

WHIR (blueprint)

LeastAuthority

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**Definition 3.1.** An error-correcting code of length  $n$  over an alphabet  $\Sigma$  is a subset  $\mathcal{C} \subseteq \Sigma^n$ . The code  $\mathcal{C}$  is a *linear code* if  $\Sigma = \mathbb{F}$  is a field and  $\mathcal{C}$  is a subspace of  $\mathbb{F}^n$ .

**Definition 1** (3.4). We define the *equality polynomial*  $\text{eq}$  as follows:

$$\text{eq}((X_0, \dots, X_{m-1}), (Y_0, \dots, Y_{m-1})) = \prod_{i=0}^{m-1} (X_i \cdot Y_i + (1 - X_i) \cdot (1 - Y_i)).$$

Note that, for every  $\hat{f} \in \mathbb{F}^{<2^{[X_0, \dots, X_{m-1}]}}$  and  $z \in \mathbb{F}^m$ ,

$$\hat{f}(z) = \sum_{b \in \{0,1\}^m} \hat{f}(b) \cdot \text{eq}(z, b).$$