

180206081104P2009H

图像处理与分析

第一讲 (II): 绪论: 图像与视觉

数字图像的获取, 成像与采样, 彩色图像

第一讲 (I): 常见问题

- 机器视觉与计算机视觉的区别是什么?
 - 通常在工业场景下的计算机视觉被称为机器视觉
 - 在工业场景下成像条件经常可控
- 本课程需要的数学基础是什么? 如何准备?
 - 线性代数, 微积分, 概率论 (参考Gonzalez第二章)
 - Justin Solomon 的讲义, 非课程要求, 仅供参考
<http://people.csail.mit.edu/jsolomon/>
- 如何才能学会做图像处理算法?
 - 针对一个图像处理问题建立合理的数学模型, 进而对模型采用数值/优化方法进行求解

内容提纲

- 图像格式示例
- 图像获取
- 图像采样与量化
- 空间分辨率与灰度分辨率
- 像素间的基本关系
- 图像处理的基本数学工具
- 彩色图像

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图像格式示例: PBM/PGM/PPM

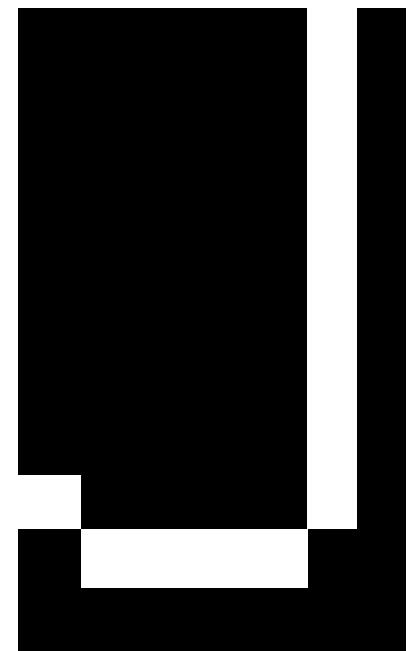
- PBM: portable bitmap format
- PGM: portable graymap format
- PPM: portable pixmap format

Magic Number	Type	Encoding
P1	Portable bitmap	ASCII
P2	Portable graymap	ASCII
P3	Portable pixmap	ASCII
P4	Portable bitmap	Binary
P5	Portable graymap	Binary
P6	Portable pixmap	Binary

http://en.wikipedia.org/wiki/Netpbm_format

例 1: PBM

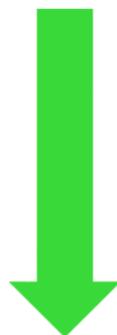
```
P1
# This is an example bitmap of the letter "J"
6 10
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
0 0 0 0 1 0
1 0 0 0 1 0
0 1 1 1 0 0
0 0 0 0 0 0
0 0 0 0 0 0
```



http://en.wikipedia.org/wiki/Netpbm_format

例 2: PGM

```
P2
# Shows the word "FEEP" (example from Netpbm main page on PGM)
24 7
15
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
0 3 3 3 3 0 0 7 7 7 7 0 0 0 11 11 11 11 0 0 15 15 15 15 0
0 3 0 0 0 0 0 7 0 0 0 0 0 11 0 0 0 0 0 15 0 0 15 0
0 3 3 3 0 0 0 7 7 7 0 0 0 0 11 11 11 0 0 0 15 15 15 15 0
0 3 0 0 0 0 0 7 0 0 0 0 0 11 0 0 0 0 0 15 0 0 0 0
0 3 0 0 0 0 0 7 7 7 7 0 0 0 11 11 11 11 0 0 0 15 0 0 0 0
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
```



http://en.wikipedia.org/wiki/Netpbm_format

例 3: PPM

P3

The P3 means colors are in ASCII, then 3 columns and 2 rows,
then 255 for max color, then RGB triplets

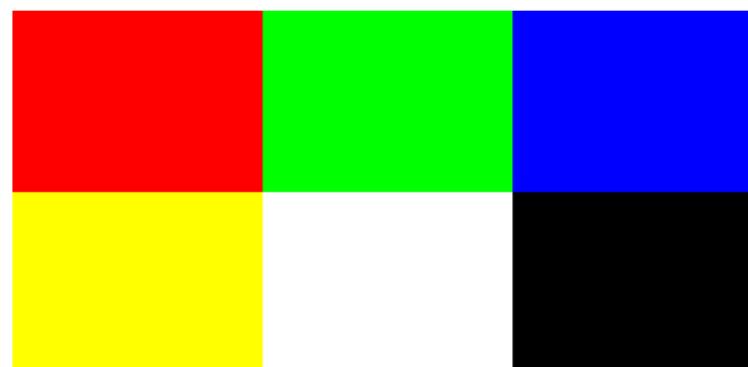
3 2

255

255	0	0
255	255	0

0	255	0
255	255	0

0	0	255
0	255	0



http://en.wikipedia.org/wiki/Netpbm_format

文件格式示例：TIFF-Tagged Image File Format

- TIFF 是一种常用无损图像格式

<https://www.adobe.io/open/standards/TIFF.html>

最新版: TIFF 6.0 (1992), TIFF Supplement 2 (2002)

- 其他常见的图像格式包括: bmp, jpeg, gif, png等等

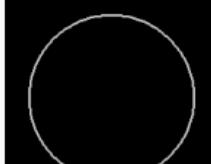
https://helpx.adobe.com/hk_en/photoshop/using/file-formats.html

- 各种图像格式之间通常可以自由转换

- 实际应用中经常连带存储关于成像条件的metadata(元数据)

文件格式示例：JPEG-Joint Photographic Experts Group

- 正式标准于1992年发布，最新一次修订于2012。早期核心专利来自IBM和Mitsubishi Electric。
- 广泛应用于数字相机图像和互联网图像，采用有损压缩，通常压缩比可达10:1，节省文件存储空间。
- 不适于一些特定类型的图像如线条图像。
- 2002-2013 年间专利纠纷部分限制了其应用。

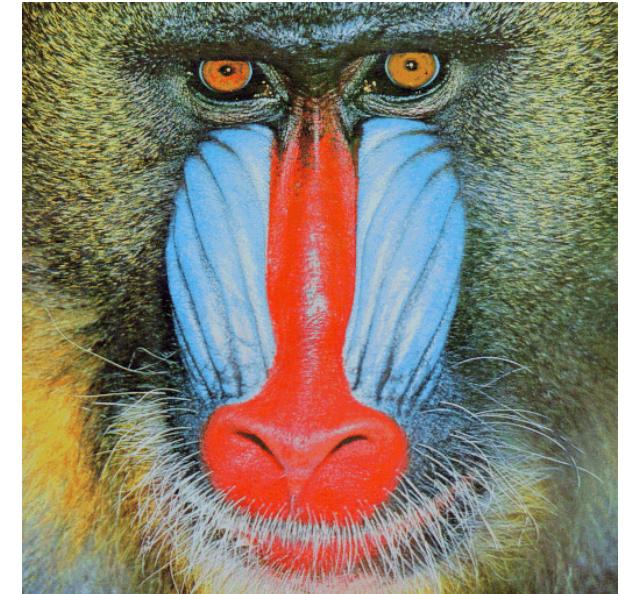
Image	Lossless compression	Lossy compression
Original		
Processed by Canny edge detector		

<https://en.wikipedia.org/wiki/JPEG>

MATLAB图像读写与显示函数

- 读写函数: imread, imwrite
- 显示函数: imshow

```
> img = imread('mandril_color.tif');  
> imshow(img, [ ]);  
  
> imwrite(img, 'tiff','compression','none');
```



mandril_color.tif

-
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数字图像采集典型场景示例 I

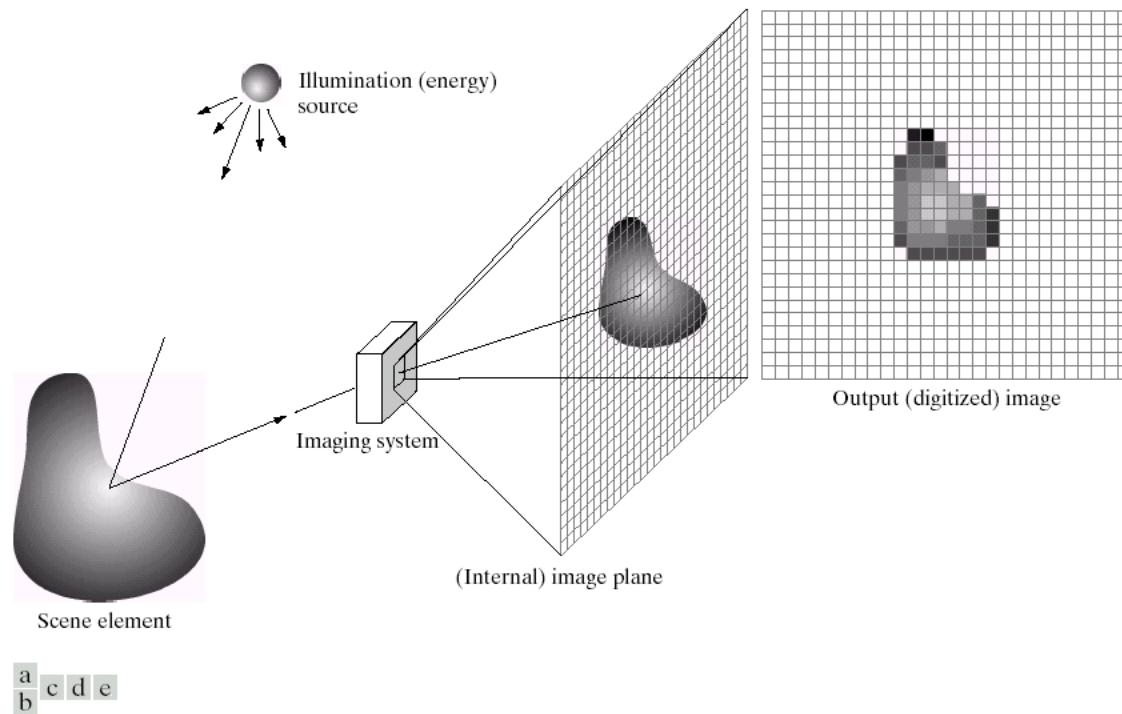
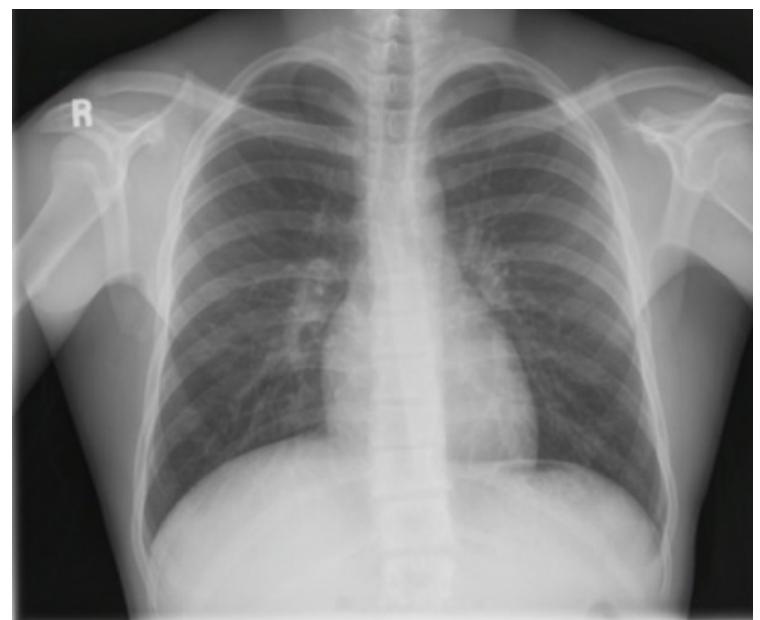
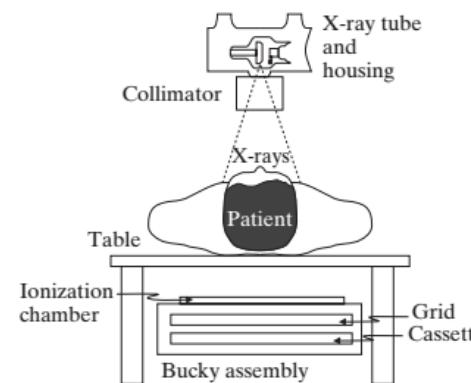
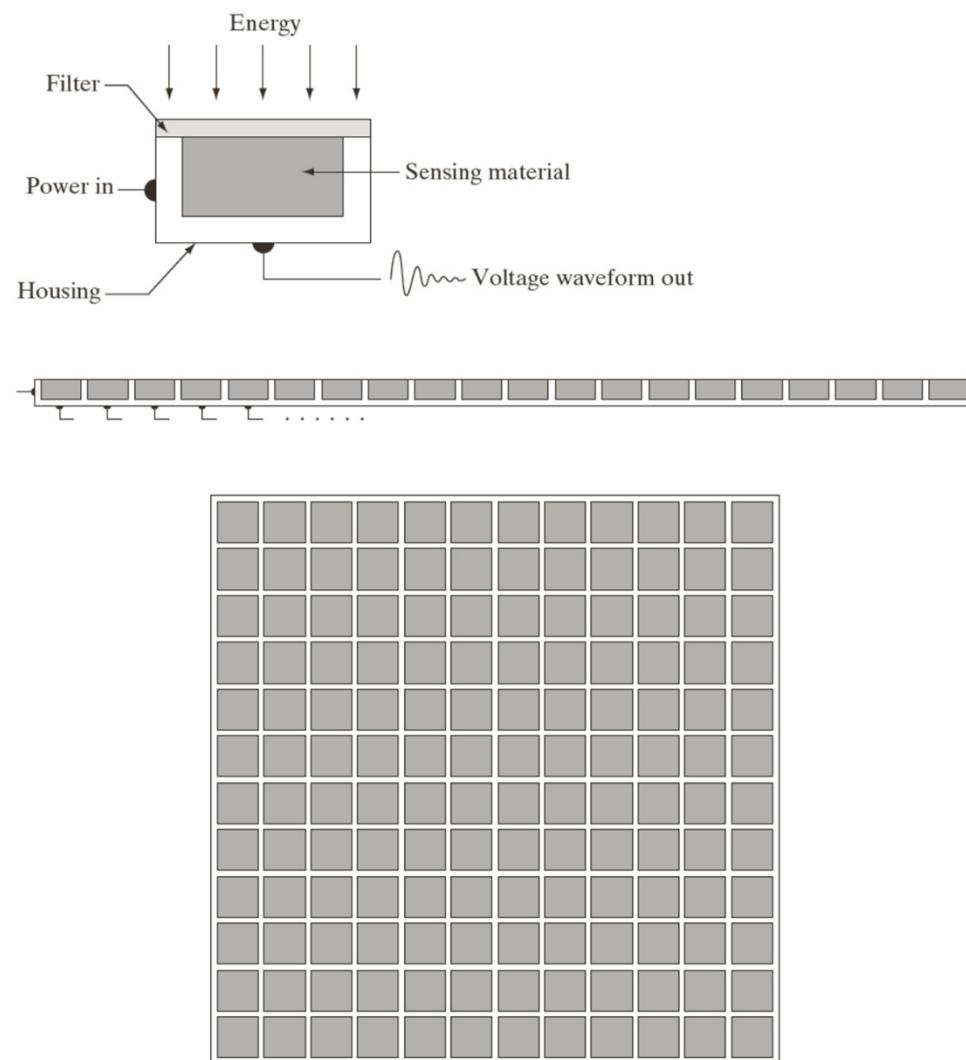


FIGURE 2.15 An example of the digital image acquisition process. (a) Energy (“illumination”) source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

数字图像采集典型场景示例 II



典型成像设备设置 (I)



a
b
c

FIGURE 2.12
(a) Single imaging sensor.
(b) Line sensor.
(c) Array sensor.

典型成像设备设置 (II)

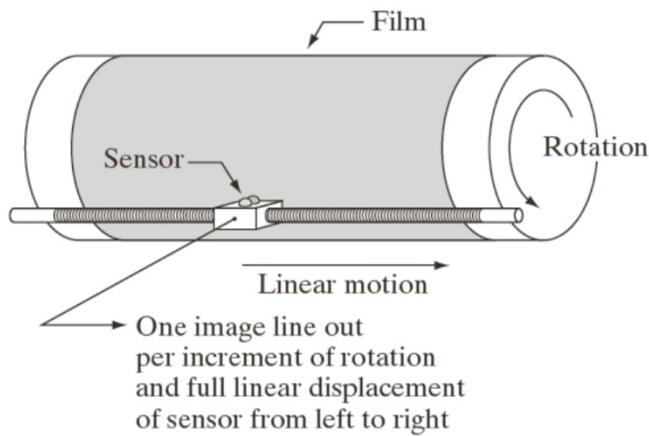
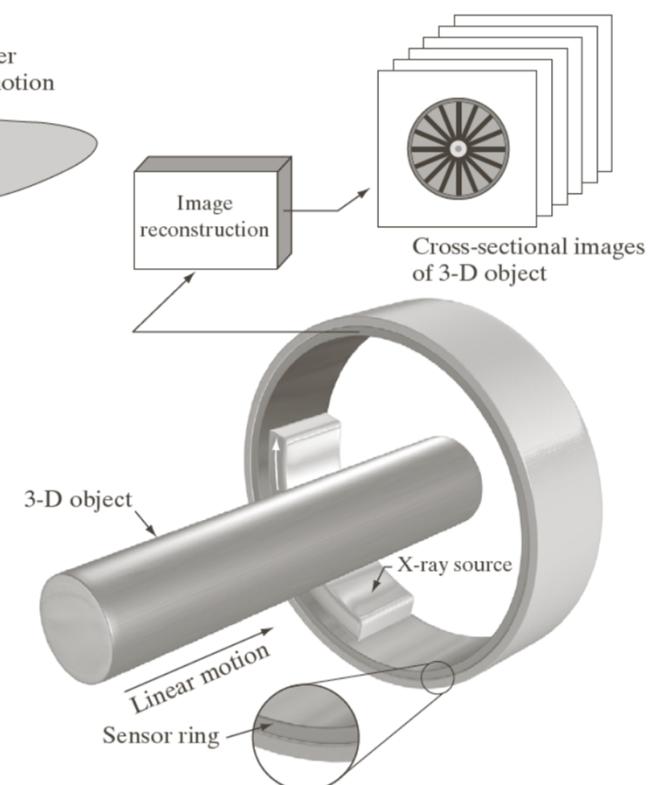
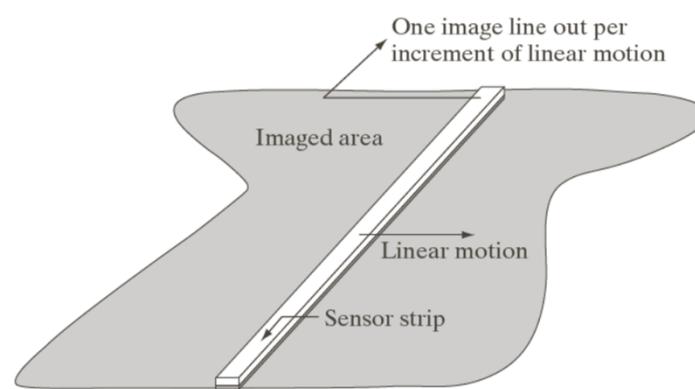


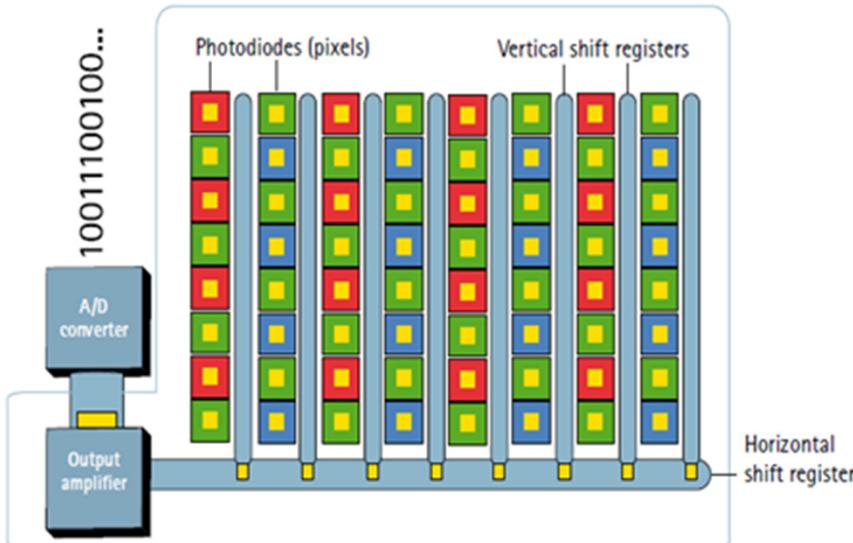
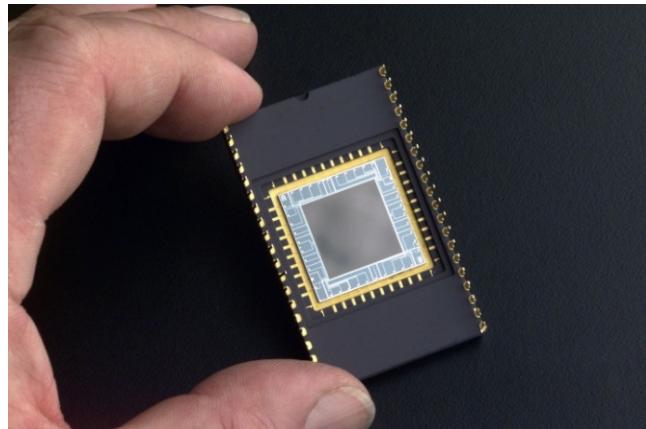
FIGURE 2.13
Combining a
single sensor with
motion to
generate a 2-D
image.



a b

FIGURE 2.14 (a) Image acquisition using a linear sensor strip. (b) Image acquisition using a circular sensor strip.

常用成像设备：CCD (电荷耦合器件)



The Nobel Prize in Physics 2009



© The Nobel Foundation. Photo: U. Montan
Charles Kuen Kao
Prize share: 1/2



© The Nobel Foundation. Photo: U. Montan
Willard S. Boyle
Prize share: 1/4

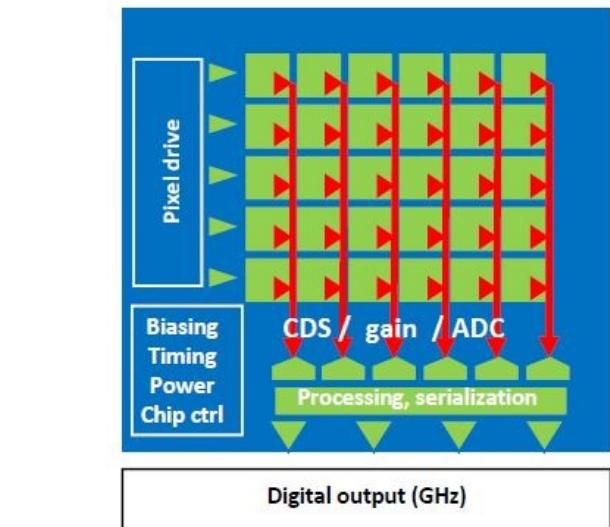
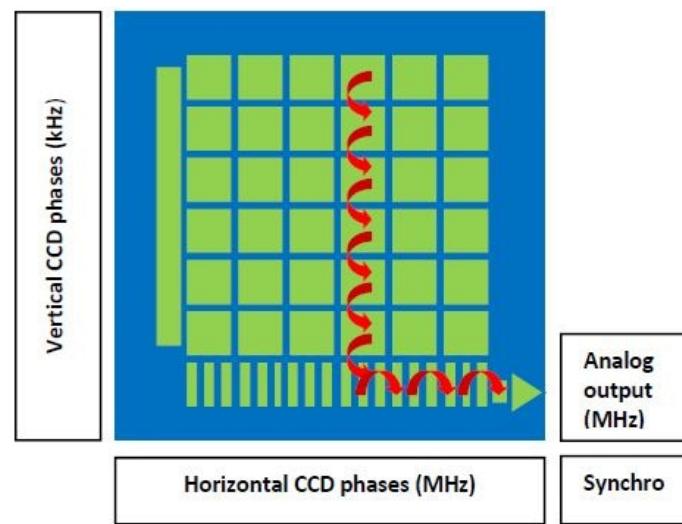
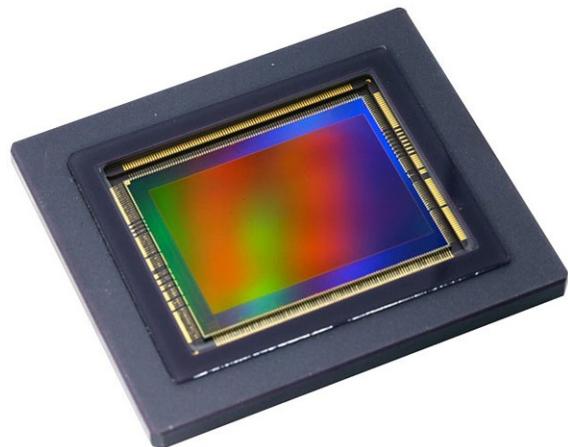


© The Nobel Foundation. Photo: U. Montan
George E. Smith
Prize share: 1/4

The Nobel Prize in Physics 2009 was divided, one half awarded to Charles Kuen Kao "for groundbreaking achievements concerning the transmission of light in fibers for optical communication", the other half jointly to Willard S. Boyle and George E. Smith "for the invention of an imaging semiconductor circuit - the CCD sensor."

<http://micro.magnet.fsu.edu/primer/java/digitalimaging/ccd/interline/index.html>

常用成像设备：CMOS (互补金属氧化物半导体)



<https://www.azom.com/article.aspx?ArticleID=16321>

<https://www.dpreview.com/news/0671207908/canon-is-now-selling-cmos-image-sensors-including-a-120mp-aps-h-beast>

像素的位深度 (I)

- 日常用相机的位深度为8
- 一般认为，典型条件下人类视觉的归一化灵敏度约为1/256.
- HDR10 (high dynamic range) 显示器对应的显示像素深度为10
- 研究用相机的像素位深度可达16



Bit Depth	Dynamic Range
8	0~255
10	0~1023
12	0~4095
16	0~65535

<http://micro.magnet.fsu.edu/primer/java/digitalimaging/ccd/interline/index.html>

<https://www.monitornerds.com/hdr-monitors-gaming/>

像素的位深度 (II)

	HDR10	HDR10+	Dolby Vision
Bit Depth	Good	Good	Great
Peak brightness	Great	Great	Excellent
Tone Mapping	Varies per Manufacturer	Better	Better
Metadata	Both	Dynamic	Dynamic
TV Support	Great	Limited	Limited
Content Availability	Good	Limited	Limited, but growing

Bit Depth

HDR10

- 10 bit
- 1.07 billion colors

HDR10+

- 10 bit
- 1.07 billion colors

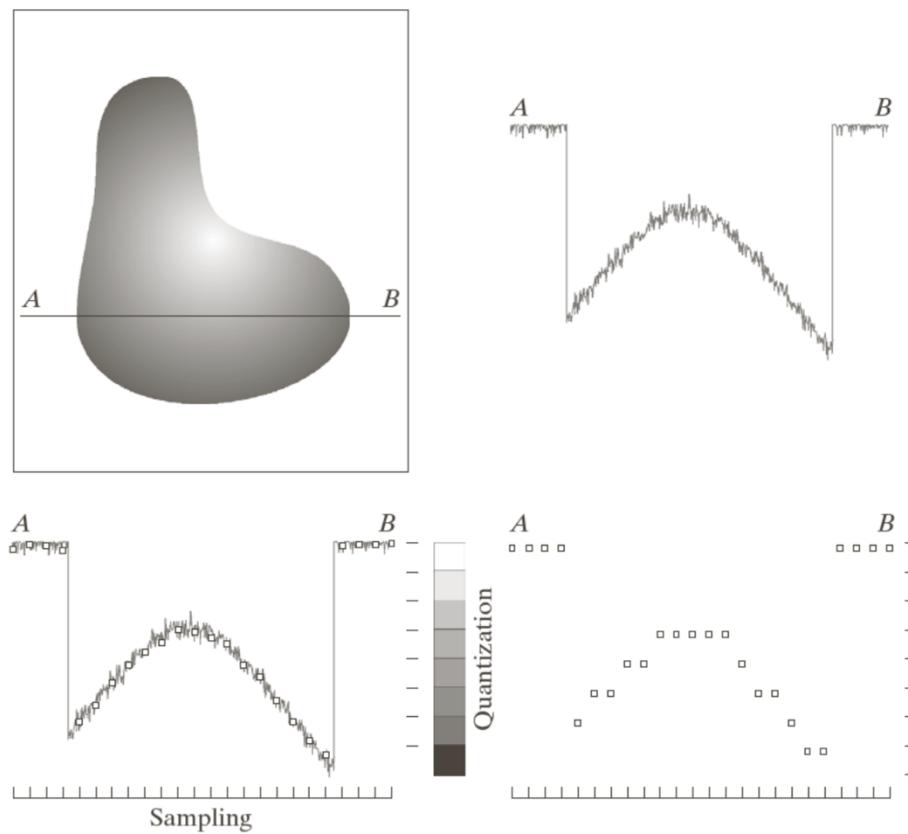
DOLBY VISION

- 12 bit
- 68.7 billion colors

<https://www.rtings.com/tv/learn/hdr10-vs-dolby-vision>

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采样与量化 (I)



a b
c d

FIGURE 2.16
Generating a digital image.
(a) Continuous image. (b) A scan line from A to B in the continuous image, used to illustrate the concepts of sampling and quantization.
(c) Sampling and quantization.
(d) Digital scan line.

采样与量化 (II)

- 空间采样与量化由物理像素决定。
- 灰度采样与量化由模拟-数字转换决定。

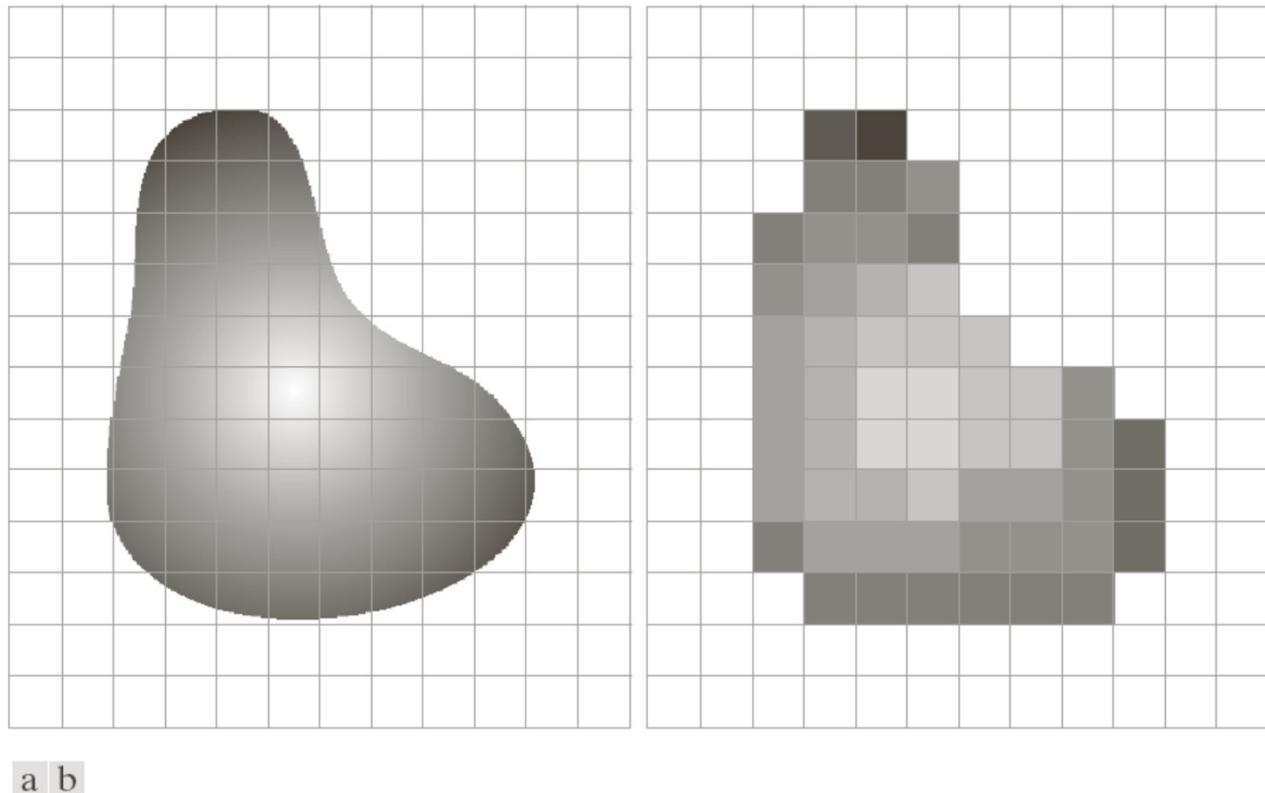
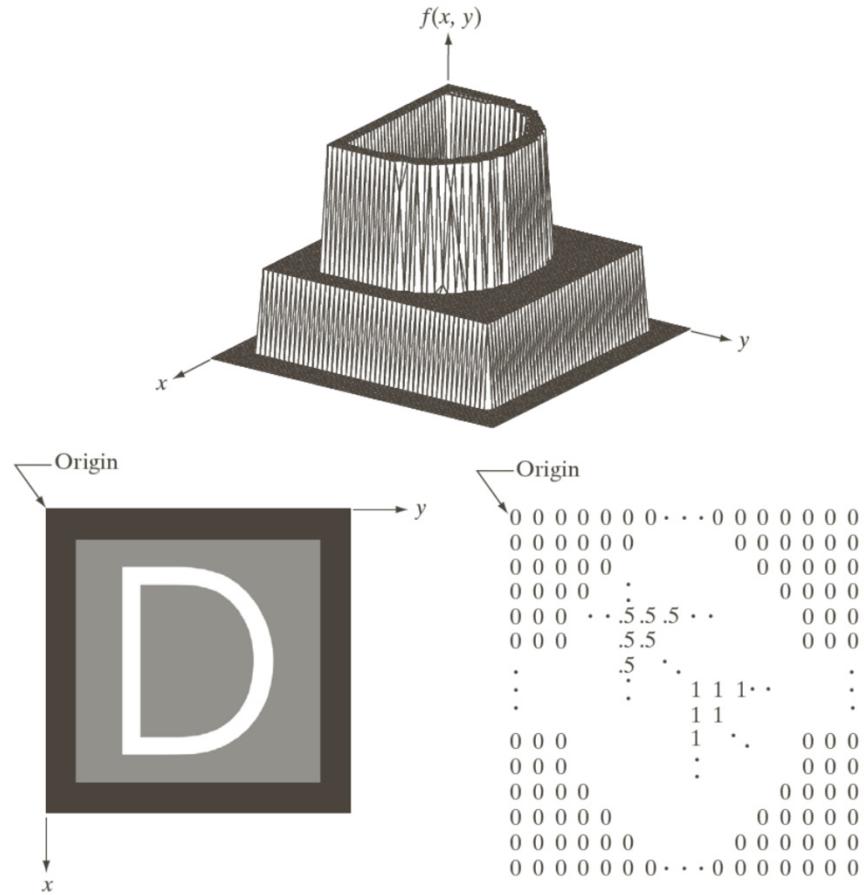


FIGURE 2.17 (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

图像的表示



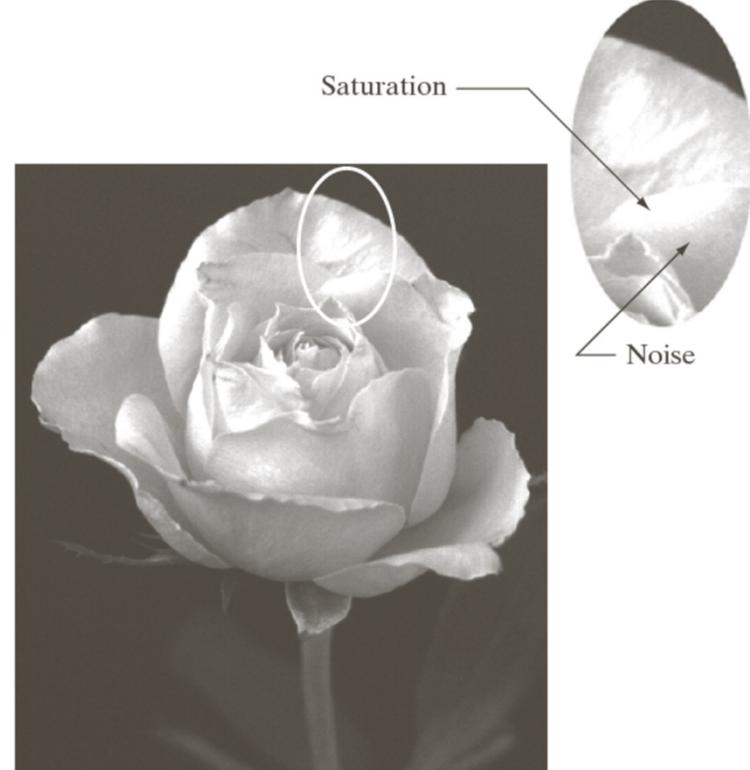
a
b c

FIGURE 2.18
 (a) Image plotted as a surface.
 (b) Image displayed as a visual intensity array.
 (c) Image shown as a 2-D numerical array (0, .5, and 1 represent black, gray, and white, respectively).

几个相关基本概念

- 动态范围 (dynamic range) -> $[I_{\min}, I_{\max}]$
- 饱和 (saturation)
- 对比度 (contrast) = I_{\max}/I_{\min}

FIGURE 2.19 An image exhibiting saturation and noise. Saturation is the highest value beyond which all intensity levels are clipped (note how the entire saturated area has a high, *constant* intensity level). Noise in this case appears as a grainy texture pattern. Noise, especially in the darker regions of an image (e.g., the stem of the rose) masks the lowest detectable true intensity level.



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图像的空间分辨率



a b
c d

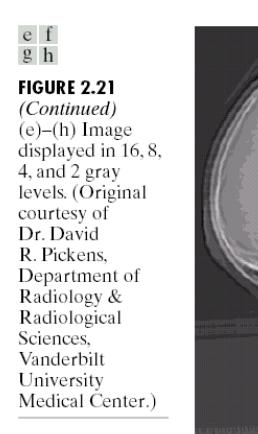
FIGURE 2.20 Typical effects of reducing spatial resolution. Images shown at: (a) 1250 dpi, (b) 300 dpi, (c) 150 dpi, and (d) 72 dpi. The thin black borders were added for clarity. They are not part of the data.

图像的灰度分辨率



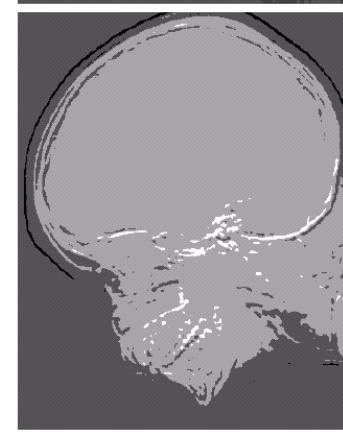
a
b
c
d

FIGURE 2.21
(a) 452×374 ,
256-level image.
(b)–(d) Image
displayed in 128,
64, and 32 gray
levels, while
keeping the
spatial resolution
constant.



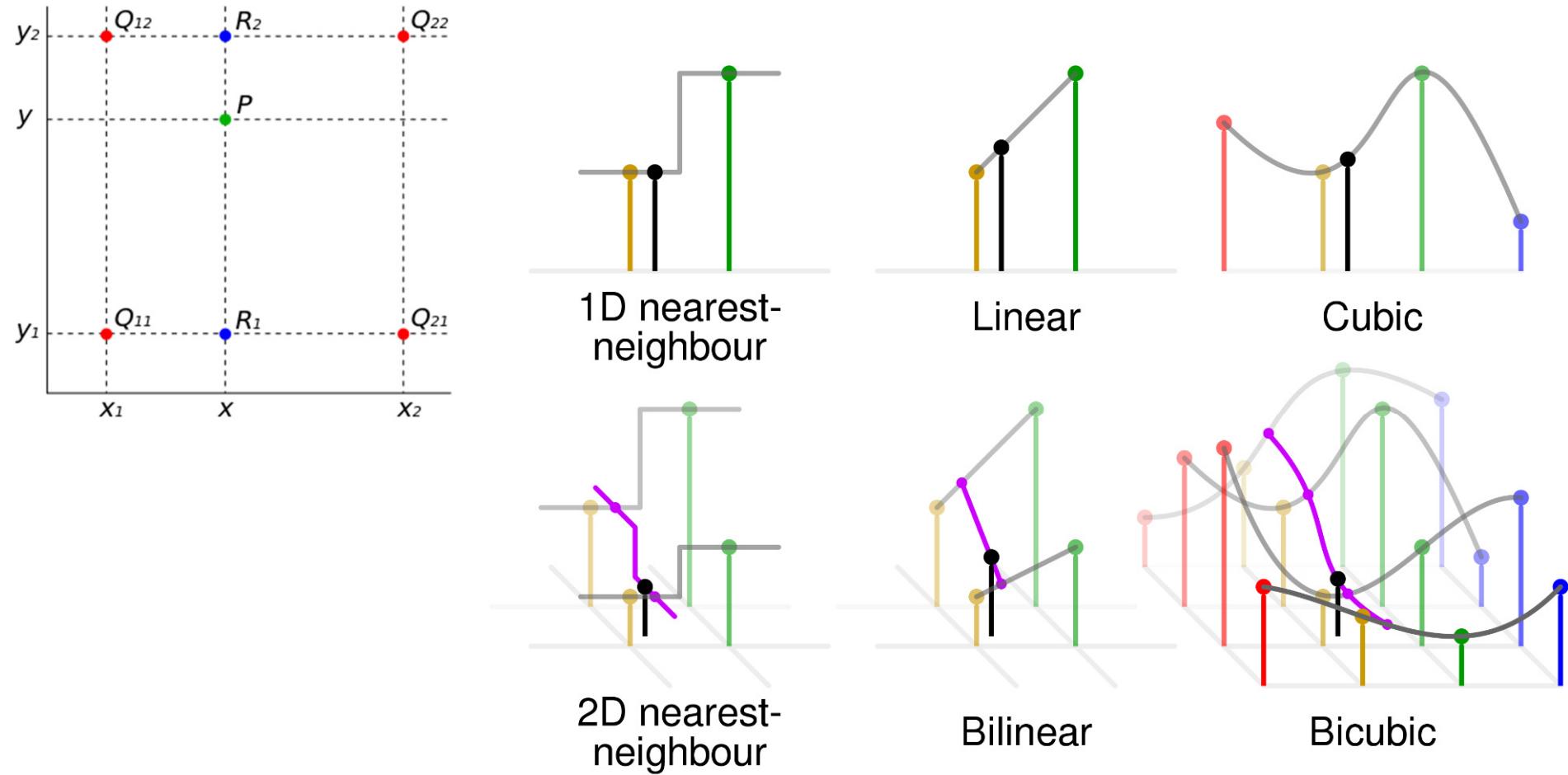
e
f
g
h

FIGURE 2.21
(Continued)
(e)–(h) Image
displayed in 16, 8,
4, and 2 gray
levels. (Original
courtesy of
Dr. David
R. Pickens,
Department of
Radiology &
Radiological
Sciences,
Vanderbilt
University
Medical Center.)



e
f
g
h

图像插值



https://en.wikipedia.org/wiki/Bilinear_interpolation

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像素间的基本关系

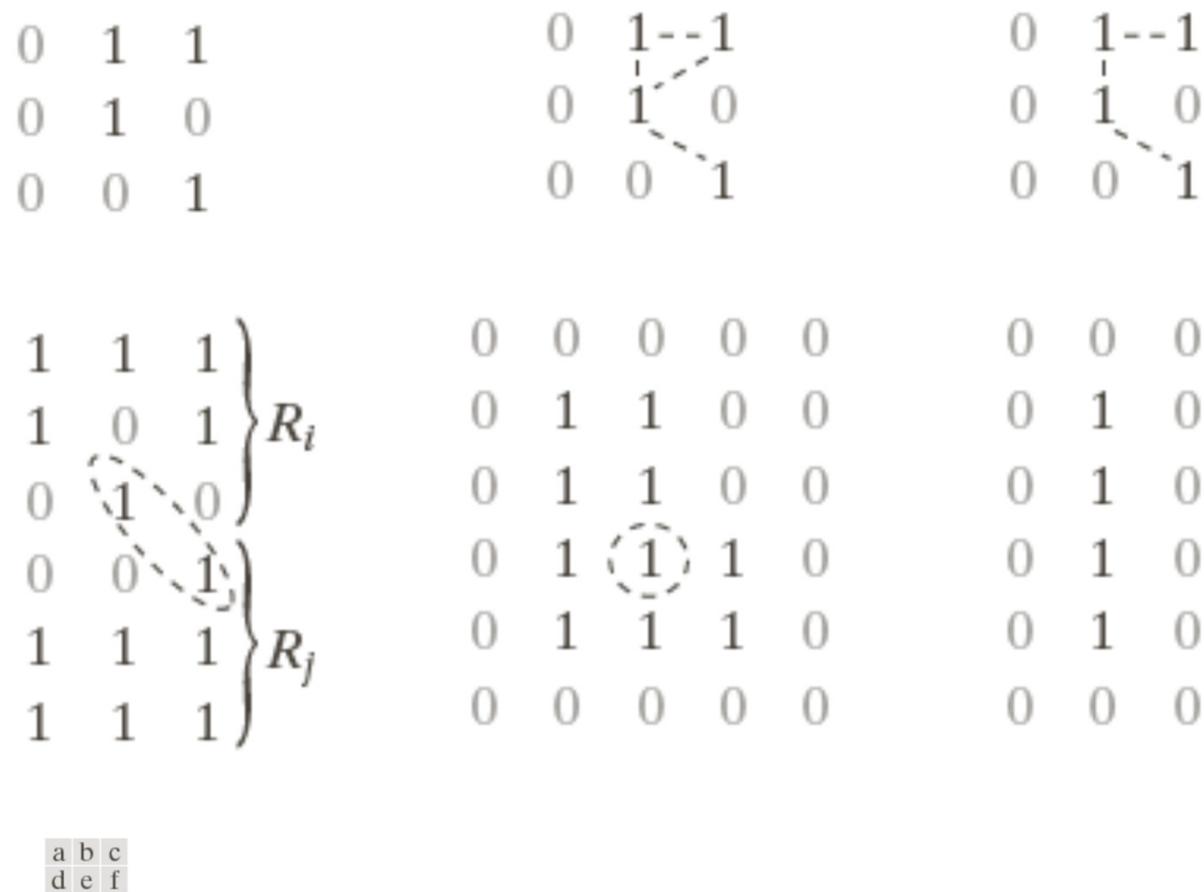
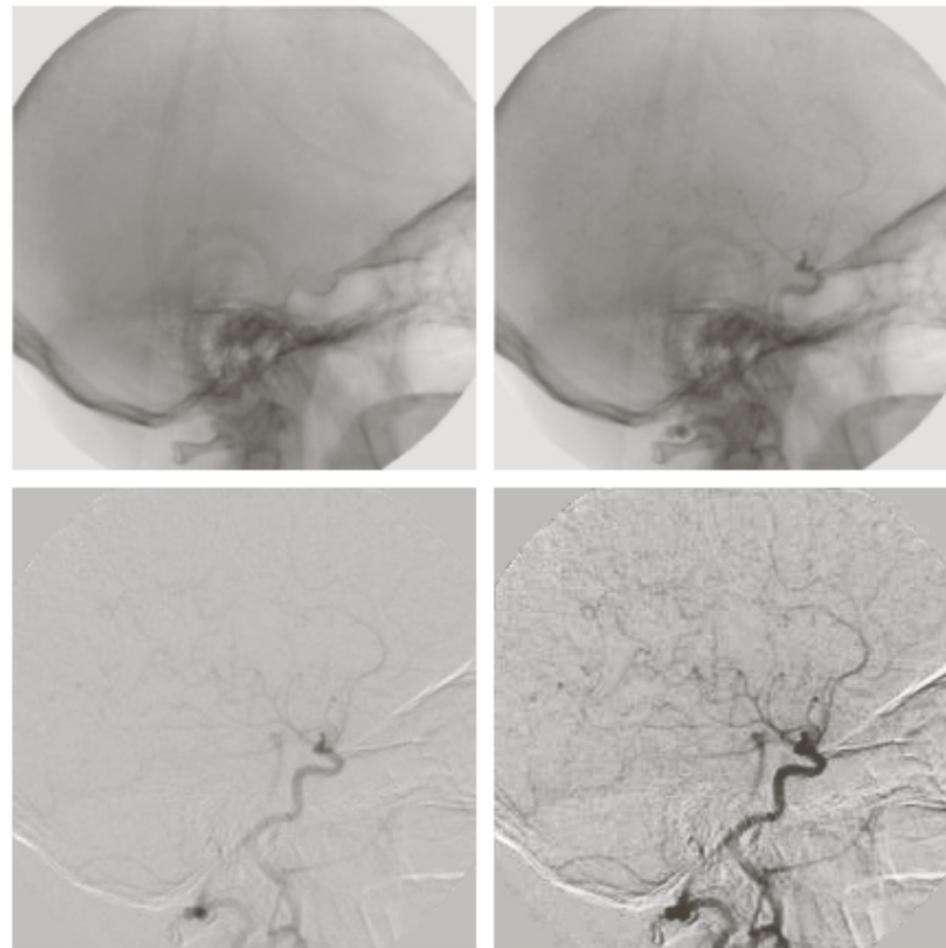


FIGURE 2.25 (a) An arrangement of pixels. (b) Pixels that are 8-adjacent (adjacency is shown by dashed lines; note the ambiguity). (c) m -adjacency. (d) Two regions that are adjacent if 8-adjacency is used. (e) The circled point is part of the boundary of the 1-valued pixels only if 8-adjacency between the region and background is used. (f) The inner boundary of the 1-valued region does not form a closed path, but its outer boundary does.

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图像的简单算数运算 (I)



a b
c d

FIGURE 2.28
Digital subtraction angiography.
(a) Mask image.
(b) A live image.
(c) Difference between (a) and (b). (d) Enhanced difference image.
(Figures (a) and (b) courtesy of The Image Sciences Institute, University Medical Center, Utrecht, The Netherlands.)

图像的简单算数运算 (II)

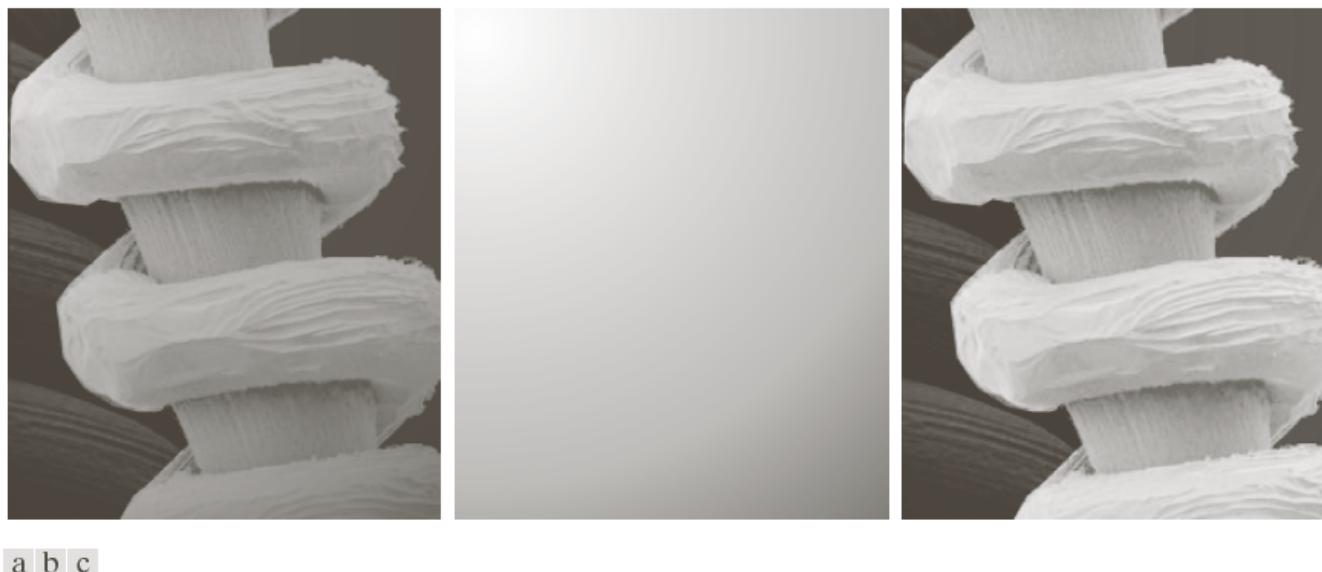


FIGURE 2.29 Shading correction. (a) Shaded SEM image of a tungsten filament and support, magnified approximately 130 times. (b) The shading pattern. (c) Product of (a) by the reciprocal of (b). (Original image courtesy of Mr. Michael Shaffer, Department of Geological Sciences, University of Oregon, Eugene.)

图像的集合与逻辑运算示例 (I)

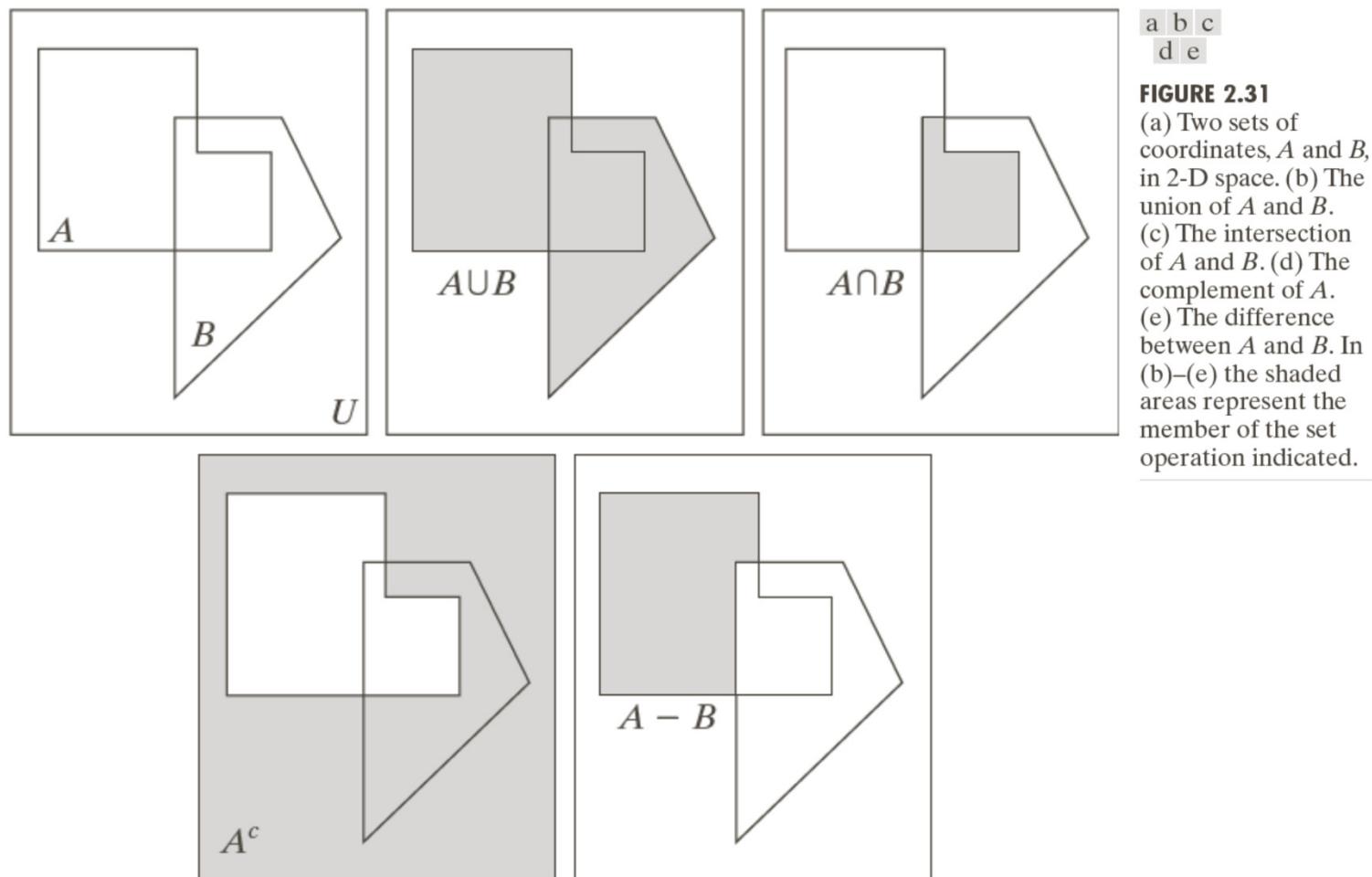


FIGURE 2.31

(a) Two sets of coordinates, A and B , in 2-D space. (b) The union of A and B .
(c) The intersection of A and B . (d) The complement of A .
(e) The difference between A and B . In (b)–(e) the shaded areas represent the member of the set operation indicated.

图像的集合与逻辑运算示例 (II)

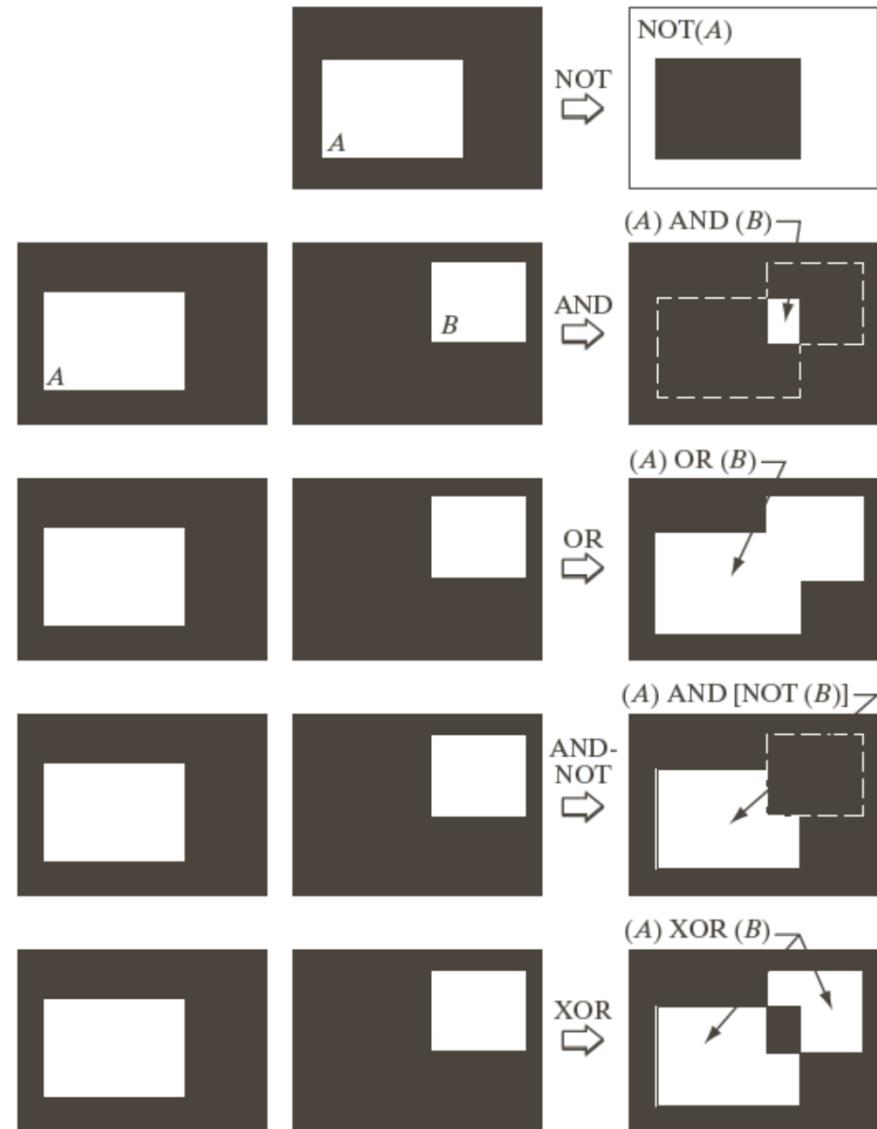


FIGURE 2.33
Illustration of logical operations involving foreground (white) pixels. Black represents binary 0s and white binary 1s. The dashed lines are shown for reference only. They are not part of the result.

线性算子的基本概念



FIGURE 2.39
General approach
for operating in
the linear
transform
domain.

$$R[f(x, y)] = g(x, y)$$

$$\begin{aligned} R[a_1f_1(x, y) + a_2f_2(x, y)] &= a_1R[f_1(x, y)] + a_2R[f_2(x, y)] \\ &= a_1g_1(x, y) + a_2g_2(x, y) \end{aligned}$$

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色彩的基本概念 (I)

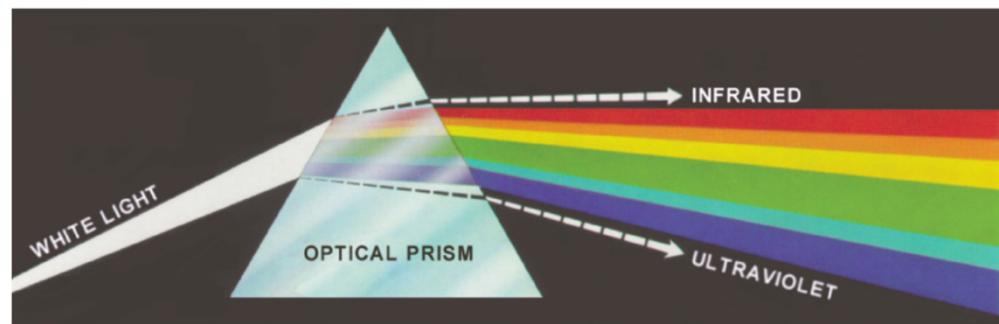


FIGURE 6.1 Color spectrum seen by passing white light through a prism. (Courtesy of the General Electric Co., Lamp Business Division.)

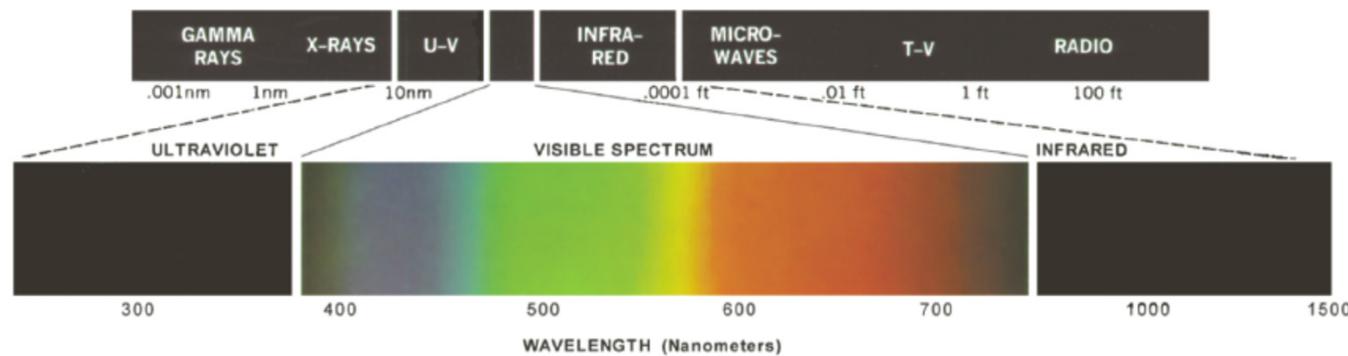


FIGURE 6.2 Wavelengths comprising the visible range of the electromagnetic spectrum. (Courtesy of the General Electric Co., Lamp Business Division.)

色彩的基本概念 (II)

- 人类的锥状感光细胞中65%对于红色敏感，33%对于绿色敏感，只有2%对于蓝色敏感。
- 国际照明委员会定义
蓝 = 435.8 nm
绿 = 546.1 nm
红 = 700 nm

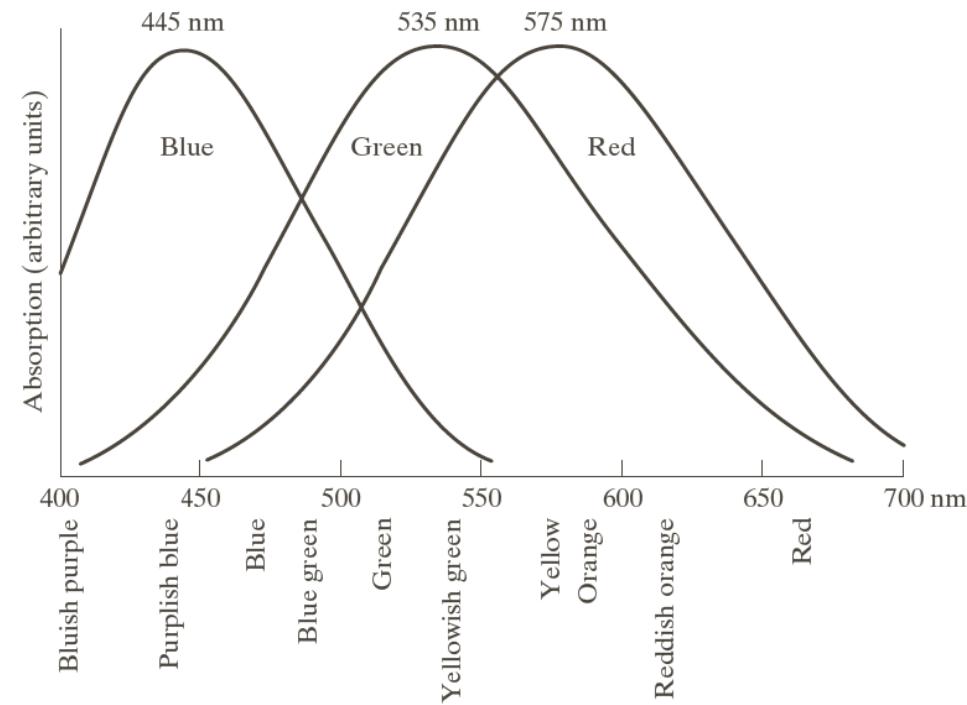


FIGURE 6.3
Absorption of light by the red, green, and blue cones in the human eye as a function of wavelength.

不同颜色的组合

- 光的原色与二次色
- 颜料的原色与二次色
- 三色值系数

$$x = X/(X+Y+Z)$$

$$y = Y/(X+Y+Z)$$

$$z = Z/(X+Y+Z)$$

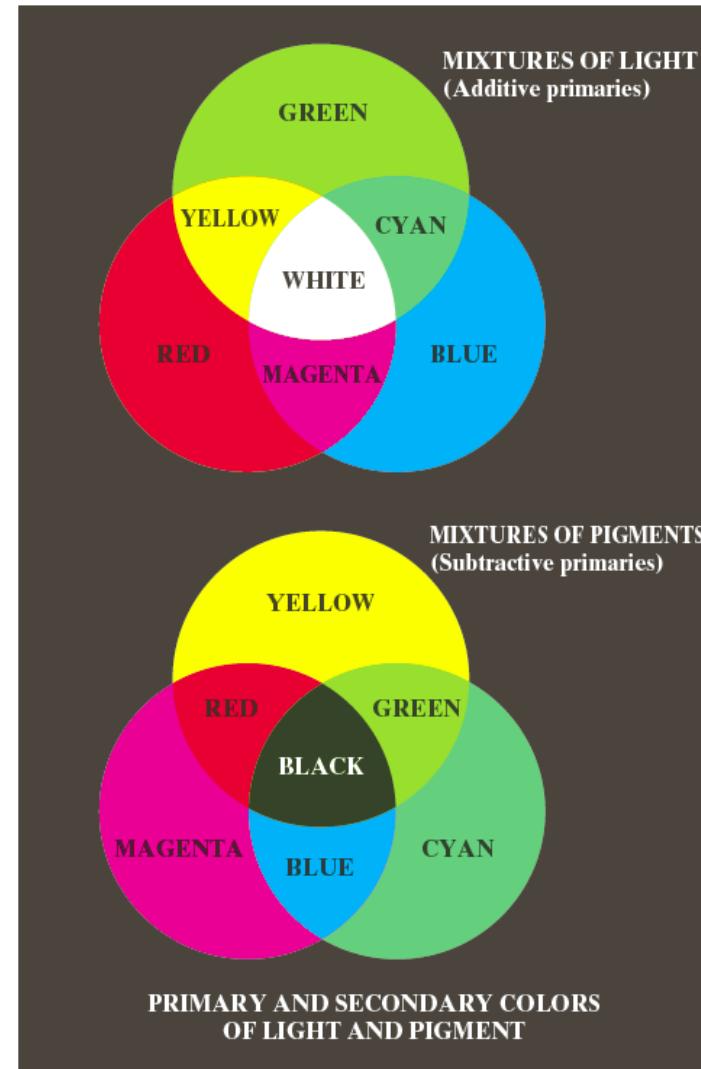


FIGURE 6.4
Primary and secondary colors of light and pigments.
(Courtesy of the General Electric Co., Lamp Business Division.)

彩色模型(I): RGB模型 (I)

- $(2^8)^3 = 16,777,216$

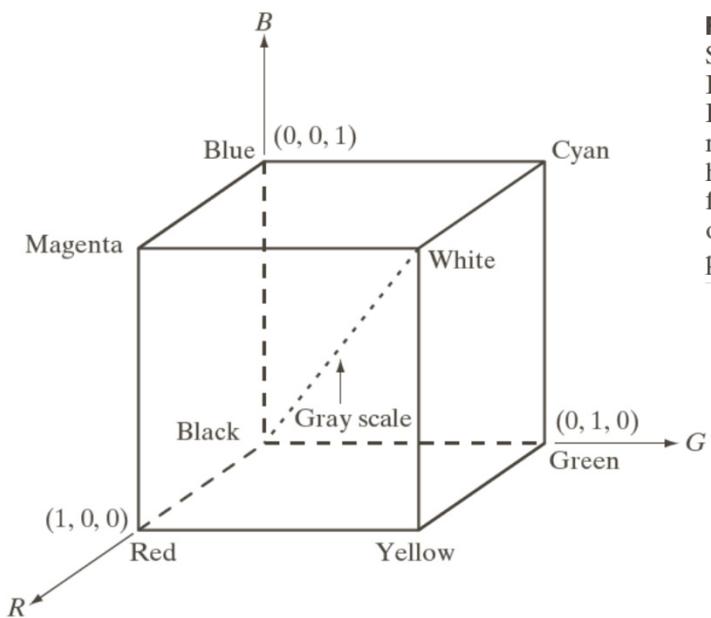


FIGURE 6.7
Schematic of the RGB color cube. Points along the main diagonal have gray values, from black at the origin to white at point $(1, 1, 1)$.

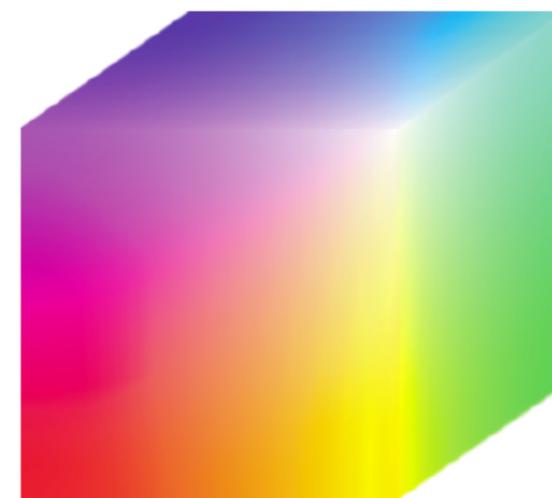
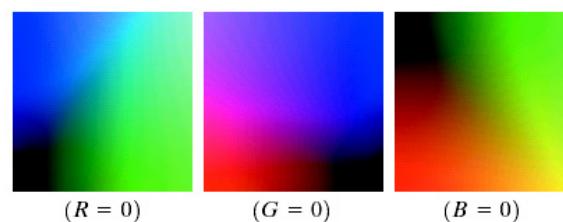
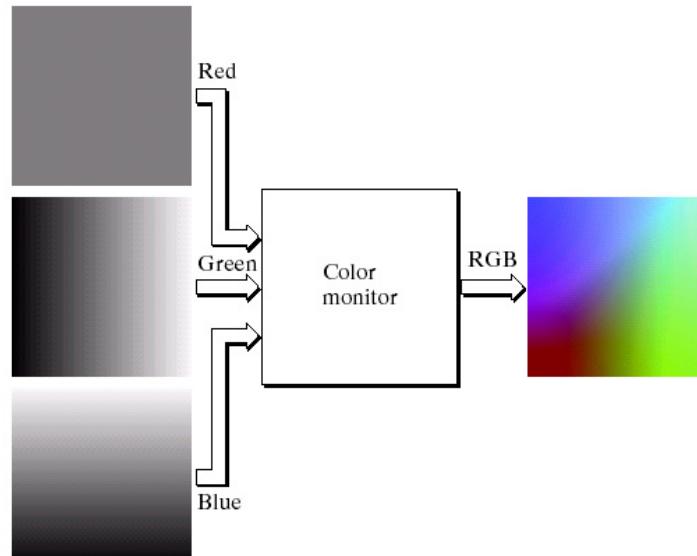


FIGURE 6.8 RGB 24-bit color cube.

彩色模型(I): RGB模型 (II)

a
b

FIGURE 6.9
(a) Generating
the RGB image of
the cross-sectional
color plane
 $(127, G, B)$.
(b) The three
hidden surface
planes in the color
cube of Fig. 6.8.



CMY 和CMYK模型

$$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

HSI 模型

- H: 色调
 - 纯度
- S: 饱和度
 - 白色的稀释度
- I: 强度

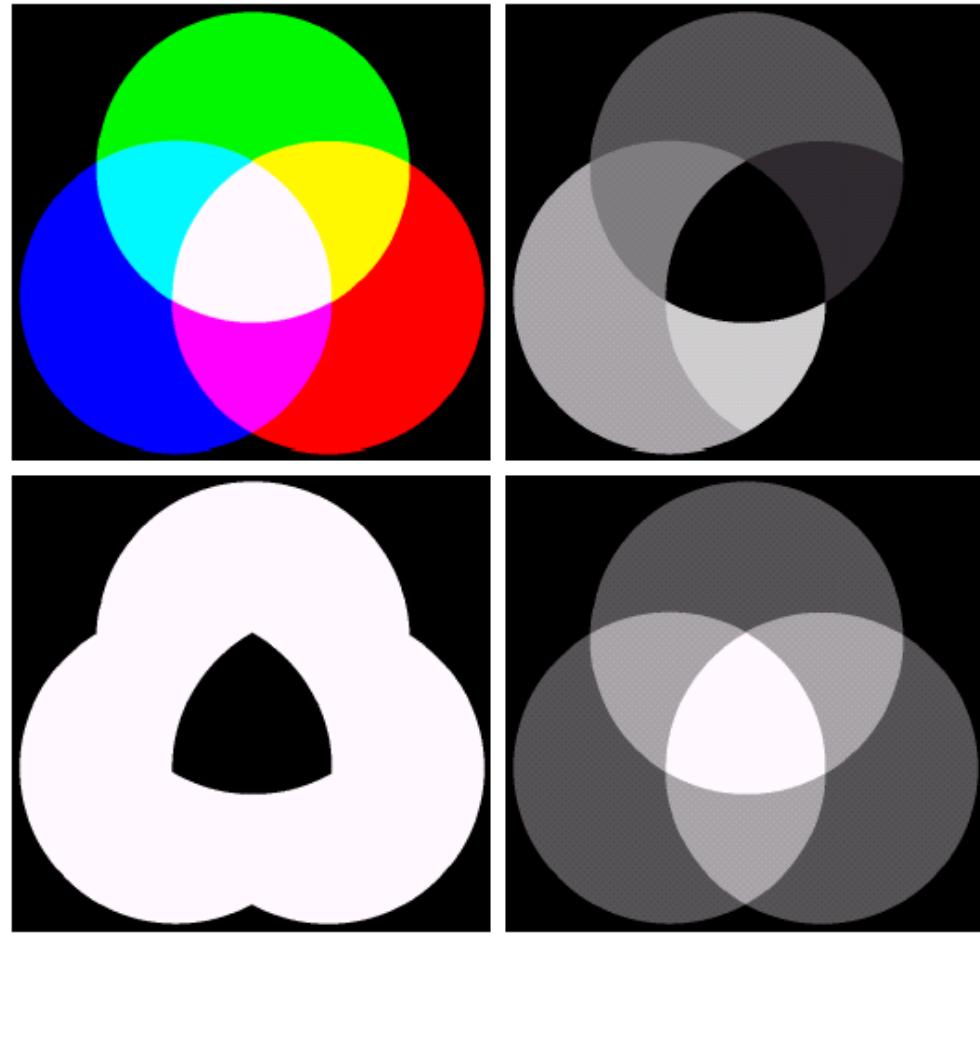
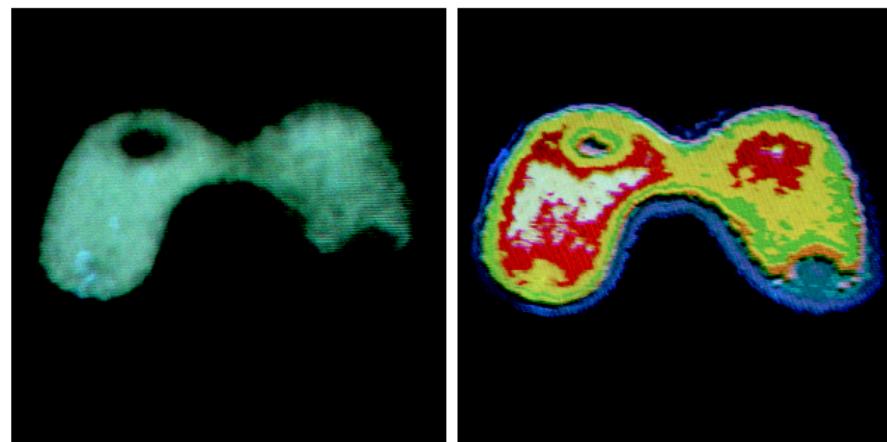


FIGURE 6.16 (a) RGB image and the components of its corresponding HSI image:
(b) hue, (c) saturation, and (d) intensity.

灰度图像转换为伪彩色图像 (I)

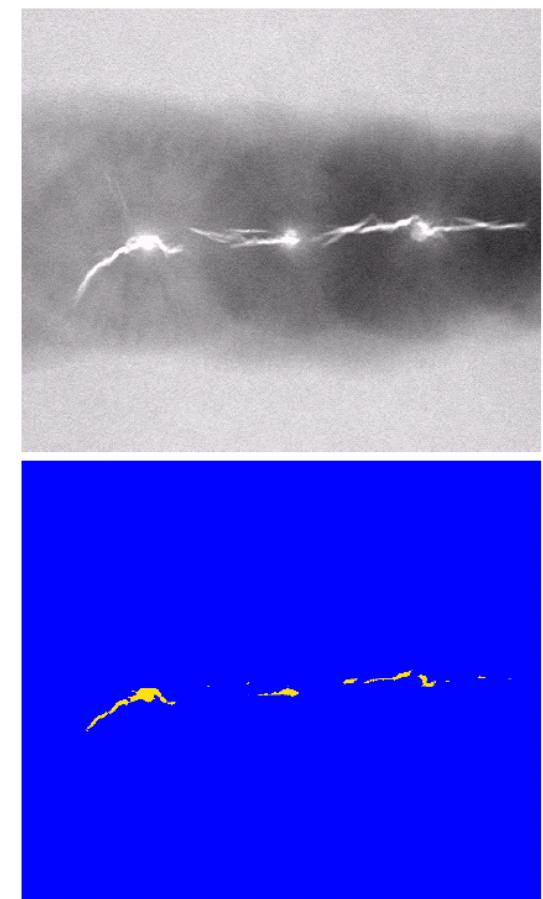


a b

FIGURE 6.20 (a) Monochrome image of the Picker Thyroid Phantom. (b) Result of density slicing into eight colors. (Courtesy of Dr. J. L. Blankenship, Instrumentation and Controls Division, Oak Ridge National Laboratory.)

a
b

FIGURE 6.21
(a) Monochrome X-ray image of a weld. (b) Result of color coding.
(Original image courtesy of X-TEK Systems, Ltd.)



灰度图像转换为伪彩色图像 (II)

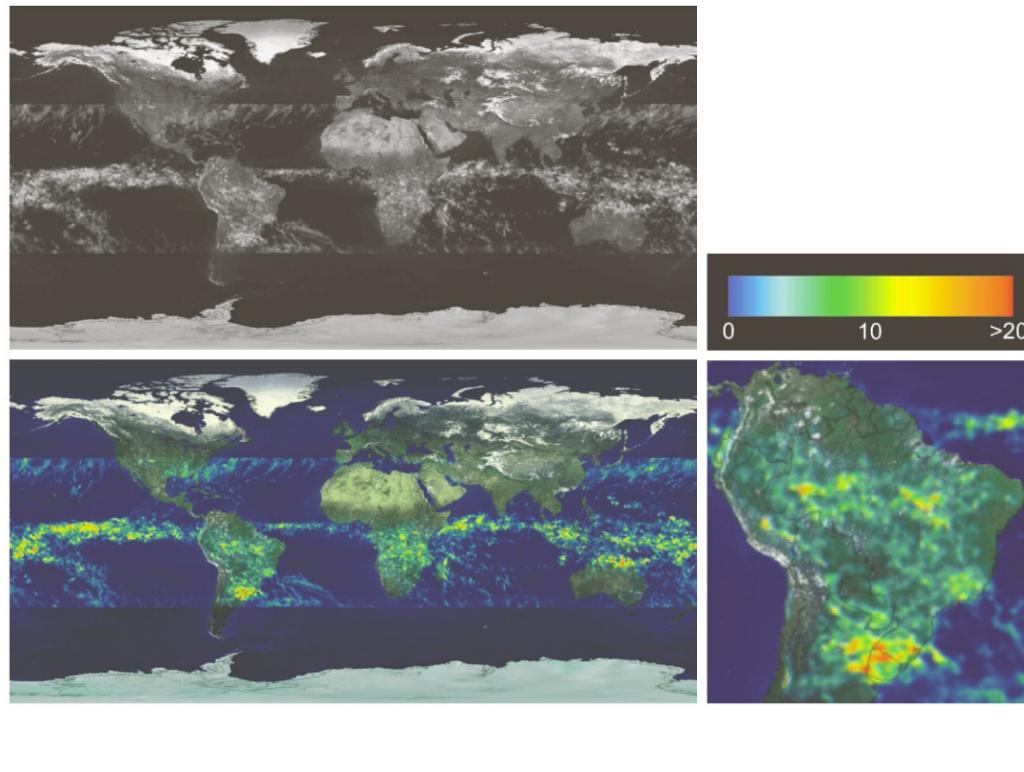


FIGURE 6.22 (a) Gray-scale image in which intensity (in the lighter horizontal band shown) corresponds to average monthly rainfall. (b) Colors assigned to intensity values. (c) Color-coded image. (d) Zoom of the South American region. (Courtesy of NASA.)

伪彩色多通道图像

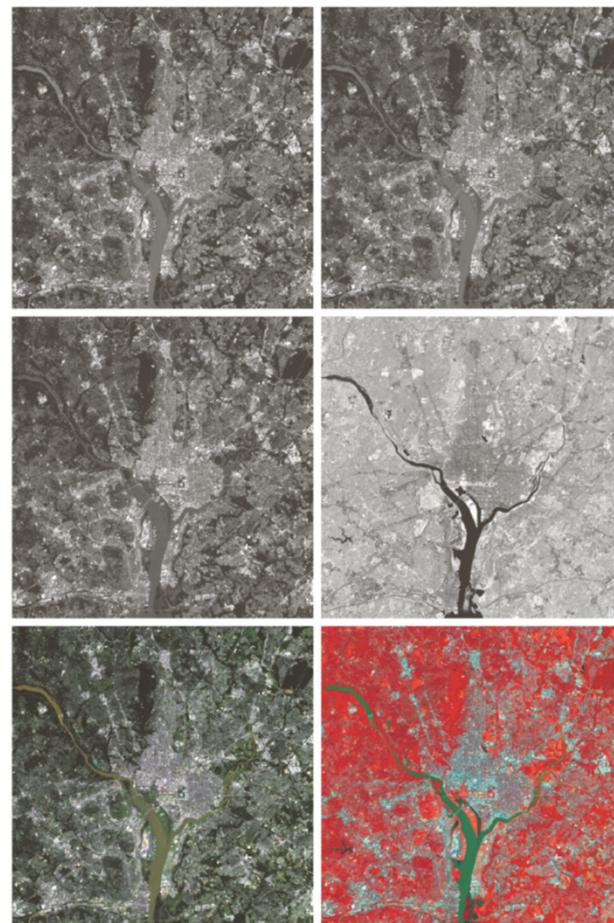
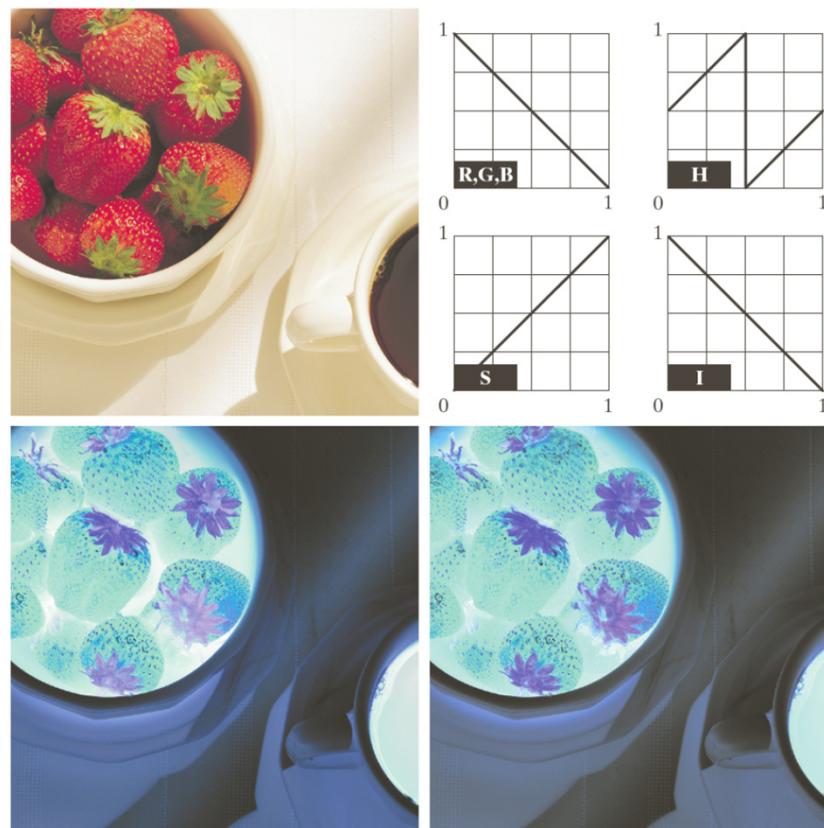


FIGURE 6.27 (a)–(d) Images in bands 1–4 in Fig. 1.10 (see Table 1.1). (e) Color composite image obtained by treating (a), (b), and (c) as the red, green, blue components of an RGB image. (f) Image obtained in the same manner, but using in the red channel the near-infrared image in (d). (Original multispectral images courtesy of NASA.)

a b
c d
e f

彩色图像变换



a b
c d

FIGURE 6.33
Color complement transformations.
(a) Original image.
(b) Complement transformation functions.
(c) Complement of (a) based on the RGB mapping functions.
(d) An approximation of the RGB complement using HSI transformations.

彩色图像色调校正

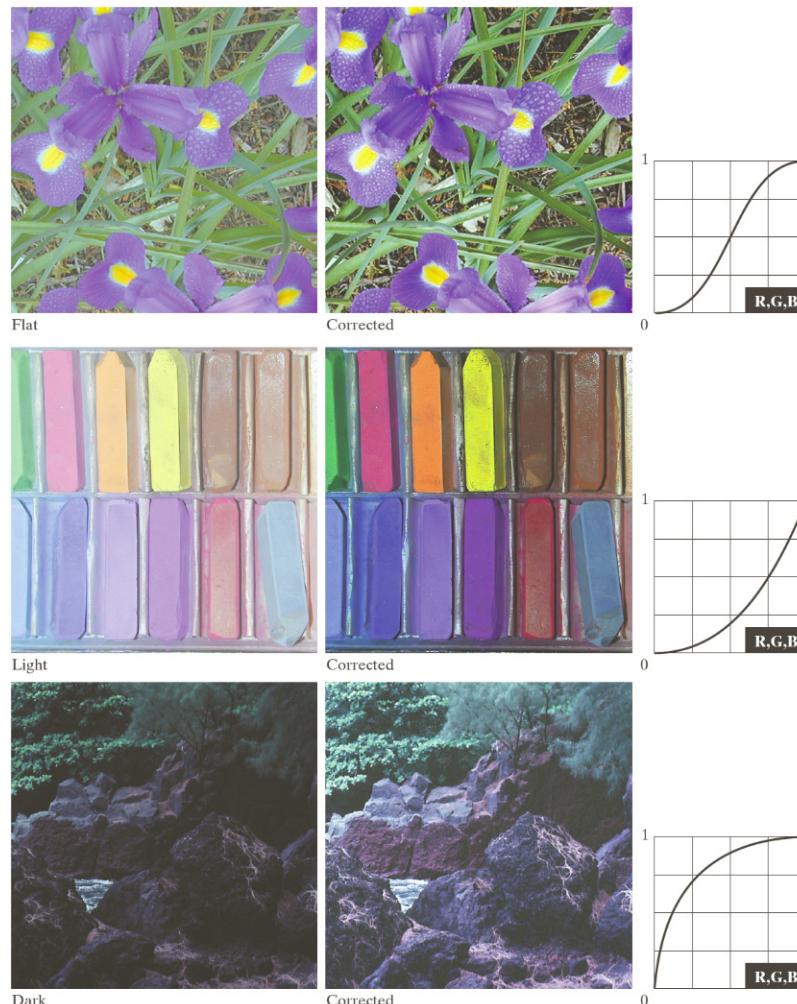


FIGURE 6.35 Tonal corrections for flat, light (high key), and dark (low key) color images. Adjusting the red, green, and blue components equally does not always alter the image hues significantly.

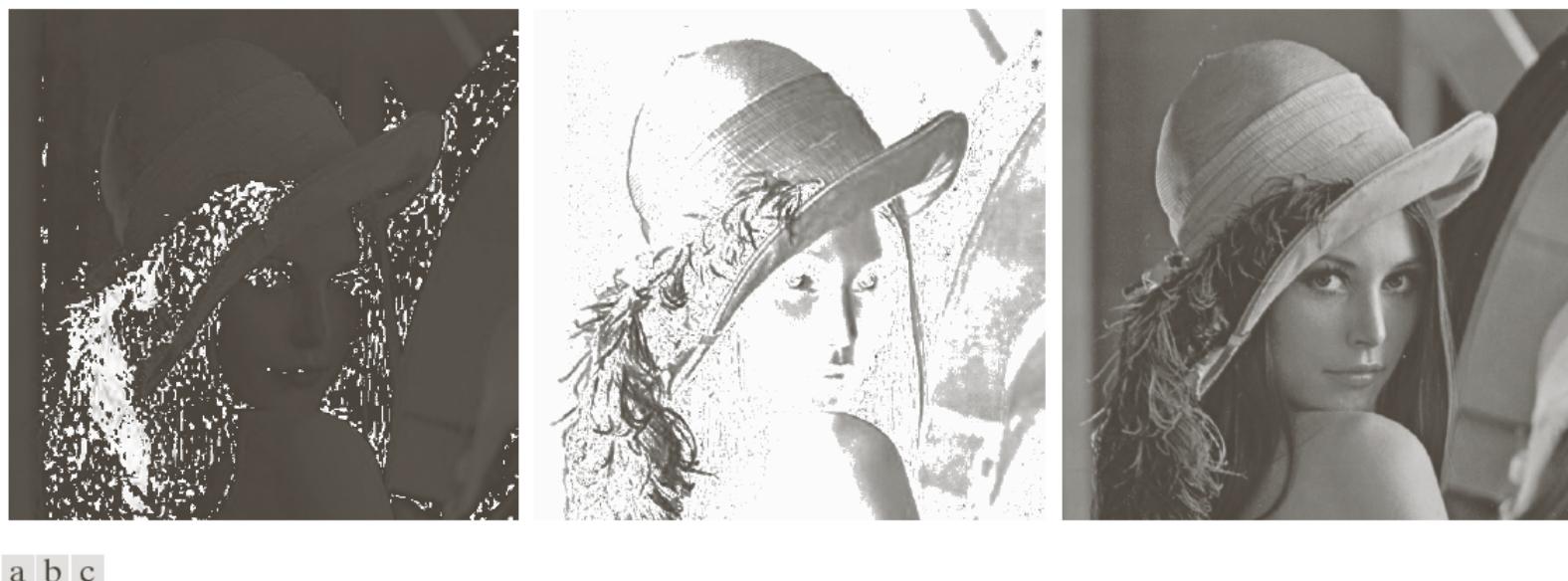
彩色图像处理示例 (I)



a b
c d

FIGURE 6.38
(a) RGB image.
(b) Red component image.
(c) Green component.
(d) Blue component.

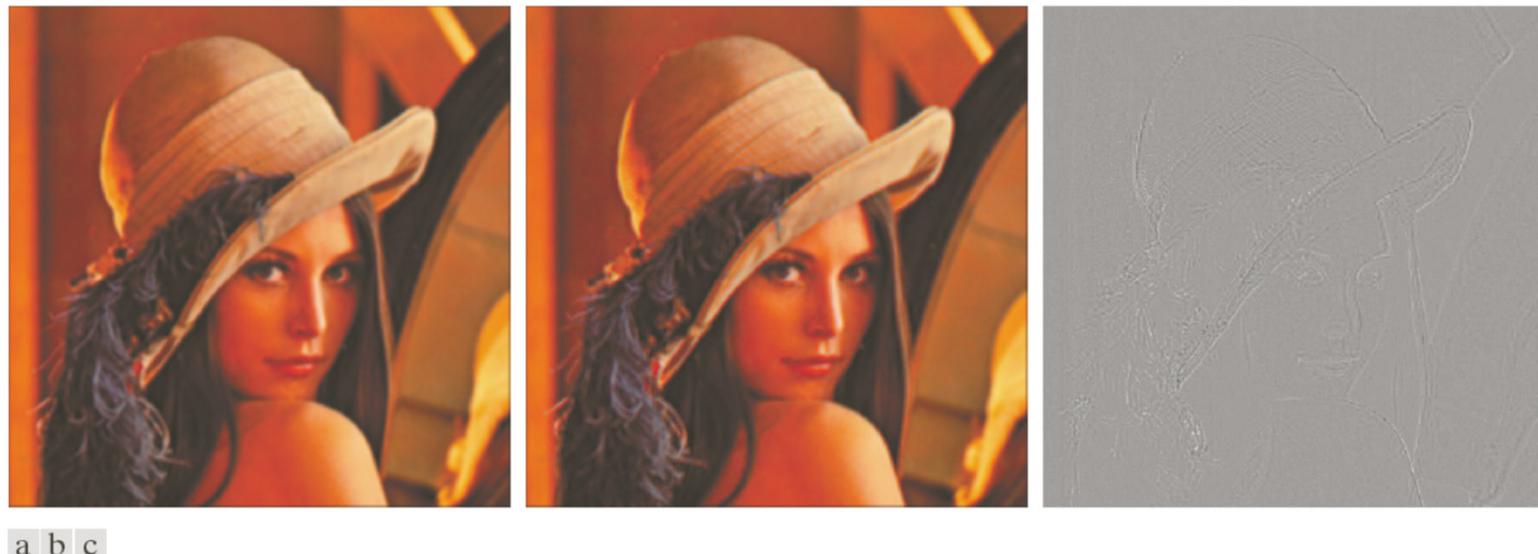
彩色图像处理示例 (II)



a b c

FIGURE 6.39 HSI components of the RGB color image in Fig. 6.38(a). (a) Hue. (b) Saturation. (c) Intensity.

彩色图像处理示例 (III)



a b c

FIGURE 6.40 Image smoothing with a 5×5 averaging mask. (a) Result of processing each RGB component image. (b) Result of processing the intensity component of the HSI image and converting to RGB. (c) Difference between the two results.

彩色图像处理示例 (IV)



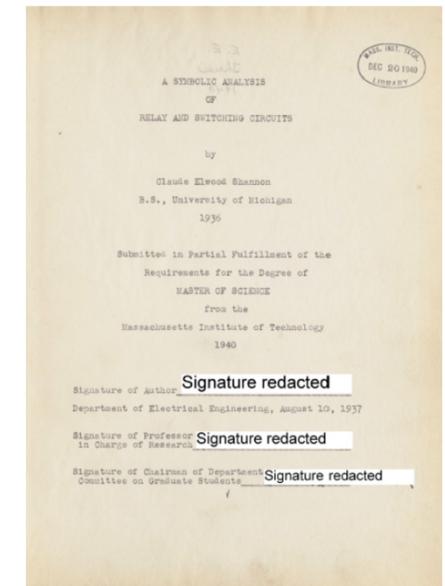
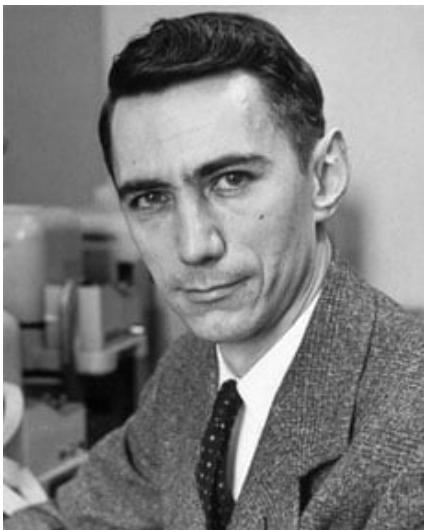
a b c

FIGURE 6.41 Image sharpening with the Laplacian. (a) Result of processing each RGB channel. (b) Result of processing the HSI intensity component and converting to RGB. (c) Difference between the two results.

Questions?

Claude Elwood Shannon (1916-2001)

- 1932-1936 University of Michigan, Double major in electrical engineering & mathematics
- 1937-1940 MIT
- MS thesis “A symbolic analysis of relay and switching circuits”



Claude Elwood Shannon (1916-2001)

- “A mathematical theory of communication”

The Bell System Technical Journal

Vol. XXVII July, 1948 No. 3

A Mathematical Theory of Communication

By C. E. SHANNON

INTRODUCTION

THE recent development of various methods of modulation such as PCM and PPM which exchange bandwidth for signal-to-noise ratio has intensified the interest in a general theory of communication. A basis for such a theory is contained in the important papers of Nyquist¹ and Hartley² on this subject. In the present paper we will extend the theory to include a number of new factors, in particular the effect of noise in the channel, and the savings possible due to the statistical structure of the original message and due to the nature of the final destination of the information.

The fundamental problem of communication is that of reproducing at one point either exactly or approximately a message selected at another point. Frequently the messages have *meaning*; that is they refer to or are correlated according to some system with certain physical or conceptual entities. These semantic aspects of communication are irrelevant to the engineering problem. The significant aspect is that the actual message is one *selected from a set* of possible messages. The system must be designed to operate for each possible selection, not just the one which will actually be chosen since this is unknown at the time of design.

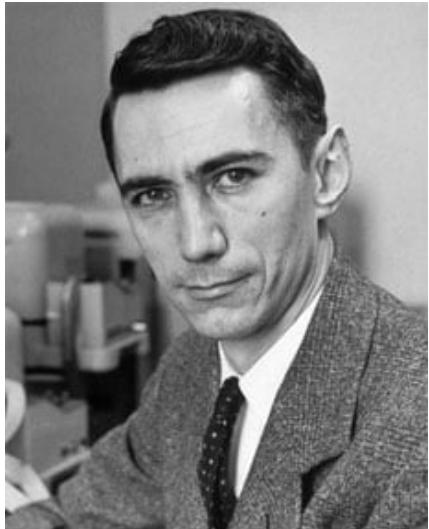
If the number of messages in the set is finite then this number or any monotonic function of this number can be regarded as a measure of the information produced when one message is chosen from the set, all choices being equally likely. As was pointed out by Hartley the most natural choice is the logarithmic function. Although this definition must be generalized considerably when we consider the influence of the statistics of the message and when we have a continuous range of messages, we will in all cases use an essentially logarithmic measure.

The logarithmic measure is more convenient for various reasons:

1. It is practically more useful. Parameters of engineering importance

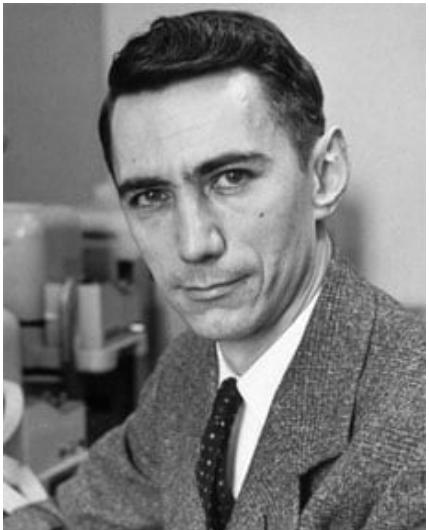
¹ Nyquist, H., "Certain Factors Affecting Telegraph Speed," *Bell System Technical Journal*, April 1924, p. 324; "Certain Topics in Telegraph Transmission Theory," *A. I. E. E. Trans.*, v. 47, April 1928, p. 617.

² Hartley, R. V. L., "Transmission of Information," *Bell System Technical Journal*, July 1928, p. 535.



Claude Elwood Shannon (1916-2001)

- “Communication in the presence of noise”

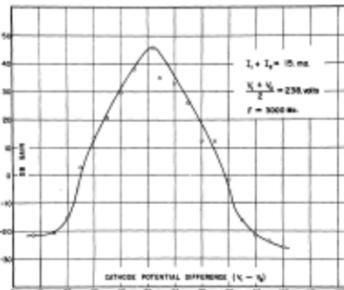


10

PROCEEDINGS OF THE I.R.E.

January

through the attenuator to the receiver. In this manner, the gain versus the cathode-potential-difference curve of Fig. 17 was obtained. This figure corresponds rather closely with the theoretical curve of propagation constant versus the inhomogeneity factor, shown in Fig. 1.



At a frequency of 3000 Mc and a total current of 15 mA, a net gain of 46 db was obtained, even though no attempt was made to match either the input or output circuits. The lack of appropriate match is responsible for the fact that the gain curve assumes negative values when the electronic gain is not sufficient to overcome the losses due to mismatch. At the peak of the curve, it is estimated that the electronic gain is of the order of 80 db.

The curves of output voltage versus the potential of the drift tube were shown in Figs. 8 and 9. Fig. 9 shows this characteristic for the electron-wave tube of the

space-charge type illustrated in Fig. 5. The shape of this curve corresponds rather closely with the shape of the theoretical curve given in Fig. 7. Fig. 8 shows the output voltage versus drift-potential characteristic for the two-velocity-type electron-wave tube. When the drift-tube voltage is high, the tube behaves like the two-cavity klystron amplifier. As the drift voltage is lowered the gain gradually increases, due to the space-charge interaction effect, and achieves a maximum which is approximately 60 db higher than the output achieved with klystron operation. With further reduction of the drift-tube potential the output drops rather rapidly, because the space-charge conditions become unfavorable; that is, the inhomogeneity factor becomes too large.

The electronic bandwidth was measured by measuring the gain of the tube over a frequency range from 2000 to 3000 Mc and retuning the input and output circuits for each frequency. It was observed that the gain of the tube was essentially constant over this frequency range, thus confirming the theoretical prediction of electronic bandwidth of over 30 per cent at the gain of 80 db.

The electron-wave tube, because of its remarkable property of achieving energy amplification without the use of any resonant or waveguiding structures in the amplifying region of the tube, promises to offer a satisfactory solution to the problem of generation and amplification of energy at millimeter wavelengths, and thus will aid in expediting the exploitation of that portion of the electromagnetic spectrum.

ACKNOWLEDGMENT

The author wishes to express his appreciation of the enthusiastic support of all his co-workers at the Naval Research Laboratory who helped to carry out this project from the stage of conception to the production and tests of experimental electron-wave tubes. The untiring efforts of two of the author's assistants, C. B. Smith and R. S. Ware, are particularly appreciated.

Communication in the Presence of Noise*

CLAUDE E. SHANNON†, MEMBER, IRE

Summary—A method is developed for representing any communication system geometrically. Messages and the corresponding signals are points in two “function spaces,” and the modulation process is a mapping of one space into the other. Using this representation, a number of results in communication theory are deduced concerning expansion and compression of bandwidth and the threshold effect. Formulas are found for the maximum rate of transmission of binary digits over a system when the signal is perturbed by various types of noise. Some of the properties of “ideal” systems which transmit at this maximum rate are discussed. The equivalent number of binary digits per second for certain information sources is calculated.

* Decimal classification: 621.38. Original manuscript received by the Institute, July 23, 1940. Presented, 1948 IRE National Convention, New York, N. Y., March 24, 1948; and IRE New York Section, New York, N. Y., November 12, 1947.

† Bell Telephone Laboratories, Murray Hill, N. J.

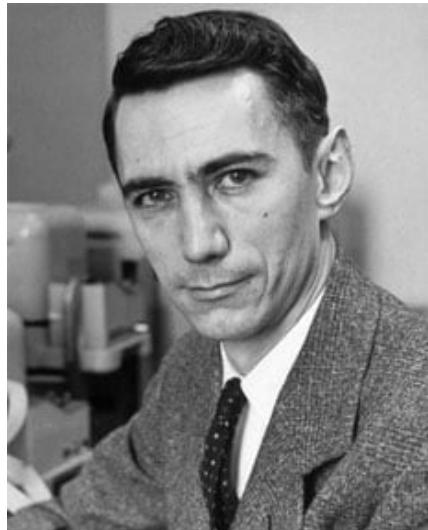
I. INTRODUCTION

A GENERAL COMMUNICATIONS system is shown schematically in Fig. 1. It consists essentially of five elements.

1. *An information source.* The source selects one message from a set of possible messages to be transmitted to the receiving terminal. The message may be of various types; for example, a sequence of letters or numbers, as in telegraphy or teletype, or a continuous function of time $f(t)$, as in radio or telephony.

2. *The transmitter.* This operates on the message in some way and produces a signal suitable for transmission to the receiving point over the channel. In teleph-

Claude Elwood Shannon (1916-2001)



- Died in 2001 of Alzheimer's disease
- Quote:

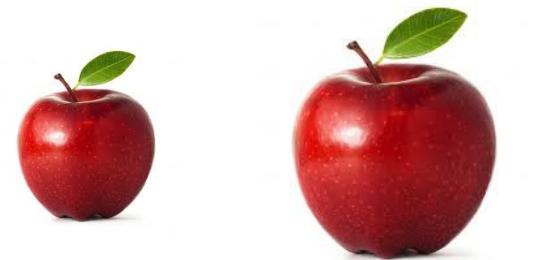
“Information is the resolution of uncertainty.”

“The fundamental problem of communication is that of reproducing at one point either exactly or approximately a message selected at another point.”

A Microscope as a Linear System

- A light microscope can be considered as a linear system.
- A linear system satisfies the following two conditions
 - Homogeneity
 - Additivity
- Homogeneity
- Additivity

$$\boxed{x(t) \rightarrow y(t)}$$
$$\Downarrow$$
$$k \cdot x(t) \rightarrow k \cdot y(t)$$



$$\boxed{x_1(t) \rightarrow y_1(t)}$$
$$x_2(t) \rightarrow y_2(t)$$
$$\Downarrow$$
$$x_1(t) + x_2(t) \rightarrow y_1(t) + y_2(t)$$



How to Characterize a Linear System

- A linear system can be characterized by
 - Impulse response
 - Frequency response
- Impulse response of a microscope: point spread function
$$I(x, y) = O(x, y) \otimes psf(x, y) = \int_{-\infty}^{+\infty} \int_{-\infty}^{+\infty} O(u, v) \cdot psf(x - u, y - v) du dv$$
- Frequency response of a microscope: optical transfer function
$$F\{I(x, y)\} = F\{O(x, y)\} \cdot F\{psf(x, y)\} = F\{O(x, y)\} \cdot OTF(\cdot)$$

Airy Disk

- Airy (after George Biddell Airy) disk is the diffraction pattern of a point feature under a circular aperture.
- It has the following form

$$y = \left[\frac{2J_1(x)}{x} \right]^2$$

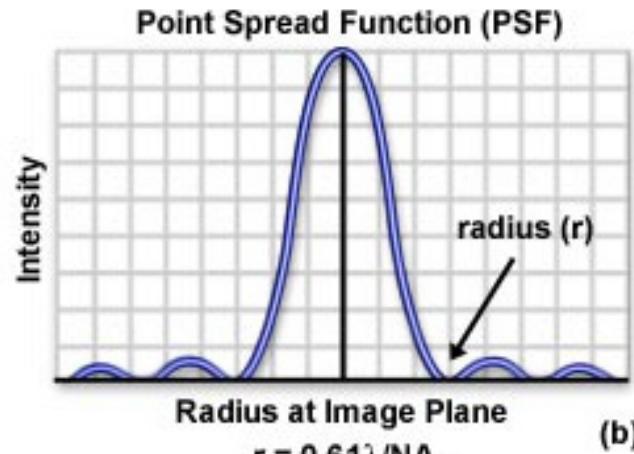


Figure 1

$J_1(x)$ is a Bessel function of the first kind.

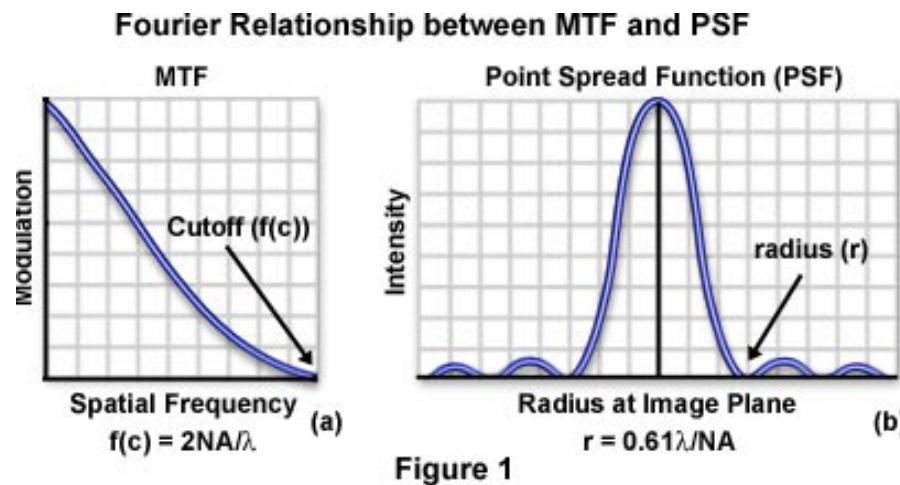
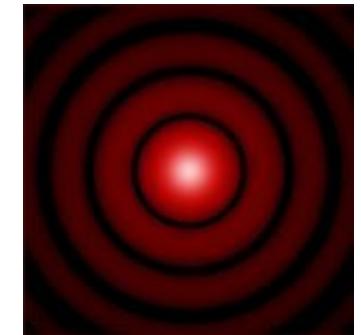
- Detailed derivation is given in
Born & Wolf, Principles of Optics, 7th ed., pp. 439-441.

Microscope Image Formation (I)

- Microscope image formation can be modeled as a convolution with the PSF.

$$I(x, y) = O(x, y) \otimes psf(x, y)$$

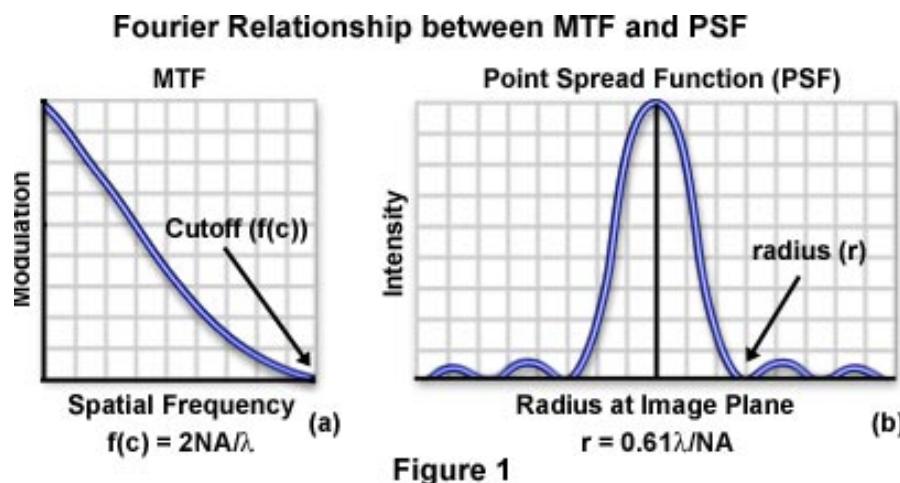
$$F\{I(x, y)\} = F\{O(x, y)\} \cdot F\{psf(x, y)\}$$



<http://micro.magnet.fsu.edu/primer/java/mtf/airydisksize/index.html>

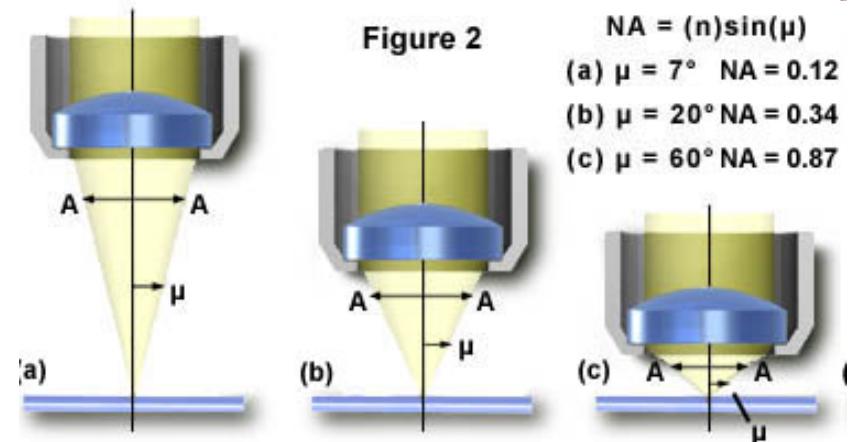
Microscope Image Formation (II)

- The impulse response of the microscope is called its point spread function (PSF).
- The transfer function of a microscope is called its optical transfer function (OTF).
- The PSF has the shape of an Airy Disk.



Numerical Aperture

- Numerical aperture (NA) determines microscope resolution and light collection power.



$$NA = n \cdot \sin \mu$$

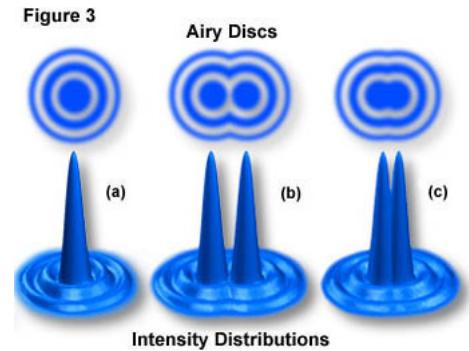
n : refractive index of the medium between the lens and the specimen

μ : half of the angular aperture

Different Definition of Light Microscopy Resolution Limit (Demo)

- Rayleigh limit
- Sparrow limit

$$D = \frac{0.61\lambda}{NA}$$



$$D = \frac{0.47\lambda}{NA}$$

<http://www.microscopy.fsu.edu/primer/java/imageformation/rayleighdisks/index.html>

Summary: High Resolution Microscopy

- Size of cellular features are typically on the scale of a micron or smaller.
- To resolve such features require
 - Shorter wavelength (electron microscopy)
 - High numerical aperture (resolution)
 - High magnification (spatial sampling)

$$D = \frac{0.61\lambda}{NA}$$