

Assignment 2

1. Find global minimum point and value for function $f(x,y) = \frac{1}{2}x^2 + 10$

Manual Calculations for 2 iterations:

1. $x = -1, y = 1, \eta = 0.1, \text{epochs} = 2$

2. $\text{iter} = 1$

3. $\frac{\partial f}{\partial x} = 2x = -2, \quad \frac{\partial f}{\partial y} = 2y = 2$

4. $\Delta x = -\eta \frac{\partial f}{\partial x} = -2(-0.1) = 0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

5. $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

6. $\text{iter} = \text{iter} + 1 = 2$

7. if ($\text{iter} > \text{epochs}$)

goto step 8

else

goto step 3

3. $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

4. $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6) = 0.16$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

5. $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

6. $\text{iter} = 2 + 1 = 3$

7. if ($\text{iter} > \text{epochs}$)

$$3 > 2$$

goto step 8

else

goto step 3

8. $x = -0.64, y = 0.64$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10 = 10.8$$