# 7. Oligopoly

#### I. Overview

- A. So far we have only looked at two extreme types of markets.
  - 1. Competitive markets have only price-taking firms (presumably lots of them).
  - 2. Monopolist markets have one firm with unilateral pricing power.
- B. We now look at markets with firms that have some pricing power, but not unilateral.

Oligopoly: from Greek, more than one but less than "many."

- C. We use game theory to study behavior in oligopolies.
  - 1. Firm decisions affect one another  $\iff$  strategic interaction.
    - a. Need an equilibrium concept that describes multiple agents trying to optimize.
  - 2. Given the way we construct equilibria in game theory, the strategic variable chosen will matter.
    - a. We solved the monopolist's problem by describing its choice of quantities.
    - b. We could have just as easily (and with the same result) had the monopolist choose a price.
    - c. This symmetry disappears in our study of oligopoly.

#### II. (Normal Form) Game theory

- A. A normal form (simultaneous play) game (NFG) is defined by three elements
  - 1. A list of N players
  - 2. A set of strategies for each player,  $s_i \in S_i$ . E.g.,  $S_i = \{s_{i1}, s_{i2}, ..., s_{ik}\}$ .
  - 3. A payoff function for each player,  $\pi_i(\mathbf{s})$ , where the profile of all players' strategies is  $\mathbf{s} = (s_i, \mathbf{s_{-i}})$ .
- B. Let  $\mathbf{s_{-i}}$  be a vector of strategies of all players other than i. The **best response** function (or correspondence) is  $BR_i(\mathbf{s_{-i}}) = argmax_{s_i \in S_i} \pi_i(s_i, \mathbf{s_{-i}})$ . In words, for a given profile  $\mathbf{s_{-i}}$  of other players' strategies, player i's best response is the strategy (or subset of strategies) that maximizes his payoff.
- C. A Nash equilibrium is a strategy profile  $s^*$  in which every player is making a best response to the other players' strategies, i.e.,

$$s_i^* \in BR_i(\mathbf{s_{-i}^*}), \quad i = 1, ..., n.$$
 (1)

D. These definitions are quite general and apply in politics, biology, business, etc. etc. Here we will apply them to oligopoly.

# III. Quantity Setting: Cournot Markets

## A. The Duopoly NFG

- 1. N=2 players, called firms.
- 2. Strategy is the output quantity  $y_i \in [0, \infty) = S_i$ .
- 3. The choices  $y_1, y_2$  are made at the same time.
- 4. We'll keep things simple in computing the payoff functions (profit functions). Set  $Y = \sum_{i=1}^{N} y_i$  to be total output, and assume a linear inverse demand curve

$$p = a - bY$$

- 5. We'll also assume a linear cost curve, i.e., identical marginal cost c for all firms and zero fixed cost.
- 6. Then the profit to any firm i is:

$$\pi_i = y_i(a - bY) - y_i c = (a - c - bY)y_i$$

7. The most important part of this is that the aggregate output quantity choices of other firms  $Y_{-i} = Y - y_i$  affects firm i's profits and therefore his optimal choice.

#### B. Best Response Function

- 1. A best response function  $BR_i$  describes firm i's best choice of quantity  $y_i$  as a function of the quantity choices of everyone else.
  - a. Note this doesn't imply that firms actually *know* the quantity choice of others.
  - b. Action is simultaneous.
- 2. We will see that in this quantity setting game,  $\frac{\partial BR_i}{\partial y_j} < 0$ 
  - a. If you know your rival's output is high, you want your output to be low.
  - b. Quantity is a *strategic substitute*.

Ex: Getting the BR from the FOCs with 2 firms.

### C. Nash Equilibrium

- 1. A Nash equilibrium is a profile of strategies at which no player has an incentive to change their behavior given what others are doing.
- 2. Or, all firms are simultaneously playing their best response.

Em: Nash equilibrium in duopoly.

## D. Asymptotics

- 1. Can we describe the equilibrium behavior of Cournot firms in terms of the number of firms (N)?
  - a. By doing this we can look at the relationship between oligopolies and both monopolies and competition.
- 2. Denoting  $s_i$  as  $\frac{y_i}{Y}$  we can derive the following condition no matter what demand and cost looks like:

$$p(y)(1+\frac{s_i}{\epsilon}) = c_i'(y_i)$$

3. If there is a constant marginal cost shared by all firms, then

$$p(Y)[1+\frac{1}{N\epsilon}]$$

- 4. The main result is a price somewhere between competition and monopoly:
  - a. If N=1 this price is just the monopoly price.
  - b. As N approaches infinity, price converges to the competitive level.
  - c. With N in between price remains above marginal cost, but below the monopoly level.

Ex: Cournot's Theorem with linear demand.

- E. Problems with Cournot Analysis
  - 1. We usually think of firms setting price not quantity.
  - 2. Where do prices come from in Cournot markets?
    - a. We know prices come from the inverse demand curve.
    - b. We don't know what strategic forces generate prices in Cournot markets!

# IV. Price Setting: Bertrand Markets

- A. Describing a Duopoly
  - 1. Two firms simultaneous choose a price to sell unit at with a given demand curve D(p).
  - 2. We'll assume firms face constant marginal costs  $c_i$ .
  - 3. Consumers will obviously buy from the lower priced firm.

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- 4. Firm i's demand is given by
  - a.  $D(p_i)$  if  $p_i < p_j$
  - b.  $D(p_i)/2$  if  $p_i = p_j$
  - c. 0 if  $p_i > p_j$
- B. Best Response

- 1. Note now that the strategic variables  $-p_i$  are strategic complements.
- 2. The lower a rival's price, the lower you'd like your price to be.

#### C. Nash Equilibrium

- 1. A Nash Equilibrium in the Bertrand game is a set of prices at which no firm has an incentive to change his or her price.
- 2. Assume, without loss of generality, that  $c_j > c_i$ .
- 3. Then in a Nash equilibrium:
  - a.  $p_i = c_j$
  - b.  $p_j \geq c_j$
- 4. The price in the market is competitive it is equal to marginal cost.
  - a. This is especially striking if we assume (as we often do) that firms share a common marginal cost.
  - b. If  $c_i = c_j = c$  then we have  $p_i = c$ .
- 5. In the price setting game, then, the prediction is that the competitive outcome obtains even with only 2 firms.
- 6. This sort of equilibrium still emerges with a number of firms.

#### D. The Bertrand Paradox

- 1. Some call the result the "Bertrand paradox."
- 2. Intuition tells us that, say, five firms should compete much more fiercely than two firms.
  - a. Indeed there is experimental evidence to this effect.
- 3. One way of reclaiming supercompetitive behavior in pricing games with few firms is to feature repeated games.
- 4. Another is to have firms selling slightly different products.
- V. (Extensive Form) Game Theory
- VI. Quantity Setting With A Leader: Stackelberg Markets
- VII. Price Setting With Differentiated Products: Hotelling Markets