General information

- The recommended tool in this course is R (with the IDE R-Studio). You can download R here and R-Studio here. There are tons of tutorials, videos and introductions to R and R-Studio online. You can find some initial hints from RStudio Education pages.
- Instead of installing R and RStudio on you own computer, see how to use R and RStudio remotely.
- When working with R, we recommend writing the report using R markdown and the provided R markdown template. The remplate includes the formatting instructions and how to include code and figures.
- Instead of R markdown, you can use other software to make the PDF report, but the the same instructions for formatting should be used. These instructions are available also in the PDF produced from the R markdown template.
- Report all results in a single, anonymous *.pdf -file and return it to peergrade.io.
- The course has its own R package aaltobda with data and functionality to simplify coding. To install the package just run the following (upgrade="never" skips question about updating other packages):
 - 1. install.packages("remotes")
 - 2. remotes::install_github("avehtari/BDA_course_Aalto",
 subdir = "rpackage", upgrade="never")
- Many of the exercises can be checked automatically using the R package markmyassignment. Information on how to install and use the package can be found here. There is no need to include markmyassignment results in the report.
- Recommended additional self study exercises for each chapter in BDA3 are listed in the course web page.
- Common questions and answers regarding installation and technical problems can be found in Frequently Asked Questions (FAQ).
- Deadlines for all assignments can be found on the course web page and in peergrade. You can set email alerts for trhe deadlines in peergrade settings.
- You are allowed to discuss assignments with your friends, but it is not allowed to copy solutions directly from other students or from internet. You can copy, e.g., plotting code from the course demos, but really try to solve the actual assignment problems with your own code and explanations. Do not share your answers publicly. Do not copy answers from the internet or from previous years. We compare the answers to the answers from previous years and to the answers from other students this year. All suspected plagiarism will be reported and investigated. See more about

the Aalto University Code of Academic Integrity and Handling Violations Thereof <a href="https://into.aalto.fi/display/ensaannot/Aalto+University+Code+of+Academic+Integrity+and+Handling-Integrity-

- Do not submit empty PDFs or almost empty PDFs as these are just harming the other students as they can't do peergrading for the empty or almost empty submissions. Violations of this rule will be reported and investigated in the same way was plagiarism.
- If you have any suggestions or improvements to the course material, please post in the course chat feedback channel, create an issue, or submit a pull request to the public repository!

Information on this assignment

This assignment is related to Chapters 1 and 2. The maximum amount of points from this assignment is 3. You may find an additional discussion about choosing priors by Andrew Gelman useful, they can be found **here**.

Reading instructions: Chapter 1 and 2 in BDA3, see reading instructions here and here.

Grading instructions: The grading will be done in peergrade. All grading questions and evaluations for assignment 2 can be found **here**

To use markmyassignment for this assignment, run the following code in R:

```
> library(markmyassignment)
> assignment_path <-
        paste("https://github.com/avehtari/BDA_course_Aalto/",
        "blob/master/assignments/tests/assignment2.yml", sep="")
> set_assignment(assignment_path)
> # To check your code/functions, just run
> mark_my_assignment()
```

Inference for binomial proportion (Computer)

Algae status is monitored in 274 sites at Finnish lakes and rivers. The observations for the 2008 algae status at each site are presented in file algae.txt ('0': no algae, '1': algae present). The data can also be accessed from the aaltobda R package as follows:

```
> library(aaltobda)
> data("algae")
> # the data is now stored in the variable 'algae'
```

So that you can test the correctness of your code implementations, we provide some results for the following **test data**. It is also possible to check the functions you need to implement with markmyassignment.

```
> algae_test <- c(0, 1, 1, 0, 0, 0)
```

Note! This data is **only for the tests**, you need to change to the full data **algae** when reporting your results.

Let π be the probability of a monitoring site having detectable blue-green algae levels and y the observations in algae. Use a binomial model for the observations y and a Beta(2, 10) prior for binomial model parameter π to formulate a Bayesian model. Here it is not necessary to derive the posterior distribution for π as it has already been done in the book and it suffices to refer to that derivation. Also, it is not necessary to write out the distributions; it is sufficient to use label-parameter format, e.g. Beta(\cdot , \cdot).

Your task is to make Bayesian inference for binomial model and answer questions based on it:

- a) formulate (1) the likelihood $p(y|\pi)$ as a function of π , (2) the prior $p(\pi)$, and (3) the resulting posterior $p(\pi|y)$. Report the posterior in the format Beta(·,·), where you replace ·'s with the correct numerical values.
- b) What can you say about the value of the unknown π according to the observations and your prior knowledge? Summarize your results with a point estimate (i.e. $E(\pi|y)$) and a 90% posterior interval. **Note!** Posterior intervals are also called credible intervals and are different from confidence intervals. **Note!** In your report, use the values from the data algae, not algae_test.

```
> beta_point_est(prior_alpha = 2, prior_beta = 10, data = algae_test)
[1] 0.2222222
> beta_interval(prior_alpha = 2, prior_beta = 10, data = algae_test, prob = 0.9)
[1] 0.0846451 0.3956414
```

c) What is the probability that the proportion of monitoring sites with detectable algae levels π is smaller than $\pi_0 = 0.2$ that is known from historical records?

```
> beta_low(prior_alpha = 2, prior_beta = 10, data = algae_test, pi_0 = 0.2)
[1] 0.4511238
```

- d) What assumptions are required in order to use this kind of a model with this type of data? (No need to discuss exchangeability yet, as it is discussed in more detail in BDA Chapter 5 and Lecture 7)
- e) Make prior sensitivity analysis by testing a couple of different reasonable priors and plot the different posteriors. Summarize the results by one or two sentences.

Hint! With a conjugate prior, a closed-form posterior is Beta form (see equations in the book). Useful functions: dbeta, pbeta, qbeta in R.