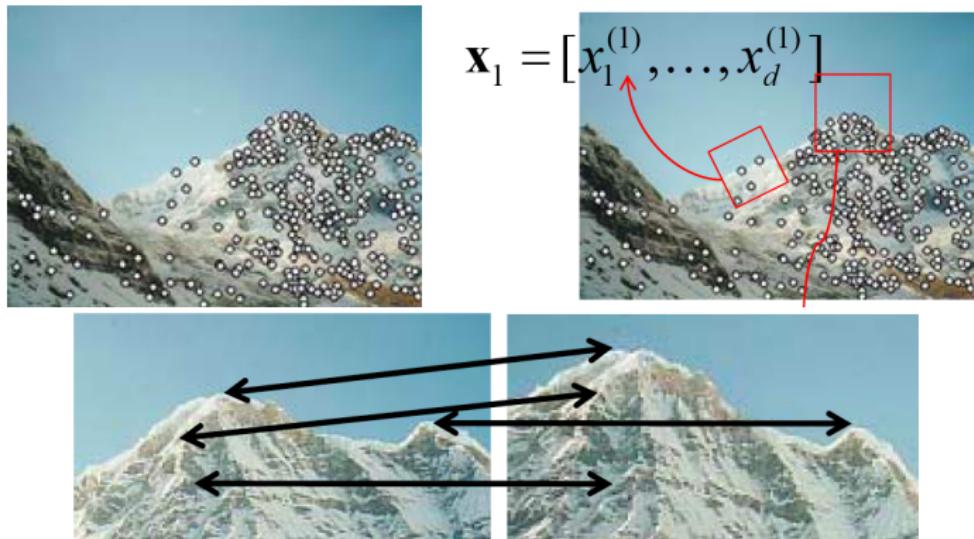


# Image Features: Local Descriptors

# Local Features

- **Detection:** Identify the interest points.
- **Description:** Extract a feature descriptor around each interest point.
- **Matching:** Determine correspondence between descriptors in two views.



[Source: K. Grauman]

# The Ideal Feature Descriptor

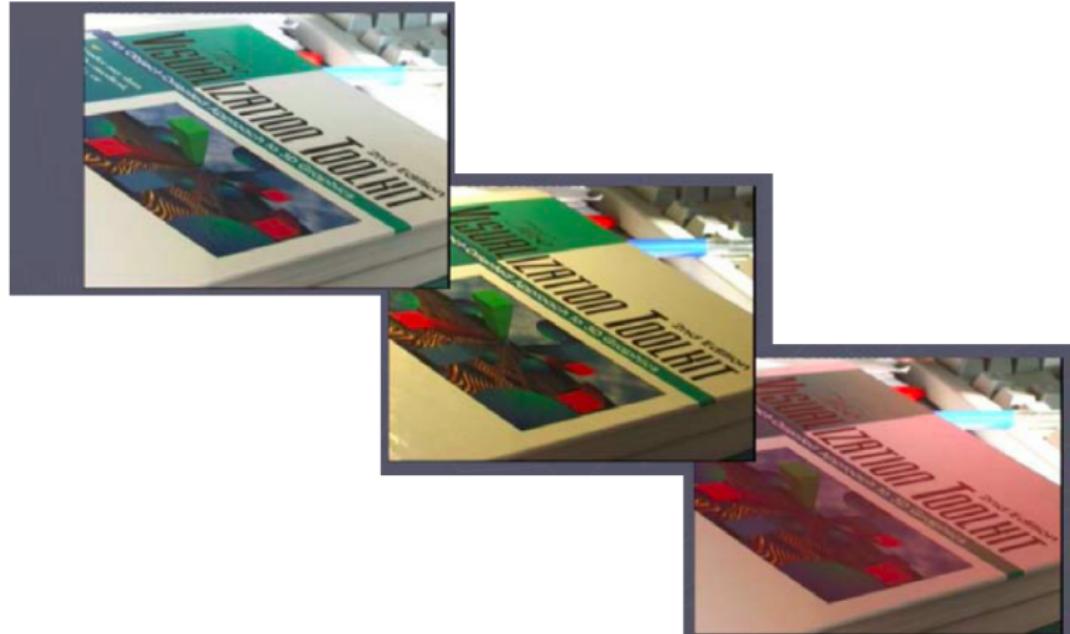
- **Repeatable:** Invariant to rotation, scale, photometric variations
- **Distinctive:** We will need to match it to lots of images/objects!
- **Compact:** Should capture rich information yet not be too high-dimensional (otherwise matching will be slow)
- **Efficient:** We would like to compute it (close-to) real-time

# Invariances



[Source: T. Tuytelaars]

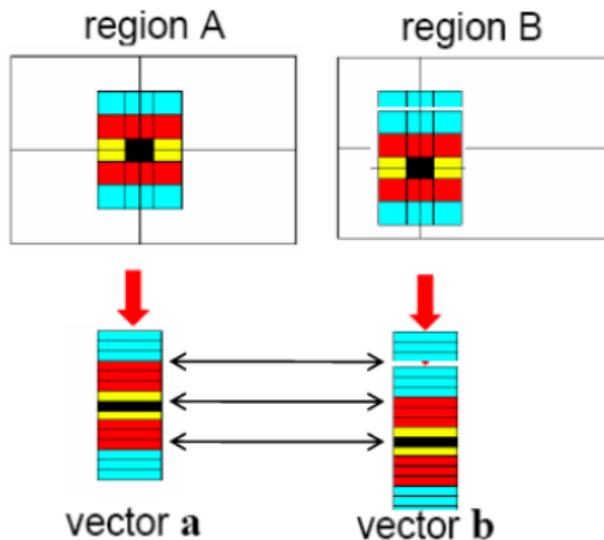
# Invariances



[Source: T. Tuytelaars]

# What If We Just Took Pixels?

- The simplest way is to write down the list of intensities to form a feature vector, and normalize them (i.e., mean 0, variance 1).
- Why normalization?
- But this is very sensitive to even small shifts, rotations and any affine transformation.



# Tons Of Better Options

- SIFT
- PCA-SIFT
- GLOH
- HOG
- SURF
- DAISY
- LBP
- Shape Contexts
- Color Histograms

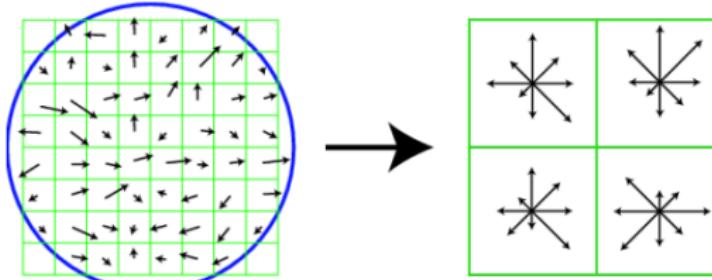
# SIFT Descriptor [Lowe 2004]

- SIFT stands for Scale Invariant Feature Transform
- Invented by David Lowe, who also did DoG scale invariant interest points
- Actually in the same paper, which you should read:

David G. Lowe

*Distinctive image features from scale-invariant keypoints*  
International Journal of Computer Vision, 2004

Paper: <http://www.cs.ubc.ca/~lowe/papers/ijcv04.pdf>



(a) image gradients

(b) keypoint descriptor

# SIFT Descriptor

- ① Our scale invariant interest point detector gives scale  $\rho$  for each keypoint

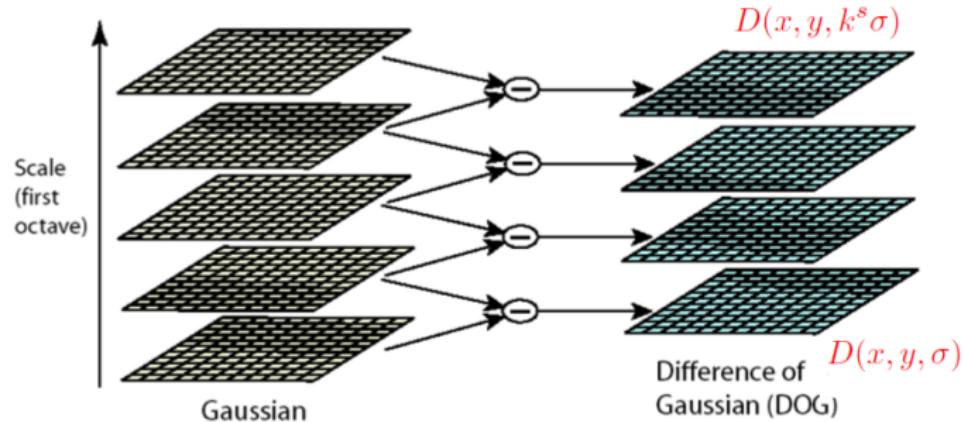
$$I_s = I * G_{k^s \sigma}$$

⋮

$$I_2 = I * G_{k^2 \sigma}$$

$$I_1 = I * G_{k \sigma}$$

$$I_0 = I * G_{\sigma}$$



[Adopted from: F. Flores-Mangas]

# SIFT Descriptor

- ② For each keypoint, we take the Gaussian-blurred image at corresponding scale  $\rho$

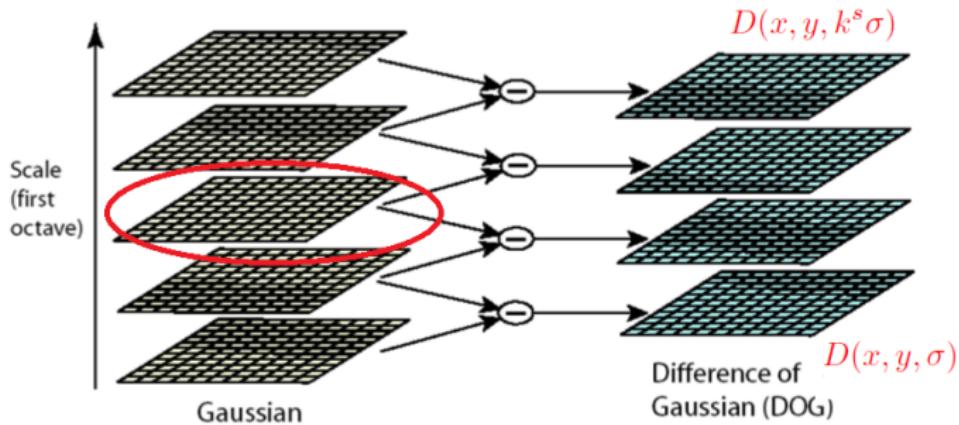
$$I_s = I * G_{k^s \sigma}$$

⋮

$$I_2 = I * G_{k^2 \sigma}$$

$$I_1 = I * G_{k\sigma}$$

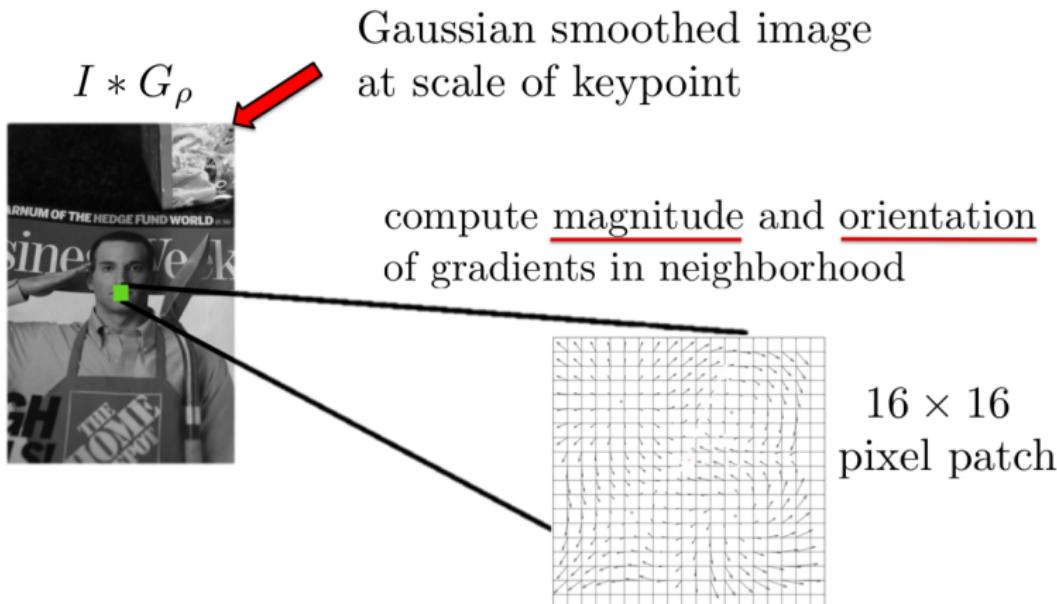
$$I_0 = I * G_\sigma$$



[Adopted from: F. Flores-Mangas]

# SIFT Descriptor

- ③ Compute the gradient magnitude and orientation in neighborhood of each keypoint proportional to the detected scale



[Adopted from: F. Flores-Mangas]

## SIFT Descriptor

- ③ Compute the gradient magnitude and orientation in neighborhood of each keypoint proportional to the detected scale

magnitude of gradient:

$$|\nabla I(x, y)| = \sqrt{\left(\frac{\partial(I(x, y) * G_\rho)}{\partial x}\right)^2 + \left(\frac{\partial(I(x, y) * G_\rho)}{\partial y}\right)^2}$$

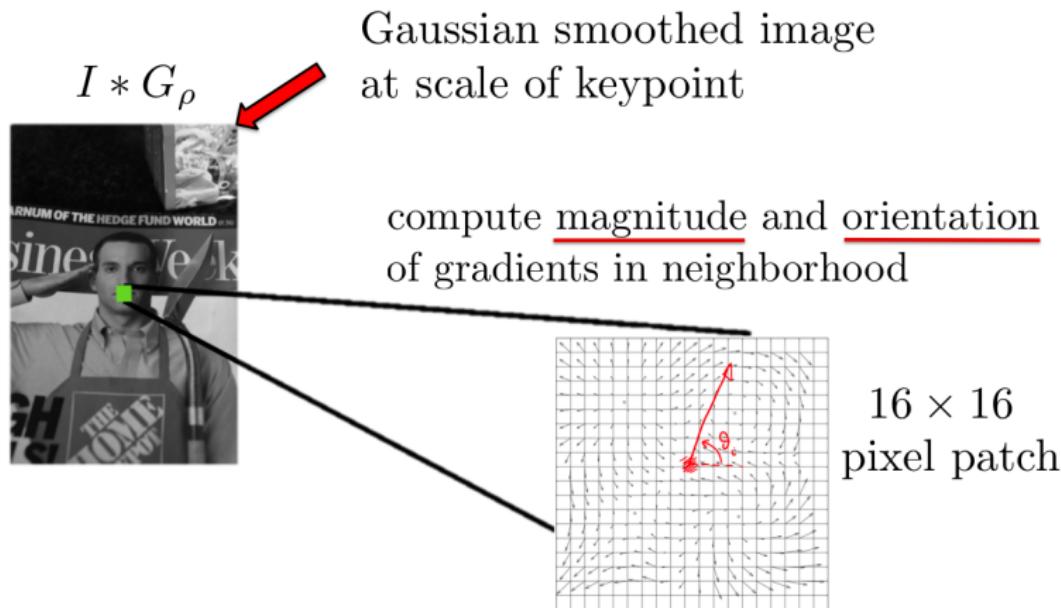
gradient orientation:

$$\theta(x, y) = \arctan\left(\frac{\partial I * G_\rho}{\partial y} / \frac{\partial I * G_\rho}{\partial x}\right)$$

(in case you forgot ;))

# SIFT Descriptor

- ④ Compute dominant orientation of each keypoint. How?

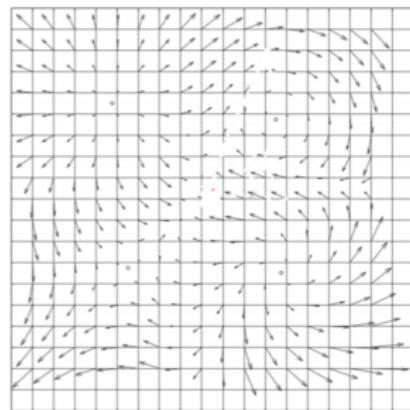


[Adopted from: F. Flores-Mangas]

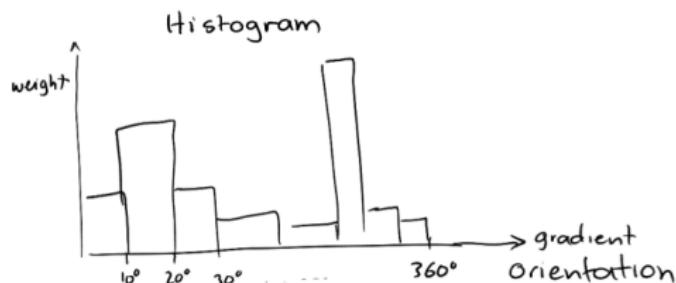
# SIFT Descriptor: Computing Dominant Orientation

- Compute a histogram of gradient orientations, each bin covers  $10^\circ$

$16 \times 16$



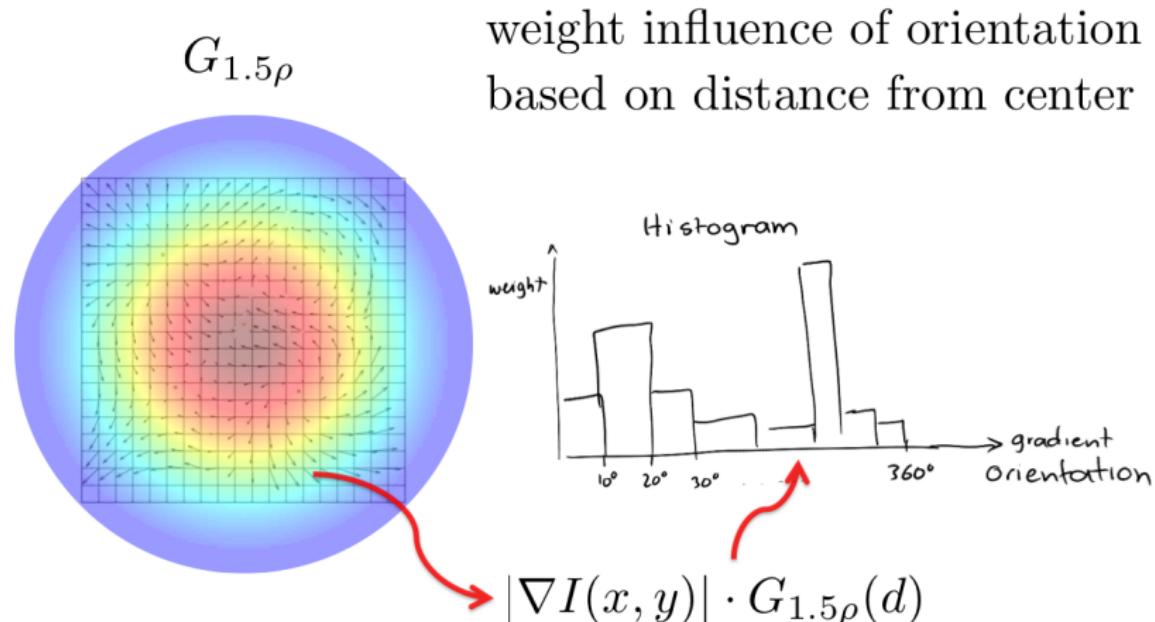
compute histograms of orientations  
by orientation increments of  $10^\circ$



[Adopted from: F. Flores-Mangas]

# SIFT Descriptor: Computing Dominant Orientation

- Compute a histogram of gradient orientations, each bin covers  $10^\circ$
- Orientations closer to the keypoint center should contribute more

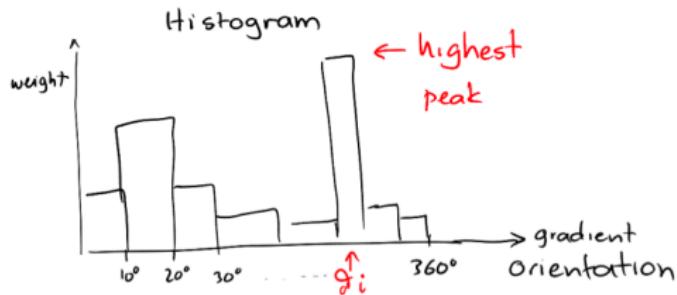
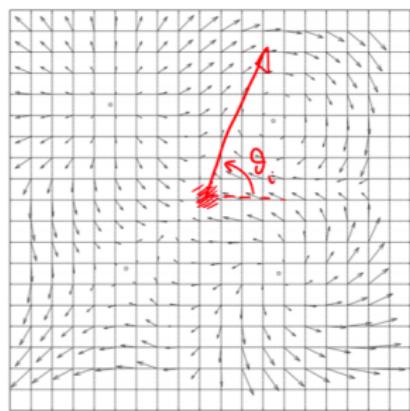


[Adopted from: F. Flores-Mangas]

# SIFT Descriptor: Computing Dominant Orientation

- Compute a histogram of gradient orientations, each bin covers  $10^\circ$
- Orientations closer to the keypoint center should contribute more
- Orientation giving the peak in the histogram is the keypoint's orientation

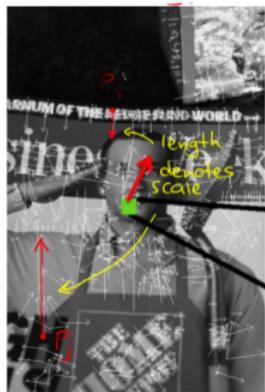
$16 \times 16$



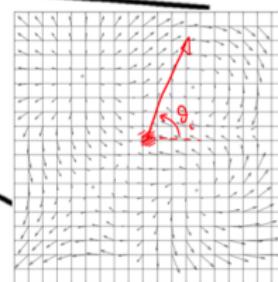
[Adopted from: F. Flores-Mangas]

# SIFT Descriptor

## ④ Compute dominant orientation



compute magnitude and orientation  
of gradients in neighborhood

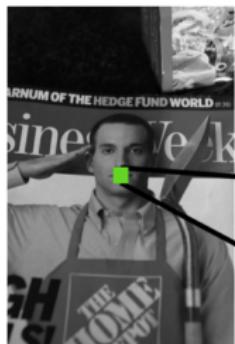


$16 \times 16$   
pixel patch

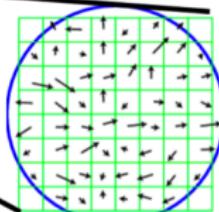
[Adopted from: F. Flores-Mangas]

# SIFT Descriptor

- ⑤ Compute a 128 dimensional descriptor:  $4 \times 4$  grid, each cell is a histogram of 8 orientation bins relative to dominant orientation



compute descriptor, relative  
to dominant orientation



128 dim  
descriptor

each descriptor has:

$$P_i = (x_i, y_i, \rho_i, \vartheta_i) \quad \text{and} \quad f_i \dots 128 \text{ dim vector}$$

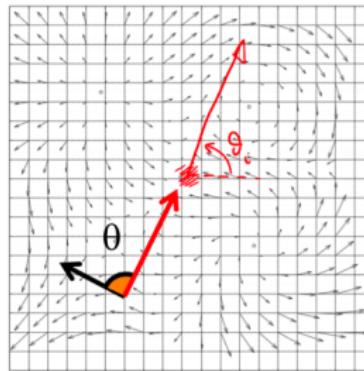
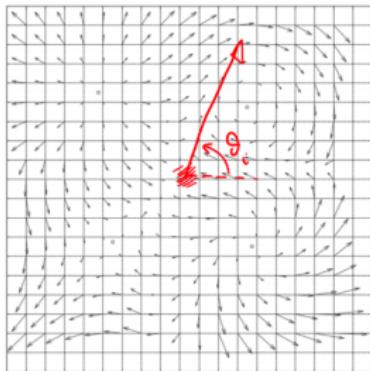
location      scale      orientation      feature vector

[Adopted from: F. Flores-Mangas]

# SIFT Descriptor: Computing the Feature Vector

- Compute the orientations **relative** to the **dominant orientation**
- Otherwise rotating an object would phase shift entries in histogram

$16 \times 16$  patch  
centered in  $(x_i, y_i)$

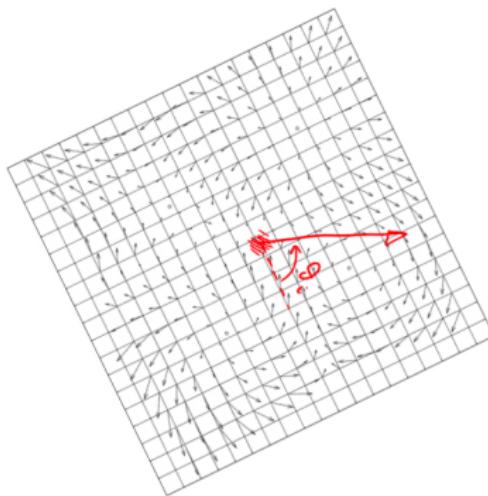
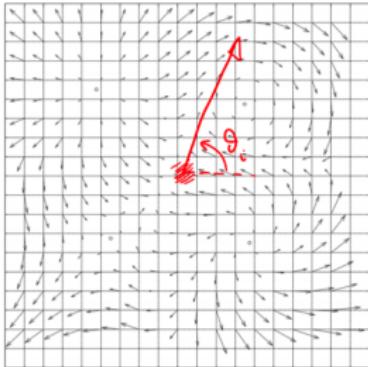


[Adopted from: F. Flores-Mangas]

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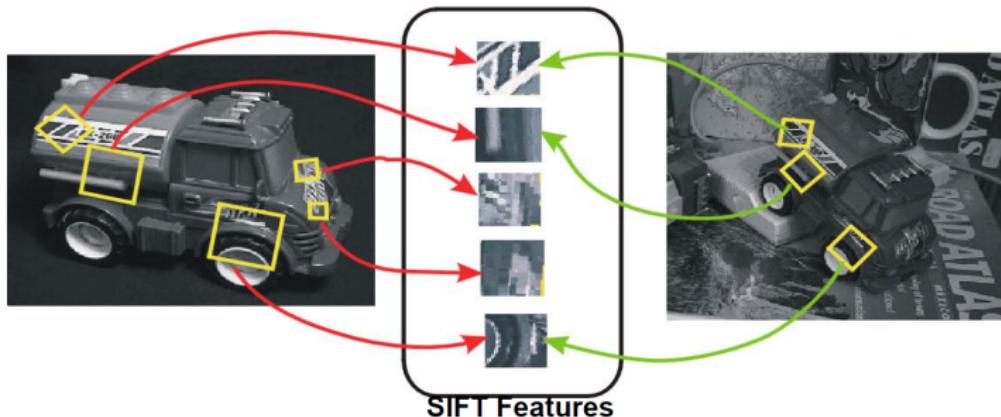
$16 \times 16$  patch  
centered in  $(x_i, y_i)$



[Adopted from: F. Flores-Mangas]

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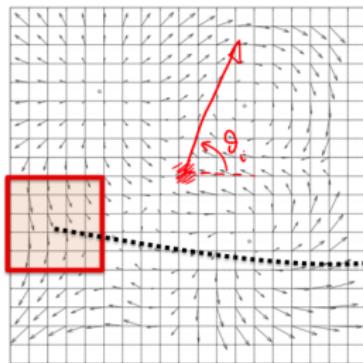
- Compute the orientations **relative** to the **dominant orientation**
- Otherwise rotating an object would phase shift entries in histogram



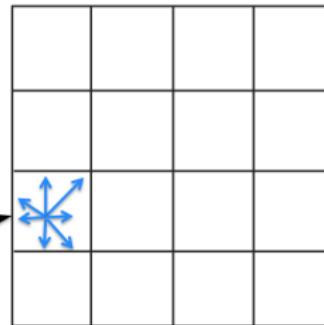
# SIFT Descriptor: Computing the Feature Vector

- Compute the orientations **relative to the dominant orientation**
- Otherwise rotating an object would phase shift entries in histogram
- Form a  $4 \times 4$  grid. For each grid cell compute a histogram of orientations for 8 orientation bins spaced apart by  $45^\circ$

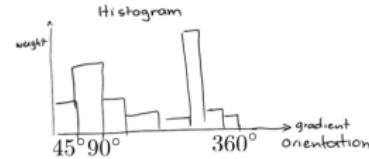
$16 \times 16$  patch  
centered in  $(x_i, y_i)$



SIFT descriptor



compute histogram of orientations  
this time 8 bins spaced by  $45^\circ$

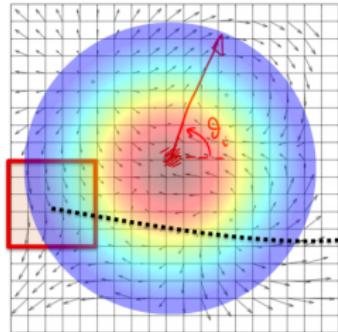


[Adopted from: F. Flores-Mangas]

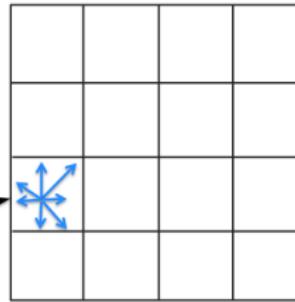
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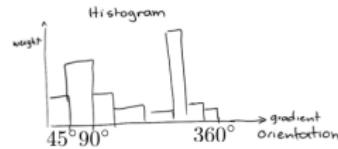
$16 \times 16$  patch  
centered in  $(x_i, y_i)$



SIFT descriptor



again weigh contributions  
this time:  $|\nabla I(x, y)| \cdot G_{0.5\rho}$

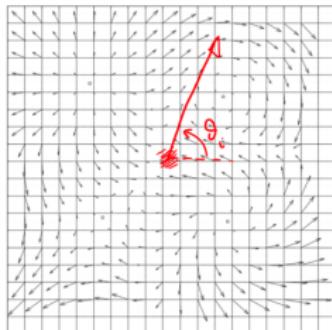


[Adopted from: F. Flores-Mangas]

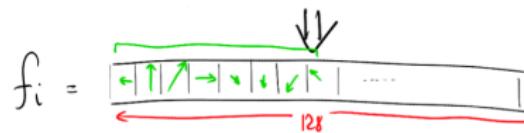
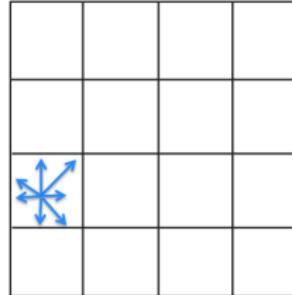
# SIFT Descriptor: Computing the Feature Vector

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- Otherwise rotating an object would phase shift entries in histogram
- Form a  $4 \times 4$  grid. For each grid cell compute a histogram of orientations for 8 orientation bins spaced apart by  $45^\circ$
- Form the 128 dimensional feature vector

$16 \times 16$  patch  
centered in  $(x_i, y_i)$



SIFT descriptor



[Adopted from: F. Flores-Mangas]

## SIFT Descriptor: Post-processing

- The resulting 128 non-negative values form a **raw version** of the SIFT descriptor vector.
- To reduce the **effects of contrast or gain** (additive variations are already removed by the gradient), the 128-D vector is normalized to unit length:  $f_i = f_i / \|f\|$

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# Properties of SIFT

Invariant to:

- Scale
- Rotation

Partially invariant to:

- Illumination changes (sometimes even day vs. night)
- Camera viewpoint (up to about 60 degrees of out-of-plane rotation)
- Occlusion, clutter (why?)

Also important:

- Fast and efficient – can run in real time
- Lots of code available

# Examples

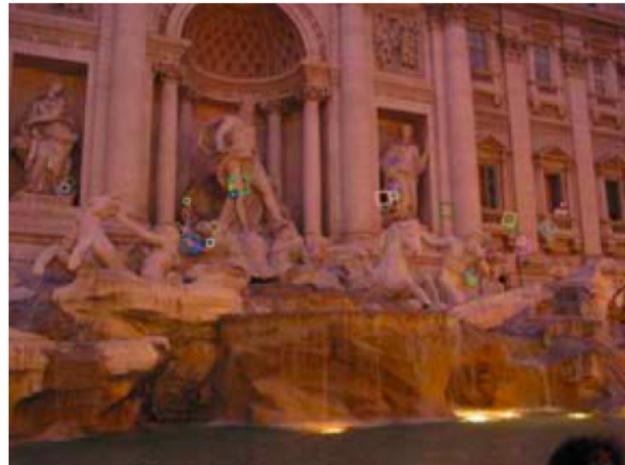
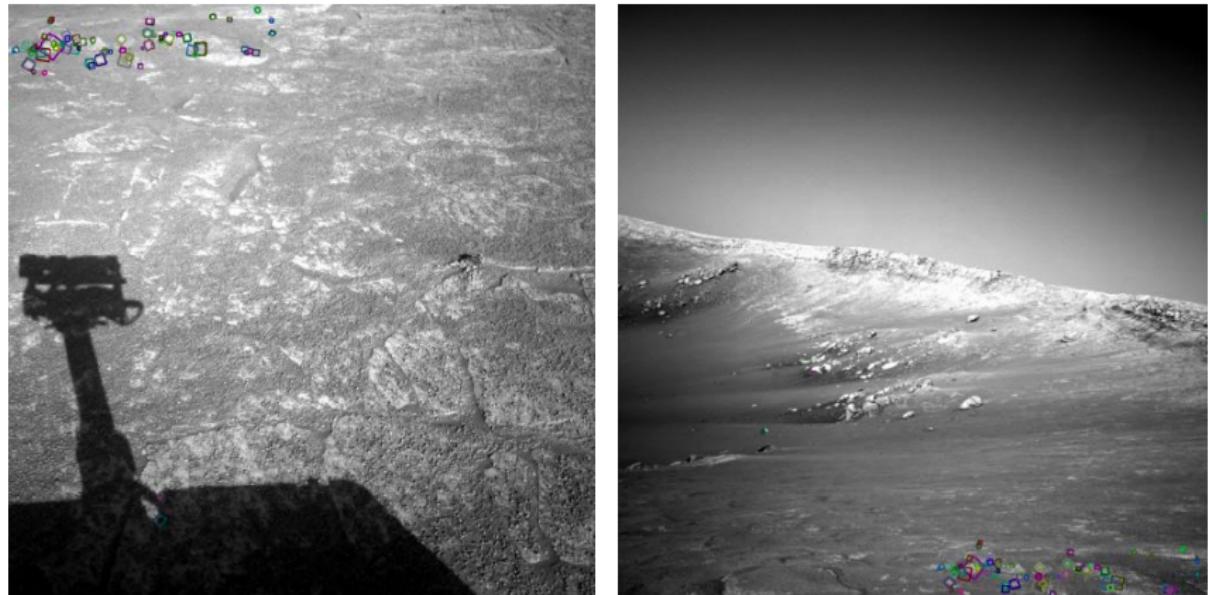


Figure: Matching in day / night under viewpoint change

[Source: S. Seitz]

# Example



**Figure:** NASA Mars Rover images with SIFT feature matches

[Source: N. Snavely]

## PCA-SIFT

- The dimensionality of SIFT is pretty high, i.e., 128D for each keypoint
- Reduce the dimensionality using linear dimensionality reduction
- In this case, principal component analysis (PCA)
- Use 10D or so descriptor

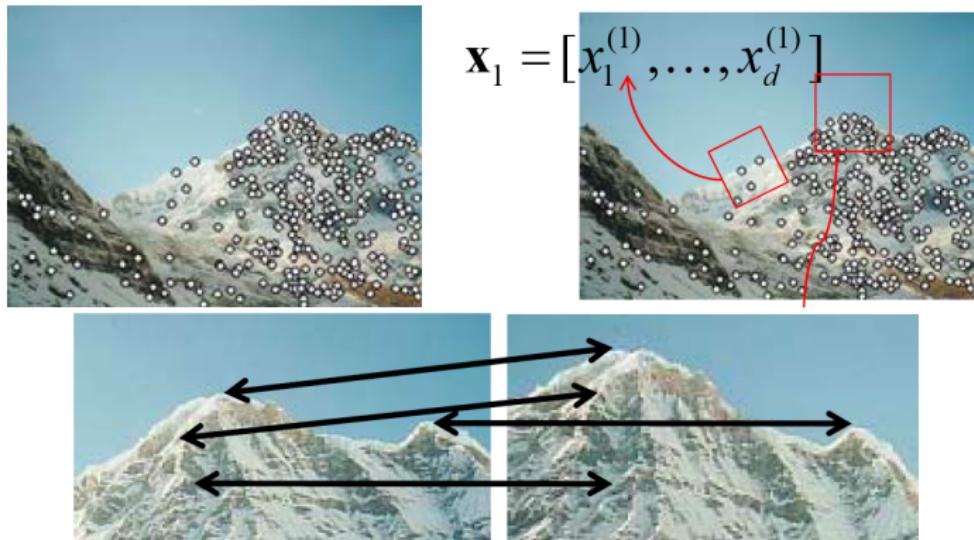
[Source: R. Urtasun]

# Other Descriptors

- SURF
- DAISY
- LBP
- HOG
- Shape Contexts
- Color Histograms

# Local Features

- **Detection:** Identify the interest points.
- **Description:** Extract feature descriptor around each interest point.
- **Matching:** Determine correspondence between descriptors in two views.



[Source: K. Grauman]

# Image Features: Matching the Local Descriptors

# Matching the Local Descriptors

Once we have extracted keypoints and their descriptors, we want to match the features between pairs of images.

- Ideally a match is a correspondence between a local part of the object on one image to the same local part of the object in another image
- How should we compute a match?



Figure: Images from K. Grauman

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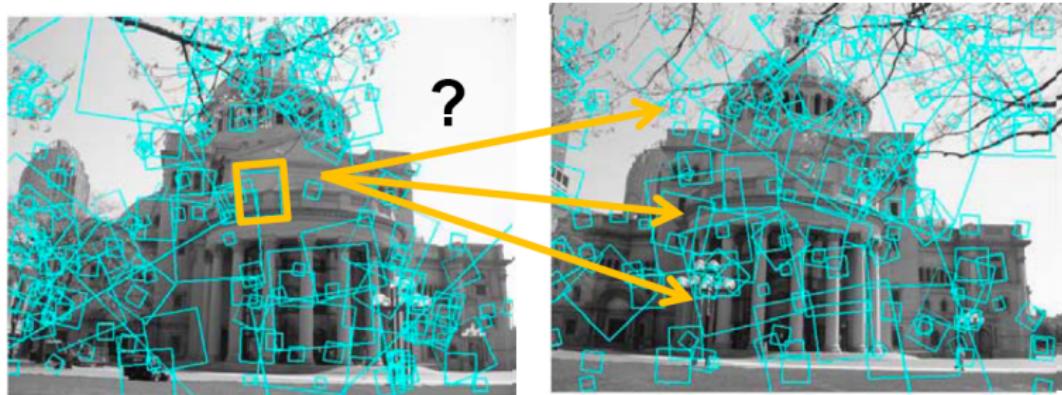
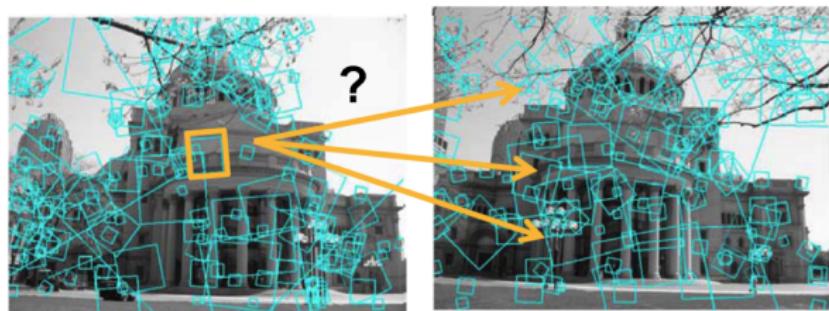


Figure: Images from K. Grauman

# Matching the Local Descriptors

- Simple: **Compare them all**, compute Euclidean distance



$$f_1 \quad \boxed{\text{---}}$$

$$f_2 \quad \boxed{\text{---}}$$

$$f_3 \quad \boxed{\text{---}}$$

$$f'_1 \quad \boxed{\text{---}}$$

$$f'_2 \quad \boxed{\text{---}}$$

$$f'_3 \quad \boxed{\text{---}}$$

$$f_{k-1} \quad \boxed{\text{---}}$$

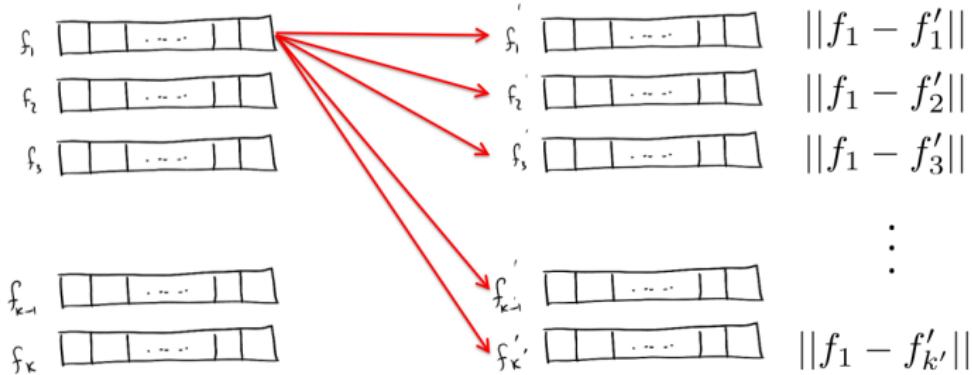
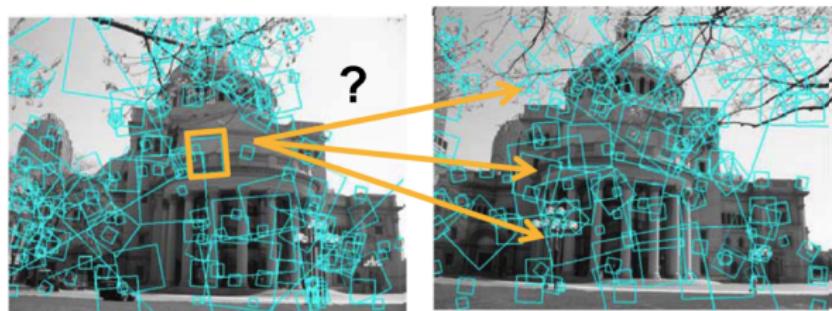
$$f_k \quad \boxed{\text{---}}$$

$$f'_{k-1} \quad \boxed{\text{---}}$$

$$f'_{k'} \quad \boxed{\text{---}}$$

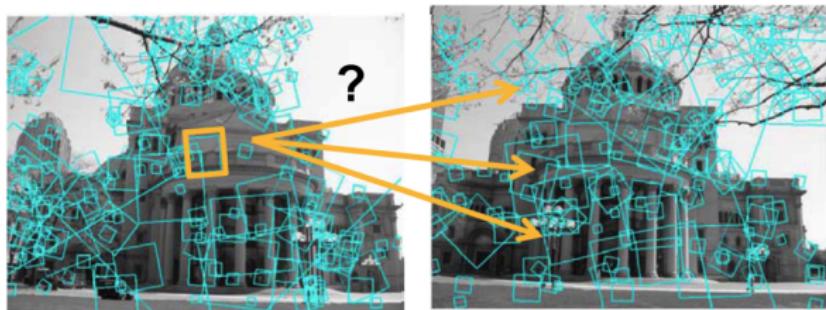
# Matching the Local Descriptors

- Simple: **Compare them all**, compute Euclidean distance



# Matching the Local Descriptors

- Find closest match (min distance). How do we know if match is **reliable**?



$$f_1 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f_2 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f_3 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f_{k1} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f_{kk'} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f'_1 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}} \quad ||f_1 - f'_1||$$

$$f'_2 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}} \quad ||f_1 - f'_2||$$

$$f'_3 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}} \quad ||f_1 - f'_3||$$

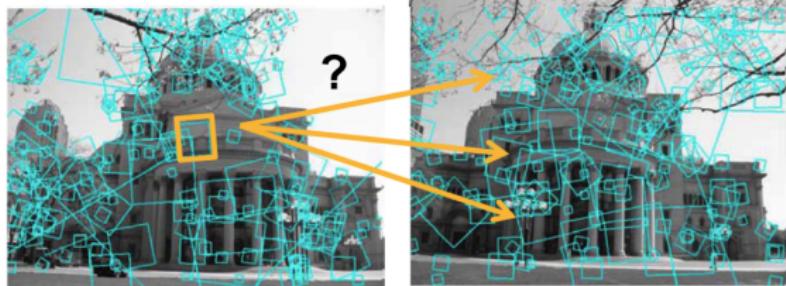
min (closest match)

$$f'_{k1} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}}$$

$$f'_{kk'} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & & \\ \hline & & & \\ \hline \end{array}} \quad ||f_1 - f'_{kk'}||$$

# Matching the Local Descriptors

- Find also the second closest match. Match reliable if first distance "much" smaller than second distance



$$f_1 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}}$$
$$f_2 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}}$$
$$f_3 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}}$$

$$f_{k-1} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}}$$
$$f_k \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}}$$

$$f_1 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}} \quad ||f_1 - f'_1||$$
$$f_2 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}} \quad ||f_1 - f'_2||$$
$$f_3 \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}} \quad ||f_1 - f'_3||$$

min (closest match)

$$f'_{k-1} \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}} \quad ||f_1 - f'_{k-1}||$$
$$f'_k \quad \boxed{\begin{array}{|c|c|c|c|} \hline & & \dots & \dots \\ \hline \end{array}} \quad ||f_1 - f'_k||$$

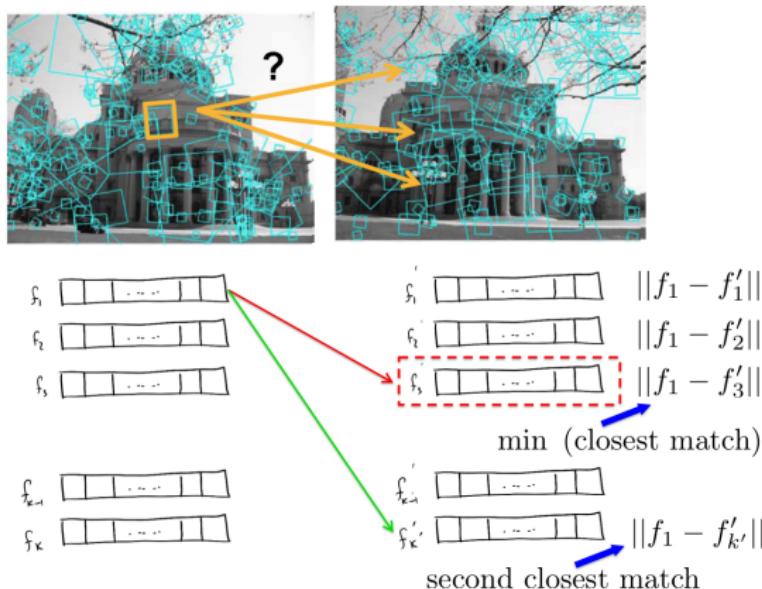
second closest match

# Matching the Local Descriptors

- Compute the ratio:

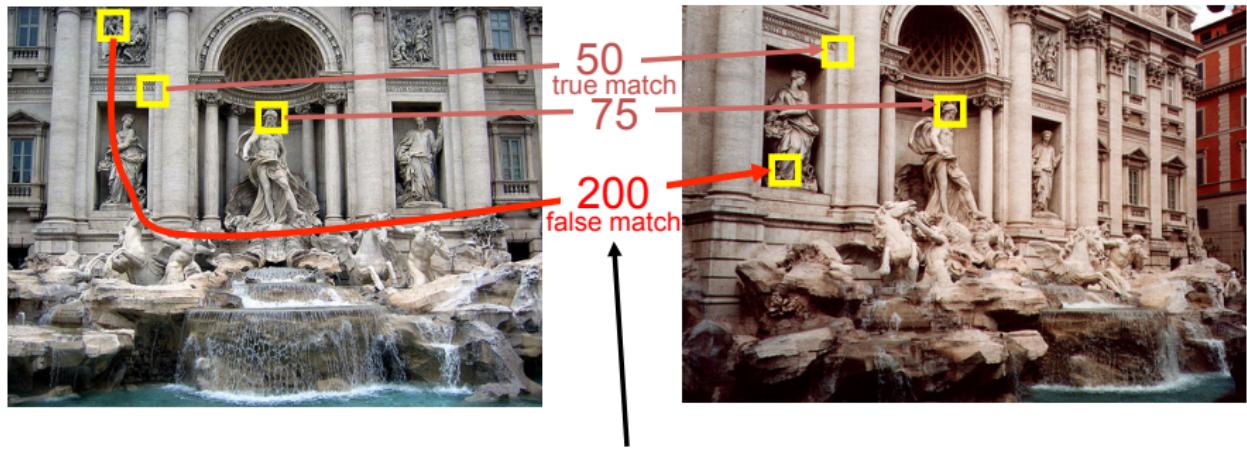
$$\phi_i = \frac{\|f_i - f'^*_i\|}{\|f_i - f'^{**}_i\|}$$

where  $f'^*_i$  is the closest and  $f'^{**}_i$  second closest match to  $f_i$ .



# Which Threshold to Use?

- Setting the threshold too high results in too many false positives, i.e., incorrect matches being returned.
- Setting the threshold too low results in too many false negatives, i.e., too many correct matches being missed



[Source: N. Snavely]

# Which Threshold to Use?

- Threshold ratio of nearest to 2nd nearest descriptor
- Typically:  $\phi_i < 0.8$

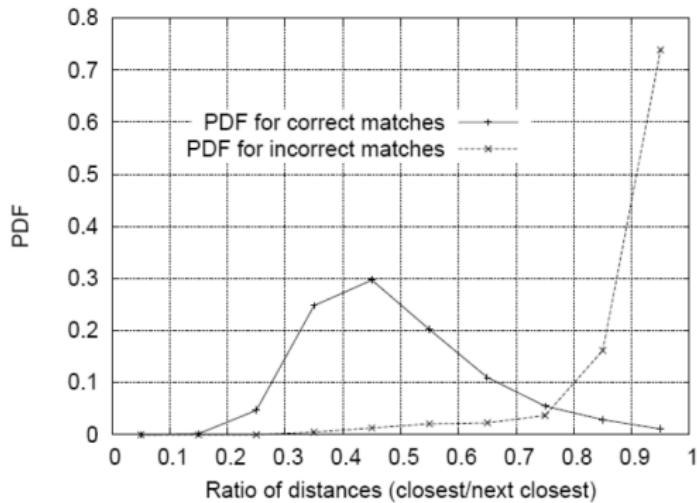


Figure: Images from D. Lowe

[Source: K. Grauman]

# Applications of Local Invariant Features

- Wide baseline stereo
- Motion tracking
- Panorama stitching
- Mobile robot navigation
- 3D reconstruction
- Recognition
- Retrieval

[Source: K. Grauman]

# Wide Baseline Stereo



[Source: T. Tuytelaars]

# Motion Tracking



Figure: Images from J. Pilet

# Now What

- Now we know how to extract scale and rotation invariant features
- We even know how to match features across images
- Can we use this to find Waldo in an even more sneaky scenario?

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template

Waldo on the road

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template

He comes closer... We know how to solve this

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template

Someone takes a (weird) picture of him!

# Find My DVD!

- More interesting: If we have DVD covers (e.g., from Amazon), can we match them to DVDs in real scenes?

