Sean  $f: \mathbb{R}^2 \to \mathbb{R}^2$  definida por  $f(x,y) = (x^2 - y, y + e^x), g: \mathbb{R}^2 \to \mathbb{R}$  diferenciable y  $h = g \circ f$ . El polinomio de Taylor de orden 2 de h en (0,0) es:

$$p(x,y) = 2x - y + x^2 + 3xy + 2y^2.$$

- (a) Calcular g(0,1) y  $\nabla g(0,1)$
- (b) Calcular, si existe,

$$\lim_{(x,y)\to(0,0)} \frac{h(x,y)}{\|(x,y)\|}$$

a) 
$$h = g(f(x))$$
  
 $h(x) = g(x^2 - g, g + e^x) = g(M, \tau)$   
queno  $g(0, 1)$   

$$\begin{cases} x^2 - g = 0 & \Rightarrow x^2 = g \\ g + e^x = 1 \end{cases}$$

$$\begin{cases} e^x = 1 - x^2 \\ 0 < x^2 < 1 \Rightarrow 0 < g < 1 \\ -1 < x < 1 \end{cases}$$

$$h(0,0) = P(0,0) = g(0,1)$$

$$= 0$$

También quieno

$$\nabla g(0,1) = ?$$

$$= \left(g_{\times}(0,1), g_{S}(0,1)\right)$$

$$\stackrel{?}{\sim} \qquad \stackrel{?}{\sim} \qquad \stackrel{?}{\sim}$$

Puedo calcular

$$P_{x}(x,y) = 2 + 2x + 3y$$
  
 $P_{x}(0,0) = 2$ 

$$P_b(x, 5) = -1 + 3x + 46$$
  
 $P_b(0, 0) = -1$ 

Como

$$P_{x}(0,0) = h_{x}(0,0)$$
 $P_{y}(0,0) = h_{y}(0,0)$ 

$$\Rightarrow h_{x}(0,0) = 2$$
 $h_{y}(0,0) = -1$ 

$$^{\circ}_{\circ}$$
  $\nabla h(0,0) = (2,-1)$ 

Pero quiro 
$$\nabla_{8}(0,1)$$

Como

 $h(x_{0}) = 8(f(x_{0})) = g(u, v)$ 
 $\Rightarrow h_{x}(x_{0}) = \frac{1}{2u}8(f(x_{0})) \cdot \frac{3u}{3x}(x_{0}) + \frac{1}{2v}8(f(x_{0})) \cdot \frac{3v}{3x}(x_{0})$ 

en  $(x_{0}) = (0,0)$ 
 $\Rightarrow 2 = gu(0,1) \cdot 2x|_{x=0} + gu(0,1) \cdot e^{x}|_{x=0}$ 
 $2 = gv(0,1)$ 

Lo mismo pero hy

 $h(x_{0}) = g(f(x_{0}))$ 
 $= g(x^{2} - y, y + e^{x})$ 
 $= g(u, v)$ 
 $\Rightarrow h_{y}(x_{0}) = gu(0,v) \cdot \frac{3u}{3y}(x_{0}) + gv(u,v) \cdot \frac{3v}{3y}(x_{0})$ 
 $h_{y}(0,0) = gu(0,1) \cdot (-1) + g_{y}(0,1) \cdot 1$ 

$$h_{3}(0,0) = g_{1}(0,1) \cdot (-1) + g_{3}(0,1) \cdot 1$$

$$-1 = -g_{1}(0,1) + 2$$

$$g_{1}(0,1) = 3$$

$$\nabla g(0,1) = (3,2)$$

Punter clave en la resolución

Solve recording
$$g(f(x,y)) \quad \text{con} \quad f(x,y) = (\mathcal{U}(x,y), \, \forall (x,y))$$
de forms que
$$(\mathcal{U}(x,y), \, \forall (x,y))$$

$$\frac{\partial}{\partial x} g(f(x,y)) = \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial \mathcal{U}} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) + \frac{\partial g(\mathcal{U}, \mathcal{V})}{\partial x} \cdot \frac{\partial \mathcal{U}}{\partial x} (x,y) +$$

$$\lim_{(x,y)\to(0,0)}\frac{h(x,y)}{\|(x,y)\|}=?$$

Sé que 
$$h(x_{15}) = P_{1}(x_{15}) + R_{1}(x_{15})$$

Con lim 
$$R_1(x,y) = 0$$
 por propieded di  
 $(x,y) \rightarrow (0,0)$   $||(x,y)||$  Resto

$$= \lim_{(x,y) \to (0,0)} \frac{h(x,y)}{\|\|\|\|} = \lim_{(x,y) \to (0,0)} \frac{p_1(x,y)}{\|(x,y)\|\|}$$

$$\begin{array}{lll}
\text{vole & e. & (x,y) = (0,0)} \\
\text{Con} & \text{P1 } (x,y) = f(0,0) + \nabla f(0,0) (x-0, y-0) \\
&= f(0,0) + f_x(0,0) \cdot x + f_y(0,0) \cdot y \\
&= 0 & 2+2x+3y|_{(0,0)} & -1+3x+4y|_{(0,0)}
\end{array}$$

$$\begin{array}{lll}
\text{P1 } (x,y) = 2 \times -y
\end{array}$$

So me over por 
$$S = X$$

$$= \lim_{X \to 0} \frac{2X - X}{\sqrt{X^2 + X^2}} = \lim_{X \to 0} \frac{X}{\sqrt{2X^2}}$$

$$= \lim_{X \to 0} \frac{X}{\sqrt{2} \cdot |X|}$$

$$= \lim_{X \to 0} \frac{X}{\sqrt{2} \cdot |X|}$$

$$= \lim_{X \to 0} \frac{1}{\sqrt{2}}$$

Pintas Clave.

Fue clave en este punto usar que el resto R1 tiende a cero cuando (x,y) tiende a (x0,y0), donde este es el punto sobre el que esta definido el polinomio de Taylor.

Esto sucede porque en el punto, el polinomio coincide con la función, por lo tanto, en el punto, no hay error o resto, ya que no hay aproximación, sino que el valor exacto que toma la función en ese punto.

Sea  $f: \mathbb{R}^2 \to \mathbb{R}$  definida por  $f(x,y) = e^{xy-1} - \frac{1}{2}x^2 - \frac{1}{2}y^2$ .

- (a) Analizar la existencia de máximos y mínimos locales y puntos silla de f en  $\mathbb{R}^2$ .
- (b) Analizar la existencia de extremos absolutos de f en la región

$$D = \{(x, y) \in \mathbb{R}^2 / x^2 + y^2 \le 2\}.$$

o) 
$$f \in \mathcal{C}^{\infty}$$
 puer es sum, prod, comp. de fincioner  $\mathcal{C}^{\infty}$ 

Colcho  $\nabla f(x,y) = (e^{xy-1} \cdot y - x \cdot e^{xy-1} \cdot x - y)$ 

$$= (0,0) \iff \int x = y \cdot e^{xy-1}$$

$$= (0,0) \iff \int x = x \cdot e^{xy-1}$$

Resolvo (sum)
$$x+y = e^{xy-1} \cdot (x+y)$$

So 
$$x+y=0$$
 $x = y \cdot e^{xy-1}$ 
 $x = -x \cdot e^{-x^2-1}$ 
 $x = x \cdot e^{-x^2-1}$ 
 $x$ 

Tengo cardidatos, busos extranor locales

Armo Hessian

$$\nabla f(x,y) = (e^{xy-1}.y - x, e^{xy-1}.x - y)$$

$$Hf = \begin{bmatrix} y^2 & e^{xy-1} - 1 & x \cdot y \cdot e^{xy-1} + e^{xy-1} \\ x \cdot y \cdot e^{xy-1} + e^{xy-1} & x^2 \cdot e^{xy-1} - 1 \end{bmatrix}$$

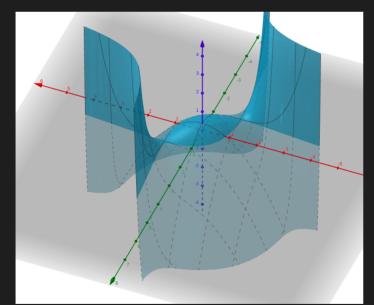
• en 
$$(0,0)$$
,

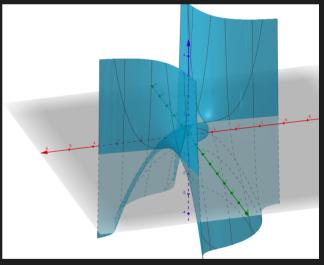
det  $H_{+}^{+}(0,0) = \begin{bmatrix} -1 \\ e^{-1} \end{bmatrix} = 1 - e^{-2}$ 

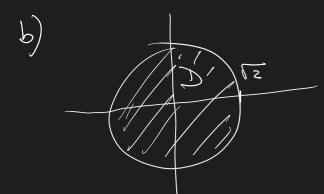
≈ 1.1353 >0

Cono det 
$$Hf(0,0) > 0$$
  
 $y = 0$  (0,0) er méximo.

$$H_{+}(-1,-1) = \begin{bmatrix} 0 & z \\ z & 0 \end{bmatrix}$$







Por a) sé que el vii a posible extremo en Derel (0,0)

Folto ver el borde:

$$\sigma(t) = (\sqrt{2} \cdot \cos t) \sqrt{2} \cdot \sin t$$

Con los X. y obtendré (52)2. cost, sin t

Recuerdo identidad:

 $2/\sqrt{2}$   $5 \times 2 \times 2/\sqrt{2}$   $5 \times 2 \times 2/\sqrt{2}$ 

$$g(t) = e^{\sin 2t} \cdot \cos 2t, z = 0$$

$$(\Rightarrow \cos zt = 0 \quad \cos t \in [0, z\pi)$$

$$P.C. \text{ ent} = \left\{ \frac{1}{4} \pi, \frac{3}{4} \pi, \frac{5}{4} \pi, \frac{7}{4} \pi \right\}$$

$$g(t) = e^{-3h^2 2t} - 1$$

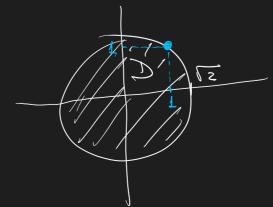
$$\Im\left(\frac{1}{4}\pi\right) = e^{500\frac{1}{2}\pi} - 1 = e - 1 \approx 1,718 \text{ Mex}$$

$$\Im\left(\frac{3}{4}\pi\right) = e^{3in\frac{3}{2}\pi} - 1 = \frac{1}{e} - 1 \approx -0.63 \text{ Hin}$$

$$g\left(\frac{5}{4}\pi\right) = e^{5in\frac{5}{2}\pi} - 1 = g\left(\frac{1}{4}\pi\right) \text{ mismo purto on } D$$

$$g\left(\frac{7}{4}\pi\right) = e^{3n\frac{7}{2}\pi} - 1 = g\left(\frac{7}{4}\pi\right) \text{ misms purto on } D$$

$$f(0,0) = \frac{1}{e} \approx 0,368$$



$$\|\text{amo }g(x,y):=x^2+y^2$$

$$\nabla g(x,y) = (2x, 2y) = 6 \iff (x,y) = (0,0)$$

$$\nabla f(x,y) = \left(e^{xy-1} \cdot y - x, e^{xy-1} \cdot x - y\right)$$

Planteo sistema

$$\begin{cases} f_{x} = \lambda. g_{x} \\ f_{y} = \lambda. g_{y} \end{cases} \Rightarrow \begin{cases} e^{xy-1}. y_{-x} = 2x. \lambda & \oplus \\ e^{xy-1}. x_{-y} = 2y. \lambda & \oplus \\ g^{(xy)} = 2 & \oplus \\ x^{2} + y^{2} = 2 & \oplus \end{cases}$$

$$\bigoplus \frac{e^{xy-1} \cdot y - x}{zx} \stackrel{\text{$\times$} \neq 0}{=} \chi$$

$$e^{xy^{-1}}$$
,  $x^z - xy = e^{xy^{-1}}$ ,  $y^z - xy$ 

$$\mathcal{C}^{xy-1}, x^{z} = \mathcal{C}^{xy-1}, y^{z}$$

$$x^{2} = 5^{2}$$

$$x^{2} = 2 - 5^{2}$$

$$2 - 5^{2} = 5^{2}$$

$$2 = 25^{2}$$

$$3^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

$$5^{2} = 1$$

Folk ver x=0;

$$\begin{cases} e^{x_{\delta^{-1}}} \cdot y - x = 2x \cdot \lambda \\ e^{x_{\delta^{-1}}} \cdot x - y = 2y \cdot \lambda \end{cases} \xrightarrow{x=0} \begin{cases} e^{-1} \cdot y = 0 \Rightarrow y=0 \\ -y = 2y \cdot \lambda \end{cases}$$

$$\begin{cases} x^{2} + y^{2} = 2 \end{cases}$$

Evalúo PCs:

$$f(-1,-1) = 0$$

$$f(-1,1) = e^{-2} - 1 \approx -0.87$$

$$f(1,-1) = e^{-2} - 1 \approx -0.87$$

$$f(1,1) = 0$$

 $f(0,0) = 1 - e^{-2} \approx 1, \dots$  Méx en (0,0)

Calcular las siguientes integrales

(a) 
$$\int_0^1 \int_{x^3}^1 y^2 sen(x^2) dx dy$$
.

(b) 
$$\iiint_E xz \ dV$$
 donde  $E$  es el sólido delimitado por el plano  $4x+y+2z=2$  en el primer octante.

a) Canbio 
$$0 \le y \le 1$$

$$0 \le y \le^3 \times \le 1$$

$$0 \le x \le 1$$

$$0 \le x \le 1$$
Rescarbo
$$\int_{x=0}^{x=1} \int_{y=0}^{3} x y^2 \cdot \sin(x^2) dy dx$$

$$= \int_{x=0}^{x=0} \sin(x^2) \cdot \frac{3}{3} \sqrt{x} dx$$

$$= \int_{x=0}^{x=0} \sin(x^2) \cdot \frac{3}{3} \sqrt{x} dx$$

$$= \int_{1}^{0} 2y u \times_{s} \frac{3}{x} dx$$

$$= -\frac{1}{16} \cos x^{2} \Big|_{0}$$

$$-\cos x^{2} \cdot \frac{1}{16} \frac{\sin x}{\cos x}$$

$$-\cos x^{2} \cdot \frac{1}{16} \frac{\sin x}{\cos x}$$

$$= -\frac{1}{6} \left( \cos(1) - \cos 0 \right)$$

$$= -\frac{1}{6} \left( \cos(1) - 1 \right)$$

$$E = \begin{cases} (x_1 \le z^2) : & 0 \le x \le \frac{1}{2} \\ 0 \le z \le -2x + 1 \end{cases}$$

$$0 \le y \le 2 - 4x - 2z$$

$$\int_{x=0}^{\frac{1}{2}} \int_{z=0}^{-2x+1} \int_{y=0}^{2x+1} |x_1 - x_2|^2 dy dz dx = 0$$

$$\int_{x=0}^{\frac{1}{2}} \int_{z=0}^{-2x+1} \int_{z=0}^{2-4x-2z} x \cdot z \, dy \, dz dx =$$

$$= \int_{X=0}^{\frac{1}{2}} X \cdot \int_{Z=0}^{-2x+1} Z \cdot (Z-4x-2z) dz dx$$

$$= \int_{x=0}^{\frac{1}{2}} x \int_{x=0}^{-2x+1} 2x - 4xz - 2z^{2} dz dx$$

$$= \int_{x=0}^{\frac{1}{2}} x \cdot \left[ \frac{1}{2} z^{2} - \frac{4}{3} x z^{2} - \frac{2}{3} z^{3} \right]_{0}^{-2x+1} dx$$

$$= \int_{x=0}^{\frac{1}{2}} x \cdot \left( 1 - 4x + 4x^{2} - x + 4x^{2} - 4x^{3} - \frac{1}{2} - \frac{1}{2}$$

Error de cuenter en algún ledo el resultado er el reguin revolución. Sea  $F: \mathbb{R}^3 \to \mathbb{R}^3$ ,

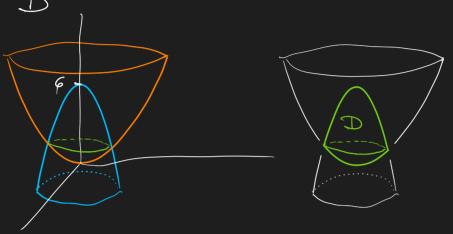
$$F(x, y, z) = \left(\frac{zx^3}{3} + zy^2x, xy^2e^{x^2}, -2xyze^{x^2}\right).$$

Calcular

$$\iiint_{D} div(F)dV,$$

donde D es la región encerrada por las superficies  $z=x^2+y^2$  y  $z=6-2x^2-2y^2$ .





$$div \mp = P_x + Q_y + R_z$$

$$= 2x^2 + 2y^2 + 2xy \cdot e^{x^2} - 2xy e^{x^2}$$

$$= 2 \cdot (x^2 + y^2)$$
Atorti! Pide combio de variables!

Plan: Cambio cilíndricas

$$Z = (6 - 2(x^2 + y^2))I or I$$
  
 $Z = (6 - 2, Z)$ 

$$\begin{cases} \mathcal{D}_{2} \\ \mathcal{D}_{3} \\ \mathcal{D}_{4} \end{cases}$$

$$X = \Gamma \cdot \cos \theta$$

$$S = \Gamma \cdot \sin \theta$$

$$Z = Z$$

$$X^{2} + y^{2} \leq Z \leq (6 - 2(x^{2} + y^{2}))$$

$$= \int_{0.0}^{2\pi} \int_{\Gamma=0}^{72} \frac{3}{2} \int_{\Gamma^{2}}^{2\pi} d\Gamma d\theta$$

$$= \int_{0}^{2} \int_{0}^{2} \int_{0}^{3} \int_$$

$$=\frac{1}{2}$$
.  $\int_{\theta}^{\pi} \int_{\Gamma}^{3} 36\Gamma^{3} - 24\Gamma^{5} + 3\Gamma^{7} d\Gamma d\theta$ 

$$= \frac{1}{2} \int_{0.0}^{2\pi} \frac{36}{4} \cdot \Gamma^4 - \frac{24}{6} \cdot \Gamma^6 + \frac{3}{8} \cdot \Gamma^8 \Big|_{0}^{\sqrt{2}} d\theta$$

$$= \frac{1}{2} \int_{a=0}^{2\pi} q \cdot z^2 - z^2 \cdot z^3 + \frac{3}{8} \cdot z^4 d\theta$$

$$=\frac{2}{2}\overline{n}$$
.

Plan: Usar cilíndricas dividiado D en Diy Da

$$Z = 6 - 2(x^{2} + y^{2})$$
 $Z = 6 - 2, Z$ 
 $Z = 2 = 0$ 

$$\begin{cases}
S = S \\
S = C, & 20, 0 \\
X = L \cdot & \cos \theta
\end{cases}$$

$$\Gamma \in [0, \phi(z)]$$

$$\phi_{L}(z) = \sqrt{x^2 + y^2}$$

$$\phi_1(z) = \sqrt{x^2 + y^2}$$
 = despejo de eq  $z = x^2 + y^3$ 

$$Z = (6 - 2x^{2} - 26^{2})$$

$$Z - 6 = -2(x^{2} + 6^{2})$$

$$3 - \frac{Z}{3} = x^{2} + 6^{2}$$

$$\phi_2(z) = \sqrt{3-\frac{z}{z}}$$



Calab sobre Dz:

$$D_{2} = \int_{2}^{2\pi} dv + r \cdot dr d\theta dz$$

$$D_{2} = \int_{2}^{2\pi} \int_{3-\frac{\pi}{2}}^{3-\frac{\pi}{2}} d\theta dz$$

$$= \int_{2=2}^{6} 2\pi \int_{9-9}^{2\pi} \frac{1}{4} \left(3-\frac{\pi}{2}\right)^{2} d\theta dz$$

$$= \int_{2=2}^{2} 2 \int_{9-9}^{2\pi} \frac{1}{4} \left(3-\frac{\pi}{2}\right)^{2} d\theta dz$$

Calab sobre D2:

$$\iint_{\mathbb{R}} dv = \iiint_{\mathbb{R}} dv = \iint_{\mathbb{R}} dv + r \cdot dr d\theta d\xi$$

$$D_{2} \qquad D_{2} \qquad = \int_{\mathbb{R}^{2}} \theta \int_{\mathbb{R}^{2}} dv \int_{\mathbb{R}^{2}} dv d\theta d\xi$$