Practica #1

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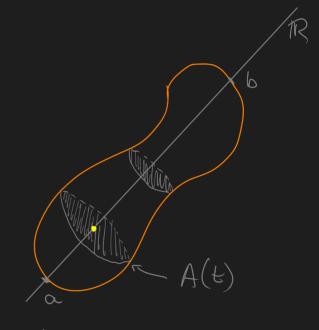
Análisis 2 : Materia Práctica

Breve Repasso de Integración (R2, R3)

Principio de Cevalier i

C CR3 C un overpo (volúmon)

 $V_{d}(w) = \int_{a}^{b} A(t) dt$



Area de rebanada: A(t)

Existe A: [a, b] -> R,0

Ejemplo: Es fera de Radio R



$$\mathbb{R}^{2} = t^{2} + \Gamma(t)^{2}$$

$$\Gamma(t)^{2} = \mathbb{R}^{2} - t^{2}$$

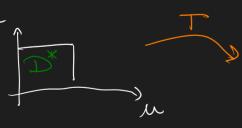
$$\bigvee_{i} \left(S(R) \right) = \int_{-R}^{R} \pi \left(R^{2} - t^{2} \right) \cdot dt$$

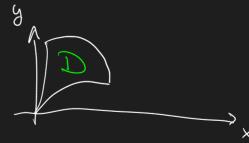
$$= \pi \left[2R^3 - \frac{t^3}{3} \right]_{-R}^{R}$$

$$= \pi \left(2R^3 - \frac{3}{3}R^3 \right)$$

$$=\frac{4}{3}\pi, R^3$$

Teorenz de Cambio de Veriable





lenemos

$$T(\mathcal{D}^*) = \mathcal{D}$$

$$\int f(x,y) \, dxdy = \int f(T(u,v)) \, . \, TT(u,v) \, . \, dudv$$

• Ejemplo con
$$f(x,y) = 1$$

$$TT(u,v) = \left| \det DT(u,v) \right|$$

$$T(u,v) = \left(\times (u,v), \times (u,v) \right)$$

$$DI(n, s) = \begin{pmatrix} \frac{1}{2} \times & \frac{1}{2} \times \\ \frac{1$$

Det.
$$(T(u,v)) = Paralebograms$$

vectorer $3x$, $3y$

() /2 2, co2 :

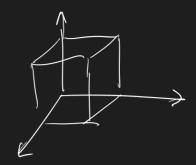
Polares
$$X = \Gamma \cdot \cos \theta$$

$$Y = \Gamma \cdot \sin \theta$$

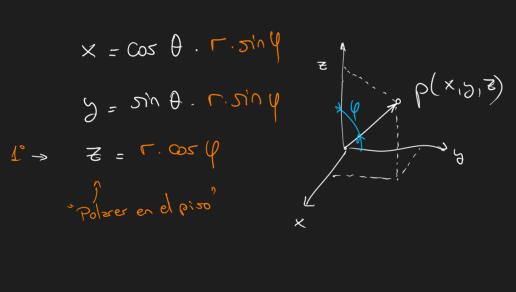
$$Y = \Gamma \cdot \sin \theta$$

$$T:\mathbb{R}^2 \to \mathbb{R}^2$$

$$T(r,\theta) = (r \cdot \cos \theta, r \cdot \sin \theta)$$



$$TT(r,\theta,z) = r$$



$$Vol\left(\mathbb{B}(0,\mathbb{R})\right) = \int_{\mathbb{B}(0,\mathbb{R})} 1 \, dV$$

$$= \int_{0}^{2\pi} \int_{0}^{\pi} \int_{0}^{R} r^{2} \cdot \sin \varphi \cdot dr$$

$$= 2\pi \cdot R^{3} \cdot \int_{0}^{\pi} \sin \varphi \, d\varphi$$

$$= 2\pi \cdot R^{3} \cdot 2$$

$$= 4\pi R^{3}$$

Curves en Rz, R3

€ CR³ (oR²) es un conjunto smægen de

 $\sigma: [a,b] \to \mathbb{R}^3$

Contímo + Sobreyectiva

Problema 1:

Estático:

 $C = \{(x,5) \in \mathbb{R}^2 : x^2 + y^2 = 1\}$

Quer emas:

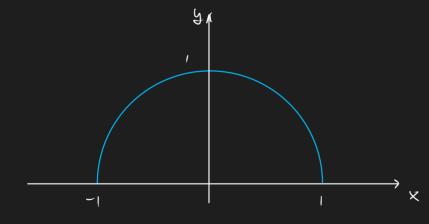
Input: Conjunto

Out put: Parametrización

$$\sigma: [0, 2\pi) \to \mathbb{R}^2$$

$$O(t) = (cort, sint)$$

$$C = \{ (x_0) \in \mathbb{R}^2 : x^2 + y^2 = 1, y > 0 \}$$



Tres paramet de C

4)
$$\gamma : [0,T] \rightarrow \mathbb{R}^2$$

$$\chi(t) = (\cos t, \sin t)$$



$$\sigma(t) = (t, \sqrt{1-t^2})$$

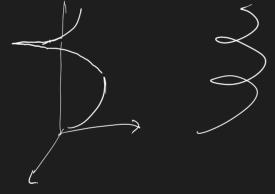
3)
$$\forall$$
: [0, π] $\rightarrow \mathbb{R}^2$

$$x(t) = (-\cos t) \sin t$$



Ejemplo:

$$\sigma: [0, 2\pi] \rightarrow \mathbb{R}$$



Velocidad à Vector Tangente

 oec^1 $o'(t) \neq \vec{o}$ regular

Perzel semi-circulo

1) •
$$Y'(t) = (-\sin t, \cos t)$$



Obs:
$$\langle \chi'(t), \chi(t) \rangle = 0$$

2) ·
$$\sigma'(t) = \left(1, \frac{-t}{\sqrt{1-t^2}}\right)$$
 con $|t| \neq 1$

con
$$|\mathcal{H}| \neq 1$$

Ret = tragente

CCR3 perametrizede por o regular (Convare)

Rects tengente en $\sigma(to) = p \in \mathbb{R}^3$

L: 2.0(to) + O(to) 26 R

Personetrizemos /2 rects L con l: R = R3

$$l(t) = (t-t_0) \cdot \sigma'(t_0) + \sigma(t_0)$$

trogent ar

Le ecusción
$$\Gamma = \Gamma(\theta)$$
 $\left(f = f(\theta) \right)$

Se interpretz como

$$\nabla (\theta) = (X(\theta), Y(\theta))$$

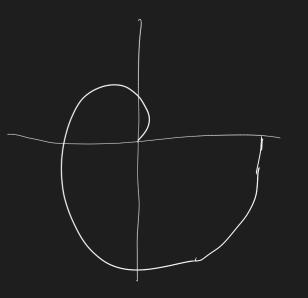
$$= (\Gamma(\theta) \cdot \cos \theta, \Gamma(\theta) \cdot \sin \theta)$$

$$= \Gamma(\theta) \cdot (\cos \theta, \sin \theta)$$

Ejemplo

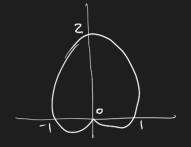
$$\Gamma(0) = 0$$
, $\theta \in [0, 2\pi]$

$$O(\theta) = O(\cos \theta, \sin \theta)$$



$$\gamma: [\Pi, \frac{3}{2}\Pi] \to \mathbb{R}^2$$
 ded par $\Gamma(\theta) = 0$

$$\Gamma(\theta) = 1 + \sin \theta \quad , \quad \theta \in [0, 2\pi]$$



Find















