Campos Conservativos

Def: $F: \mathbb{R}^3 \to \mathbb{R}^3$ se dice

Conservativo si:

F dis = P = dis Cer

V par de Curvas simples, Suaves à trozos

conel mismo punto

inicial o hind

Teorema:

 $FeC^{1}(\mathbb{R}^{3}\setminus\Omega)$

#52 (\$

Son equivaentes

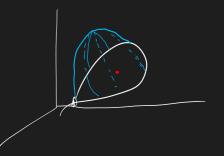
$$\boxed{4} \quad \forall \times F = 0 \qquad \text{en} \quad \mathbb{R}^3 \setminus \Omega$$

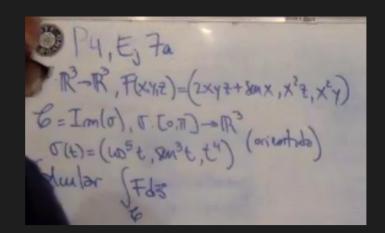
Ojo! en R² vole por sin excepcioner

con $F \in C^1(\mathbb{R}^2)$

(No puedo ermentesito con pento discontínuo, no er erco conexo)

en R³ sípuedo er quivar lo





$$\mp es C^{1}(\mathbb{R}^{3})$$

$$\nabla \times F = \left(\frac{\partial F_3}{\partial y} - \frac{\partial F_2}{\partial z} \right) - \frac{\partial F_3}{\partial x} + \frac{\partial F_1}{\partial z} \right) \frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y}$$

Calalo principo/ Pin

$$\sigma(0) = (1,0,0)$$

$$\sigma(\pi) = (-1, 0, \pi^4)$$



Si no lura gradiente Proponemos otro camino

$$\Gamma_1: derde (1,0,0) \rightarrow (-1,0,0)$$

$$\Gamma_{\perp}(t) = (t, 0, 0)$$
 (d rever)

$$\Gamma_2: [0, \pi^4] \rightarrow \mathbb{R}^3$$

$$\Gamma_{2}(t) = (1,0,t)$$
 (sortido carecto)

$$\Gamma_1^1$$
 (t) = $(1,0,0)$

Como:
$$\sqrt{\times} = \vec{0}$$

$$= -\int_{\Gamma_1} F d\vec{s} + \int_{\Gamma_2} F d\vec{s}$$

$$\int_{\Gamma_1} F d3 = \int_{-1}^{1} \langle F(\Gamma_1(t)), \Gamma'_1(t) \rangle dt$$

$$= - \cos(1) + \cos(-1)$$

$$\int_{\mathbb{C}^2} F \cdot ds = \int_{0}^{\pi^4} o dt = 0$$

$$\int_{\mathcal{E}} F d\vec{s} = 0$$

Tembién podrie haber encontrado el potencial f.

P4 = 10)

$$\mp (x_1, z) = (2xy + z^2, x^2 - 2yx, 2xz - g^2)$$

Colored de de par
$$\begin{cases} x^2 + y^2 + z^2 = 1 \\ y = x \\ (\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0) \rightarrow (0, 0, 1) \end{cases}$$

$$\nabla x F = (-2y - (-2y), 2z - 2z, 2x - 2x)$$

$$= \left(O_{j} O_{j} O_{j} \right)$$

$$\Rightarrow F = \nabla f \qquad \text{on} \quad f: \mathbb{R}^3 \to \mathbb{R}$$

$$\infty \quad f: \mathbb{R}^3 \to \mathbb{R}$$

Reer cribo I

$$0 \quad \frac{\partial f}{\partial x} = 2xy + z^2$$

$$\Rightarrow \frac{\partial f}{\partial y} = x^2 + \frac{\partial h}{\partial y}(x_1 z) = x^2 - 2y z$$

$$\frac{\partial h}{\partial y} = -2yz$$

$$\frac{\partial f}{\partial z} = 2xz - y^2 - g'(z)$$

$$\int F d\vec{s} = f(0,0,1) - f(\frac{1}{\sqrt{z}}, \frac{1}{\sqrt{z}}, 0)$$

$$= 0 - \frac{1}{2\sqrt{z}}$$

$$= -\frac{\sqrt{z}}{4}$$

$$\implies \nabla \times F = (0,0,0)$$

La Vuelta no vale

Hag que versier simplemente conexo

(R) 2

: Simplemente conexo





