

```

In [1]: import numpy as np
import matplotlib.pyplot as plt
import itertools

num_of_iter=2000
eta=0.1 # Learning rate
x_u_list = np.array([[0,0],[0,1],[1,0],[1,1]])
y_u_list = np.array([[1],[-1],[-1],[1]])
input_dim, number_of_neuron_hidden_layer, number_of_output = 2,2,1

def g_function(x):
    """Activation function

    Function:
        g(h) = tanh (beta * h)
    with beta = 1
        g'(g)= beta * (1-g ^2 )

    Args:
        x (float): input value

    Returns:
        float: output value
    """
    return np.tanh(x)

```

```

In [2]: number_of_trials = 10 # Number of time we want to run the training process w
error = np.zeros([ number_of_trials , num_of_iter])

for idx_num_of_trial in range(number_of_trials):
    # 1. Initialize the weights to small random values. (layer 1)
    layer1_wjk = np.random.uniform(size=(number_of_neuron_hidden_layer,input
    layer1_bias = np.random.uniform(size=(1,number_of_neuron_hidden_layer))

    # 1. Initialize the weights to small random values. (layer 2)
    layer2_wij = np.random.uniform(size=(number_of_output,number_of_neuron_h
    layer2_bias = np.random.uniform(size=(1,number_of_output))

    for i in range(num_of_iter):
        layer1_hj = np.dot(x_u_list,layer1_wjk.T) #Activation h_j= x*w_jk
        layer1_hj += layer1_bias #Bias

        # Propagate the signal forwards through the network
        layer1_Vj = g_function(layer1_hj) #Activation function g(x) ap

        layer2_hi = np.dot(layer1_Vj,layer2_wij.T)
        layer2_hi += layer2_bias
        layer2_Vi = g_function(layer2_hi) #Activation function g(x) applied

        # Compute the delta for the output layer
        layer2_delta_i = (1-layer2_Vi**2) * (y_u_list-layer2_Vi) # g'(h_i) *

        layer2_delta_bias = eta*np.sum(layer2_delta_i,0)

```

```

# Compute the delta for the hidden layer
layer1_delta_j = (1-layer1_Vj**2)*(layer2_delta_i.dot(layer2_wij))
layer1_delta_bias = eta*np.sum(layer1_delta_j,0)

# 6. Compute the gradient of the error with respect to the weights
layer2_delta_Wij = eta*layer2_delta_i.T.dot(layer1_Vj)
layer1_delta_wjk = eta*(layer1_delta_j.T).dot(x_u_list)

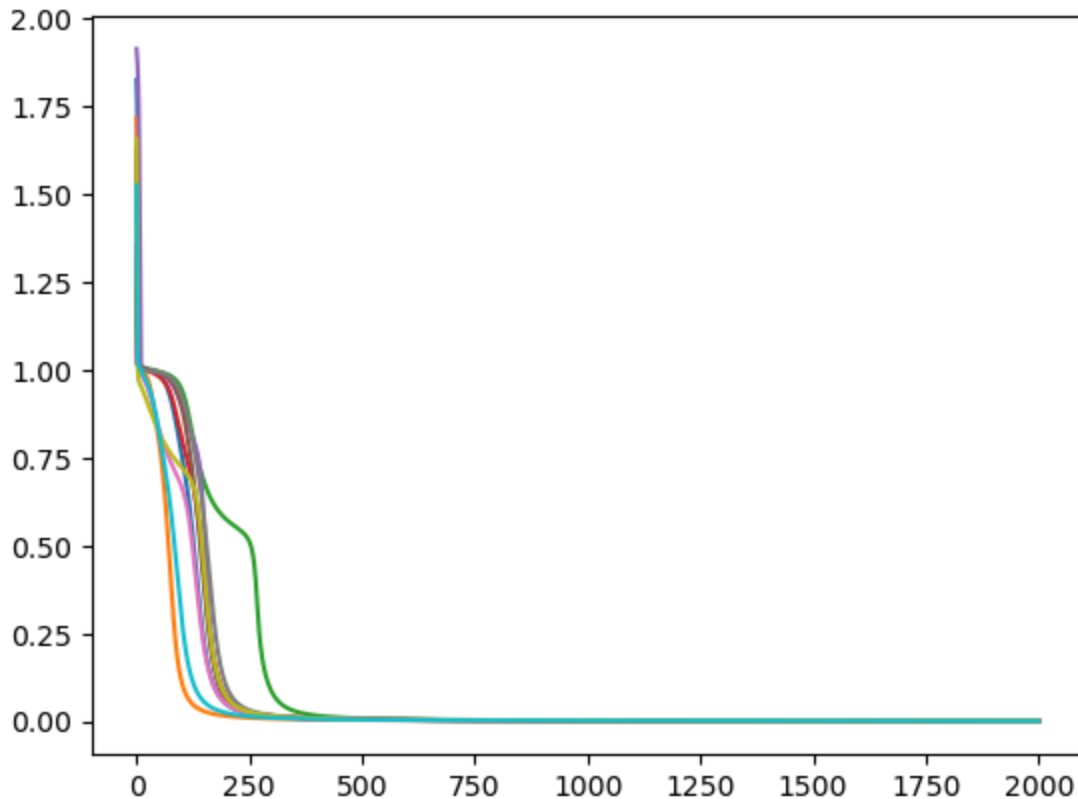
# 6.1 Update the weights
layer1_wjk += layer1_delta_wjk
layer1_bias += layer1_delta_bias
layer2_wij += layer2_delta_Wij
layer2_bias += layer2_delta_bias

# 7. Compute the error
error[idx_num_of_trial,i] = np.sum((y_u_list-layer2_Vi)**2)/4

# fig=plt.subplots(figsize=(15,5))
# plt.plot(sum(error,1))

for i_idx in range(number_of_trials):
    plt.plot(error[i_idx,:])
plt.show()

```



## Parte B

```

In [3]: number_of_trials = 10
num_of_iterations=2000
error_model_2 = np.zeros([number_of_trials,num_of_iterations])
for i_idx in range(number_of_trials):

```

```

layer1_wjk = np.random.uniform(size=(1,2))
layer1_bias = np.random.uniform(size=(1,1))

layer2_Wij = np.random.uniform(size=(1,3)) # The first two are for the i
layer2_bias = np.random.uniform(size=(1,1))

for i in range(num_of_iterations):
    layer1_hj = np.dot(x_u_list, layer1_wjk.T) #Aca hago la su
    layer1_hj += layer1_bias # Assumed that bias
    layer1_Vj = g_function(layer1_hj)

    layer2_hi = np.dot( np.concatenate( [x_u_list, layer1_Vj],axis=1) , l
    layer2_hi += layer2_bias
    layer2_0i = g_function(layer2_hi)

    # 4. Compute the delta for the output layer
    layer2_delta_i = (1-layer2_0i**2) * (y_u_list-layer2_0i) # g'(h_i) *
    layer2_delta_bias = eta*np.sum(layer2_delta_i,0)

    # 5 Compute the delta for the hidden layers
    layer1_delta_j = (1-layer1_Vj**2)*(layer2_delta_i.dot(layer2_Wij[0,2
    layer1_delta_bias = eta*np.sum(layer1_delta_j,0)

    # 6. Compute the gradient of the error with respect to the weights
    layer2_delta_Wij = eta*layer2_delta_i.T.dot(np.concatenate([x_u_list
    layer1_delta_wjk = eta*(layer1_delta_j.T).dot(x_u_list)

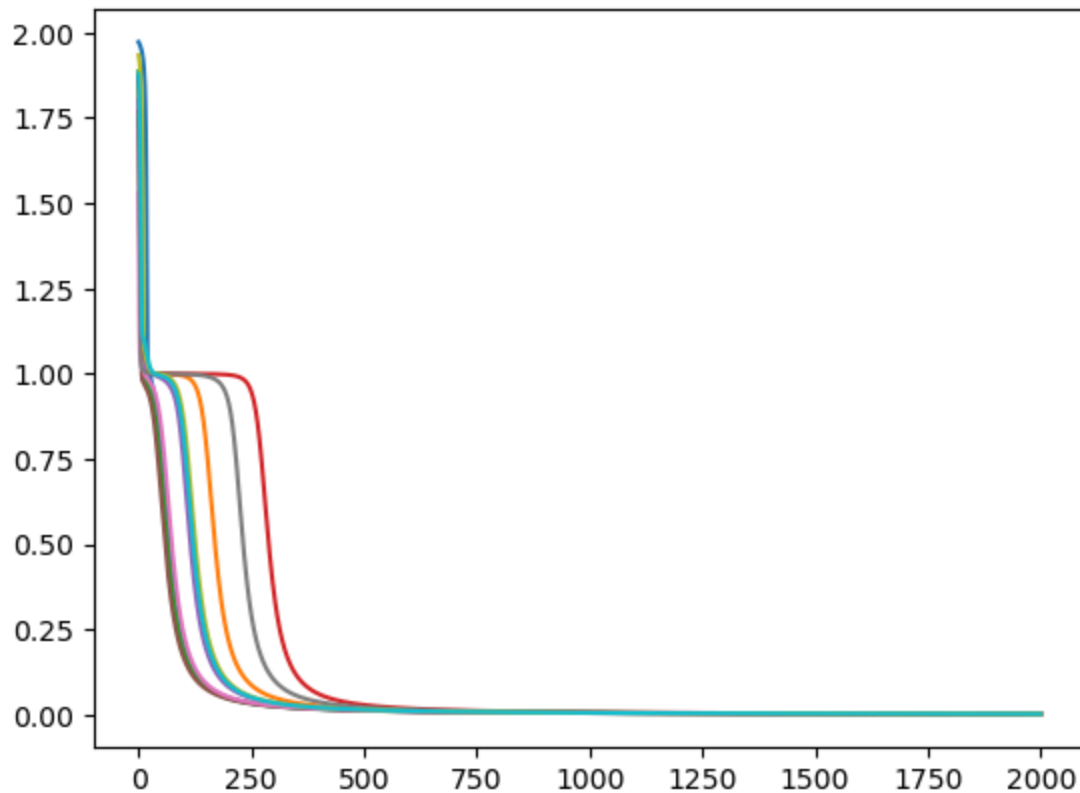
    # 6.1 Update the weights
    layer1_wjk += layer1_delta_wjk
    layer1_bias += layer1_delta_bias
    layer2_Wij += layer2_delta_Wij
    layer2_bias += layer2_delta_bias

    # 7. Compute the error
    error_model_2[i_idx,i] = np.sum((y_u_list-layer2_0i)**2)/4

# fig =plt.subplots(figsize=(15,5))
# plt.plot(sum(error_model_2,0))

for i_idx in range(number_of_trials):
    plt.plot(error_model_2[i_idx,:])
plt.show()

```



```
In [4]: fig , axes =plt.subplots(figsize=(15,15))
        axes.axis('off')

        plt.subplot(311)
        plt.title('Arquitectura 1',fontsize='xx-large')

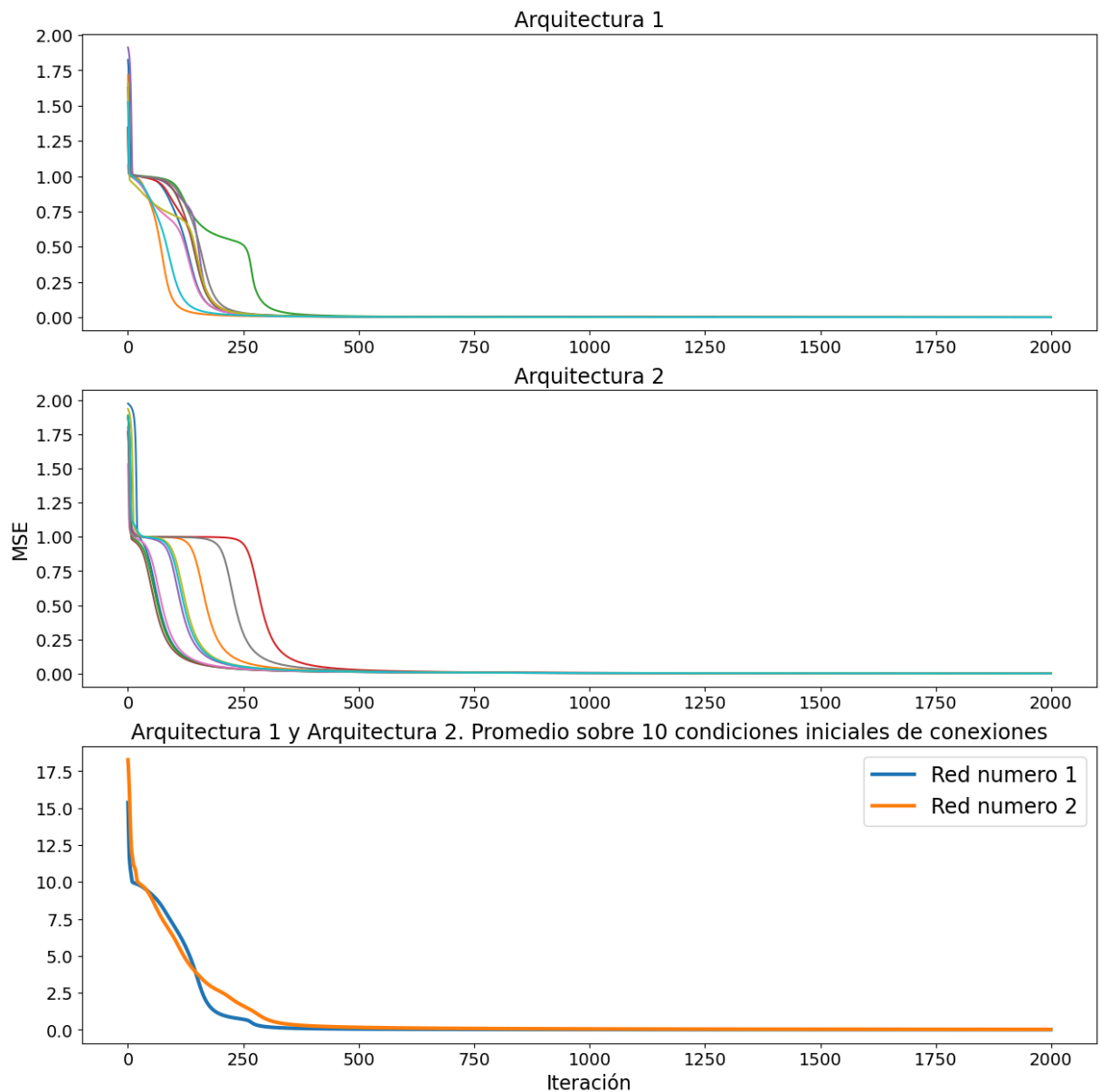
        for i_idx in range(number_of_trials):
            plt.plot(error[i_idx,:])
        plt.xticks(fontsize=14)
        plt.yticks(fontsize=14)

        plt.subplot(312)
        plt.title('Arquitectura 2',fontsize='xx-large')

        for i_idx in range(number_of_trials):
            plt.plot(error_model_2[i_idx,:])
        plt.ylabel('MSE',fontsize=16)
        plt.xticks(fontsize=14)
        plt.yticks(fontsize=14)

        plt.subplot(313)
        plt.title('Arquitectura 1 y Arquitectura 2. Promedio sobre 10 condiciones ir
        plt.plot(sum(error,0),linewidth=3)
        plt.plot(sum(error_model_2,0),linewidth=3)
        plt.legend(['Red numero 1','Red numero 2'],fontsize='xx-large')
        plt.xlabel('Iteración',fontsize=16)
        plt.xticks(fontsize=14)
        plt.yticks(fontsize=14)
```

```
Out[4]: (array([-2.5,  0. ,  2.5,  5. ,  7.5, 10. , 12.5, 15. , 17.5, 20. ]),
 [Text(0, -2.5, '-2.5'),
  Text(0, 0.0, '0.0'),
  Text(0, 2.5, '2.5'),
  Text(0, 5.0, '5.0'),
  Text(0, 7.5, '7.5'),
  Text(0, 10.0, '10.0'),
  Text(0, 12.5, '12.5'),
  Text(0, 15.0, '15.0'),
  Text(0, 17.5, '17.5'),
  Text(0, 20.0, '20.0')])
```



## Problema 2

```
In [5]: num_of_iter = 1000
eta = 0.01 # Learning rate
N = 5 # Number of model input
```

```

# Sample data
# Generate all possible combinations of N inputs, each input being either +1
x_u_list = list(itertools.product([1, -1], repeat=N))

for x_sample in x_u_list:
    # The output y is +1 if the product of inputs is +1, otherwise -1
    y_u_list = 1 if all(x_i == 1 for x_i in x_sample) else -1 if all(x_i

# Model
input_dim = N
number_of_neuron_hidden_layer = 2
number_of_output = 1

neuron_counts = [1, 3, 5, 7, 9, 11] # Neuron counts for hidden layer

number_of_trials = 10 # Number of time we want to run the training process w
error = np.zeros([ number_of_trials , num_of_iter])

for idx_num_of_trial in range(number_of_trials):
    # 1. Initialize the weights to small random values. (layer 1)
    layer1_wjk = np.random.uniform(size=(number_of_neuron_hidden_layer, input
    layer1_bias = np.random.uniform(size=(1, number_of_neuron_hidden_layer))

    # 1. Initialize the weights to small random values. (layer 2)
    layer2_wij = np.random.uniform(size=(number_of_output, number_of_neuron_h
    layer2_bias = np.random.uniform(size=(1, number_of_output))

    for i in range(num_of_iter):
        layer1_hj = np.dot(x_u_list, layer1_wjk.T) #Activation h_j= x*w_jk
        layer1_hj += layer1_bias #Bias

        # Propagate the signal forwards through the network
        layer1_Vj = g_function(layer1_hj) #Activation function g(x) ap

        layer2_hi = np.dot(layer1_Vj, layer2_wij.T)
        layer2_hi += layer2_bias
        layer2_Vi = g_function(layer2_hi) #Activation function g(x) applied

        # Compute the delta for the output layer
        layer2_delta_i = (1-layer2_Vi**2) * (y_u_list-layer2_Vi) # g'(h_i) *

        layer2_delta_bias = eta*np.sum(layer2_delta_i,0)

        # Compute the delta for the hidden layer
        layer1_delta_j = (1-layer1_Vj**2)*(layer2_delta_i.dot(layer2_wij))
        layer1_delta_bias = eta*np.sum(layer1_delta_j,0)

        # 6. Compute the gradient of the error with respect to the weights
        layer2_delta_Wij = eta*layer2_delta_i.T.dot(layer1_Vj)
        layer1_delta_wjk = eta*(layer1_delta_j.T).dot(x_u_list)

        # 6.1 Update the weights
        layer1_wjk += layer1_delta_wjk
        layer1_bias += layer1_delta_bias

```

```

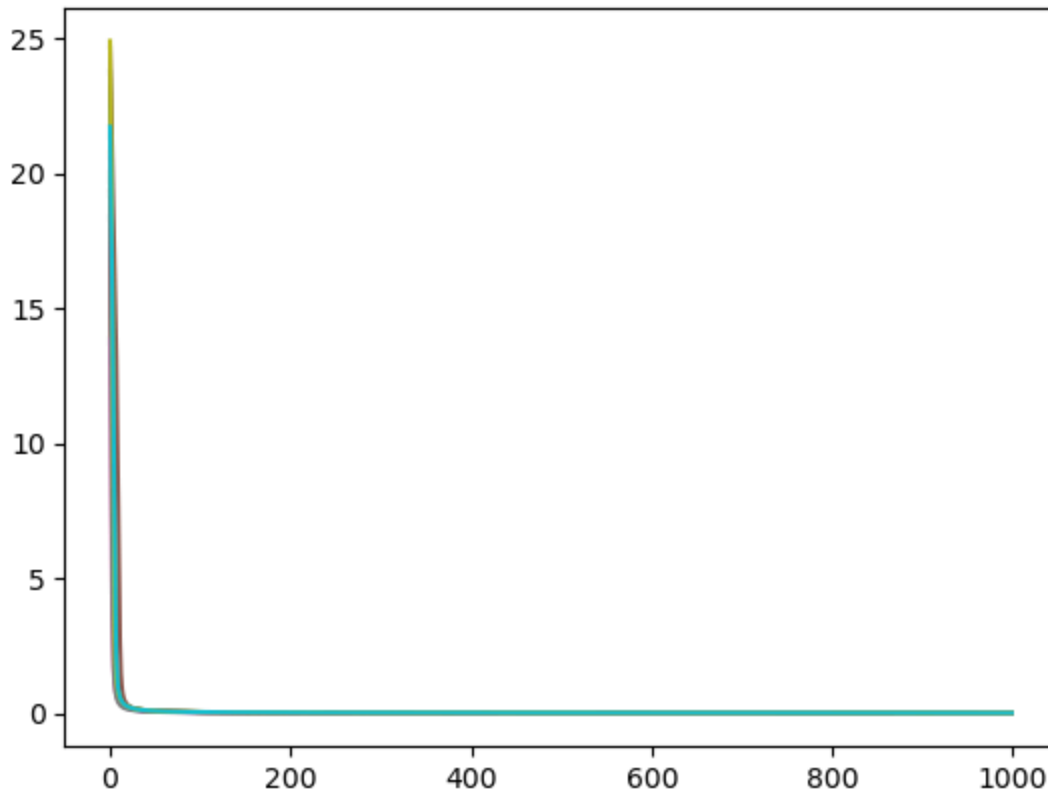
layer2_wij += layer2_delta_Wij
layer2_bias += layer2_delta_bias

# 7. Compute the error
error[idx_num_of_trial,i] = np.sum((y_u_list-layer2_Vi)**2)/4

# fig=plt.subplots(figsize=(15,5))
# plt.plot(sum(error,1))

for i_idx in range(number_of_trials):
    plt.plot(error[i_idx,:])
plt.show()

```



For multiple number of neurons in the hidden layer

```

In [6]: num_of_iter = 100
eta = 0.01 # Learning rate
N = 5 # Number of model input

# Sample data
# Generate all possible combinations of N inputs, each input being either +1
x_u_list = list(itertools.product([1, -1], repeat=N))

for x_sample in x_u_list:
    # The output y is +1 if the product of inputs is +1, otherwise -1
    y_u_list = 1 if all(x_i == 1 for x_i in x_sample) else -1 if all(x_i

# Model
input_dim = N
number_of_neuron_hidden_layer = 11

```

```

number_of_output = 1

neuron_counts = [1, 3, 5, 7, 9, 11] # Neuron counts for hidden layer

number_of_trials = 10 # Number of time we want to run the training process w
error = np.zeros([ number_of_trials , num_of_iter])

# Set up the plot
fig, axes = plt.subplots(2, 3, figsize=(18, 10))
axes = axes.ravel() # Flatten axes for easy indexing

# Loop over different numbers of neurons in the hidden layer
for idx, number_of_neuron_hidden_layer in enumerate(neuron_counts):

    for idx_num_of_trial in range(number_of_trials):
        # 1. Initialize the weights to small random values. (layer 1)
        layer1_wjk = np.random.uniform(size=(number_of_neuron_hidden_layer, i
        layer1_bias = np.random.uniform(size=(1, number_of_neuron_hidden_layer

        # 1. Initialize the weights to small random values. (layer 2)
        layer2_wij = np.random.uniform(size=(number_of_output, number_of_neur
        layer2_bias = np.random.uniform(size=(1, number_of_output))

        for i in range(num_of_iter):
            layer1_hj = np.dot(x_u_list, layer1_wjk.T) #Activation h_j= x*w_
            layer1_hj += layer1_bias #Bias

            # Propagate the signal forwards through the network
            layer1_Vj = g_function(layer1_hj) #Activation function g(x

            layer2_hi = np.dot(layer1_Vj, layer2_wij.T)
            layer2_hi += layer2_bias
            layer2_Vi = g_function(layer2_hi) #Activation function g(x) appl

            # Compute the delta for the output layer
            layer2_delta_i = (1-layer2_Vi**2) * (y_u_list-layer2_Vi) # g'(h_

            layer2_delta_bias = eta*np.sum(layer2_delta_i,0)

            # Compute the delta for the hidden layer
            layer1_delta_j = (1-layer1_Vj**2)*(layer2_delta_i.dot(layer2_wij
            layer1_delta_bias = eta*np.sum(layer1_delta_j,0)

            # 6. Compute the gradient of the error with respect to the weigh
            layer2_delta_Wij = eta*layer2_delta_i.T.dot(layer1_Vj)
            layer1_delta_wjk = eta*(layer1_delta_j.T).dot(x_u_list)

            # 6.1 Update the weights
            layer1_wjk += layer1_delta_wjk
            layer1_bias += layer1_delta_bias
            layer2_wij += layer2_delta_Wij
            layer2_bias += layer2_delta_bias

            # 7. Compute the error
            error[idx_num_of_trial,i] = np.sum((y_u_list-layer2_Vi)**2)/4

```

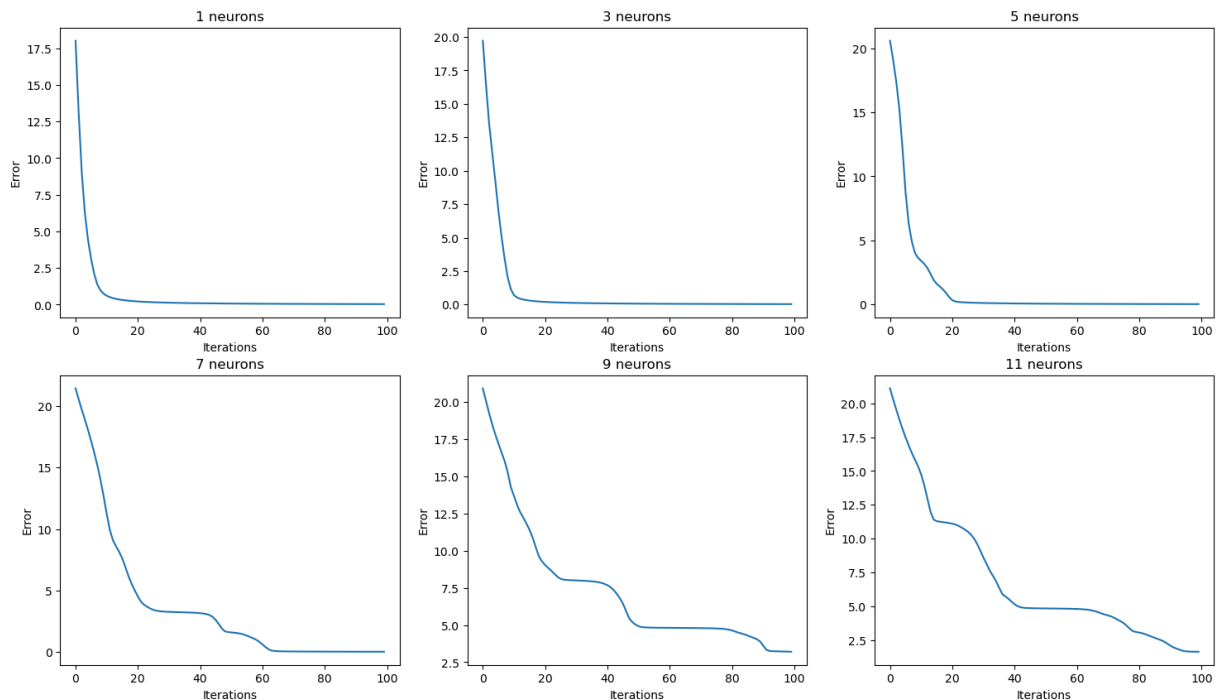


```

# Plot the average error over all trials for this number of neurons
avg_error = np.mean(error, axis=0)
ax = axes[idx]
ax.plot(avg_error)
ax.set_title(f"{number_of_neuron_hidden_layer} neurons")
ax.set_xlabel("Iterations")
ax.set_ylabel("Error")

plt.show()

```



```

In [7]: num_of_iter = 1000
eta = 0.01 # Learning rate
N = 5 # Number of model input

# Sample data
# Generate all possible combinations of N inputs, each input being either +1 or -1
x_u_list = list(itertools.product([1, -1], repeat=N))

for x_sample in x_u_list:
    # The output y is +1 if the product of inputs is +1, otherwise -1
    y_u_list = 1 if all(x_i == 1 for x_i in x_sample) else -1 if all(x_i == -1 for x_i in x_sample) else 0

# Model
input_dim = N
number_of_neuron_hidden_layer = 11
number_of_output = 1

neuron_counts = [1, 3, 5, 7, 9, 11] # Neuron counts for hidden layer

number_of_trials = 50 # Number of time we want to run the training process
error = np.zeros([number_of_trials, num_of_iter])

```

```

# Set up the plot
plt.figure(figsize=(10, 6))

# Loop over different numbers of neurons in the hidden layer
for idx, number_of_neuron_hidden_layer in enumerate(neuron_counts):

    for idx_num_of_trial in range(number_of_trials):
        # 1. Initialize the weights to small random values. (layer 1)
        layer1_wjk = np.random.uniform(size=(number_of_neuron_hidden_layer, number_of_input))
        layer1_bias = np.random.uniform(size=(1, number_of_neuron_hidden_layer))

        # 1. Initialize the weights to small random values. (layer 2)
        layer2_wij = np.random.uniform(size=(number_of_output, number_of_neuron_hidden_layer))
        layer2_bias = np.random.uniform(size=(1, number_of_output))

        for i in range(num_of_iter):
            layer1_hj = np.dot(x_u_list, layer1_wjk.T) #Activation  $h_j = x * w$ 
            layer1_hj += layer1_bias #Bias

            # Propagate the signal forwards through the network
            layer1_Vj = g_function(layer1_hj) #Activation function  $g(x)$  applied to  $h_j$ 

            layer2_hi = np.dot(layer1_Vj, layer2_wij.T)
            layer2_hi += layer2_bias
            layer2_Vi = g_function(layer2_hi) #Activation function  $g(x)$  applied to  $h_i$ 

            # Compute the delta for the output layer
            layer2_delta_i = (1-layer2_Vi**2) * (y_u_list-layer2_Vi) #  $g'(h_i)$ 

            layer2_delta_bias = eta*np.sum(layer2_delta_i,0)

            # Compute the delta for the hidden layer
            layer1_delta_j = (1-layer1_Vj**2)*(layer2_delta_i.dot(layer2_wij.T))
            layer1_delta_bias = eta*np.sum(layer1_delta_j,0)

            # 6. Compute the gradient of the error with respect to the weights
            layer2_delta_Wij = eta*layer2_delta_i.T.dot(layer1_Vj)
            layer1_delta_wjk = eta*(layer1_delta_j.T).dot(x_u_list)

            # 6.1 Update the weights
            layer1_wjk += layer1_delta_wjk
            layer1_bias += layer1_delta_bias
            layer2_wij += layer2_delta_Wij
            layer2_bias += layer2_delta_bias

            # 7. Compute the error
            error[idx_num_of_trial,i] = np.sum((y_u_list-layer2_Vi)**2)/4

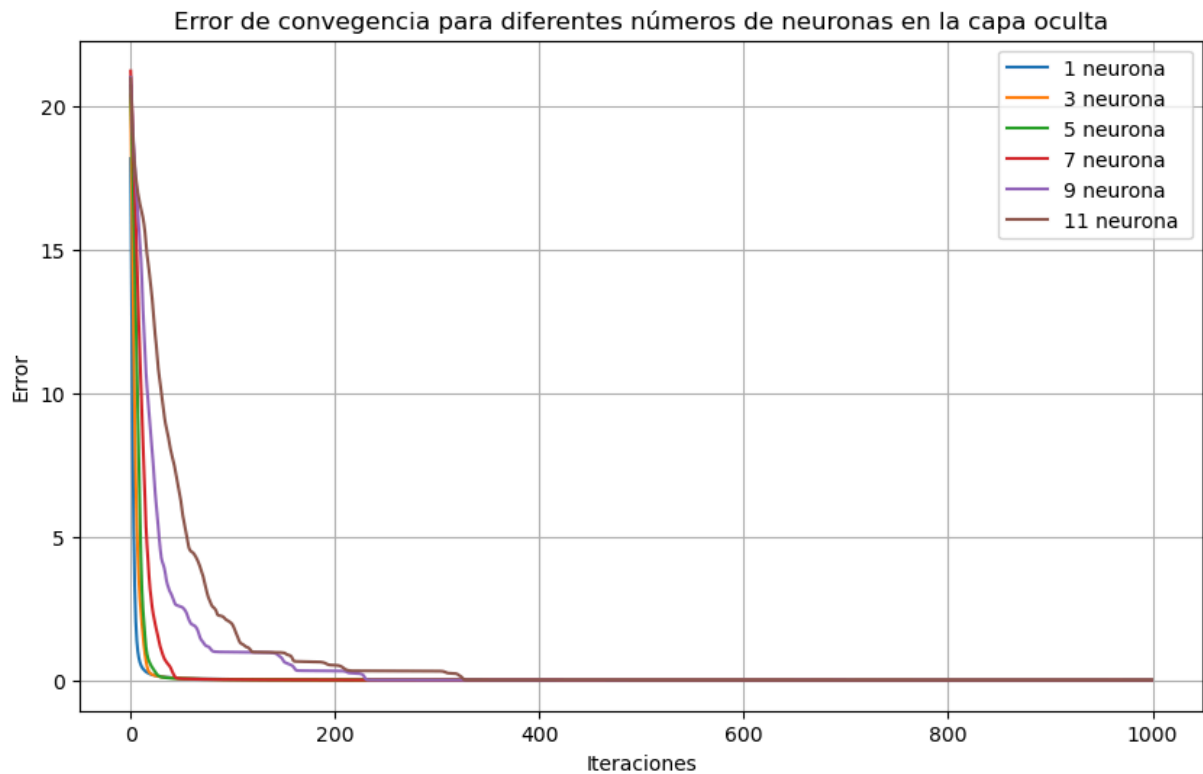
        # Plot the average error over all trials for this number of neurons
        avg_error = np.mean(error, axis=0)
        plt.plot(avg_error, label=f'{number_of_neuron_hidden_layer} neurona ')

# Add labels and legend to the plot

```

```
plt.title("Error de convegenca para diferentes números de neuronas en la ca
plt.xlabel("Iteraciones")
plt.ylabel("Error")
plt.legend()
plt.grid(True)

# Display the plot
plt.show()
```



## Problema 3

```
In [16]: """
Modeling a logistic regression using a neural network with back-propagation

"""
import tensorflow as tf
import numpy as np
import matplotlib.pyplot as plt

from sklearn.model_selection import train_test_split

# Set seed for reproducibility
seed=43
np.random.seed(seed)
tf.random.set_seed(seed)

def create_model():
    # Network architecture
```

```

input_dim=1                                # Number of neurons in the input
hidden_dim=5                              # Number of neurons in the hidden
output_dim=1                              # Number of neurons in the output

# ----- Model-----
# Input layer
input_layer=tf.keras.layers.Input(shape=(input_dim,), name='Input')
# Hidden layer - Sigmoid activation function - Name Hidden_layer
hidden_layer=tf.keras.layers.Dense(hidden_dim, activation='sigmoid', name='Hidden_layer')

# Concatenate input and hidden layer
concatenated_layer=tf.keras.layers.Concatenate(name='Concate')([input_layer, hidden_layer])

# Output layer - Linear activation function
output_layer=tf.keras.layers.Dense(output_dim, activation='linear', name='Output_layer')

# Build the model
model=tf.keras.Model(inputs=input_layer, outputs=output_layer)

# Optimizer
opt=tf.keras.optimizers.RMSprop(learning_rate=0.01)

# Compile the model
model.compile(optimizer=opt, loss='MSE')
return model

# Create the model
model=create_model()

# Summary of the model
model.summary()

# Plot the model
tf.keras.utils.plot_model(model, to_file='model.png', show_shapes=False, show_dtype=True)

n_examples_list = [5, 10, 100]

for n_examples in n_examples_list:
    # ----- Input data-----
    # Generate random data list for x
    x = np.random.uniform(low=0,high=1 ,size = n_examples).reshape(-1,1)
    print(f"valore x: {x}")

    # Generate y data
    y = 4 * x * (1 - x)
    print(f"valore y: {y}")

    x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.2, random_state=42)

    # Train the model
    history=model.fit(x=x_train, y=y_train,
                      epochs=1500,

```

```

        batch_size=4,
        shuffle=False,
        validation_data=(x_test, y_test),
        verbose=False)

# ----- Evaluate the model-----
# Evaluate the model on the train set
loss_train = model.evaluate(x_train, y_train, verbose=0)

print(f"Example with {n_examples} Samples - Train loss {loss_train}")

# Evaluate the model on the test set
loss_test = model.evaluate(x_test, y_test, verbose=0)

print(f"Example with {n_examples} Samples - Test loss {loss_test}")

# Make predictions for 0 - 1 values
x_predict = np.linspace(0, 1, 100).reshape(-1,1)
y_predict = model.predict(x_predict)

loss_predict = model.evaluate(x_predict, 4 * x_predict * (1 - x_predict))

print(f"Example with {n_examples} Samples - Predict loss {loss_predict}")

# Save the predictions in file for plotting
np.savetxt(f'lr-predictions_{n_examples}.txt', np.concatenate((x_predict

# Save error history values for plotting
np.savetxt(f'lr-error_{n_examples}.txt', np.array([history.history['loss

# encoded_log = model.predict(x_test, verbose=True)
# print(encoded_log.shape)

# # "Loss"
# plt.plot(np.sqrt(history.history['loss']))
# plt.plot(np.sqrt(history.history['val_loss']))
# plt.title('model loss')
# plt.ylabel('loss')
# plt.xlabel('epoch')
# plt.legend(['train', 'validation'], loc='upper left')
# plt.show()

```

**Model: "functional\_5"**

Layer (type)	Output Shape	Param #	Connected to
Input ( <a href="#">InputLayer</a> )	( <a href="#">None</a> , 1)	0	–
Hidden_layer ( <a href="#">Dense</a> )	( <a href="#">None</a> , 5)	10	Input[0][0]
Concate ( <a href="#">Concatenate</a> )	( <a href="#">None</a> , 6)	0	Input[0][0], Hidden_layer[
Output ( <a href="#">Dense</a> )	( <a href="#">None</a> , 1)	7	Concate[0][0]

**Total params:** 17 (68.00 B)

**Trainable params:** 17 (68.00 B)

**Non-trainable params:** 0 (0.00 B)

You must install pydot (`pip install pydot`) for `plot\_model` to work.

valore x: [[0.11505457]

[0.60906654]  
[0.13339096]  
[0.24058962]  
[0.32713906]]

valore y: [[0.40726805]

[0.95241796]  
[0.46239126]  
[0.73082502]  
[0.88047638]]

Example with 5 Samples - Train loss 0.0023474260233342648

Example with 5 Samples - Test loss 0.0046743000857532024

**4/4**  **0s** 5ms/step

Example with 5 Samples - Predict loss 0.09869936108589172

valore x: [[0.85913749]

[0.66609021]  
[0.54116221]  
[0.02901382]  
[0.7337483 ]  
[0.39495002]  
[0.80204712]  
[0.25442113]  
[0.05688494]  
[0.86664864]]

valore y: [[0.48408105]

[0.88965616]  
[0.99322269]  
[0.11268809]  
[0.78144694]  
[0.95585801]  
[0.63507015]  
[0.75876407]  
[0.21459616]  
[0.4622751 ]]

Example with 10 Samples - Train loss 0.0011201611487194896

Example with 10 Samples - Test loss 0.0036995145492255688

**4/4**  **0s** 838us/step

Example with 10 Samples - Predict loss 0.005022585857659578

valore x: [[0.221029 ]

[0.40498945]  
[0.31609647]  
[0.0766627 ]  
[0.84322469]  
[0.84893915]  
[0.97146509]  
[0.38537691]  
[0.95448813]  
[0.44575836]  
[0.66972465]  
[0.08250005]  
[0.89709858]  
[0.2980035 ]  
[0.26230482]  
[0.00512955]  
[0.54320252]

[0.47559637]  
[0.63637368]  
[0.97820413]  
[0.90866276]  
[0.91015308]  
[0.52525567]  
[0.10401895]  
[0.1809146 ]  
[0.95304022]  
[0.41195298]  
[0.86501712]  
[0.67217728]  
[0.6287858 ]  
[0.27555878]  
[0.89674727]  
[0.20689137]  
[0.40440524]  
[0.99357249]  
[0.73572708]  
[0.44506141]  
[0.56066317]  
[0.41125549]  
[0.72698799]  
[0.39919689]  
[0.67014516]  
[0.70471561]  
[0.60955987]  
[0.54003446]  
[0.20608185]  
[0.19916148]  
[0.79573886]  
[0.29033278]  
[0.65596283]  
[0.29961678]  
[0.14447838]  
[0.40395667]  
[0.31026953]  
[0.24339802]  
[0.58810404]  
[0.24534325]  
[0.74777061]  
[0.72014665]  
[0.69526087]  
[0.10274278]  
[0.94364243]  
[0.50333963]  
[0.89967362]  
[0.19857988]  
[0.59444919]  
[0.96540858]  
[0.99869825]  
[0.02416862]  
[0.48130333]  
[0.29142269]  
[0.06372057]  
[0.5696244 ]



[0.00508328]  
[0.61127759]  
[0.87018148]  
[0.88360146]  
[0.95431948]  
[0.73986382]  
[0.18471296]  
[0.43467832]  
[0.8858995 ]  
[0.25504628]  
[0.44331269]  
[0.61693698]  
[0.10335251]  
[0.49010966]  
[0.0447044 ]  
[0.31162747]  
[0.75203969]  
[0.71549909]  
[0.94155424]  
[0.77689537]  
[0.21522851]  
[0.90497118]  
[0.55226415]  
[0.84489789]  
[0.92248948]  
[0.82896128]  
[0.394198 ]]  
valore y: [[0.68870072]  
[0.96389198]  
[0.86471797]  
[0.28314212]  
[0.52878724]  
[0.51296588]  
[0.11088267]  
[0.94744619]  
[0.17376218]  
[0.98823138]  
[0.88477417]  
[0.30277517]  
[0.36925087]  
[0.83678966]  
[0.77400401]  
[0.02041295]  
[0.99253417]  
[0.99761785]  
[0.92560888]  
[0.08528322]  
[0.331979 ]  
[0.32709782]  
[0.9974486 ]  
[0.37279603]  
[0.59273802]  
[0.17901823]  
[0.96899089]  
[0.46705001]  
[0.88141994]

[0.93365688]  
[0.79850455]  
[0.37036642]  
[0.65634933]  
[0.96344657]  
[0.02554478]  
[0.77773097]  
[0.98792701]  
[0.98527992]  
[0.96849765]  
[0.79390581]  
[0.95935493]  
[0.88420249]  
[0.83236608]  
[0.95198654]  
[0.99358897]  
[0.65444849]  
[0.63798473]  
[0.6501541 ]  
[0.82415862]  
[0.90270239]  
[0.83938625]  
[0.49441751]  
[0.96310271]  
[0.85600939]  
[0.73662169]  
[0.96895071]  
[0.74059976]  
[0.7544389 ]  
[0.80614181]  
[0.84749278]  
[0.3687468 ]  
[0.21272558]  
[0.99995539]  
[0.36104399]  
[0.63658366]  
[0.9643174 ]  
[0.13357941]  
[0.00520024]  
[0.09433801]  
[0.99860174]  
[0.82598202]  
[0.23864103]  
[0.98060977]  
[0.02022978]  
[0.95046919]  
[0.4518627 ]  
[0.41139966]  
[0.17437523]  
[0.76986139]  
[0.60237632]  
[0.98293231]  
[0.40432632]  
[0.7599907 ]  
[0.9871462 ]  
[0.94530297]

```
[0.37068308]
[0.99960872]
[0.17082368]
[0.85806316]
[0.74590399]
[0.81424057]
[0.2201194 ]
[0.69331582]
[0.67562081]
[0.34399337]
[0.98907384]
[0.52418179]
[0.28601054]
[0.56713791]
[0.95522375]]
```

Example with 100 Samples - Train loss 0.0003551080299075693

Example with 100 Samples - Test loss 0.0003401233989279717

4/4 ————— 0s 642us/step

Example with 100 Samples - Predict loss 0.00035896486951969564

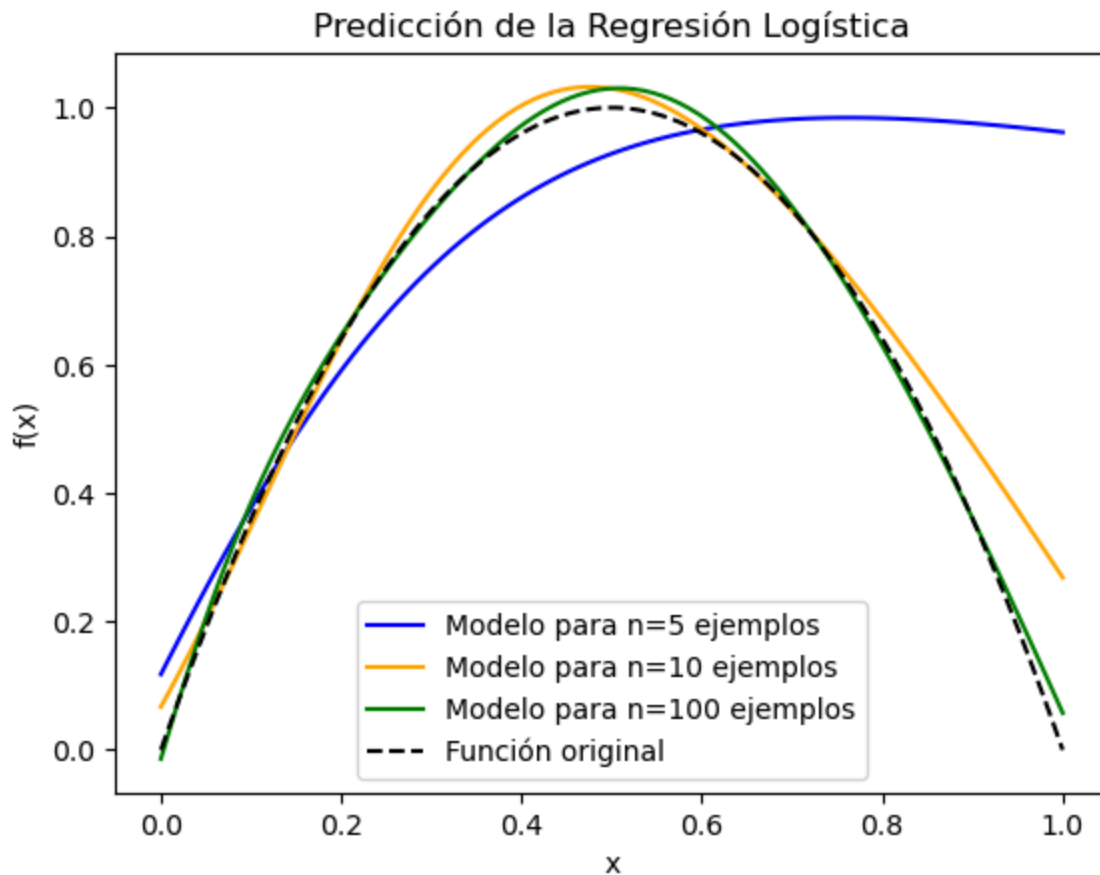
```
In [17]: # List of colors
         colors = ['blue', 'orange', 'green']

         # Open the file for n=5,10,100 and read the data
         for n_examples, color in zip(n_examples_list, colors):
             # Load
             data = np.loadtxt(f'lr-predictions_{n_examples}.txt')
             x_predict = data[:,0]
             y_predict = data[:,1]

             # Plot the data
             plt.plot(x_predict, y_predict, color= color, label=f'Modelo para n={n_ex

         # Plot the original function
         x = np.linspace(0, 1, 100)
         y = 4 * x * (1 - x)
         plt.plot(x, y, "--", color='black', label='Función original')

         # Add labels and legend
         plt.xlabel('x')
         plt.ylabel('f(x)')
         plt.legend()
         plt.title('Predicción de la Regresión Logística')
         plt.show()
```



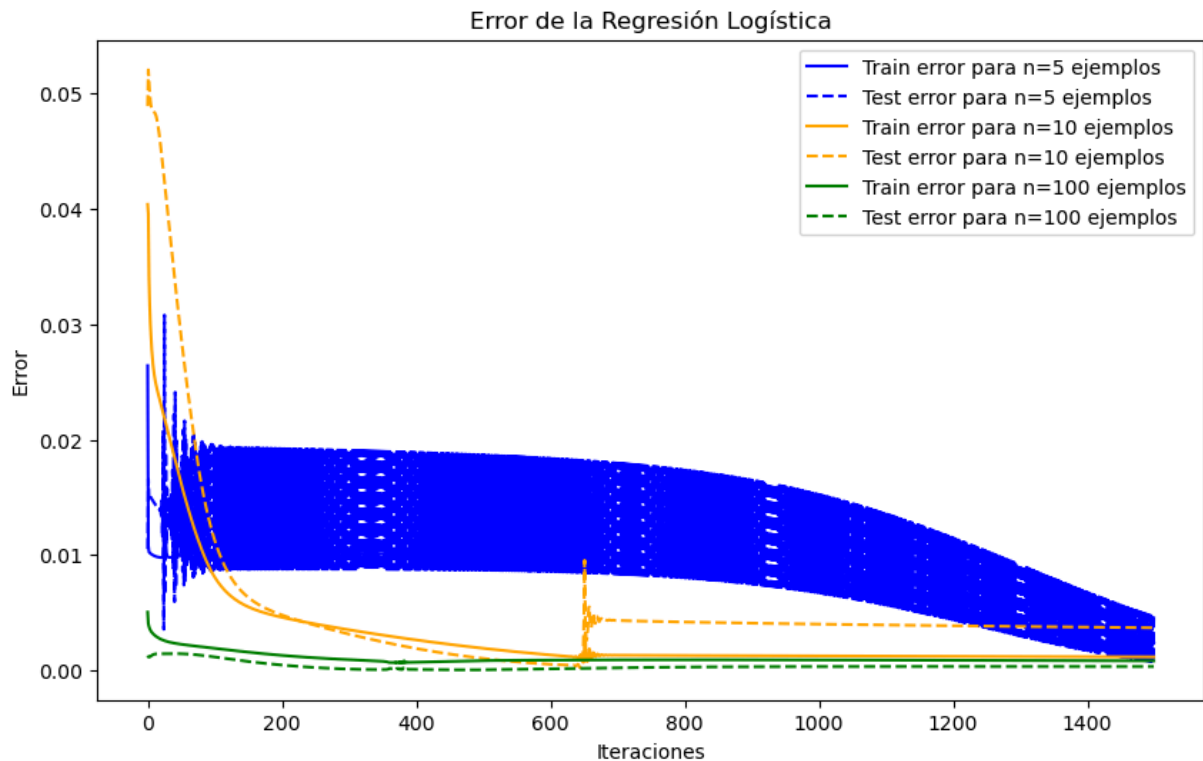
```
In [18]: # Open error files for n=5,10,100 and read the data

# Set up the plot
plt.figure(figsize=(10, 6))
# List of colors
colors = ['blue', 'orange', 'green']

for n_examples,color in zip(n_examples_list,colors):
    # Load
    data = np.loadtxt(f'lr-error_{n_examples}.txt')
    train_error = data[:,0]
    test_error = data[:,1]

    # Plot the data. Train is solid and test is dashed
    plt.plot(train_error, "-",color = color ,label=f'Train error para n={n_e
    plt.plot(test_error, "--",color = color ,label=f'Test error para n={n_ex

# Add labels and legend
plt.xlabel('Iteraciones')
plt.ylabel('Error')
plt.legend()
plt.title('Error de la Regresión Logística')
plt.show()
```



```
In [14]: # #####
# # Output files
# fout=open("lr-out.dat","wb")
# ftrain=open("lr-train.dat","wb")
# ftest=open("lr-test.dat","wb")
# #
# np.savetxt(ftrain,np.c_[x_train,y_train],delimiter=" ")
# np.savetxt(ftest,np.c_[x_test, y_test],delimiter=" ")
# np.savetxt(fout,np.c_[x_test, encoded_log],delimiter=" ")

# W_Input_Hidden = model.layers[0].get_weights()
# W_Output_Hidden = model.layers[1].get_weights()
# # B_Input_Hidden = model.layers[0].get_weights()[1]
# # B_Output_Hidden = model.layers[1].get_weights()[1]
# #print(summary)
# print('INPUT-HIDDEN LAYER WEIGHTS:')
# print(W_Input_Hidden)
# print('HIDDEN-OUTPUT LAYER WEIGHTS:')
# print(W_Output_Hidden)

# # print('INPUT-HIDDEN LAYER BIAS:')
# # print(B_Input_Hidden)
# # print('HIDDEN-OUTPUT LAYER BIAS:')
# # print(B_Output_Hidden)
```

INPUT-HIDDEN LAYER WEIGHTS:

[]

HIDDEN-OUTPUT LAYER WEIGHTS:

```
[array([[ 0.41649264, -0.88370305,  0.7433394 ,  0.22161928,  0.03575625]],
      dtype=float32), array([ 0.0649383 , -0.09769494,  0.02043273,  0.02721
332, -0.02572968],
      dtype=float32)]
```

