## Análisis I - Análisis Matemático I - Matemática I - Análisis II (C)

2do. cuatrimestre 2020

Simulacro del Primer Parcial - 14/10/2020

Ejercicio 1: Sea  $\mathcal C$  la curva que se obtiene como la intersección de las superficies

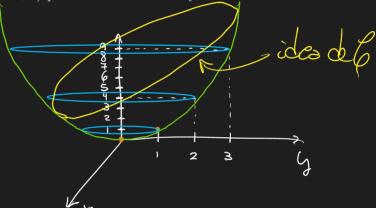
$$x^{2} + y^{2} - z = 0$$
  $y$   $x^{2} - 4x + y^{2} + z = 0$ 

- (a) Hallar una función r(t) cuya imagen describa la cur Va  $\mathcal C$
- (b) Verificar que el punto  $P=(1-\frac{\sqrt{2}}{2},\frac{\sqrt{2}}{2},2-\sqrt{2})$  pertenece a la curva  $\mathcal C$  y hallar la ecuación de la recta tangente a  $\mathcal C$  en el punto P

• 
$$x^2 + y^2 = 1$$

$$\times^2 + y^2 = 4 = 2^2$$

• 
$$x^2 + y^2 = 9 = 3^2$$



$$\begin{array}{l}
\alpha ) \begin{cases}
2 = x^2 + y^2 \\
2 = 4x - x^2 - y^2
\end{array}$$

$$0 = 2x^2 + 2y^2 - 4x$$

$$O = \left(x^2 - 2x + 1\right) - 1 + 3^2$$

$$(X-1)^2 = x^2 - 2x + 1$$

Paso a polares
$$\begin{cases}
x-1 = r \cdot \cos \theta & r = 1 \\
y = r \cdot \sin \theta & \theta \in [0, 2\pi]
\end{cases}$$

$$\begin{cases}
x = 1 + \cos \theta \\
y = \sin \theta
\end{cases}$$

$$\begin{cases}
x = x^2 + y^2 = x^2 = (1 + \cos \theta)^2 + \sin^2 \theta \\
= 1 + 2 \cos \theta + (\cos^2 \theta + \sin^2 \theta)^2 = 2 + 2 \cos \theta
\end{cases}$$

$$\begin{cases}
x = (x^2 + y^2) + 4x
\end{cases}$$

Con la otra (voitico)
$$z = -(x^2 + b^2) + 4x$$

$$= -2 - 2\cos\theta + 4(1 + \cos\theta)$$

$$= 2 + 2\cos\theta$$

Obtave
$$\begin{cases}
x = 1 + \cos \theta \\
y = \sin \theta
\end{cases}$$

$$z = 2 + 2 \cos \theta$$

$$O(t) = (1 + \cos t, \sin t, z + z \cos t) \quad t \in [0, 2\pi)$$

$$P = \left(1 - \frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}, 2 - \sqrt{2}\right)$$

$$\int_{0}^{\sqrt{2}} 1 + \cos t = 1 - \frac{\sqrt{2}}{2}$$

$$\int_{0}^{\sqrt{2}} 1 + \cos t = 1 - \frac{\sqrt{2}}{2}$$

$$2 + 2 \cos t = 2 - \sqrt{2}$$

$$1 + \cos t = 1 - \frac{12}{2}$$

$$\cos t = -\frac{12}{2}$$

$$t = \arccos(-\frac{12}{2})$$

$$t = \frac{3}{4}\pi \in [0, 2\pi)$$

$$500(\frac{3}{4}\pi) = \frac{12}{2}$$

• P existe on 
$$G$$
 y se de ando
$$L = \frac{3}{4}\pi$$
 on  $G(L)$ 

D ez, vo

$$O(t) = (1 + \infty t, mt, 2 + 2 \cos t)$$

$$\delta'(t) = (-\sin t, \cot, -2\sin t)$$

$$\delta'\left(\frac{3}{4}\pi\right) = \left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$$

$$= \left(-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$$

Armo recta L

L: 
$$(x,y,z) = P + Q \left(-\frac{\sqrt{z}}{2}, -\frac{\sqrt{z}}{2}, -\frac{\sqrt{z}}{2}\right)$$

$$Q \in \mathbb{R}$$

Otra forma: Primero paso cada ecuación a polares, después busco su intersección.

Polares
$$\begin{cases}
X = \Gamma \cdot \cos \theta \\
y = \Gamma \cdot \sin \theta
\end{cases}$$

$$\begin{array}{ccc}
\boxed{2} & = 4 \times - \left( \times^2 + y^2 \right) & \Rightarrow & \boxed{2} & = 4 \cdot \Gamma \cdot \cos \theta - \Gamma^2 \\
\times & = \Gamma \cdot \cos \theta \\
y & = \Gamma \cdot \sin \theta \\
\Gamma & \in [0, +\infty)
\end{array}$$

$$\begin{array}{cccc}
\varphi & \in [0, 2\pi)
\end{array}$$

I guelo II con II

$$X = \Gamma \cdot \cos \theta \quad \text{Coinciden en II } g \text{ IZ}$$

$$y = \Gamma \cdot \sin \theta$$

$$y = \partial \cos \theta$$

$$Z = \Gamma^{2}$$

$$Z = 4 \cdot \Gamma \cdot \cos \theta - \Gamma^{2}$$

$$\Rightarrow \Gamma^{2} = 4 \cdot \Gamma \cdot \cos \theta - \Gamma^{2}$$

$$0 = 4r \cdot \cos \theta - 2r^{2}$$

$$0 = 2r \left(2\cos \theta - r\right)$$

$$r>0$$

$$0 = 2\cos \theta - r$$

$$r = 2\cos \theta$$

$$S = L_{S}$$

$$S =$$

Finalmente, puedo de Rinir

$$\sigma(t) = \left( z \cos^2 t, z \cot, sint, 4 \cos^2 t \right)$$
con te[0,217)

b) 
$$\sigma(t) = \left( 2 \cos^2 t, 2 \cot , 5 \cot , 4 \cos^2 t \right)$$

Ignab coord. è coord.

$$\begin{cases}
1 - \frac{12}{2} = 2 \cos^2 t \\
\frac{12}{2} = 2 \cos t \cdot 5 \cot \\
2 - 12 = 4 \cos^2 t
\end{cases}$$

55

$$|\cos t| = \frac{1}{2} - \frac{1}{2}$$

$$|\cos t| = \left(\frac{1}{2} - \frac{1}{2}\right)^{1/2}$$

$$\cos t = \left(\frac{1}{2} - \frac{\sqrt{2}}{4}\right)^{1/2} \quad \textcircled{1}$$

$$\cos t = -\left(\frac{1}{2} - \frac{\sqrt{2}}{4}\right)^{1/2} \quad \textcircled{1}$$

$$t' = \frac{8}{3} \text{ M}$$

$$cs|cs|cs|cs \left( \left( \frac{5}{7} - \frac{15}{15} \right)_{15} \right)$$

Cost, 2 0,38 e to,211)

$$\begin{array}{ccc}
\textcircled{II} & t_{z=3} & \text{27CCOS} & \left(-\left(\frac{1}{2} - \frac{\sqrt{2}}{2}\right)^{1/2}\right) \\
& \text{colc} \\
& t_{z=\frac{5}{8}} & \text{IT} \\
& \text{cos} & t_{z=-0,38} \notin [0,2\pi]
\end{array}$$

oo el punto P pertenece ele curva & cuendo t = 3 T

Busco recta tangente a 6 an P

Derivo O(t):

$$\sigma(t) = \left( 2 \cos^2 t, 2 \cot t, 3 \cot t, 4 \cot^2 t \right)$$

$$\sigma'(t) = \left(-4 \cdot \cos t \cdot \sin t\right) - 2 \sin^2 t + 2 \cos^2 t - 8 \cos t \cdot \sin t$$

Evalúo en t= 3 TT

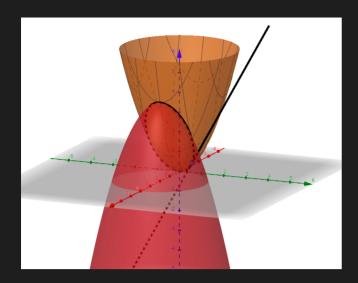
$$O'\left(\frac{3}{8}\pi\right) = \left(-\sqrt{2}, -\sqrt{2}\right)$$

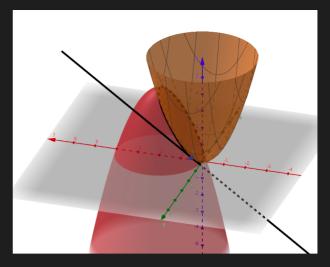
l dirección tengente e la curva

Defino recta L como

$$L: (x_{15}, z) = P + Q(-12, -12, -212)$$

 $\alpha \in \mathbb{R}$ 





Ejercicio 2: Calcular los siguientes límites:

(a) 
$$\lim_{(x,y)\to(0,0)} \frac{(x-1)^2 \operatorname{sen}(x^2)y}{x^2 + y^4}$$
.

(b) 
$$\lim_{(x,y)\to(0,0)} \frac{e^{xy}-1}{x^2+y^2}$$
.

a) Aosto
$$\frac{(x-1)^2 \cdot 5in(x^2) \cdot 5}{x^2 + 5^4} = 0 \left\{ \begin{array}{c} (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \\ \hline (x^2 + 5^4) \end{array} \right\}$$

$$= \frac{(x-1)^2 \cdot x^2}{x^2 + 5^4} \left\{ \begin{array}{c} (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \\ \hline (x^2 + 5^4) \end{array} \right\}$$

$$= \frac{x^2}{x^2 + 5^4} \left\{ \begin{array}{c} (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \\ \hline (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \end{array} \right\}$$

$$= \frac{(x-1)^2 \cdot 5in(x^2) \cdot 5}{x^2 + 5^4} \left\{ \begin{array}{c} (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \\ \hline (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \end{array} \right\}$$

$$= \frac{x^2}{x^2 + 5^4} \left\{ \begin{array}{c} (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \\ \hline (x-1)^2 \cdot \int 5in(x^2) \cdot |5| \end{array} \right\}$$

$$Six = y^3$$

$$O(t) = \begin{pmatrix} t^2, t \\ x & y \end{pmatrix}$$

$$\frac{1}{50} = \frac{(y^2 - 1)^2 - 500(y^4) - 5}{y^4 + y^4} = \frac{1}{500}$$

$$=\lim_{y\to 0}\frac{(y^2-1)^2(5)(y^4)\cdot y}{2\cdot y^4}$$

Sabenos que
$$\lim_{t\to0}\frac{\sin(t)}{t}=1$$

$$= \lim_{x \to \infty} \frac{(y^4 - zy^2 + 1) \cdot y}{2} = 0$$

$$\lim_{X \to 0} \frac{(X-1)^2 \cdot 5/5 (X^2) \cdot X}{X^2 + X^4} =$$

$$= \lim_{x \to 0} \frac{(x-1)^{2} \cdot \sin(x^{2}) \cdot x}{x^{2} \left(1 + x^{2}\right)} = \frac{(x-1)^{2} \cdot \sin(x^{2})}{x + x^{3}} = \frac{2(x-1) \cdot \sin x^{2} + (x-1)^{2} \cdot \cos x^{2}}{1 + 3x^{2}}$$

$$= \lim_{x \to 0} \frac{(x-1)^{2} \cdot x}{1 + x^{2}} \qquad (x^{2} - 2x + 1) \times \frac{x^{3} - 2x^{2} + x}{x^{2} + 1}$$

$$\int = m \cdot x$$

$$\lim_{x \to 0} \frac{(x-1)^2 \cdot \sin(x^2) \cdot m \cdot x}{x^2 + m^4 \cdot x^4}$$

$$= \lim_{x \to 0} \frac{(x-1)^2 \cdot \sin(x^2) \cdot m \cdot x}{x^2 + m^4 \cdot x^3}$$

$$\lim_{x \to 0} \frac{(x-1)^2 \cdot \sin(x^2) \cdot m \cdot x}{x^2 + m^4 \cdot x^3}$$

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$$\lim_{x \to 0} \frac{(x-1)^2 \cdot \sin(x^2) \cdot m \cdot x}{x^2 + m^4 \cdot x^3}$$

$$X = mg$$

$$\lim_{y \to 0} \frac{(my - 1)^2 \cdot 5in(m^2y^2) \cdot y}{m^2y^2 + y^4}$$

$$= (m - 1) \cdot \lim_{y \to 0} \frac{5in(m^2y^2)}{m^2 \cdot y + y^3}$$

$$\lim_{y \to 0} \frac{\cos(m^2 \cdot y^2) \cdot m^2 \cdot 2y}{m^2 + 3y}$$

$$\lim_{y \to 0} \frac{\cos(m^2 \cdot y^2) \cdot m^2 \cdot 2y}{m^2 + 3y}$$

$$\int_{0}^{2\pi} \frac{x^{2}}{x^{2}} = \frac{1}{2} \frac{1}{x^{2}} = \frac{1}{2} \frac{\cos x^{2} \cdot 2x}{2x^{3/2}} = \frac{1}{2} \frac{\cos x^{2} \cdot 2x}{2x^{3/2}} = \frac{\cos x^{2} \cdot 2x}{2x^{3/2}} = \frac{1}{2} \frac{\cos x^{2} \cdot 2x}{2x^{3/2}} = \frac{1}{2} \frac{\cos x^{2} \cdot 2x}{2x^{3/2}} = \frac{1}{2} \frac{2x \cdot \cos x^{2}}{3x^{3/2}} = \frac{1}{2} \frac{2x \cdot \cos x^{2$$

(b) 
$$\lim_{(x,y)\to(0,0)} \frac{e^{xy}-1}{x^2+y^2}$$
.

$$\lim_{x\to 0} \frac{e^{x^2}-1}{2 \cdot x^2}$$

Si
$$y = x$$

$$\lim_{x \to 0} \frac{e^{x^2} - 1}{2 \cdot x^2} = \lim_{x \to 0} \frac{e^{x^2} \cdot 2x}{2 \cdot 2x}$$

$$=\lim_{x\to 0}\frac{e^{x^2}}{z}=\frac{1}{2}$$

$$\lim_{x \to 0} \frac{e^{\circ} - 1}{x^{2}} = 0$$

Ejercicio 3: Sea  $f: \mathbb{R}^2 \to \mathbb{R}$  definida por:

$$f(x,y) = \begin{cases} \frac{x^2y^2 - \sin(x^4)}{x^2 + \frac{1}{3}y^2} + 2 & \text{si } (x,y) \neq (0,0), \\ a & \text{si } (x,y) = (0,0). \end{cases}$$

Hallar, si es posible, un valor de  $a \in \mathbb{R}$  para que f(x,y) sea continua en todo  $\mathbb{R}^2$ . ¿Es f diferenciable para algún a?

Veo 
$$x = 0$$

$$\int (0,19) = \frac{0 - \sin(0)}{0^2 + \frac{1}{3}9^2} + 2 = 2$$

$$\begin{array}{c}
\alpha & Candidato & a \\
2 - 3 \cos(x^4) & + 2 - 2
\end{array}$$

$$\begin{array}{c}
\frac{x^2 \cdot y^2 - \sin(x^4)}{3} + 2 - 2
\end{array}$$

$$\begin{array}{c}
\frac{x^2 \cdot y^2 - \sin(x^4)}{3} + 2 - 2
\end{array}$$

$$\begin{array}{c}
\frac{x^2 \cdot y^2 - \sin(x^4)}{3} \\
\frac{1}{3}x^2 & \times x^2
\end{array}$$

$$\begin{array}{c}
\frac{1}{3}(x^2 + y^2) & + \frac{1}{3}(x^2 + y^2)
\end{array}$$

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\frac{1}{3}(x^3 + y^2) & + \frac{1}{3}(x^3 + y^2)
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\frac{1$$

$$\lim_{(x,y)\to(0,0)} \frac{f(x,y) - (f(0,0) + f_x(0,0),(x-0) + f_y(0,0)(y-0))}{\|(x,y)\|} \stackrel{?}{=} 0$$

Calabo derivader parcialer

$$f_{x(x,y)} = \lim_{h \to 0} \frac{f(x+h,y) - f(x,y)}{h}$$

$$f_{\times}(0,0) = \lim_{h \to 0} \frac{f(h,0) - f(0,0)}{h}$$

$$= \lim_{h \to 0} \frac{h^2}{h^2} + 2 - 2$$

$$=\lim_{h\to 0}\frac{1}{h}\cdot\frac{5hh^4}{h^2}=\lim_{h\to 0}\frac{5hh^4}{h^3}$$

$$\stackrel{\downarrow}{=} \lim_{h \to 0} \frac{\cos(h^4) \cdot 4h^3}{3h^2} = \lim_{h \to 0} \frac{4 \cdot \cos(h^4) \cdot h}{3}$$

$$f_{\times}(0,0) = 0$$

$$f_{S}(0,0) = \lim_{h \to 0} \frac{f(0,h) - f(0,0)}{h}$$

$$= \lim_{h \to 0} \frac{(0-5h)(0)}{(0+3h)^{2}} + 2 - 2 = h$$

$$\lim_{(x,y)\to(0,0)} \frac{f(x,y) - (f(0,0) + f_x(0,0),(x-0) + f_y(0,0)(y-0))}{\|(x,y)\|}$$

$$\lim_{(x,y)\to(0,0)} \frac{1}{\|(x,y)\|} \cdot (f(x,y) - f(0,0))$$

$$\left| \frac{1}{\|(x_{i})\|} \left( \frac{x^{2} \cdot y^{2} - sin x^{4}}{x^{2} + \frac{1}{3} y^{2}} + 2 - 2 \right) \right| =$$

$$= \frac{1}{\|(xy)\|} \left| \frac{x^2 \cdot y^2 - \sin x^4}{x^2 + \frac{1}{3} y^2} \right| \left\langle \frac{1}{\|(xy)\|} \left( \frac{x^2 \cdot y^2}{\frac{1}{3}(x^2 + y^2)} + \frac{|\sin(x^4)|}{\frac{1}{3}(x^2 + y^2)} \right) \right|$$

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$$\frac{\|(x,y)\|^4}{\frac{1}{3}\|(x,y)\|^3} + \frac{\|(x,y)\|^4}{\frac{1}{3}\|(x,y)\|^3}$$

$$= 6 \|(x_1y)\| \longrightarrow 0$$

$$(x_1y) \neq 0$$

Admes f(x,5) er diforacieble 
$$Y(x,5) \in \mathbb{R}^2$$
, \{(0,0)\}

Con a=2,

es suma, resta, producto, composición y cociente (con denominador distinto de cero) de funciones diferenciables (polinomios y la función seno).

of (xy) or differentiable 
$$\forall (xy) \in \mathbb{R}^2$$

Ejercicio 4: Sea  $f: \mathbb{R}^2 \to \mathbb{R}$  una función diferenciable tal que el plano tangente a su gráfico en el punto (1,2,f(1,2)) es

$$-x - 2y + z = -1.$$

Si  $x = 3s + t^2$  e  $y = 2s^2 + 2t$  y definimos F(s,t) = f(x,y), calcular la ecuación del plano tangente al gráfico de F en el punto (0,1,F(0,1)).

$$\int x = 35 + t^2$$

$$\int y = 25^2 + 2t$$

$$\mp (s,t) = \pm (3s+t^2, 2s^2+zt)$$

$$P_{1}(0,1) = F(0,1) + \frac{\partial F}{\partial s}(s,t) (s-0) + \frac{\partial F}{\partial t}(s,t) (t-1)$$

$$\mp(0,1) = ?$$

$$\begin{cases} x = 35 + t^{2} \\ y = 25^{2} + 2t \\ (91) \end{cases} = \begin{cases} x = 1 \\ y = 2 \end{cases}$$

$$\mp(0,1) = \ddagger(1,2)$$

L Veo suplano targente en el (1,2) puer conciden

$$f(1,2) = x + 2y - 1 \Big|_{(1,2)}$$

$$\mp(0,1) = 4$$

Cel culo desivedes percia les

$$\frac{\partial}{\partial s} + (s,t) = \frac{\partial}{\partial s} (x(s,t), y(s,t)) \cdot \frac{\partial}{\partial s} (s,t) + \frac{\partial}{\partial s} (x,s) \cdot \frac{\partial}{\partial s} (s,t)$$

$$\frac{\partial f}{\partial t} + (z^{i}t) = \frac{\partial f}{\partial t} (x(z^{i}t), \beta(z^{i}t)) \cdot \frac{\partial f}{\partial x} (z^{i}t) + \frac{\partial f}{\partial t} (x^{i}s) \cdot \frac{\partial f}{\partial x} (z^{i}t)$$

Coincidn con les dérivades del pleno puer es su polinonio de grado 1.

$$\cdot \frac{\partial f}{\partial x} = f$$

$$\frac{\partial x}{\partial x}(zt) = \frac{\partial}{\partial x}(35+t^2) = 3$$

$$\frac{\partial x}{\partial x}(st) = 2t$$

$$\frac{3x}{9x}(01) = 2$$

$$\frac{\partial y}{\partial z}(z_1t) = \frac{\partial}{\partial t}(z_2z_1+z_1t) = 4z$$

$$\frac{\partial y}{\partial y}(z,t) = 2$$

The ment 
$$\frac{1}{2} = \frac{1}{2} \left( x(z,t), y(z,t) \right) \cdot \frac{1}{2} \left( x(z,t) + \frac{1}{2} \left( x(z,t) \right) \cdot \frac{1}{2} \left( x(z,t) + \frac{1}{2} \left( x(z,t) \right) \cdot \frac{1}{2} \left( x(z,t) \right) \right) \cdot \frac{1}{2} \left( x(z,t) + \frac{1}{2} \left( x(z,t) \right) \cdot \frac{1}{2} \left( x(z,t) \right) \cdot$$

$$P_{1}(0,1) = F(0,1) + \frac{2F(s,t)}{2S}(s,t)(s-0) + \frac{2F(s,t)}{2S}(s,t)(t-1)$$

$$= 4$$

$$= 3$$

$$= 6$$

$$P_1(0,1) = 4 + 35 + 6(t-1)$$

Como # er diferenciable por ser composición de funcioner diferenciables (f, x, b) => Su plano tangente existe en (0,1, F(9,1)) y en

$$TT: \omega = 3s + t - 2$$