

Formally Verified Cryptographic Proof Systems in Lean

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Chapter 1

Introduction

The goal of this project is to formalize Succinct Non-Interactive Arguments of Knowledge (SNARKs) in Lean. Our focus is on SNARKs based on Interactive Oracle Proofs (IOPs). We plan to build a general framework for IOP-based SNARKs that can state specifications of the protocols and prove their security properties in a clean and modular way.

Chapter 2

Oracle Reductions

2.1 Definitions

Definition 1 (Interactive Protocol). An n -round *interactive protocol* between two parties P, V is a sequence of messages $c_0, m_0, \dots, c_n, m_n$ where:

- c_i is a challenge sent by V to P in the i -th round.
- m_i is a message sent by P to V in the i -th round.

Each message m_i and challenge c_i may be of different types. We bundle them all together as a `ProtocolSpec` structure.

Definition 2 (Oracle Reduction). An (*interactive*) *oracle reduction* is an interactive protocol with a prover and a verifier.

2.2 Composition

Chapter 3

Commitment Schemes

3.1 Definitions

3.2 Composition

Chapter 4

Proof Systems

4.1 The Sum-Check Protocol

4.2 The Spartan Protocol

4.3 The Liger Polynomial Commitment Scheme

Chapter 5

Supporting Results

5.1 Polynomials

5.2 Coding Theory

Chapter 6

References