{obs}})^{2}}{N_{i}^{\nu} + N_{i}^{\mu} + N_{i}^{\text{HNL}} + (\sigma_{i}^{\nu})^{2} + (\sigma_{i}^{\mu})^{2} + (\sigma_{i}^{\text{HNL}})^{2}} + \sum_{j \in \text{syst}} \frac{(s_{j} - \hat{s_{j}})^{2}}{\sigma_{s_{j}}^{2}},$$
(3.1)

as the test statistic (TS), where N_i^{ν} , N_i^{μ} , and N_i^{HNL} are the expected number of events in bin i from neutrinos, atmospheric muons, and HNL, while N_i^{obs} is the observed number of events in bin i. The expected number of events from each particle type is calculated by summing the weights of all events in the bin $N_i^{\text{type}} = \sum_i^{\text{type}} \omega_i$, with the statistical uncertainty being $(\sigma_i^{\text{type}})^2 = \sum_i^{\text{type}} \omega_i^2$. The expected Poisson error is calculated using the combined expectation of neutrinos, atmospheric muons, and HNL events. The additional term in Equation 3.1 is included to apply a penalty term for prior knowledge of the systematic uncertainties of the parameters where they are known. s_j are the systematic parameters that are varied in the fit, while $\hat{s_j}$ are their nominal values and σ_{s_j} are the known uncertainties.

Do I want/need to include the description of the KDE muon estimation?

3.2.2 Systematic Uncertainties

Treatment of Detector Response Uncertainties via a Likelihood-Free Inference Method

[6]: Fischer et al. (2023), "Treating detector systematics via a likelihood free inference method"

Copy paste from OVS PRD about hypersurfaces (and interpolation of those):

To evaluate the expected impact of detection uncertainties, data sets are produced with different variations of detector response, processed to the final level of selection, and then they are parameterized following a model of the uncertainties to evaluate how the final sample would look like for any reasonable choice of parameters. The parametrizations are done at the analysis bin level, assuming that every effect considered is independent and that they can be approximated by a linear function. Under these assumptions we can compute a reweighting factor in every bin that depends on N parameters, which correspond to the number of systematic effects being considered, plus an offset c, as

$$f(p_1, ..., p_N) = c + \sum_{n=1}^{N} m_n \Delta p_n.$$
 (3.2)

Here m_n are the reweighting factors obtained from simulation sets with a systematic variation and Δp_n is the test value of a specific systematic variation.

The fit of the parameters m_n is done over all systematic MC sets, reducing the uncertainty on the MC prediction in each bin as a side effect since the error on the fitted function is smaller than the statistical error from the nominal MC set. The set of all fitted functions in all histogram bins are called "hypersurfaces". An example of such a fit from a single bin, projected onto one dimension, is shown in Fig. ??.

The event counts coming from different flavors and interactions have a different response to varying the same detector parameter. Therefore, the hypersurfaces in each bin are fit separately for three groups of events:

- $(\nu_{\text{all}} + \bar{\nu}_{\text{all}})$ NC + $(\nu_e + \bar{\nu}_e)$ CC: These events all produce cascade signatures in the detector.
- $(\nu_{\tau} + \bar{\nu}_{\tau})$ CC: These interactions may differ from the previous group because they have a production threshold of $E_{\nu} \gtrsim 3.5$ GeV and also produce muons with a branching ratio of 17%.
- $(\nu_{\mu} + \bar{\nu}_{\mu})$ CC: These interactions produce track-like signatures.

The distribution of $\chi^2/d.o.f.$ from the fits in all analysis bins is used as a diagnostic to ensure that the fitted, linear hypersurfaces provide a good estimate for the expected number of events for the full range of simulated detector configurations. We find that the means of these $\chi^2/d.o.f.$ distributions are all consistent with 1.0 as expected from good fits for each of the three categories described above (NC + ν_e CC, ν_τ CC and ν_μ CC). Attempts to use higher order polynomial fits did not yield a significantly improved $\chi^2/d.o.f.$, and in fact often rendered the fits less stable.

To produce the histograms for fitting the hypersurfaces, a choice must be made for the values of flux, cross section and oscillation parameters. We found that the hypersurface fits are sensitive to the choice of parameters that have correlations with the effect they encode. Most notably, this effect is observed between the mass splitting and DOM optical efficiency as demonstrated in Fig. ??, which shows the difference between fitted

hypersurface gradients for the DOM efficiency dimension for two values of Δm_{32}^2 .

This problem arises because we are only fitting the hypersurfaces in reconstructed phase space, without accounting for the different true energy and zenith distributions of MC in each analysis bin, which change with each detector systematic variation. To mitigate this problem, we fit the hypersurfaces for 20 different values in mass splitting between $1.5 \times 10^{-3} \, \mathrm{eV^2}$ and $3.5 \times 10^{-3} \, \mathrm{eV^2}$, and then apply a piece-wise linear interpolation to all slopes, intercepts and covariance matrix elements. The oscillation parameter fit can then dynamically adapt the hypersurfaces for each value of Δm_{32}^2 that is tested using these interpolated functions. The effects of other parameter choices were evaluated as well, but none were found to introduce a significant bias.

Free Parameter Selection

Copy paste from OVS PRD about systematic impact test:

We decide which systematic uncertainties must be included in the fit by studying the potential bias they would produce in the oscillation parameters and the change on the test statistic $\chi^2_{\rm mod}$ if we neglected them. We create data sets with their observed quantities set equal to their expected values for a wide range of values for θ_{23} and Δm^2_{32} and perform two fits: one where the oscillation parameters are fixed to their true value and one where they are left free. In both fits, the systematic parameter being tested is fixed to a value off from its nominal expectation by either 1σ or by an educated guess, if the uncertainty is not well-defined. Parameters are included in the analysis when this test creates a significant bias in the oscillation parameters, which is conservatively defined as a difference larger than 2×10^{-2} between the test statistics of the two fits.

Copy paste from OVS PRD about detector systematic nominal, prior, and ranges:

As motivated in Section ??, the DOM efficiency is constrained by a Gaussian prior to the value of 1.0 ± 0.1 . The ice model parameters are unconstrained in the fit, and allowed to vary within conservative ranges determined from calibration data. The hole ice model parameters are bounded within the ranges $-2.0 < p_0 < 1.0$ and $-0.2 < p_1 < 0.2$. The bulk ice model parameters are bounded within -0.90 < Absorption < 1.10 and -0.95 < Scattering < 1.15.

Add table with all systematic uncertainties used in this analysis (in the analysis chapter).

add final level effects of varying the axial mass parameters (or example of one)

add final level effects of varying the DIS parameter (or example of one)

3.3 Analysis Checks

Fitting to data will be performed in a *blind* manner, where the analyzer does not immediately see the fitted physics and nuisance parameter values, but first checks that a set of pre-defined *goodness of fit (GOF)* criteria are fulfilled. If those criteria are met to satisfaction the fit results are unblinded and the full result can be revealed. Before these blind fits to data are run, the robustness of the analysis method is tested using pseudo-data that is generated using the MC sets.

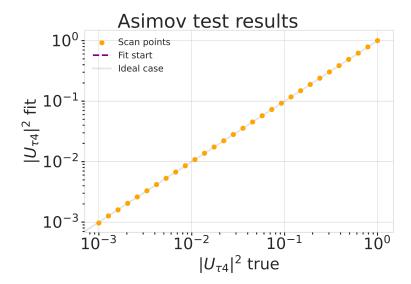


Figure 3.1: Asimov inject/recover test for the $0.6\,\text{GeV}$ mass set. Mixing values between 10^{-3} and 10^{0} are injected and fit back with the full analysis chain. The injected parameter is alwasy recovered within the statistical uncertainty.

3.3.1 Asimov Inject/Recover Tests

- descibe used minimizer and minimization routine minimize the modified χ^2 TS describe the Asimov data set (no statistical fluctuations) without fluctuations the fit is always expected to recover the injected parameters Figure 3.1
- 3.3.2 Sensitivity
- 3.3.3 Ensemble Tests
- 3.4 Results
- 3.4.1 Best Fit Parameters
- 3.4.2 Upper Limits
- 3.4.3 Post-Fit Data/MC Agreement

put in asimov inject/recover plots for other masses in the appendix

Bibliography

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