Projects and how do develop a numerical project

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Some basic ingredients for a successful numerical project

In when building up a numerical project there are several elements you should think of

- 1. How to structure a code in terms of functions
- 2. How to make a module
- 3. How to read input data flexibly from the command line
- 4. How to create graphical/web user interfaces
- 5. How to write unit tests (test functions or doctests)
- 6. How to refactor code in terms of classes (instead of functions only)
- 7. How to conduct and automate large-scale numerical experiments
- 8. How to write scientific reports in various formats (LATEX, HTML)

Additional benefits: A structured approach to solving problems

The conventions and techniques outlined here will save you a lot of time when you incrementally extend software over time from simpler to more complicated problems. In particular, you will benefit from many good habits:

- 1. New code is added in a modular fashion to a library (modules)
- 2. Programs are run through convenient user interfaces

- 3. It takes one quick command to let all your code undergo heavy testing
- 4. Tedious manual work with running programs is automated,
- 5. Your scientific investigations are reproducible, scientific reports with top quality typesetting are produced both for paper and electronic devices.

Analysis of project, Configuration Interaction theory

```
from numpy import *
from sympy import *
from matplotlib.pyplot import *
g_{array} = linspace(-1, 1, 1001)
e1_array = []
e2_array = []
for g in g_array:
      u1, v1 = linalg.eig(H1)
      u2, v2 = linalg.eig(H2)
      if g == 1./2:
             print argmin(u1)
             e1_array.append(min(u1))
      e2_array.append(min(u2))
plot(g_array, e1_array, linewidth=2.0)
#plot(g_array, e2_array, linewidth=2.0)
plot(g_array, (2-g_array), linewidth=2.0)
grid()
xlabel(r"Strength of interaction, $g$", fontsize=16)
ylabel(r'Ground state energy', fontsize=16)
#axis([-1,1,-0.4,0.05])
```

```
legend(['FCI -- Exact', 'Reference energy'])
savefig("proj1_ref2.pdf")
show()
```

Analysis of project, Many-body perturbation theory

```
from sympy import *
from pylab import *
below_fermi = (0,1,2,3)
above_{fermi} = (4,5,6,7)
states = [(1,1),(1,-1),(2,1),(2,-1),(3,1),(3,-1),(4,1),(4,-1)]
N = 8
g = Symbol('g')
def h0(p,q):
         if p == q:
                  p1, s1 = states[p]
return (p1 - 1)
         else:
                  return 0
def f(p,q):
         if p == q:
                  return 0
         s = h0(p,q)
         for i in below_fermi:
                  s += assym(p,i,q,i)
         return s
def assym(p,q,r,s):
         p1, s1 = states[p]
p2, s2 = states[q]
p3, s3 = states[r]
         p4, s4 = states[s]
         if p1 != p2 or p3 != p4:
                  return 0
         if s1 == s2 or s3 == s4:
                  return 0
         if s1 == s3 and s2 == s4:
                  return -g/2.
         if s1 == s4 and s2 == s3:
                  return g/2.
def eps(holes, particles):
         \mathbf{E} = 0
         for h in holes:
                  p, s = states[h]
E += (p-1)
         for p in particles:
                  p, s = states[p]
E -= (p-1)
```

return E

Diagram 3

```
# s = 0
# for a in above_fermi:
                                                 for b in above_fermi:
                                                                                        #
 #
                                                                                                                                                                       for j in below_fermi:
                                                                                                                                                                                                             for k in below_fermi:
 #
                                                                                                                                                                                                                                                     s \leftarrow assym(i,j,a,b)*assym(a,c,j,k)*assym(l)
#
 # print s
# ga = linspace(-1, 1, 101)
# corr2 = []
 # corr3 = []
# corrx = []
# Diagram 1
s1 = 0
for a in above_fermi:
                                       for b in above_fermi:
                                                                              for i in below_fermi:
                                                                                                                     for j in below_fermi:
                                                                                                                                                            s1 += 0.25*assym(a,b,i,j)*assym(i,j,a,b)/eps((i,j),(a,b))
# Diagram 4
s4 = 0
for a in above_fermi:
                                       for b in above_fermi:
                                                                              for c in above_fermi:
                                                                                                                     for d in above_fermi:
                                                                                                                                                            for i in below_fermi:
                                                                                                                                                                                                   for j in below_fermi:
                                                                                                                                                                                                                                          s4 += 0.125*assym(i,j,a,b)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a,b,c,d)*assym(a
# Diagram 5
s5 = 0
for a in above_fermi:
                                       for b in above_fermi:
                                                                             for i in below_fermi:
                                                                                                                     for j in below_fermi:
                                                                                                                                                            for k in below_fermi:
                                                                                                                                                                                                   for l in below_fermi:
                                                                                                                                                                                                                                          s5 += 0.125*assym(i,j,a,b)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k,l,i,j)*assym(k
# Diagram 8 (simplified)
s8 = 0
for a in above_fermi:
                                       for b in above_fermi:
                                                                              for i in below_fermi:
                                                                                                                     for j in below_fermi:
                                                                                                                                                            for k in below_fermi:
                                                                                                                                                                                                   s8 -= \overline{0.5}*assym(i,j,a,b)*assym(a,b,i,k)*f(k,j)/eps(6)
# Diagram 9 (simplified)
s9 = 0
for a in above_fermi:
```

```
for b in above_fermi:
                for c in above_fermi:
                        for i in below_fermi:
                                for j in below_fermi:
                                         s9 += 0.5*assym(i,j,a,b)*assym(a,c,i,j)*f(b,c)/eps((i,j),(a,b))
print s1
print s4
print s5
print s8
print s9
s_5 = -0.0291521990740741*g**4
s14 = -0.0308883101851853*g**4
s34 = 0.0163049768518519*g**4
s36 = -0.0145760995370371*g**4

s38 = -0.0201099537037037*g**4
s39 = 0.0176938657407407*g**4
ga = linspace(-1,1,10001)
e1 = []
corr2 = []
corr3 = []
corr4 = []
for g_val in ga:
       u1, v1 = linalg.eig(H1)
        e1.append(min(u1))
        \verb|corr2.append((s1).subs(g,g_val))|
        corr3.append((s1+s4+s5).subs(g,g_val))
        corr4.append((s1+s4+s5+2*s_5+2*s14+2*s34+2*s36+s38+2*s39).subs(g,g_val))
exact = e1 - (2-ga)
plot(ga, exact, linewidth=2.0)
plot(ga, corr2, linewidth=2.0)
plot(ga, corr3, linewidth=2.0)
plot(ga, corr4, linewidth=2.0)
xlabel(r'Interaction strength, $g$', fontsize=16)
ylabel(r'Correlation energy', fontsize=16)
axis([-1,1,-0.5,0.05])
grid()
legend(["Exact", "2. order MPBT", "3. order MPBT", "4. order MPBT"], 'lower left')
savefig("pert_2.pdf")
show()
error1 = zeros(len(exact))
error2 = zeros(len(exact))
error3 = zeros(len(exact))
for i in range(len(exact)):
        error1[i] = abs(float(exact[i]-corr2[i]))
```

```
error2[i] = abs(float(exact[i]-corr3[i]))
    error3[i] = abs(float(exact[i]-corr4[i]))

error1 = array(error1)
  error2 = array(error2)
  error3 = array(error3)
  print type(error1)

plot(ga, log10(error1))
  plot(ga, log10(error2))
  plot(ga, log10(error3))
  xlabel(r"Strength of interaction, $g$", fontsize=16)
  ylabel(r"Error, $\log_{\rm 10}({\rm abs}({\rm error})$", fontsize=16)
  legend(["2. order MPBT", "3. order MPBT", "4. order MPBT"], 'lower left')
  grid()
  savefig("logerror.pdf")
  show()
```