

# **Search for Heavy Neutral Leptons with the IceCube DeepCore**

## **Dissertation**

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**Colophon**

This document was typeset with the help of KOMA-Script and L<sup>A</sup>T<sub>E</sub>X using the open-source kaobook template class.

The source code of this thesis is available at:

[https://github.com/LeanderFischer/phd\\_thesis](https://github.com/LeanderFischer/phd_thesis)

## **Zusammenfassung**

Zusammenfassung ...

## **Abstract**

Abstract ...



# Todo list

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| Add comparions of SM cross sections between NuXSplMkr and genie . . . . .          | 11 |
| Add description of MadGraph5 decay files (Harvard needs to provide this) . . . . . | 12 |



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# Introduction

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Introduction ... + test reference [1]



## 2.1 Standard Model Particles

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### 2.1.2 Charged Fermion Masses

### 2.1.3 Neutrino Masses

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Majorana

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# Beyond the Standard Model

## Neutrinos

# 3

### 3.1 Neutrino Oscillations

#### 3.1.1 Vacuum Oscillations

#### 3.1.2 Oscillations in Matter

#### 3.1.3 Atmospheric Neutrino Oscillations

Neutrino Production in the Atmosphere

Oscillations of Atmospheric Neutrinos

Matter Effects

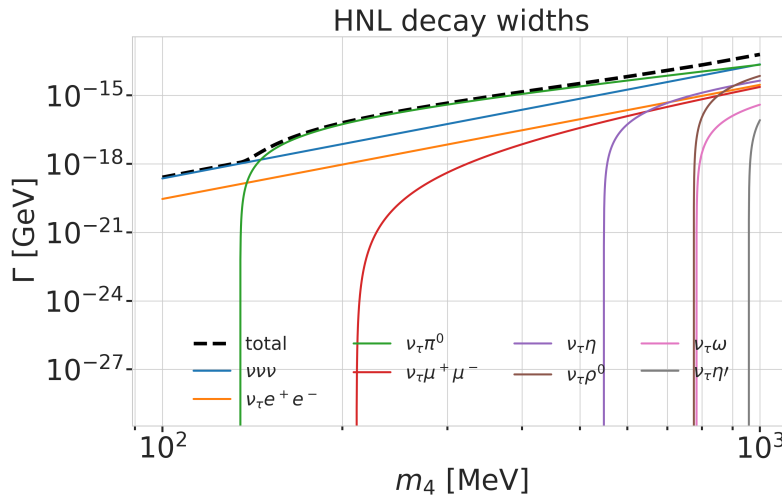
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#### 3.2.2 Extending the Standard Model

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**Figure 3.1:** Decay widths of the HNL within the mass range considered, calculated based on the results from [2]. Given the existing constraints on  $|U_{e4}|^2$  and  $|U_{\mu 4}|^2$ , we consider that the corresponding decay modes are negligible.

### **3.3 Open Questions in Neutrino Particle Physics**

# The IceCube Neutrino Observatory

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## 4.1 The IceCube In-Ice Array

### 4.1.1 In-Ice Array

DeepCore

### 4.1.2 IceTop

### 4.1.3 Digital Optical Modules

## 4.2 Propagation of particles in ice

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# Heavy Neutral Lepton Signal Simulation

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## 5.1 Model Independent Simulation

### 5.1.1 Generator Functions

### 5.1.2 Simplistic Sets

### 5.1.3 Realistic Set

## 5.2 Model Specific Simulation

### 5.2.1 Custom LeptonInjector

Signal events are simulated using a **custom LeptonInjector (LI) tool** [3], modified from its standard version to include the HNL particle and the description of the HNL decays needed to produce the double cascade signature (currently only  $\nu_\tau$  related). In its SM work mode, LI injects a lepton and a cascade (under the general name *Hadrons*) at the interaction vertex of the neutrino. Both objects have the same (x,y,z,t) coordinates. In the modified version, the lepton at the interaction vertex is replaced by the HNL. After a chosen distance the HNL is forced to decay. The decay is sampled from the kinematically accessible decay modes shown in Figure 5.2.

A big addition to the standard LI is that the decay products of the HNL are added to the list of particles in the I3MCTree with a displaced position and delayed time from the interaction vertex. These daughter particles form a second cascade, not in the form of a *Hadrons* object, but as the explicit particles forming the shower. The kinematics of the two-body decays are computed analytically, while the three-body decays are dealt with using MadGraph5. To do so, we randomly pick an event from a list that we generated for each three-body decay mode. Independent of the number of particles in the final state of the HNL decay, the kinematics are calculated/simulated at rest and then boosted along the HNL momentum. The decay mode is randomly chosen based on the mass dependent branching ratios shown in Figure 5.2.

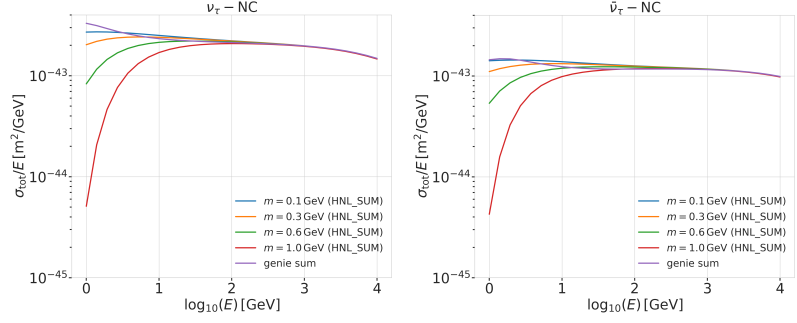
Each file is produced by running the **generation level processing script** using the filename as random seed and the above settings for the sampling distributions. The main part is calling the *MultiLeptonInjector* module in *volume mode* adding two generators (for  $\nu_\tau$  and  $\bar{\nu}_\tau$ ) with 50% of the events. The generators are provided with the custom double-differential/total cross section splines described in Section 5.2.1 and the parameters defining the sampling distributions. For each frame *OneWeight* and a reference weight are also calculated and stored using the **weighting functions** and a baseline atmospheric  $\nu_\tau$  flux + oscillation spline. The weight will later be calculated inside of the analysis framework

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Re-write/re-formulate this section (copied from HNL technote).

[3]: Abbasi et al. (2021), *LeptonInjector and LeptonWeighter: A neutrino event generator and weighter for neutrino observatories*

**Figure 5.1:** Custom HNL total cross sections for the four target masses compared to the total ( $\nu_\tau/\bar{\nu}_\tau$  neutral current) cross section used for SM neutrino simulation production with GENIE.



**PISA**, based on the input OneWeight. In addition to the i3 file itself, a LeptonInjector configuration file is written which stores the needed information to produce event weights using LeptonWeighter. Optionally the script can also produce an hdf5 file with the same name in the same location. This will store a fixed set of keys, extracted from the i3 file.

We are using *volume mode*, for the injection of the primary particle on a cylindrical volume. The main generation/sampling happens in `VolumeLeptonInjector::DAQ` inside

`LeptonInjector.cxx`. After writing the config (s) frame (currently not kept), the energy is sampled from a power law distribution, then the cosine(zenith) and azimuth angles are sampled from uniform distributions. The (x,y) position is sampled uniform in  $r, \phi$  (for position on disk) and the z position is sampled from a uniform distribution. After the primary properties have been sampled the *EventProperties* is created and handed over to the `FillTree` functions which is where the custom HNL simulation happens:

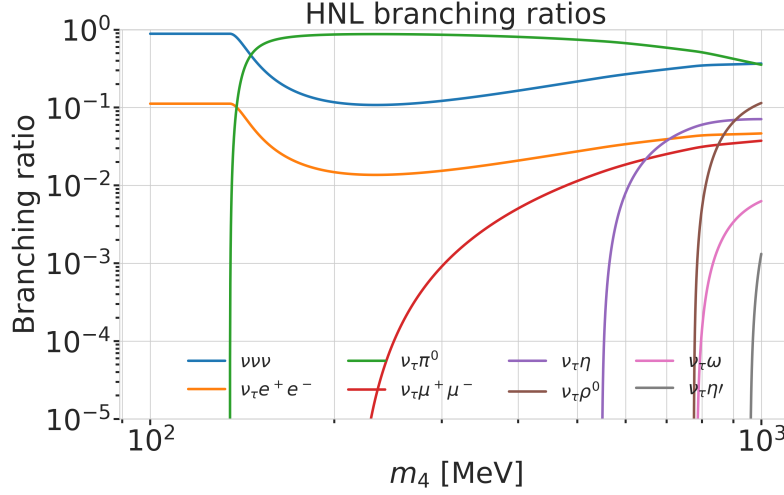
## Cross Sections

The cross sections are calculated using a **modified version** of Carlos Argüelles' **NuXSplMkr**, which is a tool to calculate neutrino cross sections from parton distribution functions (PDFs) and then produce splines that can be read and used with IceCube software. The main modification to calculate the cross sections for the  $\nu_\tau$  neutral current interaction into the new heavy mass state is the addition of a kinematic condition to ensure that there is sufficient energy to produce the heavy mass state. It is the same condition that needs to be fulfilled for the charged current case, where the outgoing lepton mass is non-zero. Following [4] (equation 7), the condition

$$(1 + x\delta_N)h^2 - (x + \delta_4)h + x\delta_4 \leq 0, \quad (5.1)$$

is implemented for the neutral current case. Here  $\delta_4 = \frac{m_4^2}{s-M^2}$ ,  $\delta_N = \frac{M^2}{s-M^2}$ , and  $h \stackrel{\text{def}}{=} xy + \delta_4$ , with  $x, y$  being the Bjorken variables,  $m_4$  and  $M$  the mass of the heavy state and the target nucleon, respectively, and  $s$  the center of mass energy squared. Since the (SM) neutrino background simulation used for this analysis was created using GENIE (version 2.12.8), interfaced through the IceCube software package *genie-icetray*, with the **GRV98LO** PDFs, those were added as *GRV98lo\_patched* to the cross section spline maker, to ensure the best possible agreement. Double-differential ( $dsdx dy$ ) and total ( $\sigma$ ) cross sections were produced for the

[4]: Levy (2009), *Cross-section and polarization of neutrino-produced tau's made simple*



**Figure 5.2:** Branching ratios of the HNL within the mass range considered, calculated based on the results from [2]. Given the existing constraints on  $|U_{e4}|^2$  and  $|U_{\mu4}|^2$ , we consider that the corresponding decay modes are negligible.

| Channel  | Opens [MeV] | Max BR [%] |
|--|-------------|------------|
| $\nu_4 \rightarrow \nu_\tau \nu_\alpha \bar{\nu}_\alpha$ | 0           | 100.0      |
| $\nu_4 \rightarrow \nu_\tau e^+ e^-$                     | 1           | ?          |
| $\nu_4 \rightarrow \nu_\tau \pi^0$                       | 135         | ?          |
| $\nu_4 \rightarrow \nu_\tau \mu^+ \mu^-$                 | 211         | ?          |
| $\nu_4 \rightarrow \nu_\tau \eta$                        | 548         | ?          |
| $\nu_4 \rightarrow \nu_\tau \rho^0$                      | 770         | ?          |
| $\nu_4 \rightarrow \nu_\tau \omega$                      | 783         | ?          |
| $\nu_4 \rightarrow \nu_\tau \eta'$                       | 958         | ?          |

**Table 5.1:** xx

four target HNL masses and then splined. The produced cross section splines are stored in the resources of the custom **LeptonInjector** module. Figure 5.1 shows the total cross sections that were produced compared to the cross section used for the production of the SM  $\nu_\tau/\bar{\nu}_\tau$  neutral current background simulation.

Add comparisons of SM cross sections between NuXSS-plMkr and genie

### Decay Channels

The accessible decay channels are dependent on the mass of the HNL and the allowed mixing. For this analysis, where only  $|U_{\tau4}|^2 \neq 0$ , the considered decay channels are listed in Table 5.1 and the corresponding branching ratios are shown in Figure 5.2. The individual branching ratio for a specific mass is calculated as  $BR_i(m_4) = \Gamma_i(m_4)/\Gamma_{\text{total}}(m_4)$ , where  $\Gamma_{\text{total}}(m_4) = \sum \Gamma_i(m_4)$ . The formulas to calculate the decay width show up in multiple references, but we chose to match them to [2], which also discusses the discrepancies in previous literature.

[2]: Coloma et al. (2021), *GeV-scale neutrinos: interactions with mesons and DUNE sensitivity*

**2-Body Decay Widths** The decay to a neutral pseudoscalar mesons is

$$\Gamma_{\nu_4 \rightarrow \nu_\tau P} = |U_{\tau4}|^2 \frac{G_F^2 m_4^3}{32\pi} f_P^2 (1 - x_P^2)^2, \quad (5.2)$$

with  $x_P = m_P/m_4$  and

$$f_{\pi^0} = 0.130 \text{ GeV}, \quad f_\eta = 0.0816 \text{ GeV}, \quad C_2 = f_{\eta'} = -0.0946 \text{ GeV}, \quad (5.3)$$

while the decay to a neutral vector meson is given by

$$\Gamma_{\nu_4 \rightarrow \nu_\tau V} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^3}{32\pi} \left( \frac{f_V}{m_V} \right)^2 g_V^2 (1 + 2x_V^2)(1 - x_V^2)^2, \quad (5.4)$$

with  $x_V = m_V/m_4$ ,

$$f_{\rho^0} = 0.171 \text{ GeV}^2, \quad f_\omega = 0.155 \text{ GeV}^2, \quad (5.5)$$

and

$$g_{\rho^0} = 1 - 2 \sin^2 \theta_w, \quad g_\omega = \frac{-2 \sin^2 \theta_w}{3}, \quad \sin^2 \theta_w = 0.2229 \quad (5.6)$$

[5]: Tiesinga et al. (2021), CODATA recommended values of the fundamental physical constants: 2018

[5].

**3-Body Decay Widths** The (invisible) decay to three neutrinos is

$$\Gamma_{\nu_4 \rightarrow \nu_\tau \nu_\alpha \bar{\nu}_\alpha} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^5}{192\pi^3}, \quad (5.7)$$

while the decay to two charged leptons (using  $x_\alpha = (m_\alpha/m_4)^2$ ) of the same flavor reads

$$\Gamma_{\nu_4 \rightarrow \nu_\tau l_\alpha^+ l_\alpha^-} = |U_{\tau 4}|^2 \frac{G_F^2 m_4^5}{192\pi^3} [C_1 f_1(x_\alpha) + C_2 f_2(x_\alpha)], \quad (5.8)$$

with the constants defined as

$$C_1 = \frac{1}{4}(1 - 4s_w^2 + 8s_w^4), \quad C_2 = \frac{1}{2}(-s_w^2 + 2s_w^4), \quad (5.9)$$

the functions as

$$f_1(x_\alpha) = (1 - 14x_\alpha - 2x_\alpha^2 - 12x_\alpha^3)\sqrt{1 - 4x_\alpha} + 12x_\alpha^2(x_\alpha^2 - 1)L(x_\alpha), \quad (5.10)$$

$$f_2(x_\alpha) = 4[x_\alpha(2 + 10x_\alpha - 12x_\alpha^2)\sqrt{1 - 4x_\alpha} + 6x_\alpha^2(1 - 2x_\alpha + 2x_\alpha^2)L(x_\alpha)], \quad (5.11)$$

and

$$L(x) = \ln \left( \frac{1 - 3x_\alpha - (1 - x_\alpha)\sqrt{1 - 4x_\alpha}}{x_\alpha(1 + \sqrt{1 - 4x_\alpha})} \right). \quad (5.12)$$

Add description of Mad-Graph5 decay files (Harvard needs to provide this)

### Madgraph 3-body Decay Kinematics

## 5.2.2 Sampling Distributions

This is the description of the signal simulation generator used to (re-)start simulation production in December 2023. The underlying sampling distributions are listed in Table 5.2. Judging from how the generation/processing efficiency was for the 190607 set, we target 1e04 files per set with 5e05 events per file at generation, resulting in a maximum of 5e09 events per set at generation level. Note here that the actual number of events



| variable           | distribution                 | range                                    |
|--------------------|------------------------------|--|
| energy             | $E^{-2}$                     | $[2, 10^4]$ GeV                          |
| zenith             | uniform (in $\cos(\theta)$ ) | $[180^\circ, 80^\circ]$                  |
| azimuth            | uniform                      | $[0^\circ, 360^\circ]$                   |
| vertex $(x, y)$    | uniform                      | $r = 600$ m                              |
| vertex $z$         | uniform                      | $[-600, 0]$ m                            |
| $m_{\text{HNL}}$   | fixed                        | $[0.3, 0.6, 1.0]$ GeV                    |
| $L_{\text{decay}}$ | $L^{-1}$                     | $[0.0004, 1000.0]$ m / $[1.0, 1000.0]$ m |

**Table 5.2:** Sampling distributions of HNL simulation generation.

per set at generation might be a little lower since some events won't be allowed if they don't have enough energy to produce the HNL.

### 5.2.3 Weighting Scheme

The weighting for the HNL signal simulation happens in a **custom stage of PISA**. The only input is the stored OneWeight and the variable physics parameter  $|U_{\tau 4}|^2$ , which is the mixing strength of the new heavy mass state and the tau sector. The custom re-weighting is needed to go from the used sampling PDF (1/L with fixed range in lab frame decay length) to the target PDF (exponential defined by proper lifetime of the HNL). For each event the re-weighting factor is calculated using the gamma factor

$$\gamma = \frac{\sqrt{E_{\text{kin}}^2 + m_{\text{HNL}}^2}}{m_{\text{HNL}}}, \quad (5.13)$$

with the HNL mass  $m_{\text{HNL}}$  and it's kinetic energy  $E_{\text{kin}}$ . The speed of the HNL is calculated as

$$v = c \cdot \sqrt{1 - \frac{1}{\gamma^2}}, \quad (5.14)$$

where  $c$  is the speed of light. With these the lab frame decay length range can be converted into the rest frame lifetime range for each event

$$\tau_{\text{min/max}} = \frac{s_{\text{min/max}}}{v \cdot \gamma}. \quad (5.15)$$

The proper lifetime of each HNL event can be calculated using the total decay width  $\Gamma_{\text{total}}$  shown in Figure 3.1 and the chosen mixing strength  $|U_{\tau 4}|^2$  as

$$\tau_{\text{proper}} = \frac{\hbar}{\Gamma_{\text{total}}(m_{\text{HNL}}) \cdot |U_{\tau 4}|^2}, \quad (5.16)$$

where  $\hbar$  is the reduced Planck constant. Since the decay length/lifetime of the events is sampled from an inverse distribution instead of an exponential as it would be expected from a particle decay we have to re-weight accordingly to achieve the correct decay length/lifetime distribution. This is done by using the wanted exponential distribution

$$\text{PDF}_{\text{exp}} = \frac{1}{\tau_{\text{proper}}} \cdot e^{-\frac{\tau}{\tau_{\text{proper}}}}, \quad (5.17)$$

and the inverse distribution that was sampled from

$$\text{PDF}_{\text{inv}} = \frac{1}{\tau \cdot (\ln(\tau_{\text{max}}) - \ln(\tau_{\text{min}}))}. \quad (5.18)$$

The lifetime re-weighting factor is calculated as

$$w_{\text{lifetime}} = \frac{\text{PDF}_{\text{exp}}}{\text{PDF}_{\text{inv}}} = \frac{\Gamma_{\text{total}}(m_{\text{HNL}}) \cdot |U_{\tau 4}|^2}{\hbar} \cdot \tau \cdot (\ln(\tau_{\text{max}}) - \ln(\tau_{\text{min}})) \cdot e^{\frac{-\tau}{\tau_{\text{proper}}}}. \quad (5.19)$$

Adding another factor of  $|U_{\tau 4}|^2$  to account for the mixing at the interaction vertex the total re-weighting factor becomes

$$w_{\text{total}} = |U_{\tau 4}|^2 \cdot w_{\text{lifetime}}, \quad (5.20)$$

which can be applied on top of flux and oscillation weight to get the final HNL weight for a given mixing (and mass).

# Standard Model Background Simulation and Data Processing

# 6

## 6.1 Event Generation

### 6.1.1 Neutrinos

### 6.1.2 Muons

## 6.2 Detector Simulation

### 6.2.1 Photon Propagation

### 6.2.2 Detector Responses

## 6.3 Processing

### 6.3.1 Trigger and Online Filter

### 6.3.2 Offline Filter

### 6.3.3 FLERCNN Event Reconstruction and Classification

## 6.4 Systematic Uncertainties

### 6.4.1 Detector Property Variations

### 6.4.2 Atmospheric Flux

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# Search for an Excess of Heavy Neutral Lepton Events

# 7

## 7.1 Statistical Analysis

### 7.1.1 Test Statistic

### 7.1.2 Free Parameter Selection

### 7.1.3 Signal and Background in Analysis Binning

## 7.2 Modelling of Detector Response via Likelihood-Free Inference

## 7.3 Analysis Checks

### 7.3.1 Minimzer Stability

### 7.3.2 Ensemble Tests

### 7.3.3 Background Only Three-Flavor Oscillation Measurement

### 7.3.4 Heavy Neutral Lepton Sensitivity

## 7.4 Results

### 7.4.1 Best Fit Parameters

### 7.4.2 Upper Limits

### 7.4.3 Post-Fit Data/MC Agreement

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## 8.1 Summary

### 8.1.1 Three-Flavor Oscillation Measurement

### 8.1.2 Heavy Neutral Lepton Search

Double Cascade Sensitivity

Shape Excess Search

## 8.2 Outlook

### 8.2.1 Shape Analysis Improvements

- ▶ estimate full contribution from cascade only events (underestimated due to limited sampling distributions)
- ▶ include double cascade classifier into Binning
- ▶ further optimize binning

### 8.2.2 Test Coupling to Electron/Muon Flavor

### 8.2.3 IceCube Upgrade

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9.1 Conclusion

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# APPENDIX



# A

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## First Appendix

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