

Plaintext Herbert Yardley

h	e	r	b	e	r	t	y	a	r	d	l	e	y
8	5	18	2	5	8	20	25	1	18	4	12	5	25

$$\begin{bmatrix} 3 & 7 \\ 5 & 12 \end{bmatrix} \begin{bmatrix} 8 \\ 5 \end{bmatrix} \begin{matrix} h \\ e \end{matrix} = \begin{bmatrix} 59 \\ 100 \end{bmatrix} = \begin{bmatrix} 7 \\ 22 \end{bmatrix} \begin{matrix} G \\ V \end{matrix} \pmod{26}$$

$$\begin{aligned} 3 \times 8 + 7 \times 5 &= 59 = 7 \\ 5 \times 8 + 12 \times 5 &= 100 = 22 \end{aligned} \pmod{26}$$

$$\begin{bmatrix} 3 & 7 \\ 5 & 12 \end{bmatrix} \begin{bmatrix} 8 & 18 & 5 & 20 & 1 & 4 & 5 \\ 5 & 2 & 18 & 25 & 18 & 12 & 25 \end{bmatrix} = \begin{bmatrix} 7 & 16 & 11 & 1 & 25 & 18 & 8 \\ 22 & 10 & 7 & 10 & 13 & 8 & 13 \end{bmatrix} \pmod{26}$$

Ciphertext GV PJ KG AJ YM RH HM

Calculator commands

`mod([3, 7; 5, 12]*[8; 5], 26)`

`mod([3, 7; 5, 12]*[8, 18, 5, 20, 1, 4, 5; 5, 2, 18, 25, 18, 12, 25], 26)`

Mathematica commands

In[1]:=

`Mod[{{3, 7}, {5, 12}}.{ {8}, {5}}, 26]`

Out[1]=

`{{7}, {22}}`

In[4]:=

`Mod[{{3, 7}, {5, 12}}. { {8, 18, 5, 20, 1, 4, 5}, {5, 2, 18, 25, 18, 12, 25}}, 26]`

Out[4]=

`{{7, 16, 11, 1, 25, 18, 8}, {22, 10, 7, 10, 13, 8, 13}}`