

## Problem 1.1 solution

Given,

Graph  $G = (V, E)$  with

$V = \{a, b, c, d, e, f\}$

$E = \{(a,b), (a,e), (a,f), (b,c), (b,f), (c,d), (c,f), (d,e), (d,f), (e,f)\}$

Now, let's construct a spanning tree  $G(V, E')$  using Kruskal's algorithm

<b>Start</b>	$E = \{\}$ $A = \{\{a\}, \{b\}, \{c\}, \{d\}, \{e\}, \{f\}\}$	$C=0$
<b>Step 1:</b>	$E = \{(a, f)\}$ $A = \{\{a, f\}, \{b\}, \{c\}, \{d\}, \{e\}\}$	$C=1$
<b>Step 2:</b>	$E = \{(a, f), (b, c)\}$ $A = \{\{a, f\}, \{b, c\}, \{d\}, \{e\}\}$	$C=3$
<b>Step 3:</b>	$E = \{(a, f), (b, c), (d, e)\}$ $A = \{\{a, f\}, \{b, c\}, \{d, e\}\}$	$C=6$
<b>Step 4:</b>	$E = \{(a, f), (b, c), (d, e), (d, f)\}$ $A = \{\{a, f, d, e\}, \{b, c\}\}$	$C=10$
<b>Step 5:</b>	$E = \{(a, f), (b, c), (d, e), (d, f), (c, f)\}$ $A = \{\{a, f, d, e, b, c\}\}$	$C=15$
<b>End</b>	$E = \{(a, f), (b, c), (d, e), (d, f), (c, f)\}$ $V = \{a, b, c, d, e, f\}$	$C=15$

Hence, the minimum value of the cost function is 15.

## Problem 1.2 Solution

Given:

$\Sigma = \{L, R, F, P\}$

$t = \text{FFLFLFRFRFFLFRF}$

$n = 15$  (length of text  $t$ )

$p = \text{FFLFR}$

$m = 5$  (length of pattern  $p$ )

### 1.2a solution)

Using naïve string search algorithm,

FFLFLFRFRFFLFRF

FFLFR

FFlfr

Fflfr

FFlfr

Fflfr

FFlfr

Fflfr

FFlfr

Fflfr

FFLFR

No. of alignments = 10

No. of comparisons = 22

### 1.2a solution)

Using Boyer-Moore bad character rule algorithm,

```
FFLFLFRFRFFLFRF
fflfr
  FFLFR
    fflfr
      ffLFR
        fflfr
          FFLFR
```

No. of alignments = 6

No. of comparisons = 16

### 1.2c solution)

Post. Σ \	F 0	F 1	L 2	F 3	R 4
F	-	-	0	-	0
L	0	1	-	0	1
R	0	1	2	3	-
P	0	1	2	3	4

Positions of Pattern p FFLFR  
01234

No. of alignments that can  
be skipped if comparison  
does not match.

“-” means Comparison matches

The values in the table denote the number of alignments that can be skipped if there is a mismatch. Hyphen means the comparisons match.

## Problem 1.3 solution

### 1.3a Answer

The operators which are neither right associative nor left associative are called non-associative operators. If such operators having same precedence level appear multiple times in an expression, then we will get a **precedence error**. The non-associative operators in Haskell are ==, /=, <, <=, >=, > which have precedence level 4.

e.g.

In [1]: 3 == 5 <= 4 /= 5



Cannot decide which operator to execute first because they are non-associative and have same precedence level.

### 1.3b Answer)

The precedence of \$ is zero in Haskell and it is **right associative**.

The infix notation of (^) 2 \$ (\*) 5 \$ (+) 2 3 is 2^(5\*(2+3)).