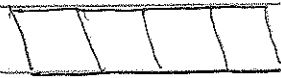


LFSR

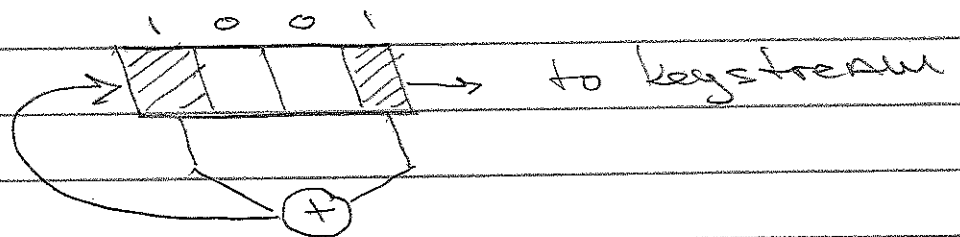
4-cell register



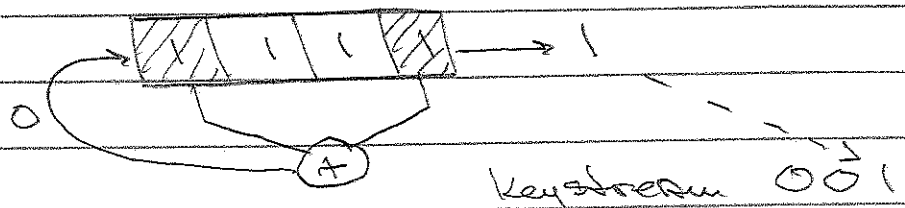
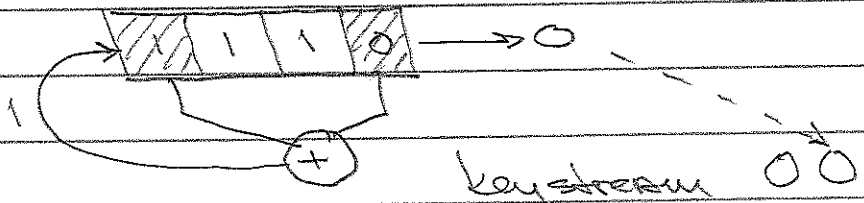
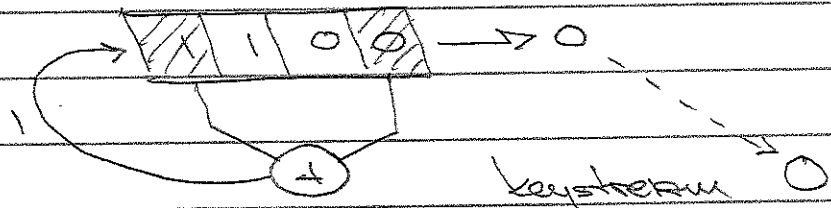
4-bit seed

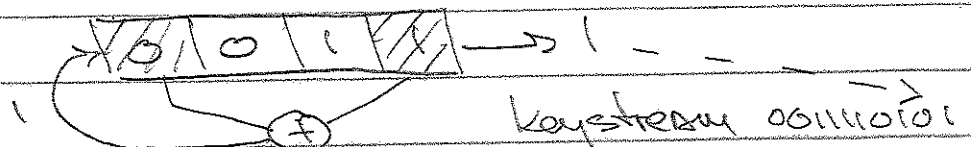
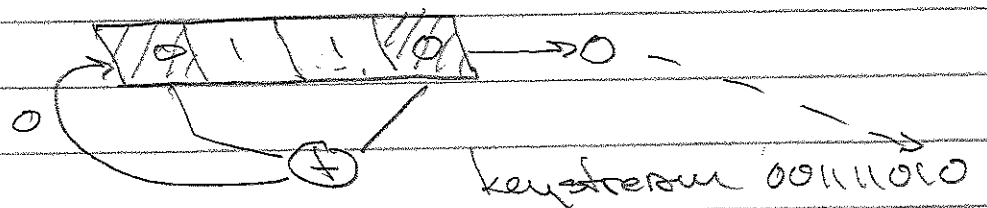
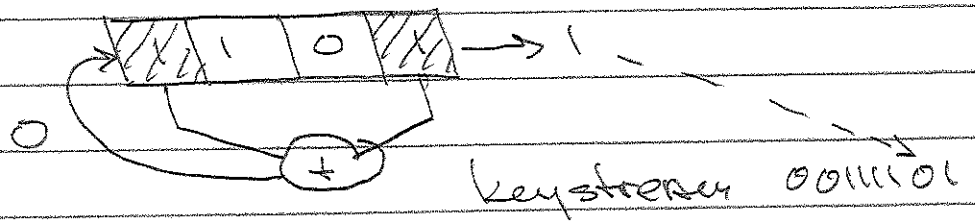
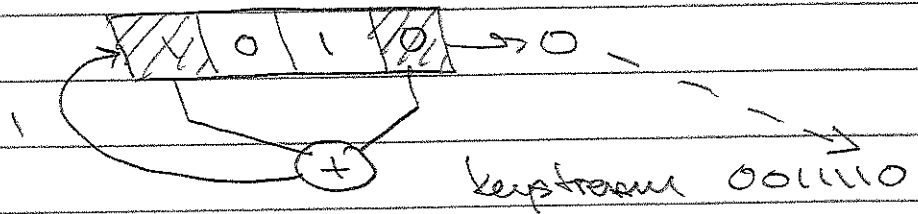
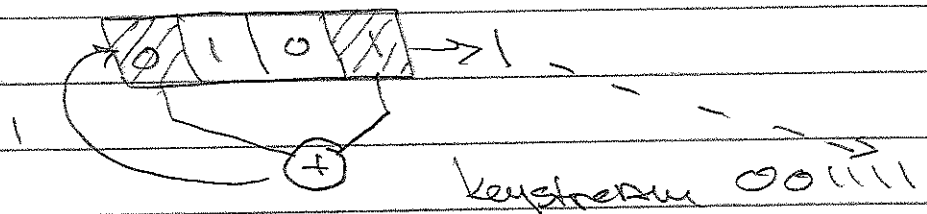
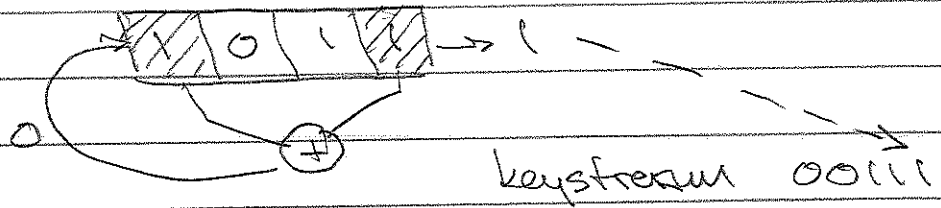
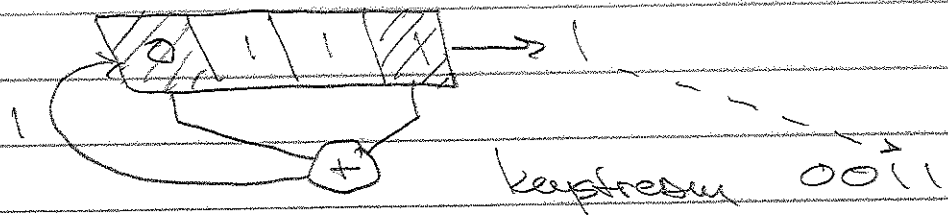
$$\text{Max period} = 2^4 - 1 = 15$$

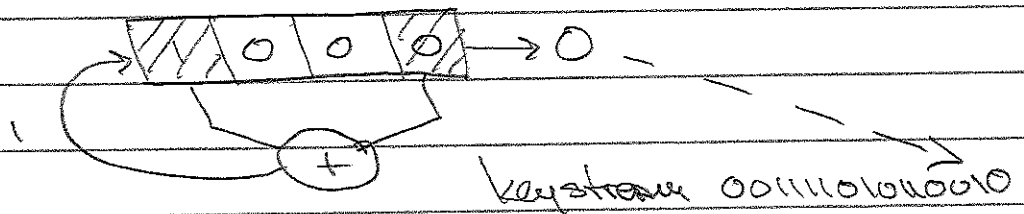
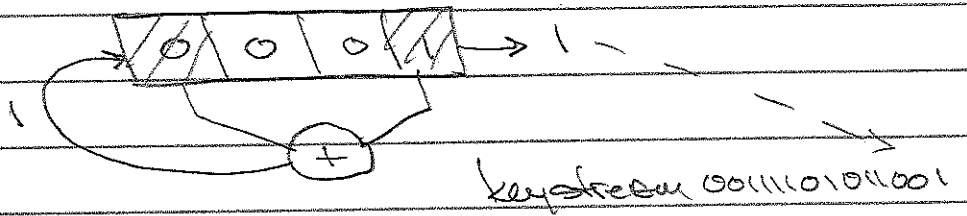
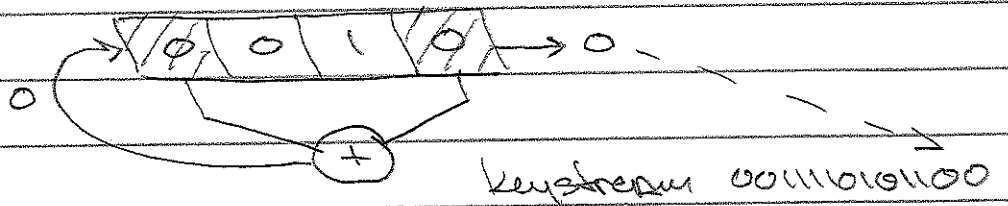
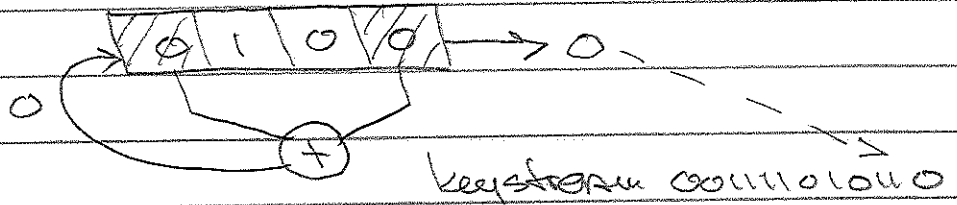
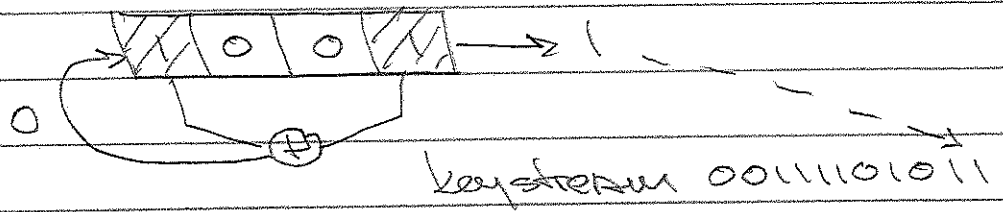
taps 9 1001



seed 1 1100







repeats

keystream 0011101010010010

MAX period

known pt attack

4-bit register

key stream

... 11101011 ...
8 bits

LFSR
linear function

$$f(b_4, b_3, b_2, b_1) = a_3 b_4 \oplus a_2 b_3 \oplus a_1 b_2 \oplus a_0 b_1$$

1 1 1 0 1 0 1 1
 $b_1 b_2 b_3 b_4 b_5 b_6 b_7 b_8$

$$f(b_4, b_3, b_2, b_1) =$$

$$a_3 \oplus a_2 \oplus a_0 = 1$$

$$a_3 \oplus a_1 \oplus a_0 = 0$$

etc.

$$a_2 \oplus a_0 = 1$$

$$a_3 \oplus a_1 = 1$$

b_5

b_6

b_7

b_8

solve

$$\begin{cases} a_3 \oplus a_2 \oplus a_0 = 1 \\ a_3 \oplus a_1 \oplus a_0 = 0 \\ a_2 \oplus a_0 = 1 \\ a_3 \oplus a_1 = 1 \end{cases}$$

$$\begin{array}{rcl}
 a_3 & \oplus & a_1 \oplus a_0 = 0 \\
 a_2 & \oplus & a_1 \oplus a_0 = 1 \\
 a_2 & & \oplus a_0 = 1 \\
 a_3 & \oplus & a_1 = 1
 \end{array}$$

$$\begin{array}{rcl}
 a_3 & \oplus & a_1 \oplus a_0 = 0 \\
 a_2 & \oplus & a_1 \oplus a_0 = 1 \\
 a_2 & & \oplus a_0 = 1 \\
 & & a_0 = 1
 \end{array}$$

$$\begin{array}{rcl}
 a_3 & \oplus & a_1 \oplus a_0 = 0 \\
 & & a_1 = 0 \\
 a_2 & & \oplus a_0 = 1 \\
 & & a_0 = 1
 \end{array}$$

$$\begin{array}{rcl}
 a_3 & \oplus & a_1 \oplus a_0 = 0 \\
 & & a_1 = 0 \\
 a_2 & & = 0 \\
 & & a_0 = 1
 \end{array}$$

$$\begin{array}{rcl}
 a_3 & & = 1 \\
 & & a_1 = 0 \\
 & & a_2 = 0 \\
 & & a_0 = 1
 \end{array}$$

$$f(b_4, b_3, b_2, b_1) = b_4 \oplus b_1$$

