



DSA SERIES

- Learn Coding



Topic to be Covered today

Graph



What Is a Graph?

A **graph** is a way to represent **connections** or **relationships**

between things.

- The **things** are called **nodes** or **vertices**.
- The **connections** between them are called **edges**.

So a graph = **Vertices + Edges**



Types of Graphs

1. Directed Graph (Digraph)

Edges have direction →

$A \rightarrow B$ is different from $B \rightarrow A$.

Use case: Instagram follow system

A follows B but B may not follow A.

2. Undirected Graph

Edges don't have a direction

$A - B$ means both are connected.

Use case: Facebook friends.



3. Weighted Graph

Edges have weights (cost, distance, time).

Example:

Road length between two cities.

4. Unweighted Graph

Edges don't have weights.

5. Cyclic Graph

Has at least one cycle

($A \rightarrow B \rightarrow C \rightarrow A$)

6. Acyclic Graph

Has no cycle.



Graph Representation

1. Adjacency Matrix

A 2D matrix of size $N \times N$

$\text{matrix}[i][j] = 1$ (edge exists) or weight if weighted

$\text{matrix}[i][j] = 0$ (no edge)

✓ Easy, but uses a lot of space.

2. Adjacency List (Most Important)

For each node, store a list of connected nodes.

Graph Traversal

Once we build a graph, we usually need to explore it.

Two main algorithms:

✓ BFS — Breadth First Search

Level by level traversal

Used for:

- Shortest path in unweighted graph
- Checking connectivity
- Bipartite checking

✓ DFS — Depth First Search

Go as deep as possible

Used for:

- Cycle detection
- Topological sort
- Connected components
- Strongly connected components



DFS Implementation

```
#include <bits/stdc++.h>
using namespace std;

void dfs(int node, vector<int> adj[], vector<int> &vis) {
    vis[node] = 1;
    cout << node << " ";

    for (int nbr : adj[node]) {
        if (!vis[nbr]) {
            dfs(nbr, adj, vis);
        }
    }
}

int main() {
    int n = 4;
    vector<int> adj[n];
```



```
// Graph
adj[0] = {1, 2};
adj[1] = {0, 3};
adj[2] = {0, 3};
adj[3] = {1, 2};

vector<int> vis(n, 0);

cout << "DFS Traversal: ";
dfs(0, adj, vis);
}
```



BFS Implementation

```
#include <bits/stdc++.h>
using namespace std;

void bfs(int start, vector<int> adj[], int n) {
    vector<int> vis(n, 0);
    queue<int> q;

    q.push(start);
    vis[start] = 1;

    while (!q.empty()) {
        int node = q.front();
        q.pop();

        cout << node << " ";

        for (int nbr : adj[node]) {
            if (!vis[nbr]) {
                vis[nbr] = 1;
                q.push(nbr);
            }
        }
    }
}
```



```
    }
}
}

int main() {
    int n = 4;
    vector<int> adj[n];

    adj[0] = {1, 2};
    adj[1] = {0, 3};
    adj[2] = {0, 3};
    adj[3] = {1, 2};

    bfs(0, adj, n);
}
```



Learn coding

THANK YOU