Ejercicio 1. Calcular la integral de línea del campo $\mathbf{F}:\mathbb{R}^3 \to \mathbb{R}^3$ dado por

$$\mathbf{F}(x,y,z) = \left(e^{xz}(xyz^2 + yz) + y, xze^{xz}, e^{xz}(x^2yz + xy)\right)$$

a lo largo de la curva parametrizada por $\sigma:[0,1]\to\mathbb{R}^3$,

$$\sigma(t) = \left(t, 3t^2 - 2t, \frac{1}{\ln 7} \ln \left(1 + 6t^8\right)\right).$$

$$\int_{C} f \cdot d\vec{s} = \int_{C} \left(f(t) \right) f(t) dt$$

$$F(x_{15,12}) = (e^{xz}(+), xze^{xz}, e^{xz}(+)) + (y_{10,0})$$

$$= e^{xz}(xyz^{2} + yz, xz, x^{2}yz + xy) + (y_{0})$$

$$P Q R$$

$$\nabla \times \tilde{T} = \det \begin{pmatrix} \dot{0} & \dot{3} & k \\ 3x & 3y & 3z \\ P & Q & R \end{pmatrix} =$$

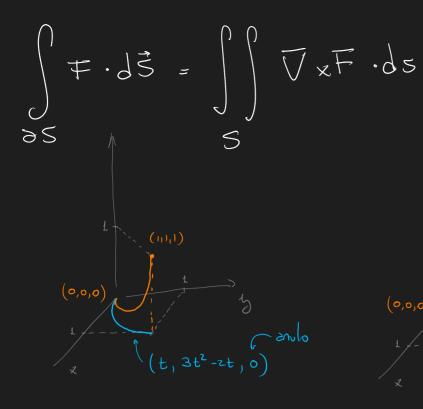
$$= \left(\frac{\partial R}{\partial y} - \frac{\partial Q}{\partial z}\right) - \frac{\partial R}{\partial x} + \frac{\partial P}{\partial z}\right) \frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y}$$

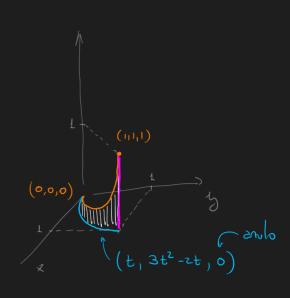
$$= \left(x^{2}z + x - x \right) - 2xyz - y + 2xyz + y , z - xz^{2} - z \right)$$

$$= \left(\chi^2 + \chi^2 + \chi^2 \right)$$

$$\nabla_x F = (0,0,-1)$$

Por Stokes





Como er compo gradiente

$$\int_{C} \nabla g \, ds = g(\sigma(1)) - g(\sigma(0))$$

$$= g(0,0,0) - g(1,1,1)$$

Para obtener q:

$$G = e^{xz} \left(xyz^2 + yz, xz, x^2yz + xy \right)$$

$$P = \frac{\partial g}{\partial x} = e^{xz} \left(xyz^2 + yz \right)$$

$$Q = \frac{\partial g}{\partial y} = e^{xz} \left(x^2yz^2 + yz \right)$$

$$R = \frac{\partial g}{\partial y} = e^{xz} \left(x^2yz^2 + xy \right)$$

$$\begin{cases}
e^{xz} \cdot xyz + C \\
e^{xz} \cdot xyz + C
\end{cases} = e^{xz} \cdot xyz$$

$$e^{xz} \cdot xyz + C$$

$$e^{xz} \cdot xy$$

Justo to do

$$\int_{C} F = \int_{C} G + \int_{C} H$$

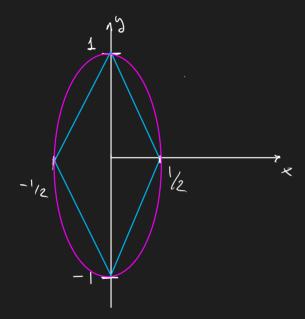
$$= C + O = C$$

Ejercicio 2. Sean \mathcal{C} la curva poligonal cerrada de vértices (0,1), (0,-1), (1/2,0) y (-1/2,0) y \mathcal{E} la elipse $4x^2 + y^2 = 1$, ambas orientadas positivamente. Sean

$$\mathbf{F}(x,y) = \frac{1}{4x^2 + y^2} (-y, x), \quad \mathbf{G}(x,y) = (x, y\sqrt{4x^2 + y^2}).$$

- (a) Hallar $\int_{\mathcal{E}} \mathbf{F} \cdot d\mathbf{s}$.
- (b) Hallar $\int_{\mathcal{E}} \mathbf{G} \cdot d\mathbf{s}$ y $\int_{\mathcal{C}} \mathbf{G} \cdot d\mathbf{s}$.

Sugerencia: integrar una función impar con respecto a x sobre un dominio simétrico con respecto a x da 0.



a)
$$\int F.d\vec{s} =$$
elipse => $4x^2 + y^2 = 1$
=> C_{1} compange $F(E)$
=> $4x^2 + y^2$ seré igual a 1 .

Peremetrizo
$$\mathcal{E}$$

$$O(t) = \left(\frac{1}{2}\cos t, \sin t\right)$$

$$O'(t) = \left(-\frac{1}{2}\sin t, \cos t\right)$$

$$F(\delta(t)) = \frac{1}{2}\cos t, \cos t$$

$$= 1 \text{ pure or } |_{\delta} \text{ as } dx \text{ is dispse}$$

$$\left(\left(-\sin t, \frac{1}{2}\cos t\right), \left(-\frac{1}{2}\sin t, \cos t\right)\right) dt =$$

$$= \int_{\delta}^{2\pi} \frac{1}{2}\sin t + \frac{1}{2}\cot t = \Pi$$

$$\vdots$$

$$G = \left(X, y, \sqrt{4x^2 + y^2}\right)$$

$$G : ds = \int_{\delta}^{2\pi} \left(\sigma(t), \sigma'(t)\right) dt$$

$$= \int_{\delta}^{2\pi} \left(\frac{1}{2}\cot t, \sin t\right), \left(-\frac{1}{2}\sin t, \cot t\right) dt$$

$$= \int_{\delta}^{2\pi} \frac{1}{4}\sin t \cot t + \sin t \cot t dt$$

$$= \int_{\delta}^{2\pi} \frac{3}{4}\sin t \cot t dt$$

$$u = 51nt$$

$$du = cort dt$$

$$3 = \frac{3}{4}$$

$$u = 0$$

$$31n0 (51n^2t)' = 251nt \cdot cort$$

