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EcoN 2048 W13 Final Exam Answer Key 1. a b A 5.5 0.4
<u>4.</u> a b
A 5,5 0,4 7
8 4,0 1,1
The pure NE is (A, a) which yields (5.5) and (B, b) which yields (1,1).
And the mixed NE is (\$A+\$B, \$a+\$b) which yields (\$\frac{1}{2},\frac{1}{2}).
In real life, since it is just a 2x2 one-shot game, I'd say (A, a) is most
likely to be played by human players. This is because Oit is more likely that people consider
pure strategy rather than mixed strategy in such a small game; @ since the game is played once
and the pay off is easy to calculate, the probability of a trumble - hand is very very small.
is Denote & as the proportition of the population that plays a, then for a now player
he has $u(A) = 59 + 0 \cdot (1 - 8) = 58$ $3 = 40 \cdot (1 - 8) = 38 + 1$ $(4) - u(B) = 28 - 1 = 0 \text{ if } 8 = \frac{1}{2}$
So the EF is (A, a) and (B, b)
And the basin of attraction of (B, b)
1 8 15 {8; 058 < \frac{1}{2}},
and the basin of attraction of (A, a)
is { 8: \frac{1}{2}.
7 77 QX 1
(c) The EE's the two pure NE in part (a). The mixed NE is not a EE in
part (b) because it is unstable. A &= \frac{1}{2} + \xi , for any \xi close to 0, would
lead the whole population to either (A, a) or (B, b) though start from (1A+1B, 1a+1b)
So my guess of human players' choice is quite consistent with the result, if we get that the prior belief is at least slightly above \$. 2 = 1/2.
And it is reasonable to believe so since (A, a) generates (5,5) which is higher
than (1,1), the result of (B,b). However, of for some reason that the prior is
slightly below 2 = 2, then the population would eventually choose (B, b)
But I think it is more reasonable to have a prior above &= 3-
#3/18

a) For II, a is dominated by b. Then II will always play b.

I knows this, and does better by playing B.

=> (B,b) is the pure NE by IDDS / indeed, (OS)

Because It's Etrategy is, dominant, a human player would probably play, especially in a one-shot game. I would figure this out and play B. Perhaps (A, a) is possible with more periods, but not in the one-shot game.

The neverse argument is the as well, as B is dominant for I is so DS)

b) , 5 o one population

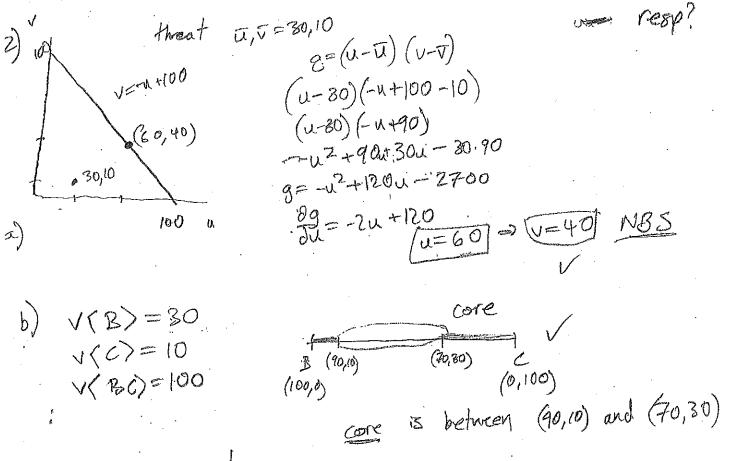
5p + O(1-p) = 5p6p+0(1-p) = 6p+1-p= Sp+1

To me, this implies everyone plays B. Say we had 5.1 instead of 5

3.1p = 5p.+1 1p-1 p-1.02 < 1 = 1Then there is an anotable equ. at 198 => 5.1p=5p+1 But in our question, the slope is flato

c) These are consistent, B is a dominant strategy for bothi iplayers, and as such each has incentive to cheat if the and an indefinite gun indefinite gun of the players, this can be remedied, but there is no indication that this is the

case in prolutionary game in part (b).

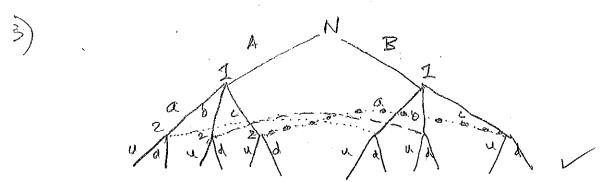


BC 30 70 CB 90 10 0 $\phi(v)$ 120/2 80/2

Ø(v)= 60,40 => some as NBS /

[#3 continued]

- Partial pooling is not possible with only two Norstates
 Hybrid is a mixed messaging shrutegy, which may be possible
 here, although I am not sure.
- d) This is a signalling game. Nature moves, then the informed player, then the uninformed player.



- a) we also need a common belief about the probabilities of Nuture more t.
- b) Because of the info sets, we con't really break apart any subgames. For PBE, ne need is to be the posterior given a common prior (not defined here) and each player's strategy profile. "We also need each component of the profiles to be a BR given M. For PBE, this needs to hold in every subgame.

Then we would have [m*, k*, ii] s.T.

- 1) m' Eargmax u (m, x";t) yt => P] sonds the message that maks utility given P2's BK to that minght what does that hum
- 2) X" E argmax Z. M. U(X, m,t) = mich action that max expected utility.
- 3) u is consistent with Boyes rule given nature more and mr etc.
- c) For separating m*(A) 7 m*(B) = PI has a different optimal message in each state of nature -=> Up also need that sending a fake message is too costly

For pooling mx(A)=mx(B)

no matter the state of => PI sends the same message nature & that is BR.



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Wei Xu

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4.(a) In the basic Bertrand model, the NE is pi= Ps = Ps = Mc = 2,
and the corresponding pay offs is $\pi_1 = \pi_2 = \pi_3 = 0$.
167 In the basic Cournot model, we have
4=38-Q=38-8,-8-8=38-6i-6-i
$\Rightarrow firm i \max_{g_i} (p-c) f_i = (38 - f_i - f_i - 2) f_i$
Best response of firm i is $6i - \frac{36 - 6 - i}{2}$
Since this a symmetric game, we have &, = &= &s = &
$\frac{1}{2} = \frac{3b-2b}{2} \Rightarrow b = 3$
$\exists T_i = (p-c) = (38-32-2) = 8/ \forall i=1,2,3$
So the NE is $8 = 8 = 8 = 9$, and $T_1 = T_2 = T_3 = 81$ is the corresponding
payoffs.
co) If the incumbent is the monopolist, then it seeks to
max (p-c) = (36-8) &
$\Rightarrow 9^{+} = 18, \ 7^{+} = (7^{+} - c) 8^{+} = (36 - 8^{+}) 8^{-} = 324. \ \checkmark$
So if it is going to play Bertrand as in part (a), then the incumbent is
willing to pay up to 324 to prevent entry;
if it is going to play Cournot as in part (b), then the incumbent is
willing to pay up to 324-81=243 to prevent entry.
(d) If post-entry competition is Bertrand, then the profits to each firm will be drawn down to zero if more than one firmenter, so only ONE firm
will enter in the SPNE. If post-entry competition is Cournot, then the profits to each firm is
(p-mc) ^a 36 ^a = 1296 when J firms enter. So in the SPNE (J+1) ^a = (J+1) ^a (J+1) ^a
(J+1) = (J+1) 2 (J+1) 2
only $J^* = [\sqrt{\frac{1296}{k}} - 1] = [7.2 - 1] = [6.2] = 6$ firms will enter



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Wel Xu

5(a)
The consumer's reservation price is $r(0) = 0 + \frac{1}{2} \cdot \frac{1}{2} = \frac{5}{4}0$.
<u> </u>
At price P, only the consumers whose reservation prices are above the price
would like to purchase So the range of Ois
\[\[\frac{4}{5}p, 1207 \frac{4}{5}0\frac{5}{5}0 \]
$\frac{1}{\sqrt{2}} \Rightarrow \frac{1}{\sqrt{2}} \Rightarrow 1$
(C) In the compositive equil. firms are making zero profits, therefore me must have
$E(0 0 \ge \frac{4}{5}p) = \frac{1}{5}(\frac{4}{5}p + 120) = p \Rightarrow p^* = 100. \sqrt{2}$
And the gain are
And the gains are $ \int_{\frac{4}{7}}^{120} f(\theta) - p^{2} d\theta = \int_{80}^{120} \frac{1}{4}\theta - 100 d\theta = \frac{5}{8}\theta^{2} - 100\theta \Big _{80}^{120} $
= 1000. (in \$ thousands per year)
(d) Absent information constraints, then the consumer whose expected loss is O
should buy the insurance at price p=0, so the gains is
$\int_{0}^{120} r(0) - 0 d0 = \int_{0}^{120} \frac{1}{40} d0 = \frac{1}{80} \int_{0}^{120} = 1800$
(in \$ thousands per year)
(e) Firms could use screening strategies by offering different in surance contracts
with different converges (or deductables) at different prices.
Or firme may require consumers to provide health reports before purchasing
the same and not the a see according to the least the remote there it is the
the incurance and set the prices according to the health reports. Here, the health reports give a signal / information about the un observable O. (though the
message /information is noisy)