

# Optimizing Offshore Wind Farm Design

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Team 9

산업경영공학부 2013170811 이성계  
산업경영공학부 2014170810 김기호

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2-1 modeling analysis

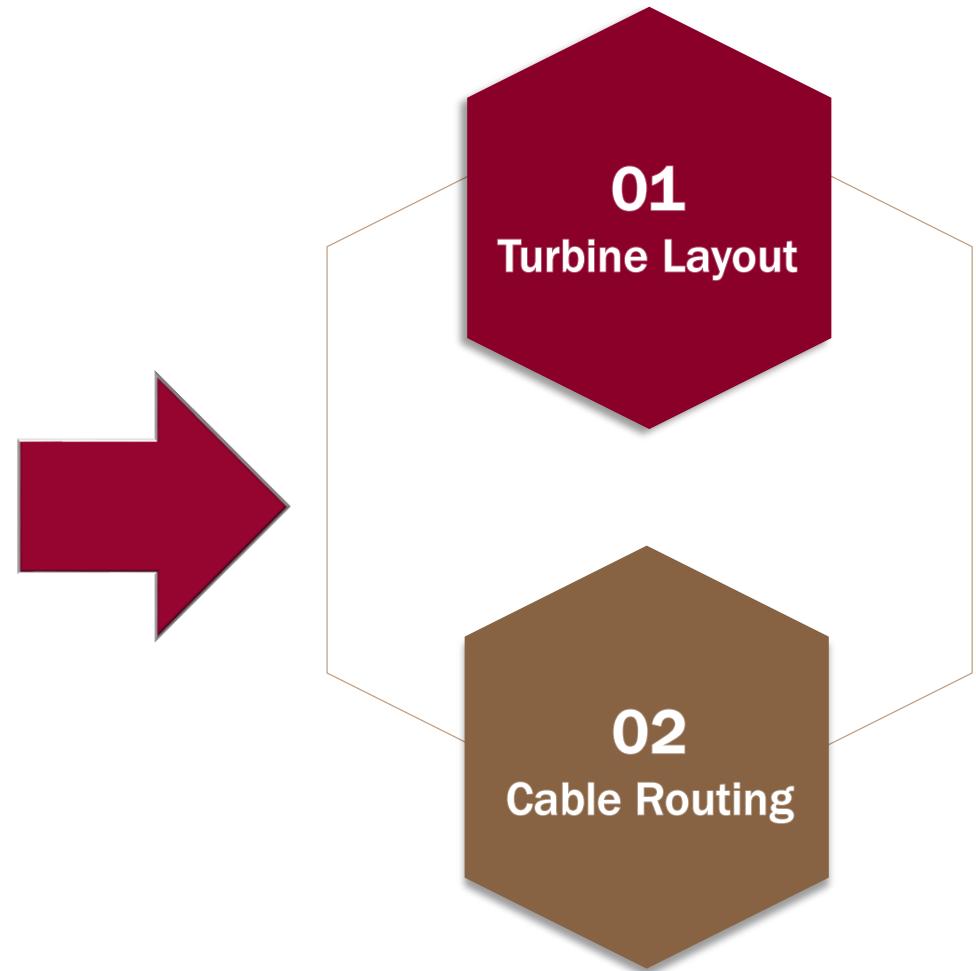
2-2 discussion

## 3 Cable Routing

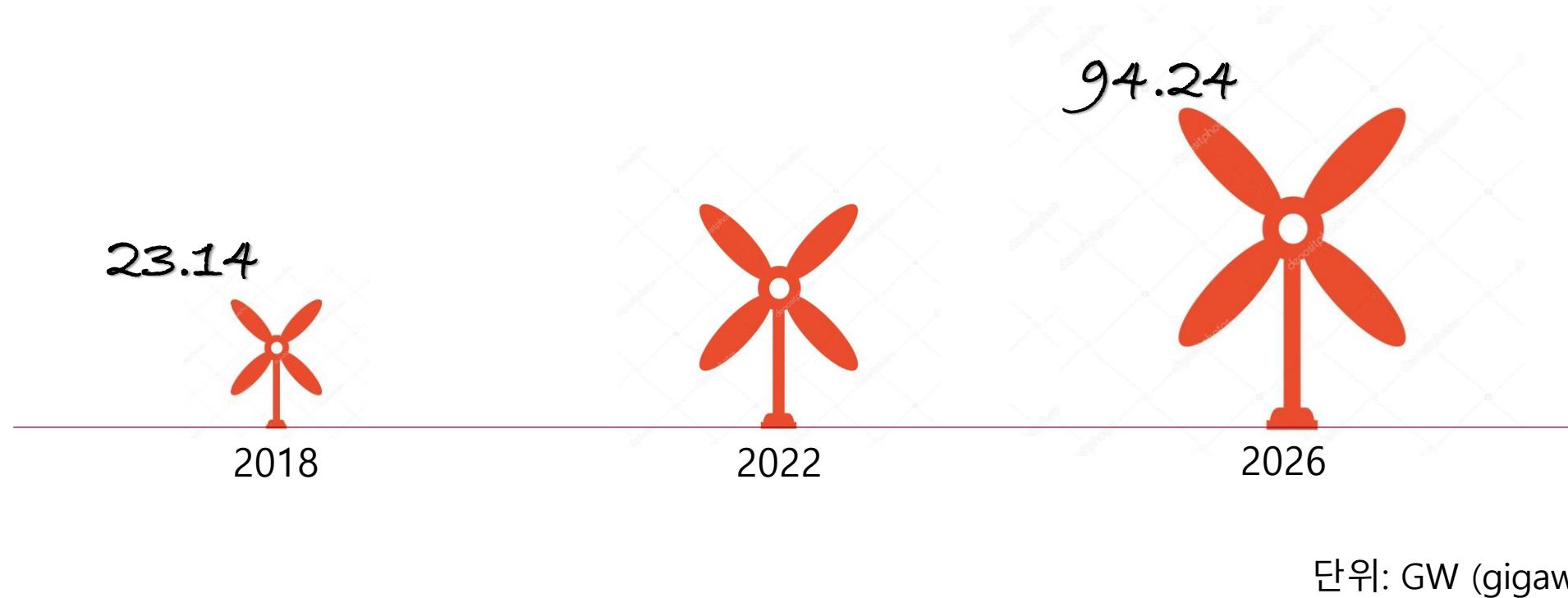
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# 1 About System Offshore Wind Farm Design



# Why to optimize it : Floating Offshore Wind Power Market



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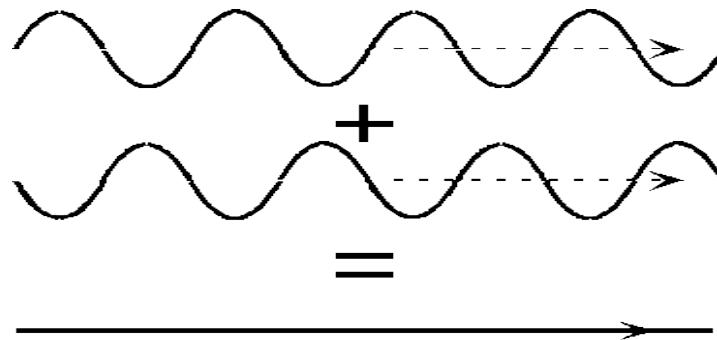
**2** 1) Turbine Layout – modeling analysis

## What to optimize : Turbin Layout

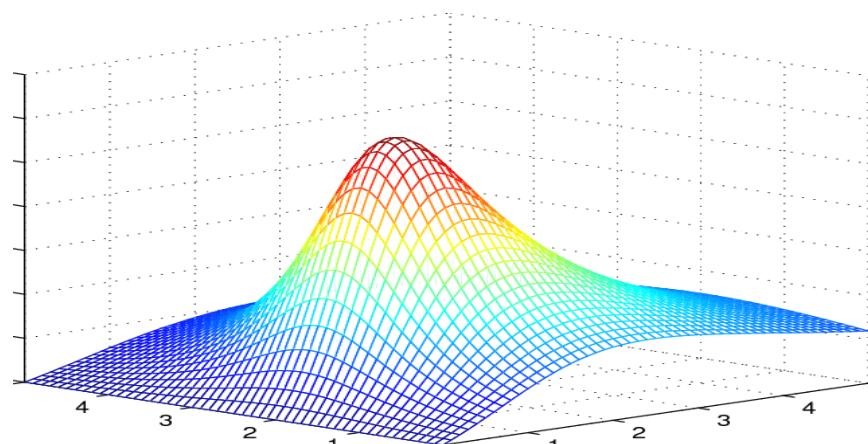


## 2 1) Turbine Layout – modeling analysis Considerations

- ◊ Power loss by interference (Wake Effect)



- ◊ Maximize power



1) Turbine Layout – modeling analysis

## 2 How to optimize real-problem

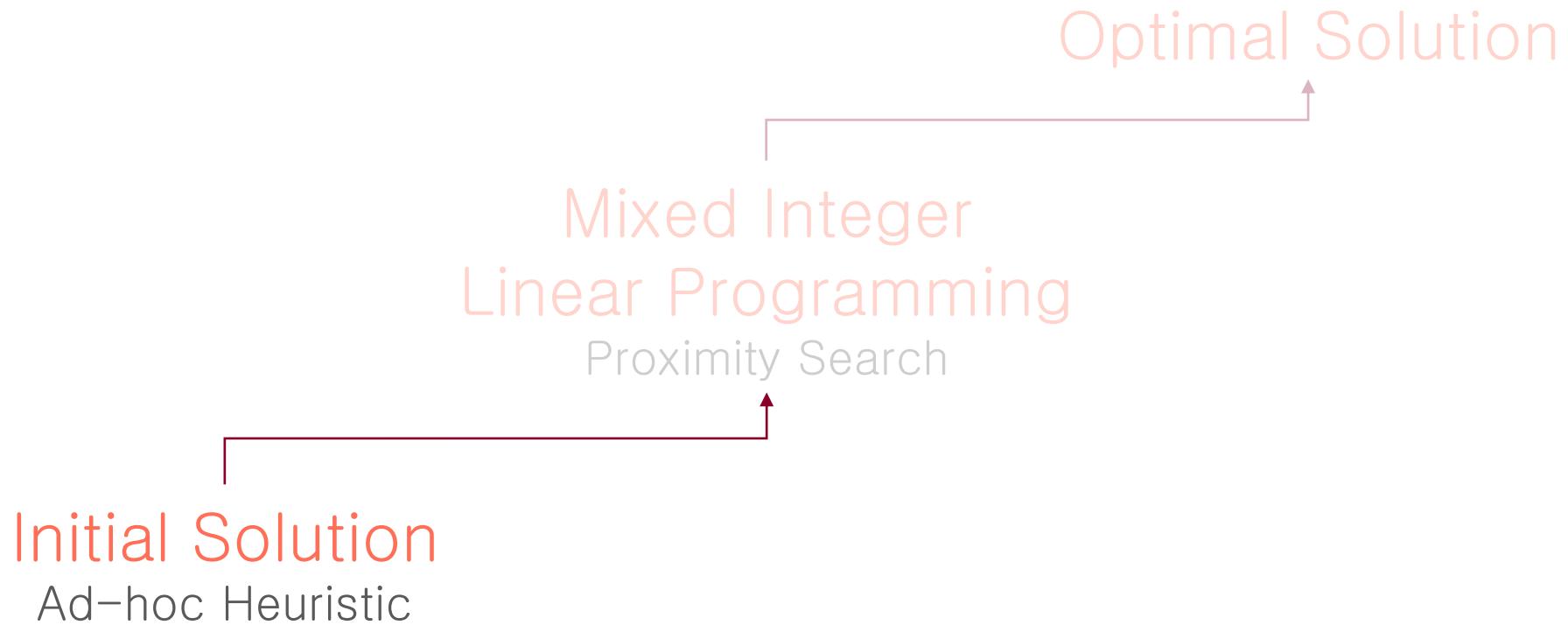
To solve 20,000+ possible positions



**2** 1) Turbine Layout – modeling analysis

## How to optimize real-problem – 1) Ad-hoc Heuristic

To solve 20,000+ possible positions



## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic (iter 0)

1
0

X1	X2	X3	X4	X5	X6	X7	X8

## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic (iter 1, improved)

1
0



# 2 1) Turbine Layout – modeling analysis

## Ad-hoc Heuristic (iter 2 , improved)

1
0

	1	1				1	1
X1	X2	X3	X4	X5	X6	X7	X8

## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic (iter 3 , improved)

1
0



## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic (iter 4, not improved)

1
0



## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic (iter 4, not improved)

Initial Solution!

1
0



## 2 1) Turbine Layout – modeling analysis Ad-hoc Heuristic

Maximize.  $\delta_j + FLIP(j)$

$$\delta_j = \begin{cases} P_j - \sum_{i \in V: x_i=1} (I_{ij} + I_{ji}) & \text{if } x_j = 0; \\ -P_j + \sum_{i \in V: x_i=1} (I_{ij} + I_{ji}) & \text{if } x_j = 1 \end{cases}$$



Profit by flip

$$FLIP(j) = \begin{cases} -HUGE & \text{if } x_j = 0 \text{ and } \gamma \geq n_2 \\ -HUGE & \text{if } x_j = 1 \text{ and } \gamma \leq n_1 \\ +HUGE & \text{if } x_j = 0 \text{ and } \gamma < n_1 \\ +HUGE & \text{if } x_j = 1 \text{ and } \gamma > n_2 \\ 0 & \text{otherwise} \end{cases}$$



Bound Constraints

1) Turbine Layout – modeling analysis

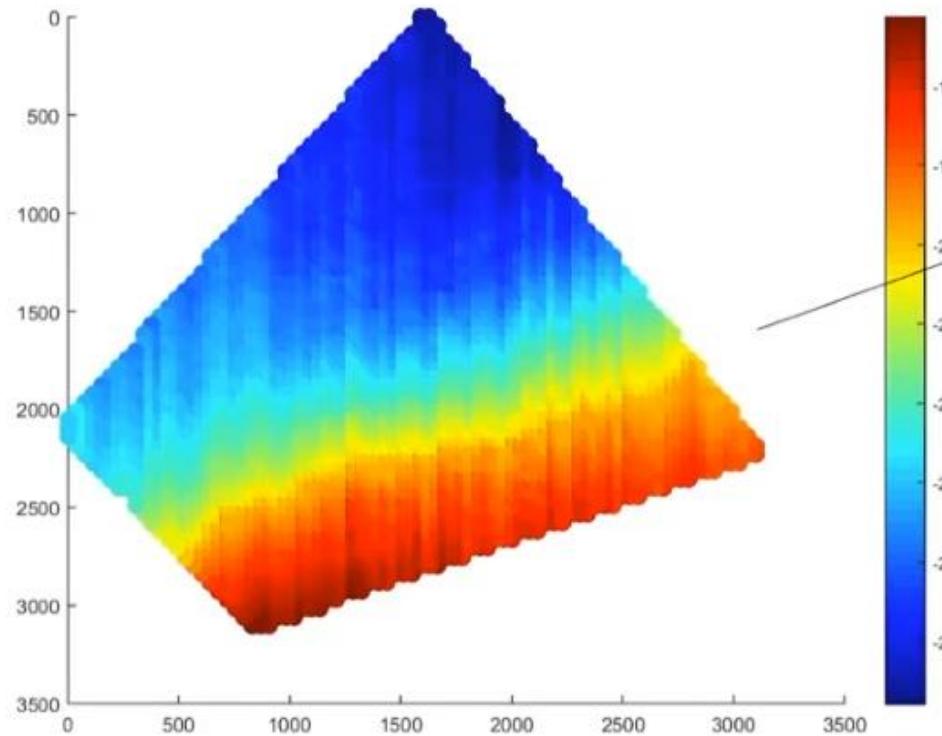
## 2 How to optimize real-problem – 2) Mixed Integer Linear programming

To solve 20,000+ possible positions



## 1) Turbine Layout – modeling analysis

# 2 Mixed Integer Linear programming - Discretization



The layout problem can be formulated as a MIP problem.  
Variables:

$$x_i = \begin{cases} 1 & \text{if a turbine is built at position } i \in V; \\ 0 & \text{otherwise} \end{cases} \quad (i \in V)$$

where  $V$  is the set of potential turbine positions.

## 1) Turbine Layout – modeling analysis

# 2 Mixed Integer Linear programming – Stochastic Programming

$$P_i := \sum_{k=1}^K \pi_k P_i^k \quad \forall i \in V$$

$$I_{ij} := \sum_{k=1}^K \pi_k I_{ij}^k \quad \forall i, j \in V$$

# 2

1) Turbine Layout – modeling analysis

## Mixed Integer Linear programming – Quadratic Assignment

$$\sum_{i \in V} P_i x_i - \sum_{i \in V} \left( \sum_{j \in V} I_{ij} x_j \right) x_i$$

Third-Order

$$w_i := \left( \sum_{j \in V} I_{ij} x_j \right) x_i = \begin{cases} \sum_{j \in V} I_{ij} x_j & \text{if } x_i = 1; \\ 0 & \text{if } x_i = 0. \end{cases}$$

Second-Order

# 2

1) Turbine Layout – modeling analysis

## Mixed Integer Linear programming – Quadratic Assignment

$$\sum_{i \in V} P_i x_i - \sum_{i \in V} \left( \sum_{j \in V} I_{ij} x_j \right) x_i$$

Third-Order

$$w_i := \left( \sum_{j \in V} I_{ij} x_j \right) x_i = \begin{cases} \sum_{j \in V} I_{ij} x_j & \text{if } x_i = 1; \\ 0 & \text{if } x_i = 0. \end{cases}$$

Second-Order

**2**

1) Turbine Layout – modeling analysis

## Mixed Integer Linear programming – Proximity Search

$$\sum_{i \in V} (P_i x_i - w_i) \geq \sum_{i \in V} (P_i \tilde{x}_i - \tilde{w}_i) + \theta$$

➤ Constraints (by  $\theta$ )

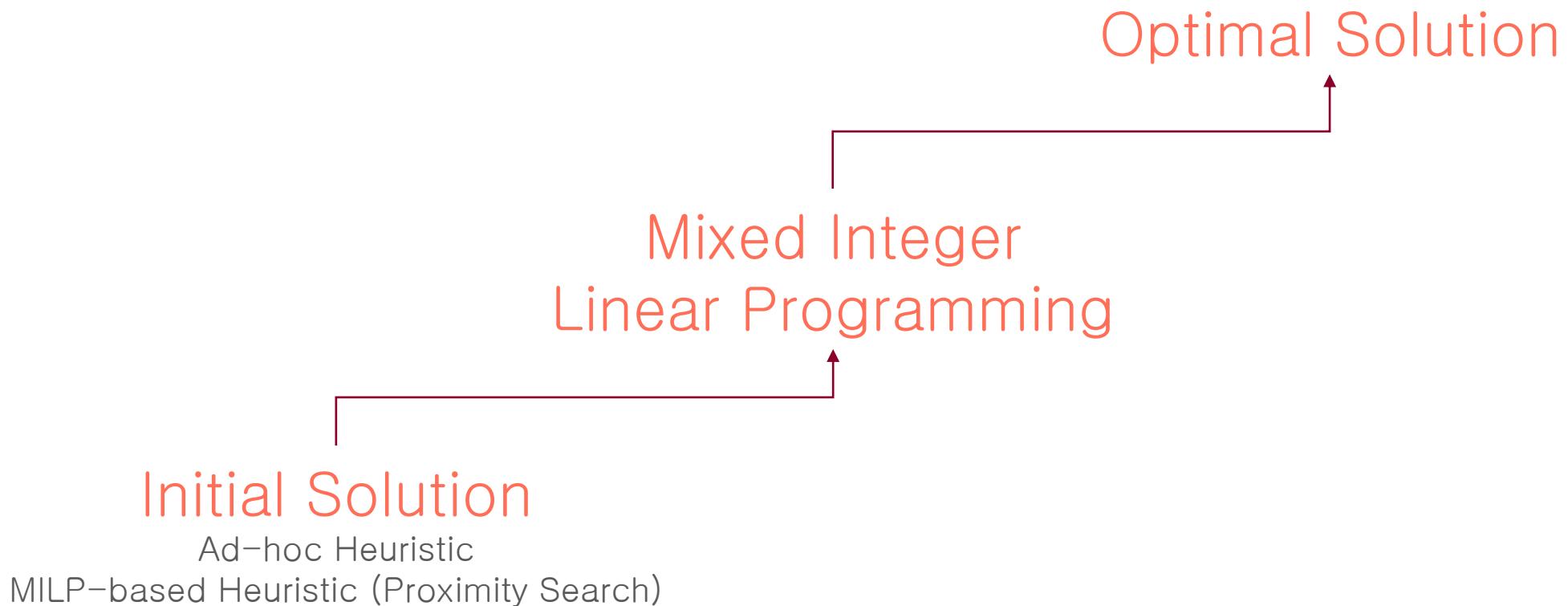
$$\Delta(x, \tilde{x}) = \sum_{j \in V: \tilde{x}_j=0} x_j + \sum_{j \in V: \tilde{x}_j=1} (1 - x_j)$$

➤ Objective Function  
- Minimize Proximity

1) Turbine Layout – modeling analysis

## 2 How to optimize real-problem

To solve 20,000+ possible positions



## 2) Turbine Layout – discussion

### What is different?



VS



1000+ possible positions

~~Wind Variability~~

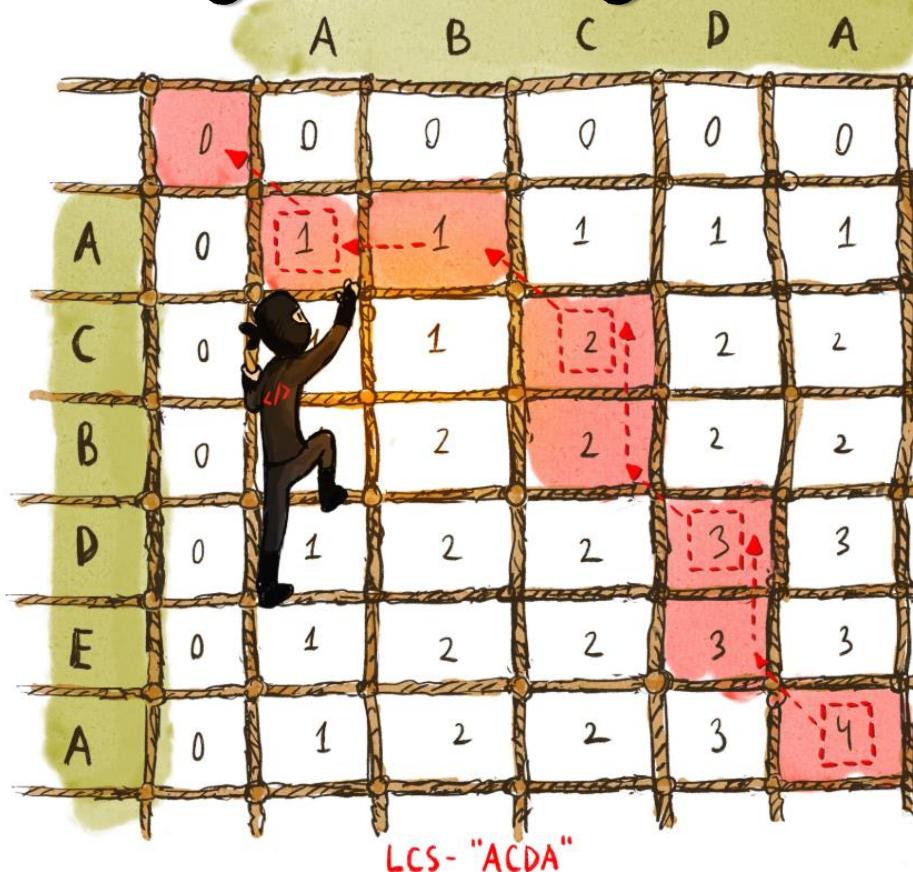
20000+ possible positions

Wind Variability

## 2) Turbine Layout – discussion

### Criticism : So many heuristic

# Dynamic Programming



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# 3

1) Cable Routing – modeling analysis

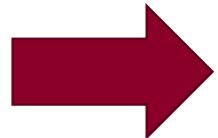
## What to optimize? – set and decision variables

$V$ : 전체 node의 집합

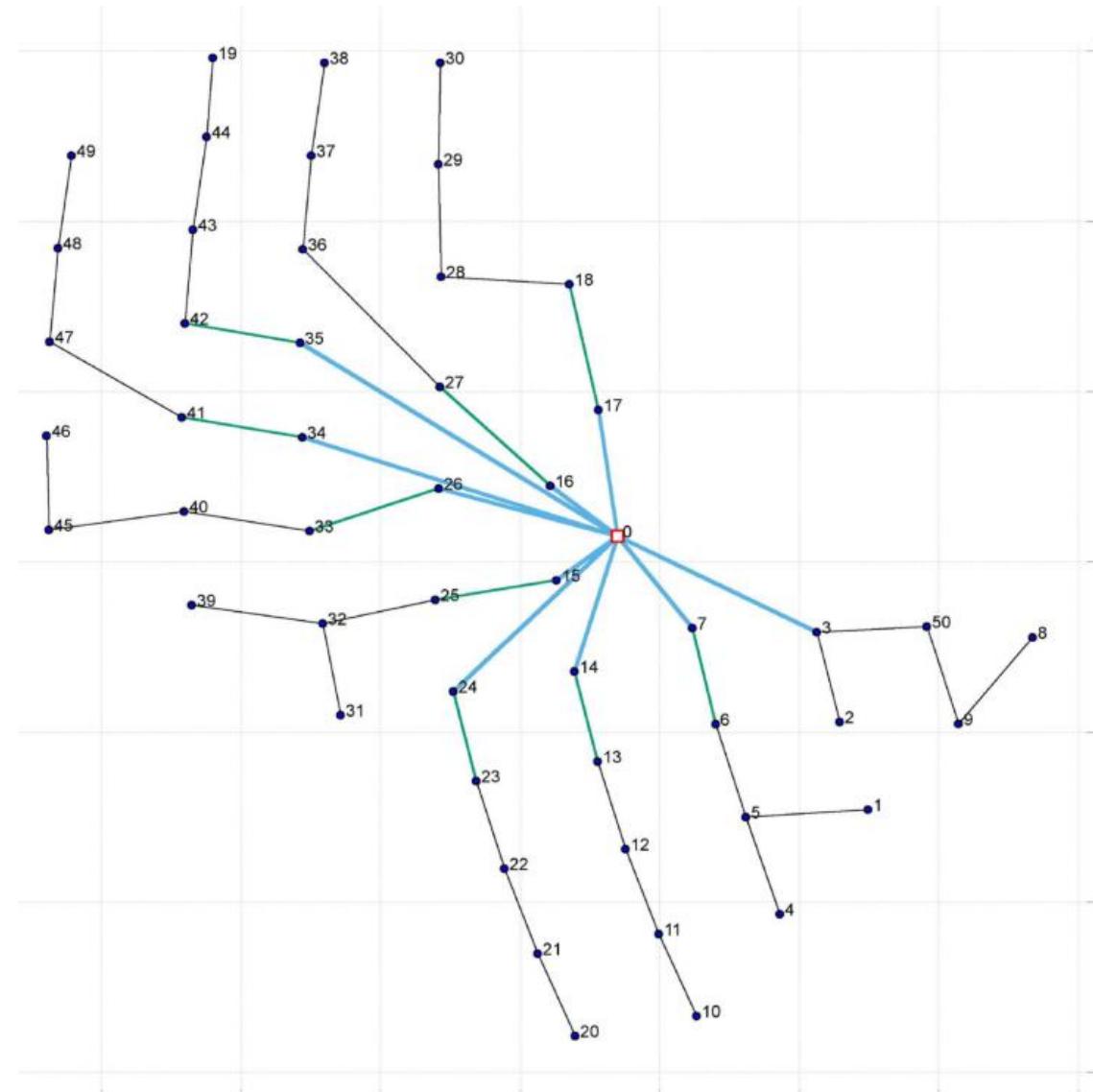
$V_T$ : Turbine node

$V_O$ : Substation node

$V_S$ : Steiner node

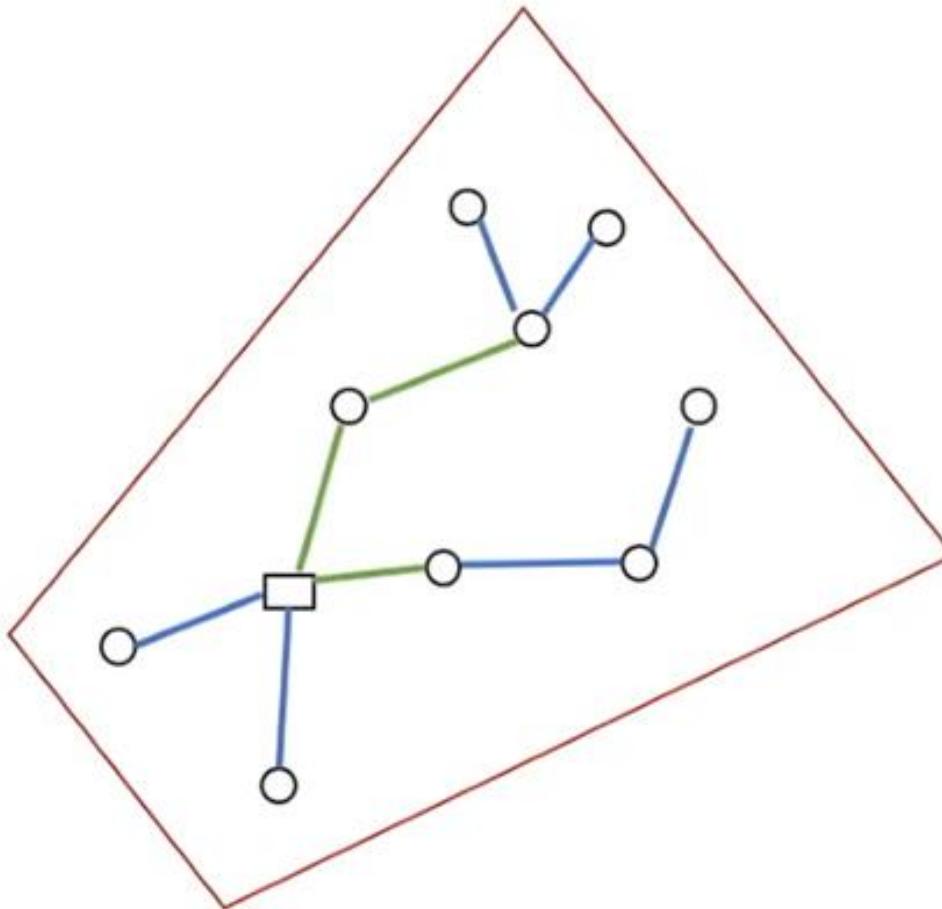


$$V = V_T \cup V_O \cup V_S$$



### 1) Cable Routing – modeling analysis

## 3 What to optimize? – set and decision variables



VARIABLES (on the arcs):

$f_{i,j} \geq 0$  is the flow (current) from  $i$  to  $j$

$$x_{i,j}^t = \begin{cases} 1 & \text{if arc } (i,j) \text{ is built with cable } t \\ 0 & \text{otherwise} \end{cases}$$

$y_{i,j} = 1$  if an arc from  $i$  to  $j$  is built,  
with any type of cable ( $\sum_{t \in T} x_{i,j}^t = y_{i,j}$ )

### 3 1) Cable Routing – modeling analysis

## What to optimize? – basic model

$$\min \sum_{(i,j) \in A} \sum_{t \in T} c_{i,j}^t x_{i,j}^t \quad \rightarrow \quad \text{비용 최소화}$$

$$\sum_{t \in T} x_{i,j}^t = y_{i,j}, \quad (i,j) \in A \quad \rightarrow \quad \text{주어진 케이블 종류 외의 케이블은 사용 불가}$$

$$\sum_{i \in V : i \neq h} (f_{h,i} - f_{i,h}) = P_h, \quad h \in V_T \cup V_S \quad \rightarrow \quad \text{전하량 보존}$$

$$\sum_{t \in T} k_t x_{i,j}^t \geq f_{i,j}, \quad (i,j) \in A \quad \rightarrow \quad \text{케이블에 흐르는 전류는 capacity를 넘길 수 없음}$$

### 3 1) Cable Routing – modeling analysis

## What to optimize? – basic model

$$\sum_{j \in V: j \neq h} y_{h,j} = 1, \quad h \in V_T$$



모든 Turbine에 1개의 케이블이 연결

$$\sum_{j \in V: j \neq h} y_{h,j} = 0, \quad h \in V_0$$



발전소에서 나가는 전류가 없어야 함

$$\sum_{j \in V: j \neq h} y_{h,j} \leq 1, \quad h \in V_S$$



Steiner node에는 케이블이 1개 이하로 연결

$$\sum_{i \in V: i \neq h} y_{i,h} \leq 1, \quad h \in V_S$$



발전소에 연결할 수 있는 최대 케이블의 수

$$\sum_{i \in V: i \neq h} y_{i,h} \leq C, \quad h \in V_0$$

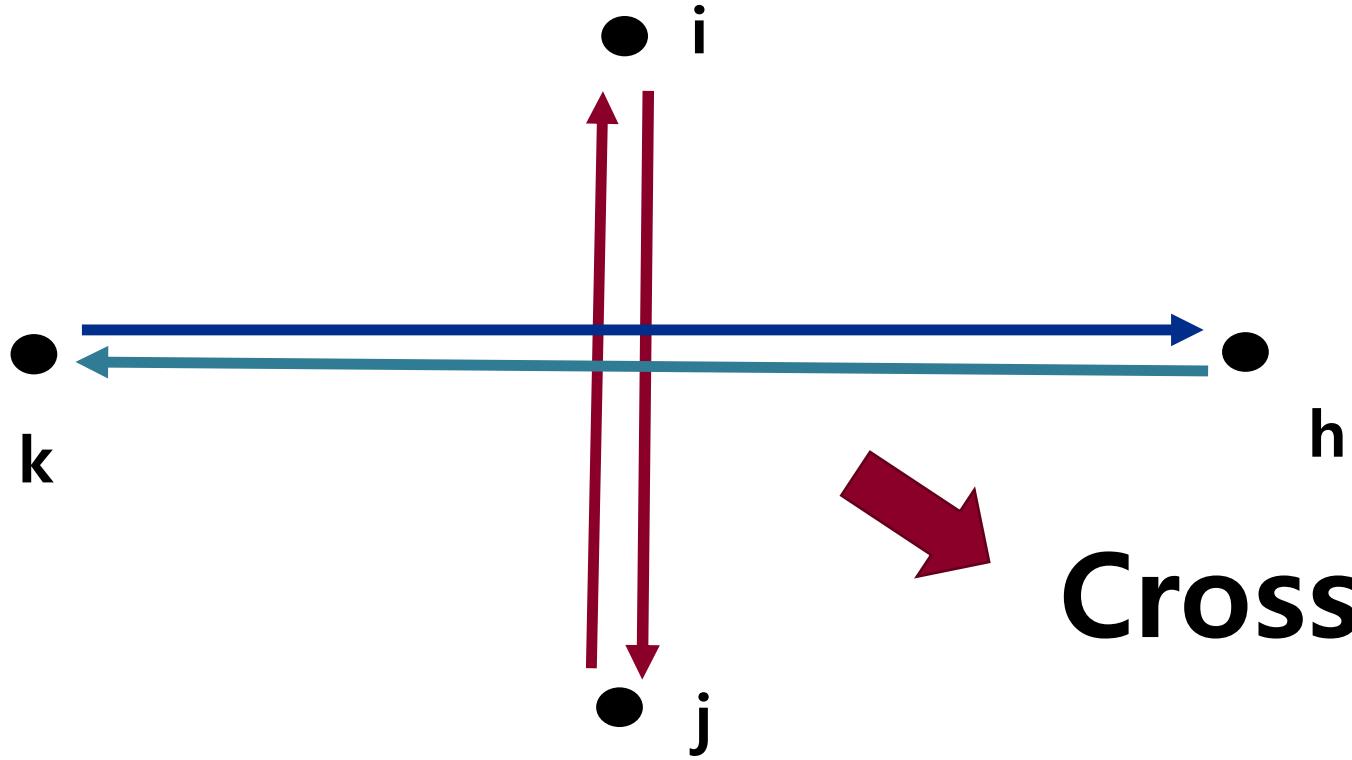
## 3

1) Cable Routing – modeling analysis

## What to optimize? – basic model

$$y_{i,j} + y_{j,i} + y_{h,k} + y_{k,h} \leq 1, \quad \text{for all crossing segments } [i,j] \text{ and } [h,k]$$

→ 케이블 끼리 교차하지 않아야 한다.



$$x_{i,j}^t \in \{0, 1\}, (i,j) \in A, t \in T$$

$$y_{i,j} \in \{0, 1\}, (i,j) \in A$$

$$f_{i,j} \geq 0, (i,j) \in A.$$

**Crossing**

# 3

## 1) Cable Routing – modeling analysis

### What to optimize? – Branching penalty model

$$\min \sum_{(i,j) \in A} \sum_{t \in T} c_{i,j}^t x_{i,j}^t + \sum_{d \in D} \pi_d \sum_{j \in V_T} z_j^d$$

$$\sum_{i \in V : i \neq j} y_{i,j} = \sum_{d \in D} d z_j^d, \quad j \in V_T$$

$$\sum_{d \in D} z_j^d \leq 1, \quad j \in V_T$$

$$D = \{1, \dots d_{\max}\}$$

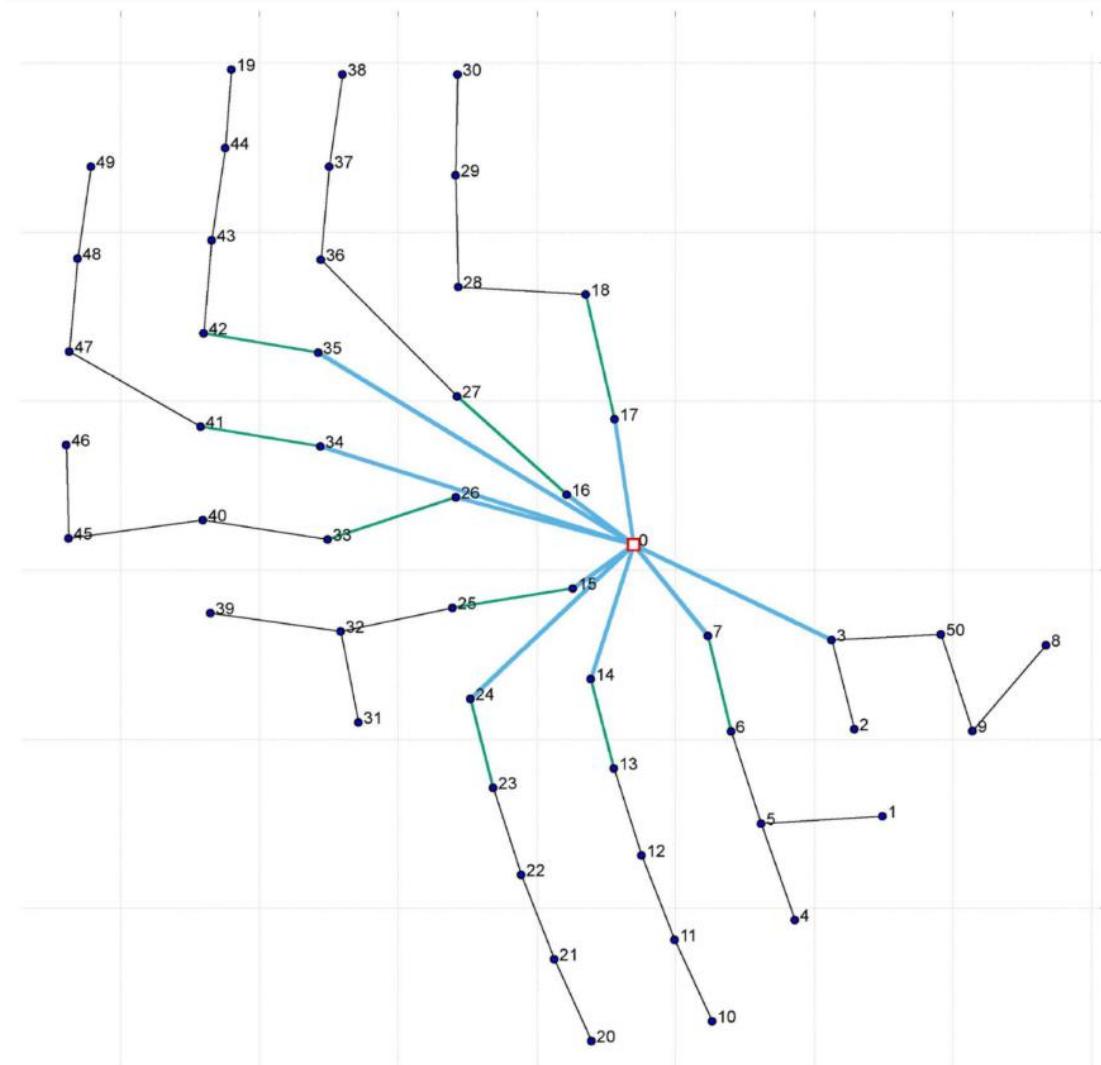
$\pi_d$  : branching으로 인한 extra fee

$$\pi_1 = 0, \pi_2 = 25 k\text{\AA}$$

$z_j^d$  with  $j \in V_T$  and  $d \in D$

$z_j^d = 1$  node j의 가지 갯수가 d인 경우

$z_j^d = 0$  node j의 가지 갯수가 d가 아닌 경우



# **3** 1) Cable Routing – modeling analysis **What to optimize? – 3) closed loop model**

$q_{i,j} = 0$  node i, j 에 redundant 케이블이 연결 되지 않는 경우

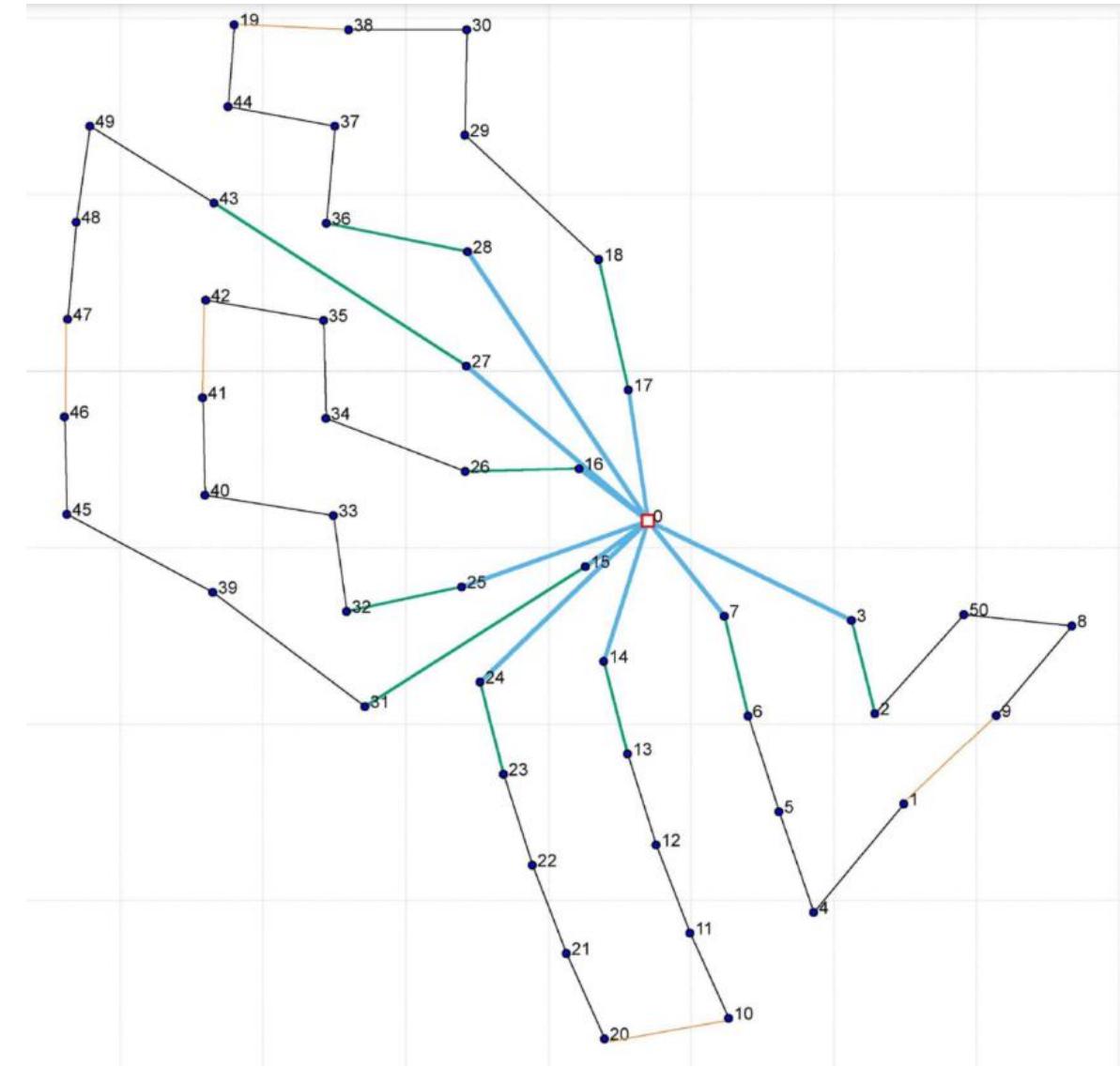
$q_{i,j} = 1$  node i, j 에 redundant 케이블이 연결 되는 경우

$$q_{i,j} = 0, \quad (i,j) \in A : i > j$$

$$q_{i,j} \in \{0, 1\}, \quad (i, j) \in A$$

$$\min \sum_{(i,j) \in A} \sum_{t \in T} c_{i,j}^t x_{i,j}^t + \sum_{(i,j) \in A} c_{i,j}^{t_{\min}} q_{i,j}$$

$$\sum_{i \in V: i \neq h} (y_{i,h} + y_{h,i} + q_{i,h} + q_{h,i}) = 2 \sum_{j \in V: j \neq h} y_{h,j}, \quad h \in V_T \cup V_S$$



### 3 2) Cable Routing – discussion Criticism

전력손실을 제약식에 고려하지 않음

$$\sum_{i \in V: i \neq h} (f_{h,i} - f_{i,h}) = P_h, \quad h \in V_T \cup V_S \quad \rightarrow \quad \sum_{i \in V: i \neq h} (f_{h,i} - f_{i,h}) = P_h - \underline{(f_{i,h})^2 r_t}$$

Extra branching cost의 지나친 단순화

$\pi_1 = 0, \pi_2 = 25 k\ell$   $\rightarrow$  각 노드의 위치에 따른 특성에 대한 고려 없이 branching cost를 상수로 고정함

Branching의 개수를 2로 제한

$D = \{1, \dots d_{\max}\}, d_{\max} \leq 2 \quad \rightarrow \quad d_{\max}$  의 값을 다양화하여 더 많은 니즈를 충족 가능

감사합니다