"Burbujoide"

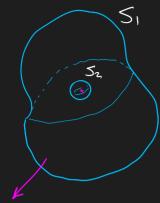
## Teorema de Geuss

$$= \int F dS$$

$$\partial \Omega_{ext}$$

## Extensiones / observaciones

## 1) Regiones con hu ecos



hacia

hacia de Jí misma

de sí mismo

Noter:

cuendo la oriento:

$$(2\Omega)^{\text{ext}} = 5^{\text{ext}} \cup 5^{\text{int}}$$

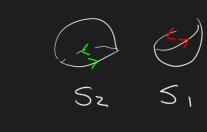
065:

$$\Omega \subset \mathbb{R}^3$$
  
 $\partial \Omega = 5$  cereson,  $\eta \in \mathbb{R}^4$   
 $T \in \mathbb{C}^2 (\Omega)$ 

$$\int \nabla_x F d\vec{s} = \int div (\nabla_x F) dV = 0$$



Puedo separalo en dos carcaras con borde



Sto ker

Divergencia, fuentes y sumi deros

Interpreter div F(p), pe R3 compo de velocido des

 $F: \mathbb{R}^3 \to \mathbb{R}^3$ 

div F: R3 ->R

Br(p): bols centro p, redio rso

Lo pierzo como velocided

$$\int dv \mp (p) dV = \int \mp d\vec{s}$$

$$\mathcal{B}_{r}(p)$$

$$\mathcal{B}_{r}(p)_{ext}$$

$$\frac{1}{|B_r(p)|} \int dx \, \mp (p) \, dV = \frac{1}{|B_r(p)|} \pm d\tilde{s}$$

$$\frac{1}{|B_r(p)|} \frac{1}{|B_r(p)|} \frac{1}$$

Por Teorens de Vilor integral:

$$div \mp (q) = \frac{1}{|B_r(p)|} \cdot \int div \mp dv$$

$$\exists_{r(p)}$$

$$= \frac{1}{|\mathcal{B}_{r}(p)|} \cdot \int_{\partial \mathcal{B}_{r}(p)_{ex}} \mp d\vec{s}$$

Pronedio del Flujo obtante o trové de la superficie:

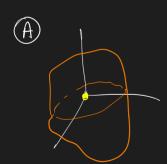
$$= \lim_{r \to 0} \frac{1}{|B_r(p)|} \int f ds$$

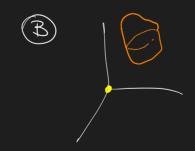
## Ley de Genss

$$\stackrel{\Rightarrow}{\Gamma}: \mathbb{R}^3 \to \mathbb{R}^3$$

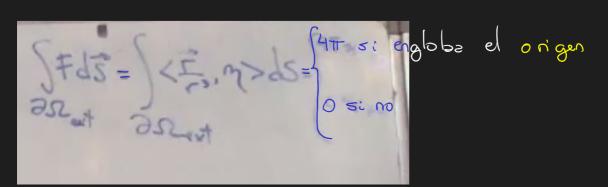
$$\Gamma : \mathbb{R}^3 \to \mathbb{R}$$

$$\Omega \subset \mathbb{R}^3$$
 tipo  $\overline{\mathbb{N}} / \vec{o} \notin \partial SZ$ 





C) Si d'está
en la cáscara
no puedo hacer
na da



$$\begin{array}{ccc}
\mathbb{B} & \int \mp d\vec{s} &= \int d\vec{v} \mp d\vec{V} = 0
\end{array}$$

$$\mathbb{A}$$
  $\mathbb{B}_{\epsilon}$ (3),  $\epsilon > 0$ 

$$\int F d\vec{S} + \int F d\vec{S} = 0$$

$$\partial \Omega_{\text{ext}} \qquad \partial \Omega_{\epsilon}(0) = 0$$

$$\int \mp d\vec{s} = \int \mp ds$$

$$3\pi_{\text{ext}} = 3\pi_{\epsilon}(0)_{\text{ext}}$$

$$= \int_{\mathcal{E}(0)} \left\langle \frac{\vec{r}}{r^3}, \frac{\vec{r}}{r} \right\rangle dS$$

$$= 3B_{\mathcal{E}}(0)$$

Recorder

$$\frac{1}{\epsilon^2} \int_{\mathbb{R}^2} 1 ds$$

$$= \frac{1}{\varepsilon^2} \cdot 4\pi \cdot \Gamma^2$$

