Final Exam

- terminology, there are two states of Nature -- (Dog knows Thief, Dog doesn't know In A.C. Doyle's famous story "Silver Blaze," detective Sherlock Holmes solves the case by pointing out that the guard dog didn't bark at the horse thief. In 204b Thief? --, and two possible actions by the Dog -- {Bark, Don't Bark}
 - VERY briefly, define the 204b terms: adverse selection, signaling and smanning
- advorse selection is the (unfortunate) event

Which is a consumant by-product of an asymetri

game where the uninformed player would like a particular result (song hard worker or low-risk client) but but because of uninformedress, gots the low-type of ninh-risk client instant.

a way for an informed player Signaling

in all asymetric game to let an uninformed

player knows his type for the purpose of differentiation from other types.

player in an asym game to differentiate Screening is a way for an uninformed

types of the informed plauser

"curious instance" of the dog not barking? In your answer, please refer to pooling versus separating equilibrium, even if you can't relate either of them to the non-Can any of these terms help explain the inference Sherlock made from the barking dog. (8 pts)

you. In this case we can use the idea

of signating where the dog is the informed &

Sherlack is Unintermed Athle would

pooling equilibrium Idag backs at everyone or no and shortock obtermished, howeven

1/10 Seponative equilibrium in which Jas a

"Barreyon" dog signalled a person was a thick he know.

by not Borking" and would haine 414201

4 and emand ite ponses	SOING FOOT 9x = 13-3-398	98 = 12.5 - 298 98 = 12.5 - 2(13 - 298) = 12.5 - 6.5 + 298	=> 396 - 6 => 198 - 8 L	X=9-4	Then 18=56-2(9)-2(8)=56-19-16	50 TA = (22-4)(9) $= 18*9$ $= 162 V$	$11_{R} = (22-6)(8)$ $= 6.8 $ $= 8.08 $	ASSUMBING NO FIXED COSTS ! U.
2. Two firms, Ace and Best, produce brisquets at respective marginal costs $c_A = 4$ and $c_B = 6$. Consumers treat the two brands of brisquets as perfect substitutes. a. Suppose that the two firms independently choose output and that inverse demand is $p = 56 - 2Q$, where $Q = q_A + q_B$ is the total output for the two firms. Write down the payoff (i.e., profit) functions for the two firms, find their best responses and the Nash equilibrium outputs and profits. Be sure to mention any other assumptions required to obtain your answer. (10pts)	(h) choose 9 4, 9 6 (covernot) P = 56-29,-29B	$\Box A = (P-C)g_A = (56-29A-29B-CA)g_A$ FOC WIT g_A : $56+4g_A-2g_B-C_A=0$	= 742A = 56 - 328 - CA $= 56 - 228 - CA$ $= 56 - 228 - CA$	IIB = (P-CB) & = (56-298-29x-CB) 9B	FOC witgs: 56-998-292-CB=0	-V & 56 - 294 - CB = 50 - 294	30 (BRa(9B) = 13- = 9B BRB(9A) = 12.5- = 9A	

firm gains the entire market. Assume that this firm sells a quantity consistent with Now suppose that the two firms independently choose price, and the lowest price the inverse demand function above. Again find the payoff functions for the two firms, and find their best responses and the Nash equilibrium prices and profits. ച

Be sure to mention any other assumptions required to obtain your answer. (8pts) (Bertrand) ب ح Q. C/0,00% (5)

PA < PB PA = PB PA > PB	Pa < Pr
2(02-CA) (56-8) 2(02-CA) (56-20)	(PB-CB) (56-PB)
TA=	118=

focs (of discordingous), but we each player can't be each olayariwill try to play ROY The Best res Portse Know that ROUND From

(80 - 88) H

118

This conting Haring E TO Carlothravily small). In this way gain the whole market of if ladow mounding on the , -, i, 21.79 MOULA

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Best Will not CR # CB, 5,nce In this case (necause Te = 0 is TO 20) SINCE "ACE'S" MC=456, PB=62CB produce below preferable to to price Pa<6 offwos in ->

ne is willing

whole market whiest l equilibrium, we have that Q NO : 2 ń Profits 26-6 4 10 = ¥ 0 П +420S 56-Pa MONG 11 11 H \bigcirc And

which sort of industries is the game in part a more descriptive than the game 4) xed aposts 0 a SSUMING

rt b? Explain very briefly. (2pts)

1 goess this would be a better model if a company like may be capacity concerns (constraints 78.0

तिंकि गृत् ग्राप्त may not be able to produce that grown it's r harso VOU CRN A Factory Whome

- ئع profitability is $u_2 = 0.5(1.5 - s_2) = 0.5(s_1 + 0.5)$ when fraction $s_2 = 1 - s_1$ of the output An industry consists of a large population of firms, each of which must choose one of when rare and increasing returns when common; its profitability can be expressed as $u_1 = 2s_1^2 - 2s_1 + 1$, where s_1 is the fraction of industry output produced using that two alternative technologies. The first technology has decreasing returns to scale technology. Technology 2 has moderately decreasing returns at all scales; its is produced using it.
 - Write down the payoff difference $D = u_1 u_2$ as a function of s_1 , and graph this function. (6pts)

Two technologies

 $\{ tech 1 \quad M_1 = 25,^2 - 25, +1 \}$ $\{ tech 2 \quad \{ M_2 = 0.5, \{ S_1 + 0.5 \} \}$ $\{ tech 2 \quad \{ M_2 = 0.5, \{ S_1 + 0.5 \} \}$

is produced Using it

 $0 = U_1 - U_2$ $= 25^2 - 25 + 1 - \left[\frac{2}{2}(5_1 + \frac{1}{2})\right]$ $= 25^2 - 25 + 1 - \frac{1}{2}(5_1 + \frac{1}{2})$

D= 252-2,58, + 0,75

0.75

95, -2,5:0 5, = 2 = 0.675 = 0.035 = 0.035 = -0.03125 \

- . Does this game have any pure strategy NE? I.e., is $s_1 = 0$ or 1 a NE? Please verify your answer. (4pts)
- Size, then Diol = 0.75 >0, means people tend to whose Si, so hot a NE Si=1, than Dill= orty >0. we are people wouth deviate to Sz

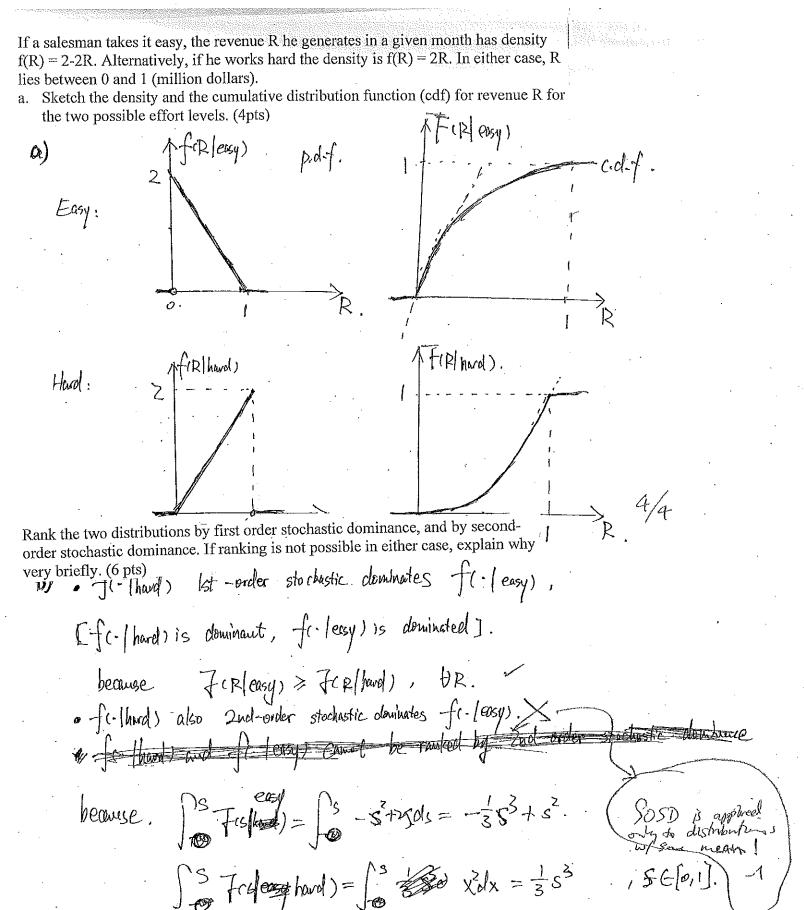
Thus, SI=1 is a pure NE.

- Suppose that sign preserving dynamics describe the evolution of technology adoption in the industry. Find the evolutionary equilibria and their basins of attraction, using the graph from part a. (6pts)
- arracuon, usung ure grapu moun recent. Predict the long-run shares of d. Suppose that the second technology is more recent. Predict the long-run shares of the two technologies. (Zpts)

A Participation of Manager And Manager A

Diagram shows that \$1 % 4 separates boxins of attaction for stall and small to EED

If 2000 tech is none recent, then thirtied stade is 5,=1.50 evolutionen (Sepripreserving) dynamics never leave its back \$ 5,= (in the LR.



Interval [0:1], $\int_{0}^{S} \overline{f(s|easy)} - \overline{f(s|had)} ds = -\frac{z}{3}s^{3} + s^{2} = s^{2}(1-\frac{2}{3}s) \geqslant 0.$ (w, o) U(1, +00), -7(-1easy)=7(-1hurd)

c. If the salesman has Bernoulli function
$$v(x) = 2x^{0.5}$$
 and is paid a 25% commission (i.e., $x = R/4$), then what is his certainty-equivalent for the payment received when working hard? For taking it easy? (6 pts)

$$E[uP] = \int_{0}^{1} f(P) easy) uP dR = \int_{0}^{1} (2-2P) \cdot J_{R} dR = 2 \cdot \left(\frac{2}{3}R^{32} - \frac{1}{5}R^{\frac{1}{2}}\right) \int_{0}^{1} = \frac{8}{15}$$

- 5. The salesman's boss just hired you advise on incentive pay. You believe that the salesman in problem 4 has utility cost g=0 for taking it easy, has utility cost g=0.5 for working hard, and could obtain utility 1.0 if he quit.
 - What is the salesman's optimal effort choice under the current 25% commission plan? Show your work. (4pts)

15 e observable?
15 principal/boss risk neutral?
c. What does the standard formula (involving unknown parameters γ and μ) tell you about how to revise the payment schedule to motivate the salesman to work hard?
formula: $w'(\omega(n)) = f(n e)$ $e^* \in [e_i, e_i]$
Here, Boss wants to motivate hard work so ex=en v'(win) = (v(w)) = (2was) = w
=0 W0.5 = W0.5 V
P(R/R) 2-2R 1 2 R
Let's assume R & (0,1) S.t. we don't have a
Problem
then 1-F(RIE) = 1-R+1 =2-1/R
$= b w^{0.5} = 8 + \mu [2 - 1/R]$
 d. What are some important caveats to mention to the boss about actually using the formula in c.? (2 pts) e. For extra credit, time permitting, compute γ and μ and thus the specific payment
e. For extra credit, time permitting, compute γ and μ and thus the specific payment schedule for the salesman in part c. (1) IN actuality, we may not know things.
like v(x), f(Tilen), etc. Even it
we did, there could be a regative effect of
Maybe the sales man will find a schedule distasteful &
Maybe the sales man will find a schedule distasteful 4
smight even demand higher compensation if he's forced

b. What else (if anything) do you need to know about the salesman or the boss to apply techniques learned in Econ 204b? Be explicit. (4 pts)

6. The characteristic function in a 3 player game gives total payoff 1 to the coalitions K={1,2}, {1,3} and {1,2,3}, and total payoff 0 to all other coalitions.
a. Is this game convex? (2pts) (M Changing "1,2,3" to "A,19,C" for my
own ease hope that's okay.
V3A3=V(B)=V(C)=0
V(A,B) = 1 $V(B,C) = 0$
(i) adding B to A in creases benefit by 1
(ii) adding B to (A,C) increases by 0.
It should increase by [more than] one intii),
Not convex.
b. What is the Core of this game? (4pts)
= blocked by (A,B)
= blocked by (A,C)
A (1,0,0) B (0,1,0)
thus the core is the single point (1,0,0) B C c. What is the Shapley Value of this game? (4pts)
ABC 0 1 0
Bhc 1 0 0
CAB 1 0 0
total 9 1 1
n! 6 6 6
P(A,B,C) = (3,1/6,1/6)