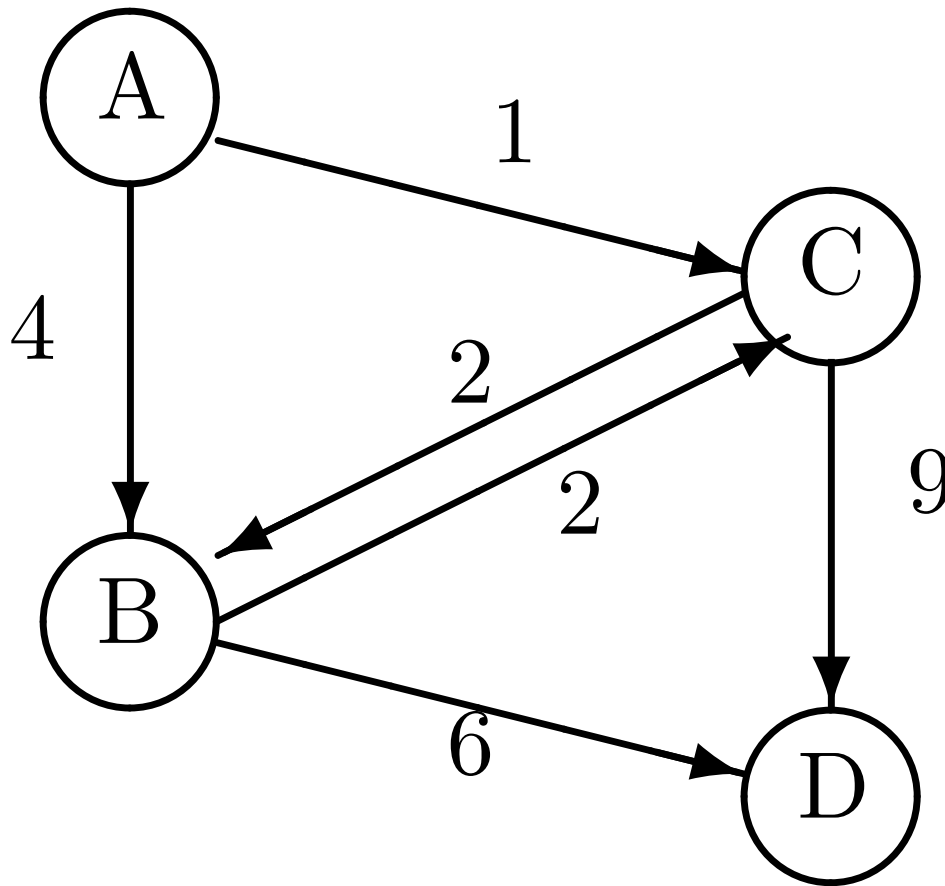


# A\* Example



$$h(A) = 8$$

$$h(B) = 3$$

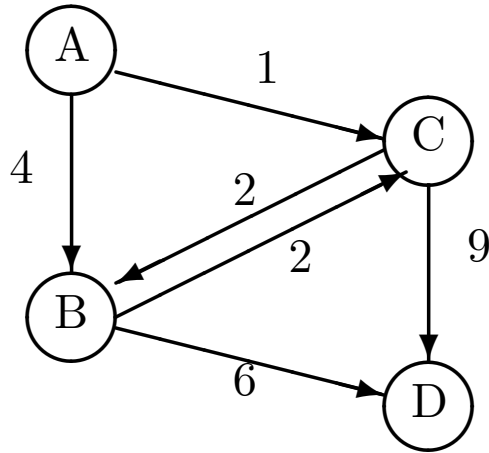
$$h(C) = 7$$

$$h(D) = 0$$

START = A

GOAL = D

# A\* Example



START = A

GOAL = D

$$h^*(A) = 9$$

$$h^*(B) = 6$$

$$h^*(C) = 8$$

$$h^*(D) = 0$$

$$h(A) = 8$$

$$h(B) = 3$$

$$h(C) = 7$$

$$h(D) = 0$$

- This heuristic is admissible

# A\* with cycle checking

---

OPEN:

1. 8 {<A> (g-val+h-val=f-val)} == {<A> (0+8= 8)}
2. 7 {<A,B> (4+3=7), <A,C> (1+7=8)}
3. 8 {<A,C> (1+7=8), <A,B,D> (10+0=10)}
4. 6 {<A,C,B> (3+3=6), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
5. 9 {<A,C,B,D> (9+0=9), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
6. Return solution path <A,C,B,D>

Sequence of f-values of the paths-expanded.

8, 7, 8, 6, 9

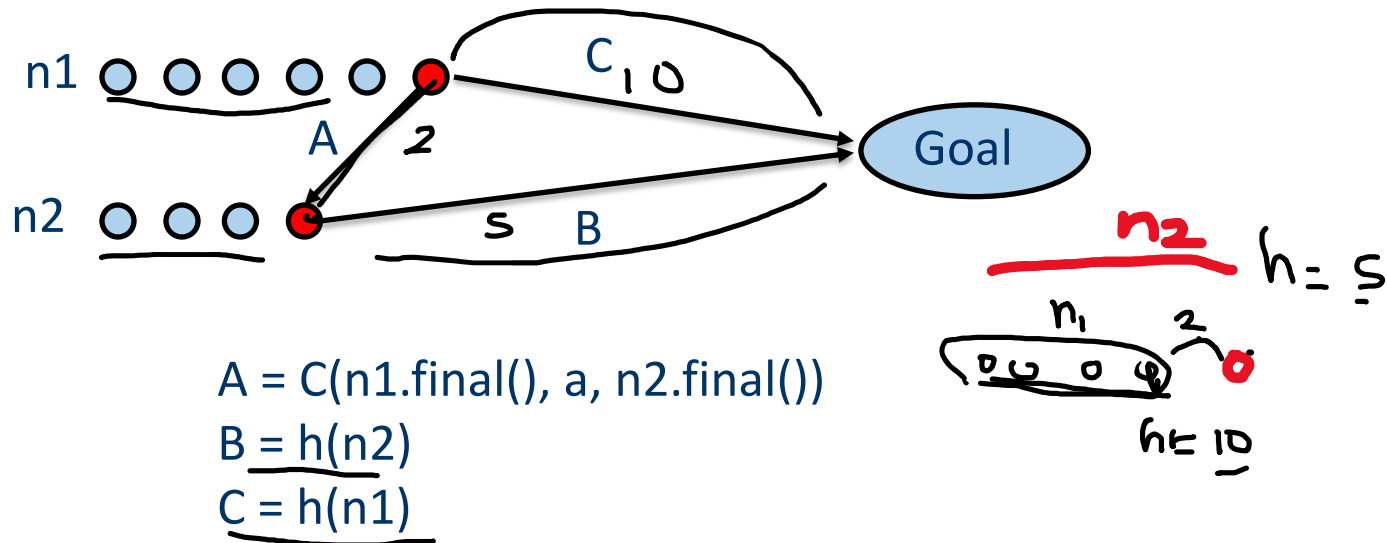
Proposition 2 (slide 139) A\* with an admissible heuristic never expands a node with f-value greater than C\* (the cost of an optimal solution)

At every stage some prefix of an optimal path is on OPEN

# Monotone Heuristics

- For all paths  $n1$  and  $n2$  and all actions  $a$ :

$$\underline{h(n1)} \leq C(n1.final(), a, n2.final()) + h(n2)$$



Triangle inequality

# Consequences of monotonicity

---

1. The sequence of  $f$ -values of the paths expanded by  $A^*$  is non-decreasing. That is, if  $n_2$  is expanded **after**  $n_1$  by  $A^*$  then  $f(n_1) \leq f(n_2)$ . (Not necessarily true for an admissible heuristic as that heuristic might be non-monotone)
2. With a monotone heuristic, the first time  $A^*$  expands a path  $n = \langle s_0, \dots, s_n \rangle$  that reaches the state  $s_n$ ,  $n$  must be a minimum cost path to  $s_n$

# A\* with cycle checking

---

OPEN:

1. 8 {<A> (g-val+h-val=f-val)} == {<A> (0+8= 8)}
2. 7 {<A,B> (4+3=7), <A,C> (1+7=8)}
3. 8 {<A,C> (1+7=8), <A,B,D> (10+0=10)}
4. 6 {<A,C,B> (3+3=6), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
5. 9 {<A,C,B,D> (9+0=9), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
6. Return solution path <A,C,B,D>

Sequence of f-values of the paths-expanded.

8, 7, 8, 6, 9

Not non-decreasing ( $f(x_i) \leq f(x_{i+1})$  for all  $i$ )

# A\* with cycle checking

---

OPEN:

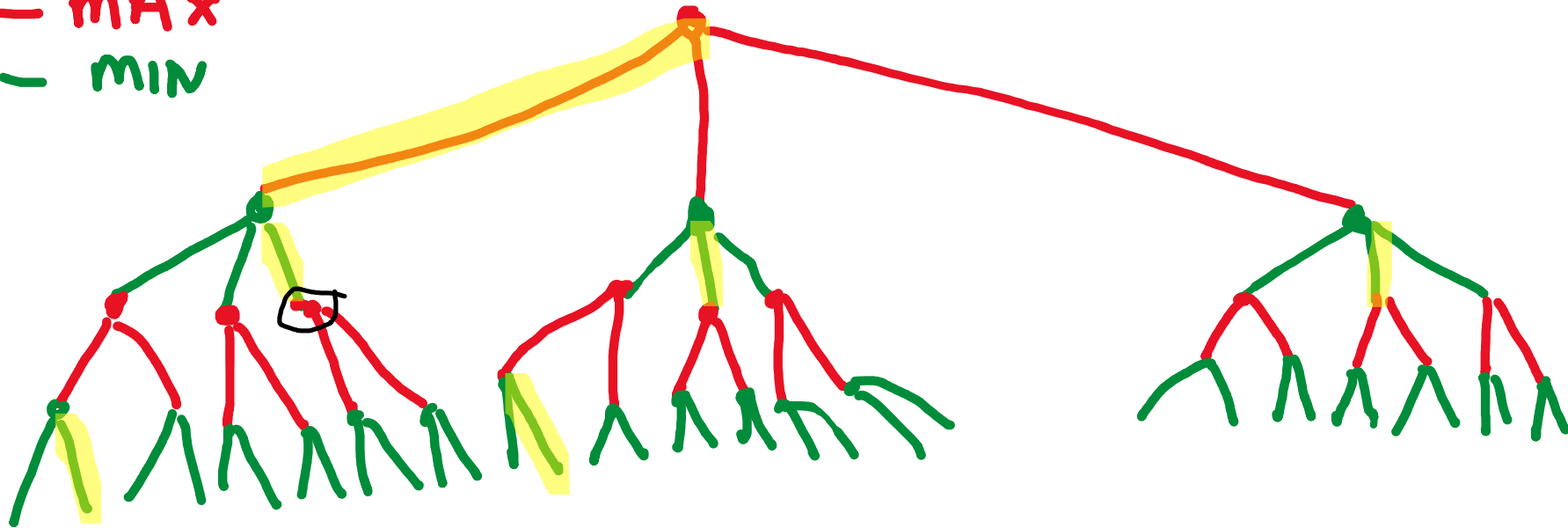
1. 8 {<A> (g-val+h-val=f-val)} == {<A> (0+8= 8)}
2. 7 {<A,B> (4+3=7), <A,C> (1+7=8)}
3. 8 {<A,C> (1+7=8), <A,B,D> (10+0=10)}
4. 6 {<A,C,B> (3+3=6), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
5. 9 {<A,C,B,D> (9+0=9), <A,B,D> (10+0=10), <A,B,C> (6+7=13)}
6. Return solution path <A,C,B,D>

First path expanded that reaches B

# Game Trees

— MAX

— MIN

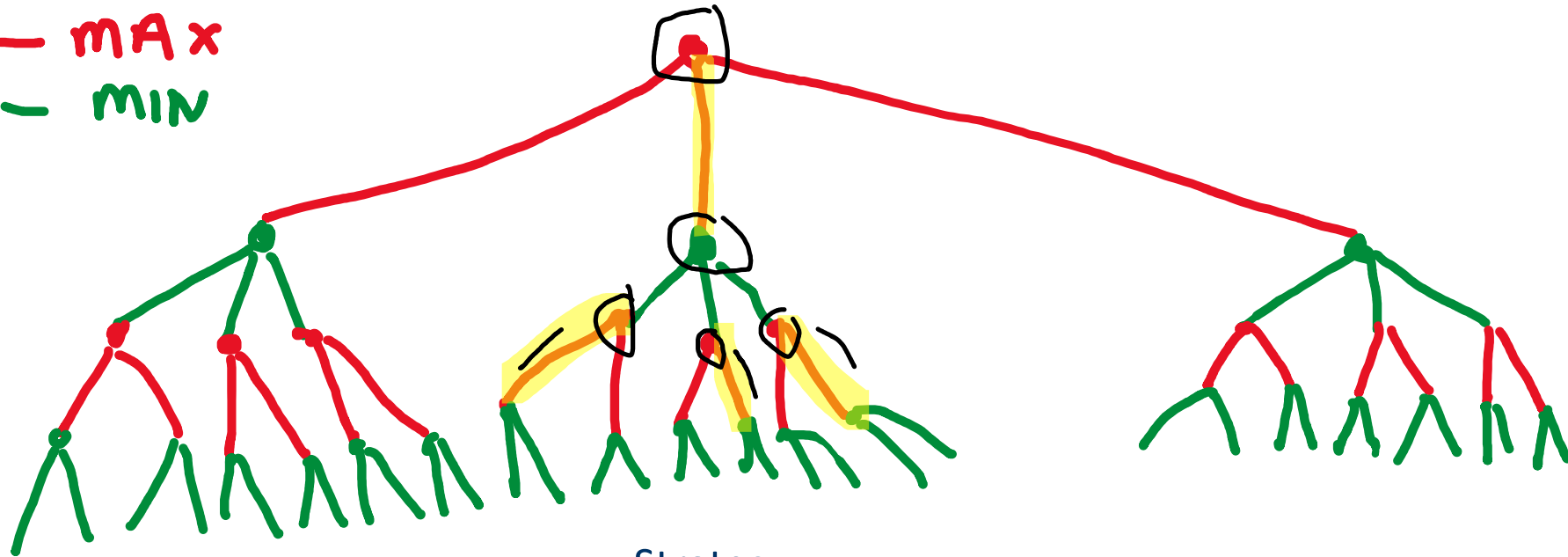




# Game Trees

— MAX

— MIN



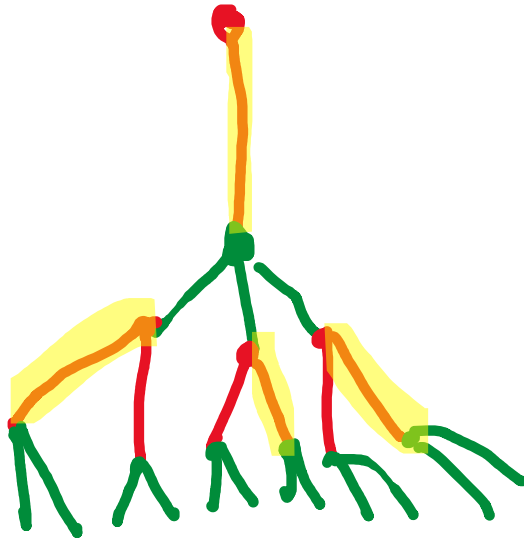
Strategy

# Game Trees

---

— MAX

— MIN

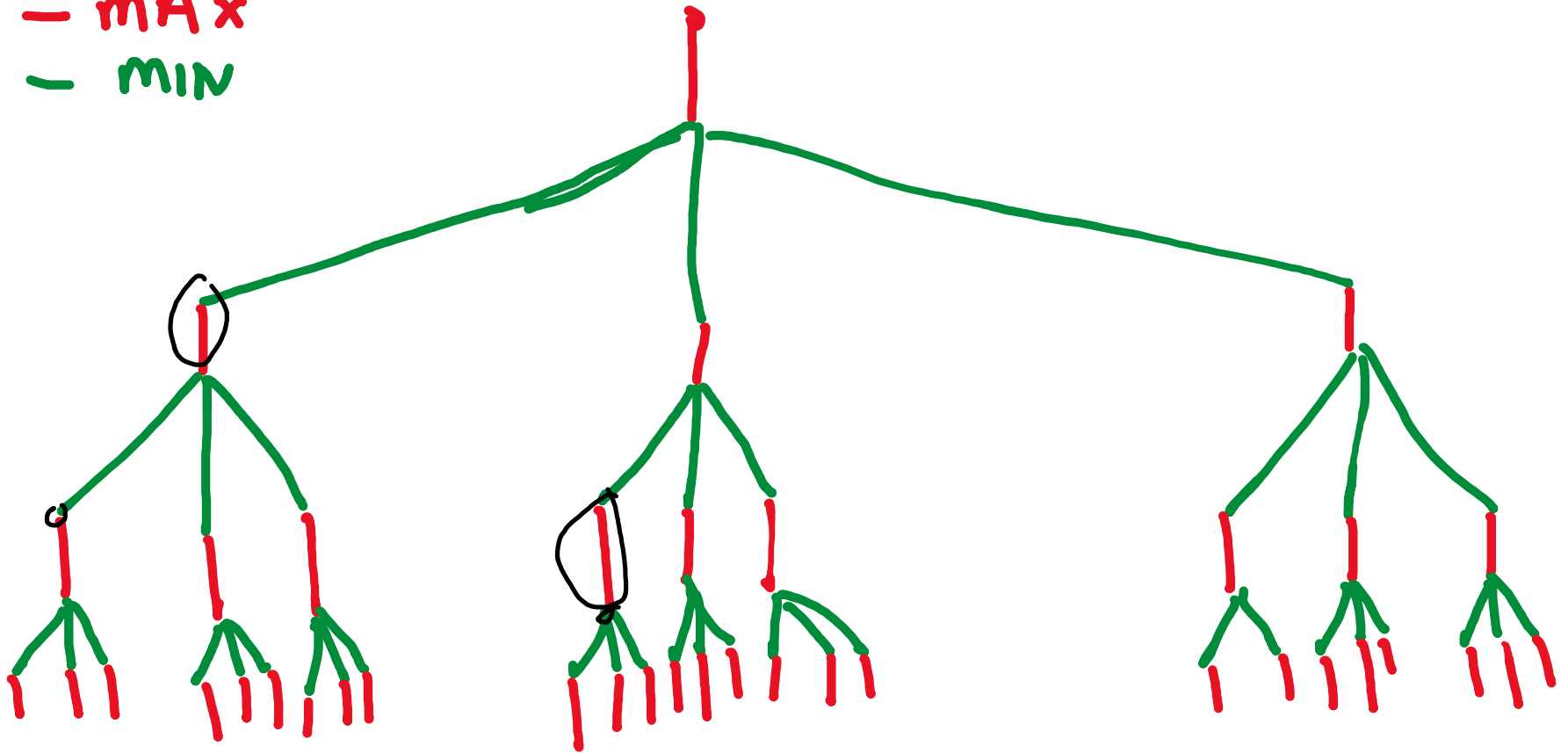


Strategy

# Game Trees

— MAX

— MIN



Strategy