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QMB 6911
Capstone Project in Business Analytics

Solutions: Problem Set #4

0.1 Introduction

This note summarizes the findings in the script `Tractor_Price_Density.R`, which analyzes the prices of fly reels, the dependent variable in the `TRACTOR7.csv` dataset. The output includes plots of the histogram and kernel-smoothed densities, using a selection of tuning parameters.

0.2 Relative Histogram of Fly Reel Prices

First plot a histogram with the default options.

```
hist(tractor_sales[, 'saleprice'],  
     main = 'Relative Histogram of Tractor Prices',  
     xlab = 'Price',  
     probability = TRUE)
```

Figure 1 is a histogram of the tractor prices generated by the code block above. Notice that there are some very large values. Consider taking logs

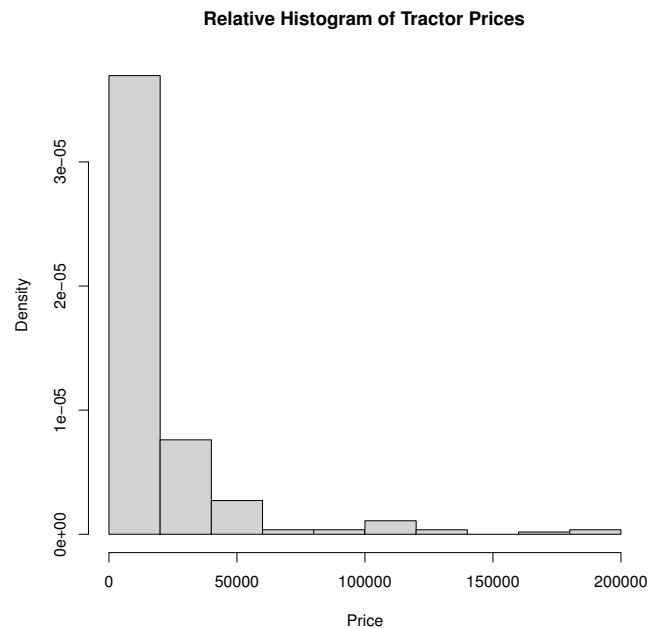


Figure 1: Relative Histogram of Tractor Prices

to bring outliers closer to the others.

```
# Generate a new variable log_saleprice.  
tractor_sales[, 'log_saleprice'] <- log(tractor_sales[, 'saleprice'])
```

Now plot the histogram for log of saleprice, depicted in Figure 2.

```
hist(tractor_sales[, 'log_saleprice'],
     main = 'Histogram of the Logarithm of Tractor Prices',
     xlab = 'Logarithm of Price',
     probability = TRUE)
```



Figure 2: Relative Histogram of the Logarithm of Tractor Prices

With this transformation, the variable appears much better behaved. It looks almost normally distributed.

Now we will consider adjusting the tuning parameter for the number of bars in the chart for the histogram. A low number of breaks may give a smoother plot but it may not be very informative, as in Figure 3.

```
hist(tractor_sales[, 'log_saleprice'], breaks = 5,
     main = c('Histogram of the Logarithm of Tractor Prices',
              'Number of Breaks: 5'),
     xlab = 'Logarithm of Price',
     probability = TRUE)
```

On the other extreme, a high number of breaks gives a sparsely populated and jagged plot. Figure 4 shows such an example.

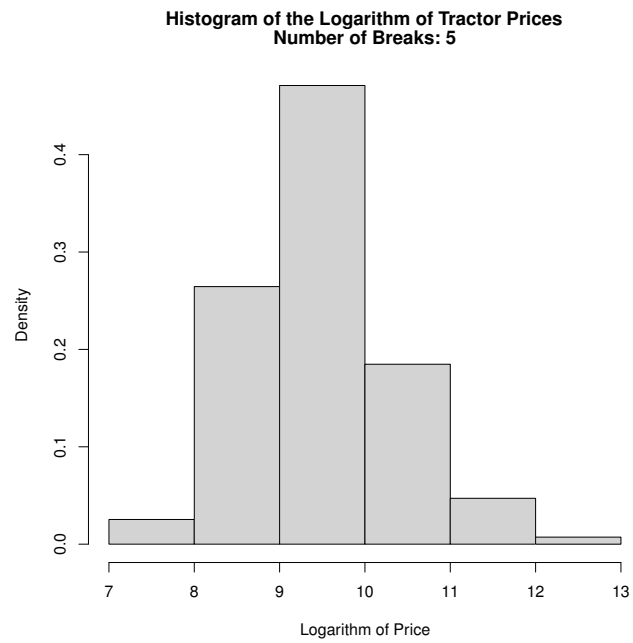


Figure 3: Relative Histogram of the Logarithm of Tractor Prices (Breaks: 5)

```
hist(tractor_sales[, 'log_saleprice'], breaks = 50,  
     main = c('Histogram of the Logarithm of Tractor Prices',  
              'Number of Breaks: 5'),  
     xlab = 'Logarithm of Price',  
     probability = TRUE)
```

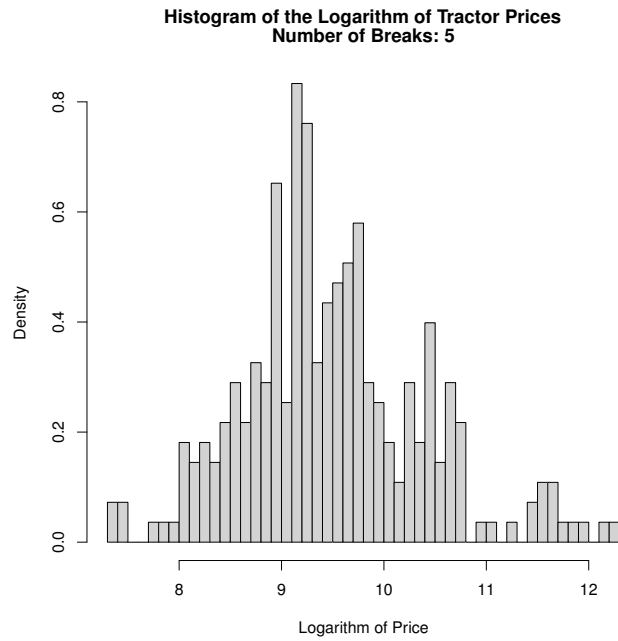


Figure 4: Relative Histogram of the Logarithm of Tractor Prices (Breaks: 50)

In the limit, the bars can be very small to the point that each bar is a pixel wide: approximating a continuous function. To smooth it out, the nonparametric technique of kernel smoothing with produce a continuous function.

0.3 Probability Density Function of Tractor Prices

Kernel-density smoothing is an example of a nonparametric method, that is, a model without parameters, such as the slope coefficients β in a regression model. You may have used nonparametric methods to plot a density. In fact, we have just used a rudimentary form of nonparametric method when we plotted the histograms above.

Figure 5 depicts the kernel-smoothed probability density function of the natural logarithm of price.

```
price_density <- density(tractor_sales[, 'saleprice'])  
plot(price_density,  
      main = 'Kernel-Smoothed Density of Tractor Prices',  
      xlab = 'Price')
```

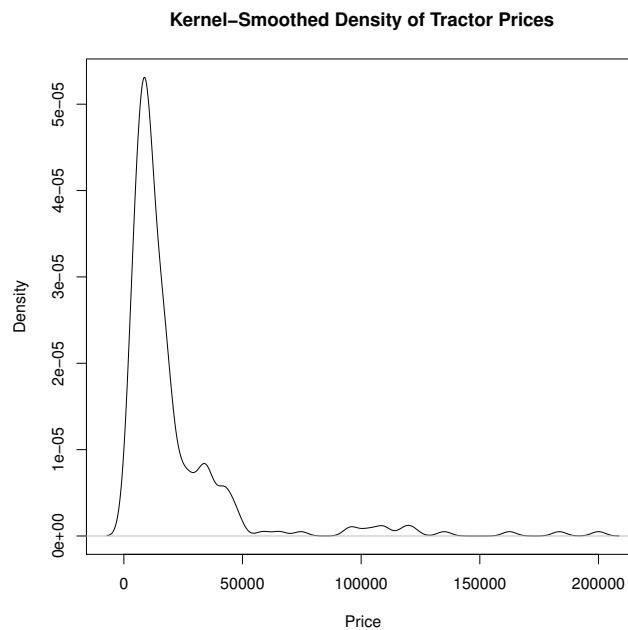


Figure 5: Probability Density Function of Tractor Prices

In the default, the bandwidth is chosen using an algorithm. See the help for `density`.

```
> attributes(price_density)
$names
[1] "x"          "y"          "bw"          "n"
[5] "call"       "data.name"  "has.na"

$class
[1] "density"

> price_density$bw
[1] 2875.455
>
```

The default algorithm for this variable sets the bandwidth to \$2,875. You can choose the bandwidth as a tuning parameter. Try a larger value as in the following code block.

```
price_density <- density(tractor_sales[, 'saleprice'],
                          bw = 10000)
plot(price_density,
     main = c('Kernel-Smoothed Density of Tractor Prices',
              'Bandwidth: 10,000'),
     xlab = 'Price')
```

Figure 6 depicts the kernel-smoothed probability density function with a bandwidth of 10,000.

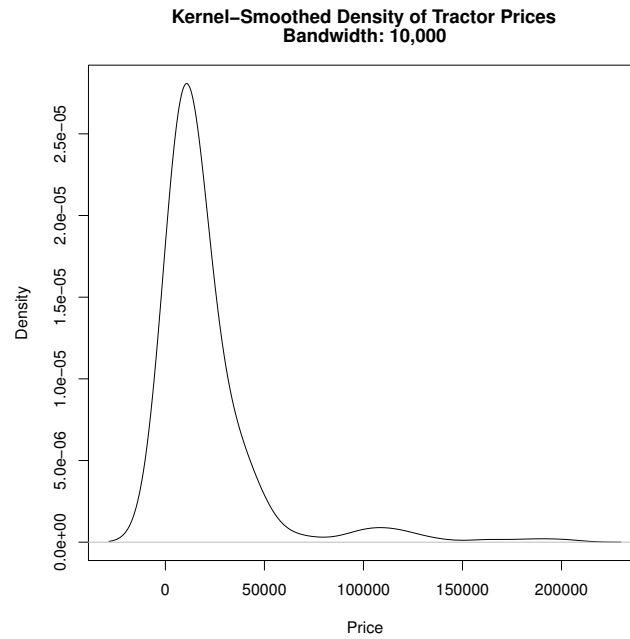


Figure 6: Probability Density Function of Tractor Prices (Bandwidth: 10,000)

A bigger bandwidth gives you a smooth density, but might smooth over the details. A smaller bandwidth might make the density too noisy.

```
price_density <- density(tractor_sales[, 'saleprice'],
                          bw = 1000)
plot(price_density,
     main = c('Kernel-Smoothed Density of Tractor Prices',
              'Bandwidth: 1,000'),
     xlab = 'Price')
```

In Figure 7, we see many jagged changes that are more closely related with the particular values observed than with the population density.

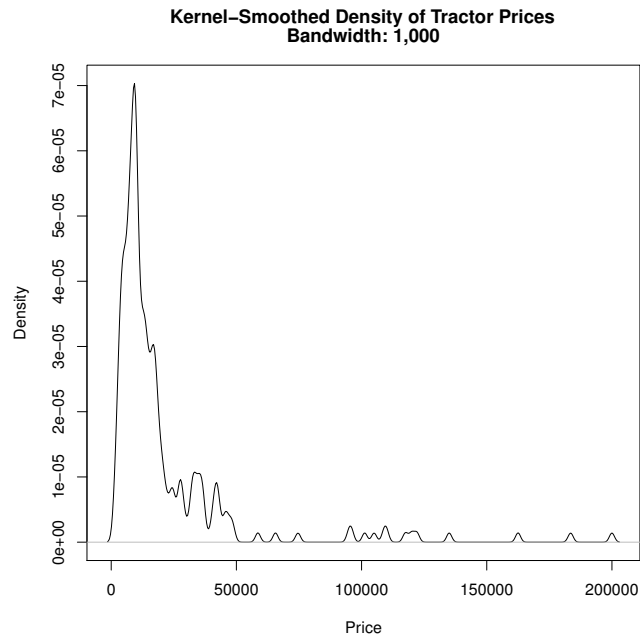


Figure 7: Probability Density Function of Tractor Prices (Bandwidth: 10,00)

We can do something similar to predict one variable with the others. Before that, we will transform the dependent variable, after analyzing it in greater detail in future problem sets. For now, we can plot the logarithm of the dependent variable, with a bandwidth of 0.20, which is appropriate for the price levels on a log scale..

```
log_price_density <- density(tractor_sales[, 'log_saleprice'],
                             bw = 0.20)
plot(log_price_density,
     main = c('Density of the Logarithm of Tractor Prices',
              'Bandwidth: 0.20'),
     xlab = 'Logarithm of Price')
```

The density plot shown in Figure 8 is much better behaved and is a good starting point to analyze the data in a regression model.

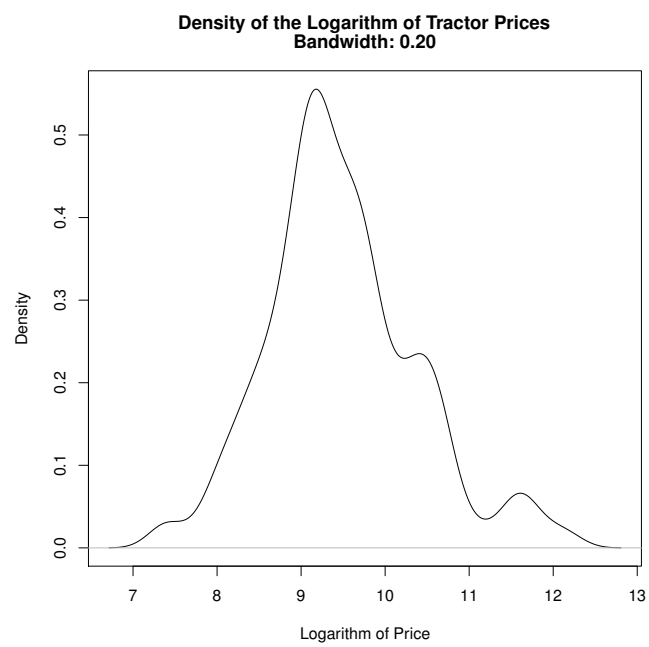


Figure 8: Probability Density Function of the Logarithm of Tractor Prices
(Bandwidth: 0.20)