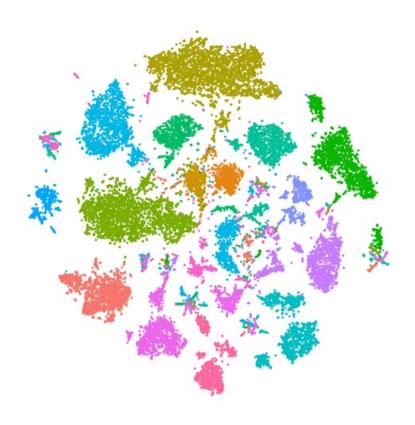
Trajectory Inference

Ahmed Mahfouz

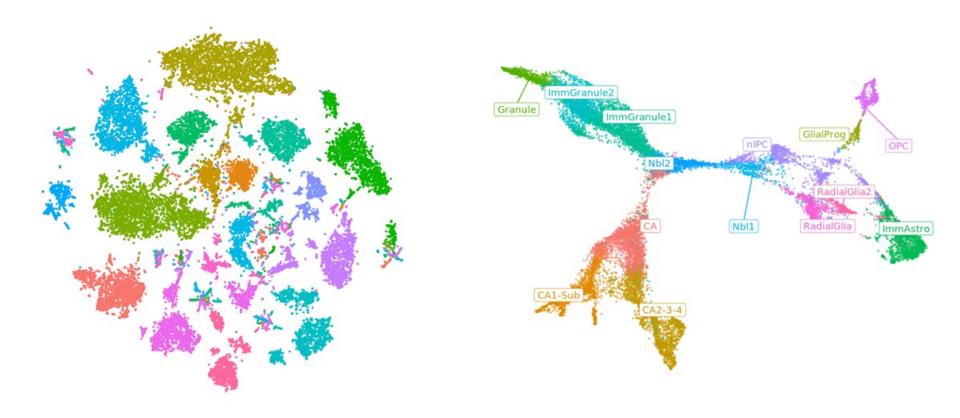
Department of Human Genetics, Leiden University Medical Center Pattern Recognition and Bioinformatics, TU Delft



Clustering of differentiating cells

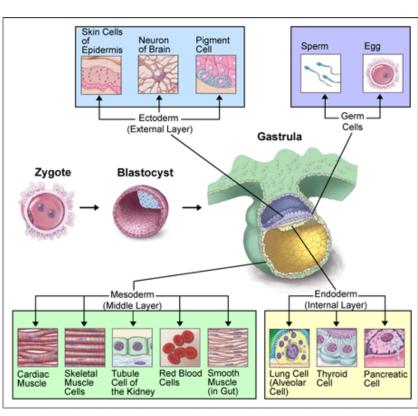


Clustering of differentiating cells



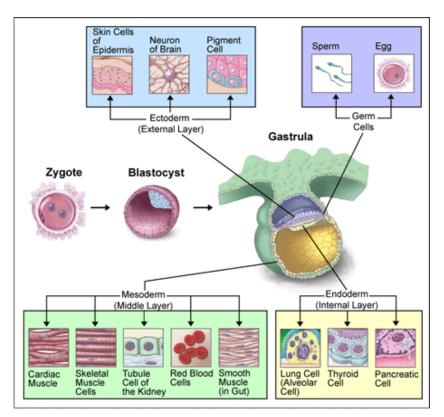
When do continuous structures pop up?

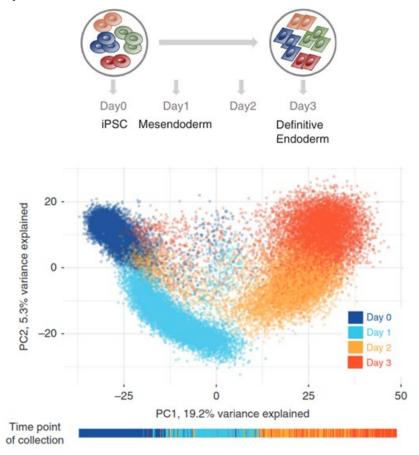
Embryonic development



When do continuous structures pop up?

Embryonic development



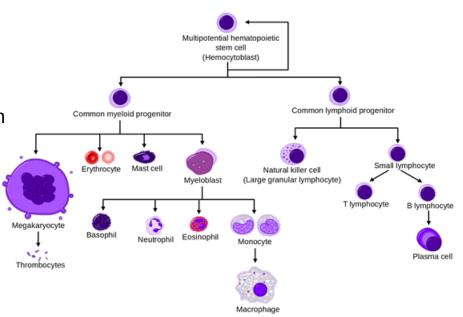


When do continuous structures pop up?

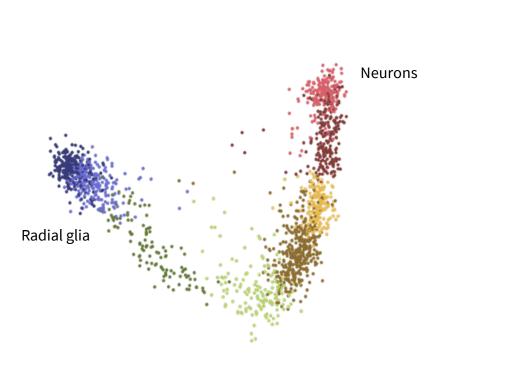
Cell differentiation

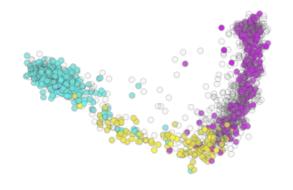
- Individual cells will differentiate in an unsynchronized manner
- Each cell is a snapshot along the differentiation trajectory

Hematopoiesis



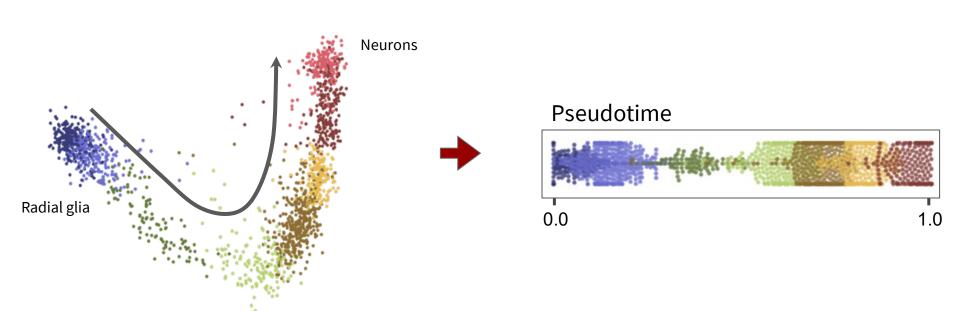
Trajectory inference / pseudotime inference





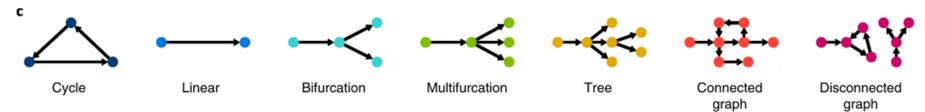


Trajectory inference / pseudotime inference



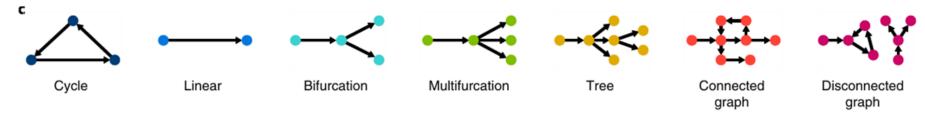
Trajectory structure

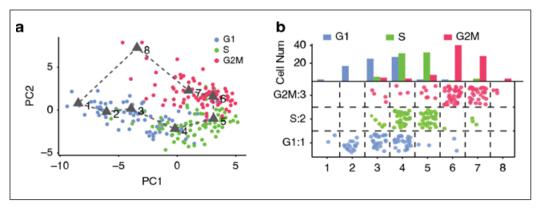
Saelens et al. (https://doi.org/10.1038/s41587-019-0071-9)



Trajectory structure

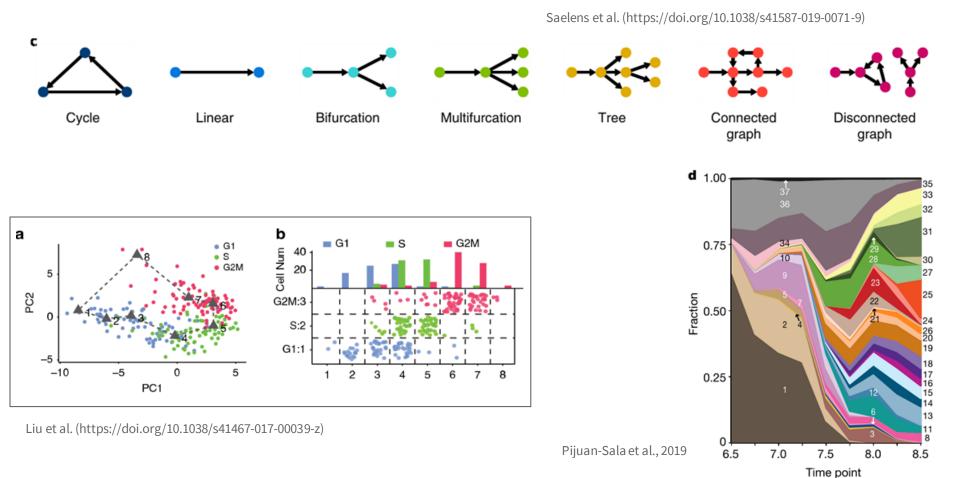
Saelens et al. (https://doi.org/10.1038/s41587-019-0071-9)





Liu et al. 2017

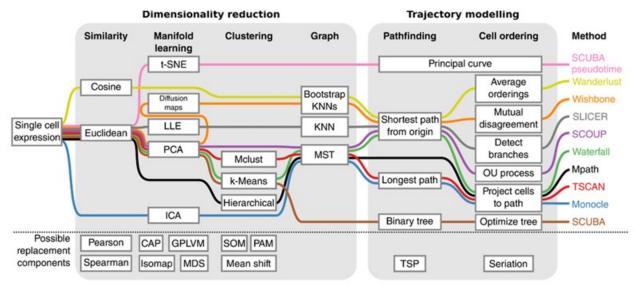
Trajectory structure



Methodology

General trajectory inference pipeline

- 1. Dimensionality reduction
- 2. Trajectory fitting
- 3. Pseudotime assignment



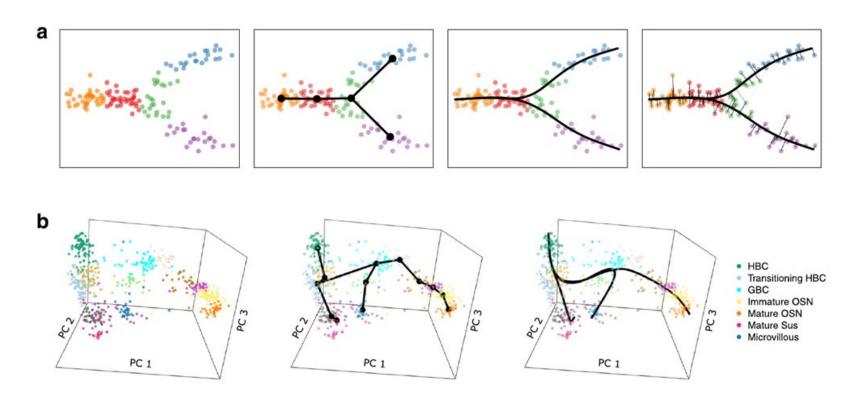
Trajectory inference methods

Four methods will be discussed

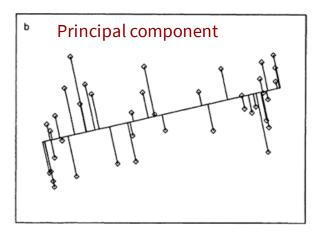
- Monocle 1, Slingshot Trapnell et al., 2014, Street et al., 2018
 - o Apply the general pipeline of dimensionality reduction, curve fitting, and pseudotime assignment
- Monocle 2 Cole et al., 2017
 - A popular tool in trajectory inference
- Ouija Campbell et al., 2018
 - Gene-based fitting
- RNA velocity La Manno et al., 2018
 - O Biologically-driven identification of trajectories

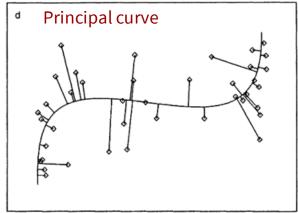
Slingshot

Fit multiple principle curves simultaneously, ensuring a shared trunk



Principle curves





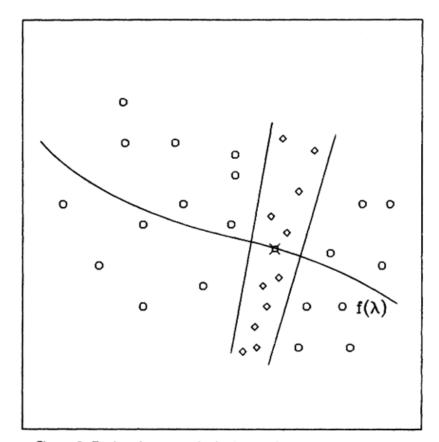
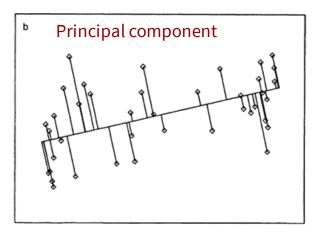
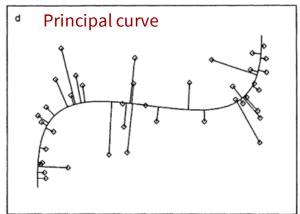


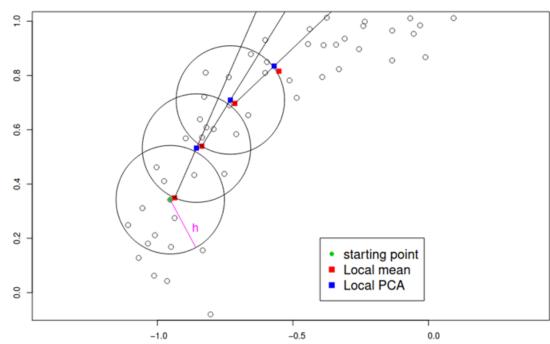
Figure 3. Each point on a principal curve is the average of the points that project there.

Principle curves



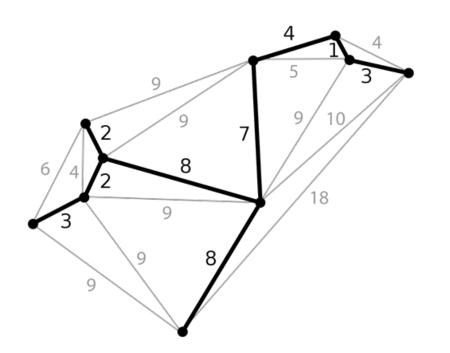


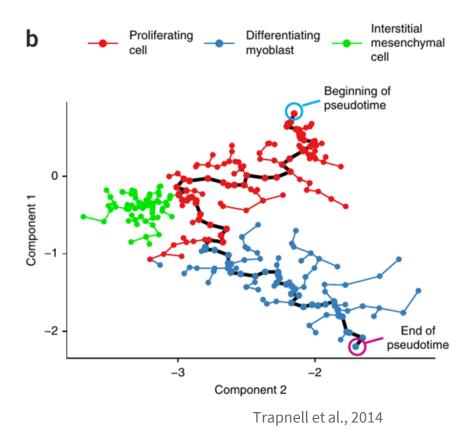




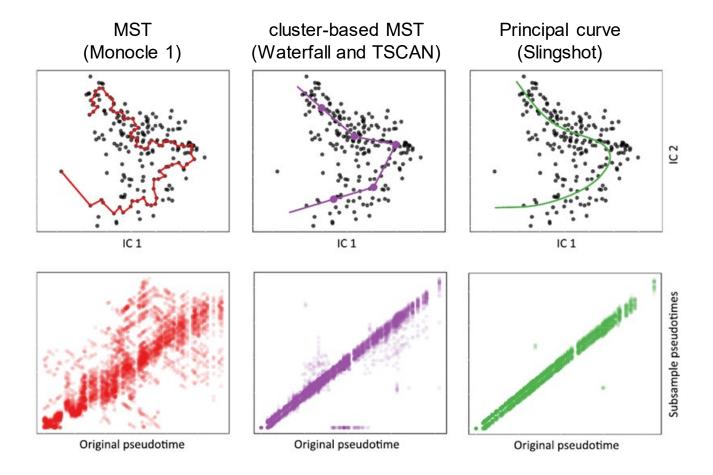
Monocle 1

Minimum spanning tree (MST)



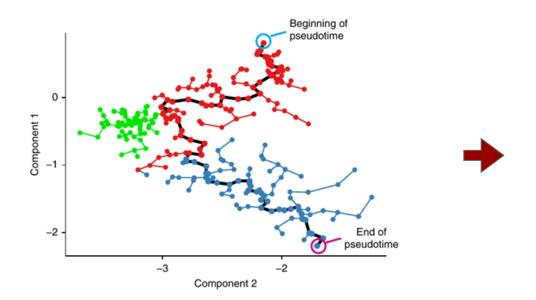


Robustness: principal curves vs MST

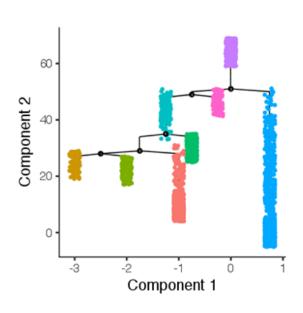


Monocle 2

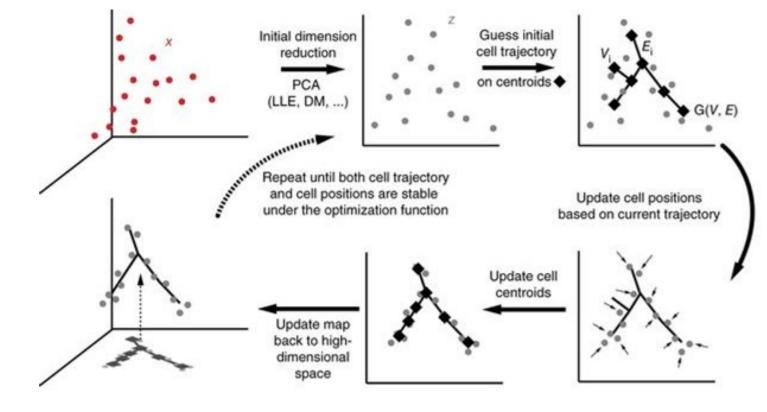
- Successor to Monocle 1
- End goal: Fit any arbitrary graph on the data
 - O Curves, bifurcations, loops





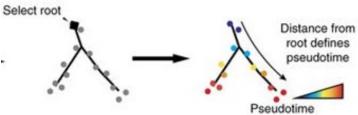


Monocle 2



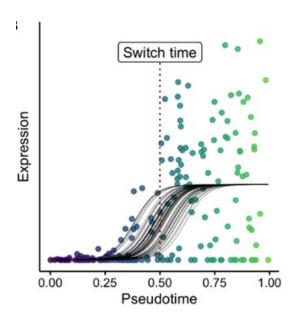
$$\min_{\boldsymbol{W}, \boldsymbol{B}, \boldsymbol{R}, \boldsymbol{Y}, \mathcal{Z}} \sum_{i=1}^{N} ||\boldsymbol{x}_{i} - \boldsymbol{W}\boldsymbol{z}_{i}||^{2} + \frac{\lambda}{2} \sum_{k, k'} b_{k, k'} ||\boldsymbol{W}\boldsymbol{y}_{k} - \boldsymbol{W}\boldsymbol{y}_{k'}||^{2}$$

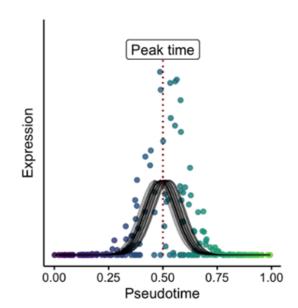
$$+ \gamma \left[\sum_{k=1}^{K} \sum_{i=1}^{N} r_{i, k} (||\boldsymbol{z}_{i} - \boldsymbol{y}_{k}||^{2} + \sigma \log r_{i, k}) \right]$$



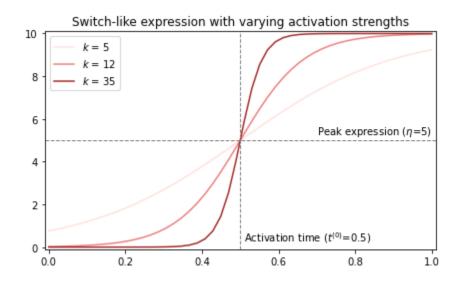
Ouija

- Model a small set of marker genes instead of fitting trajectory on complete transcriptome
- Switch focus to interpretability

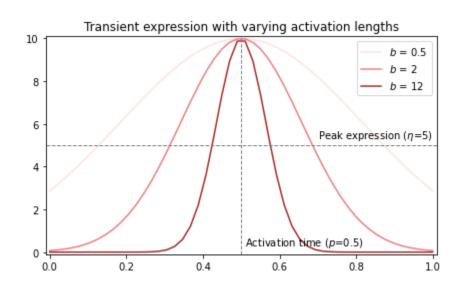




Interpretable function parameters



$$f(t)=rac{2\eta}{1+\exp(-k(t-t^0))}$$



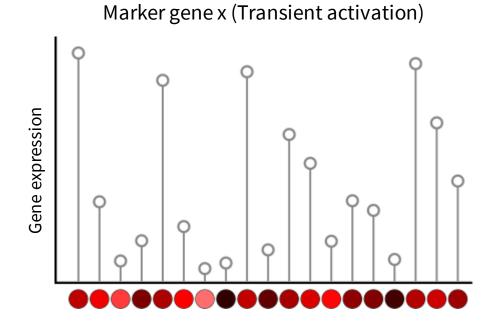
$$f(t) = \eta \cdot \exp(b \cdot (t-p)^2)$$

Ouija intuition

True ordering:

Random cell ordering:

Goodness-of-fit: low

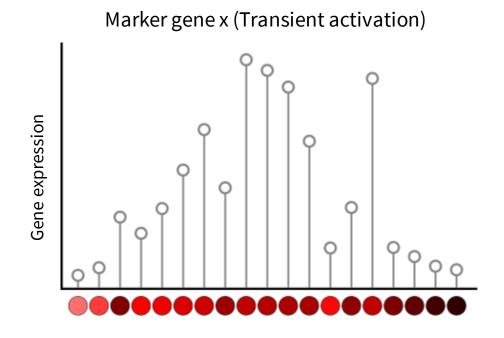


Ouija intuition

True ordering:

Optimize iteration: 100

Goodness-of-fit: mid

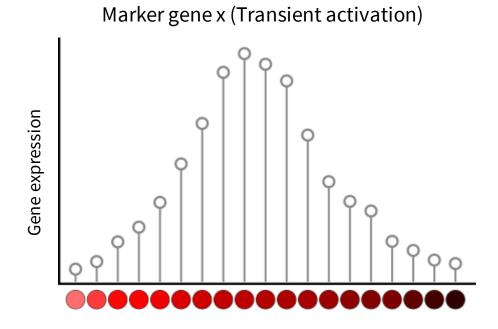


Ouija intuition

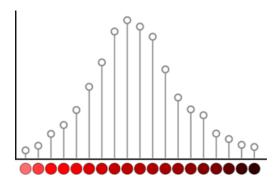
True ordering:

Optimize iteration: 500

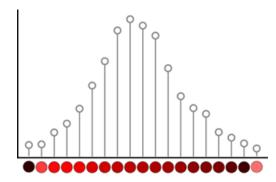
Goodness-of-fit: high



Marker gene x

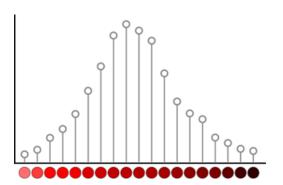


Goodness-of-fit: high

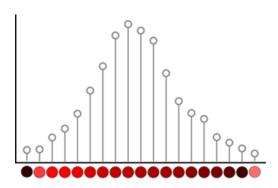


Goodness-of-fit: high

Marker gene x

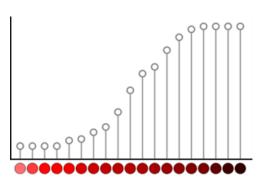


Goodness-of-fit: high

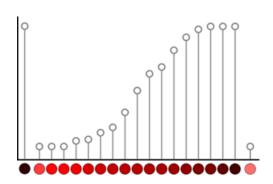


Goodness-of-fit: high

Marker gene y

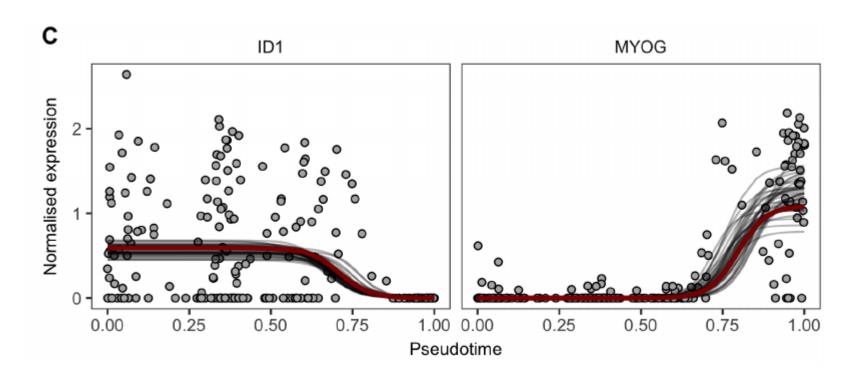


Goodness-of-fit: high



Goodness-of-fit: mid

Ouija probabilistic modelling



Fundamental limits on dynamic inference from single-cell snapshots

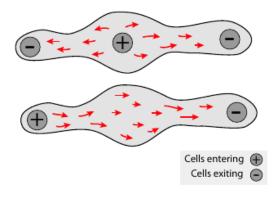
Caleb Weinreb^a, Samuel Wolock^a, Betsabeh K. Tusi^b, Merav Socolovsky^b, and Allon M. Klein^{a,1}

"The general challenge, even with perfect data, is that many regulatory mechanisms can generate the same dynamic process, and many dynamic processes can give rise to the same distribution."

No unique solution



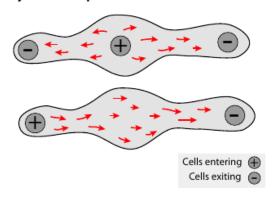
Entry and exit points direct the flow of cells



No unique solution



Entry and exit points direct the flow of cells



Rotations in state space do not alter cell density

Simple fluctuations

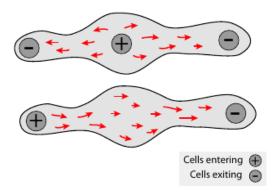


Periodic oscillations

No unique solution

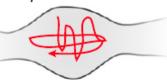


Entry and exit points direct the flow of cells



Rotations in state space do not alter cell density

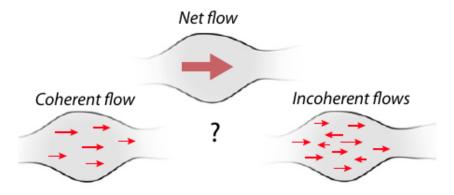


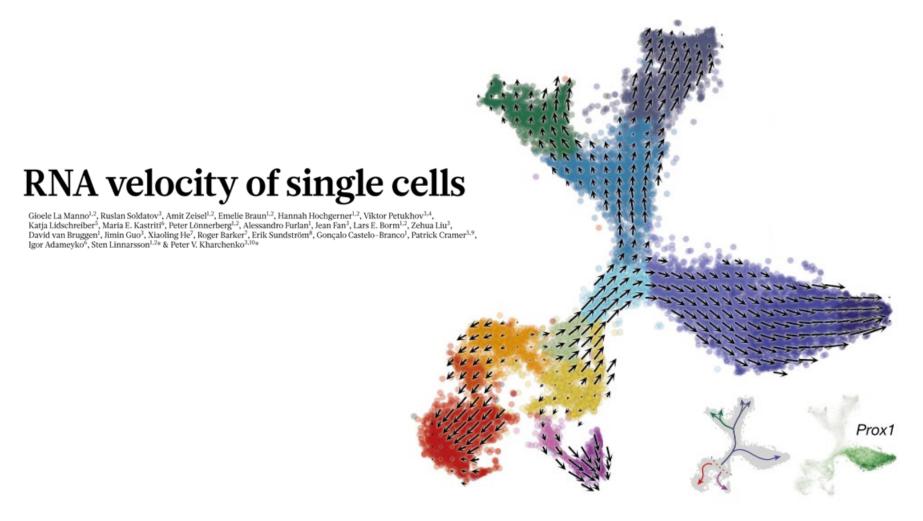


Periodic oscillations



Net velocity may not equal actual velocity

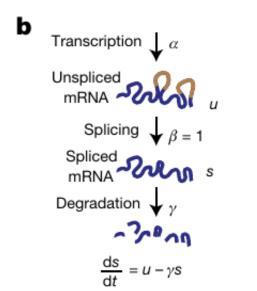


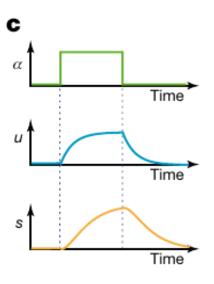


RNA velocity of single cells

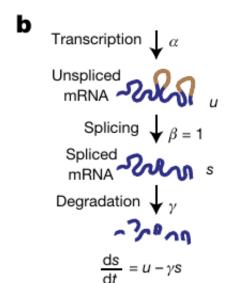
Transcription $\int \alpha$ Unspliced mRNA u Splicing $\oint \beta = 1$ Degradation ψ_{γ}

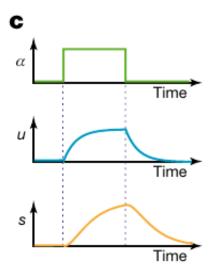
RNA velocity of single cells





RNA velocity of single cells

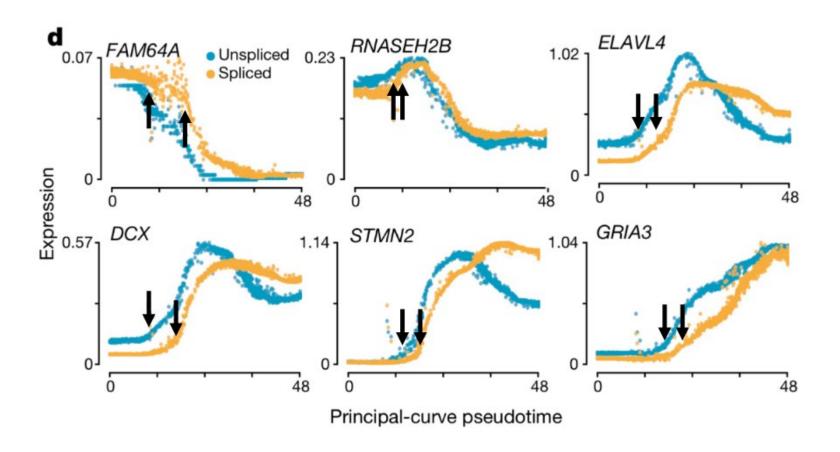




The ratio unspliced-to-spliced is proportional to length of (de)activation of a gene

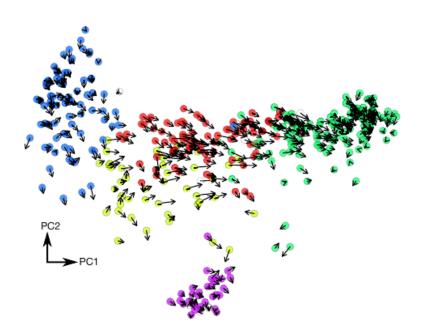
- u/s > 1: gene was recently activated
- u/s < 1: gene was recently deactivated

RNA velocity of single cells



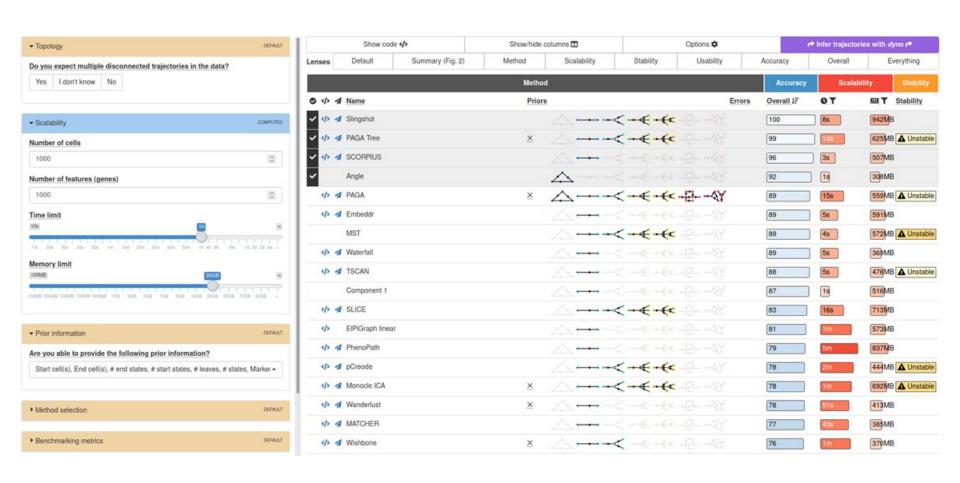
RNA velocity of single cells

- The velocity of a gene is the predicted increase or decrease of its expression in the cell
- Used to extrapolate future state of a cell



Which method should you use?

http://guidelines.dynverse.org/

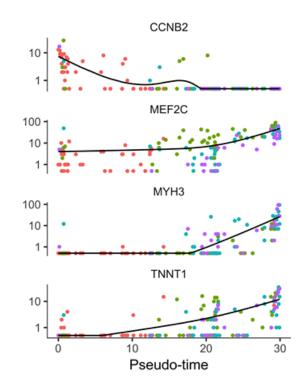


Pseudotime analysis

Interpretation of gene behaviour

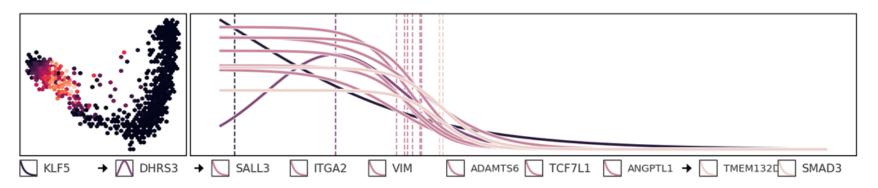
- Plot the gene expression as a function of pseudotime
- What do we see?

Pseudotime-gene expression pattern



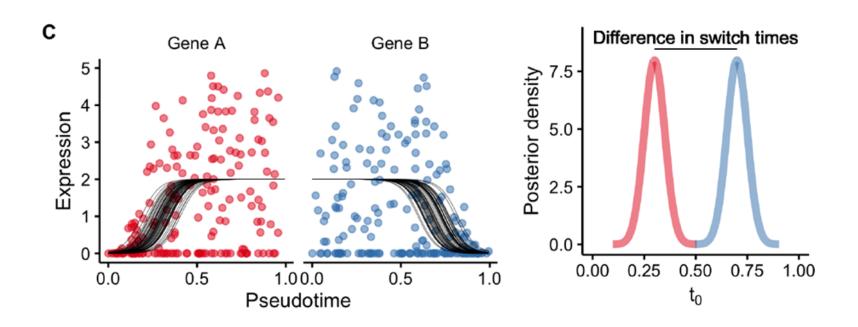
Interpretation of gene behaviour

Charrout et al., 2020

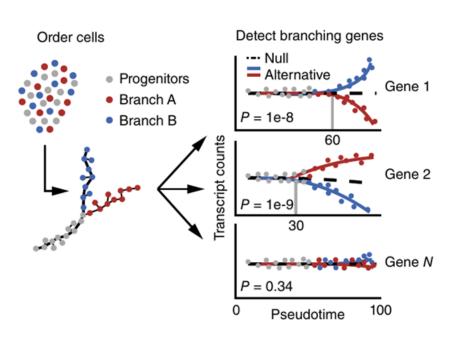


- KLF5 member of Kruppel-like family of transcription factors
 - Repressor of neurite growth, down-regulation linked to cell cycle arrest
- VIM, highly variable gene
 - Known marker of gliogenesis

Differential activation testing



Branch-dependent gene expression



Null model:

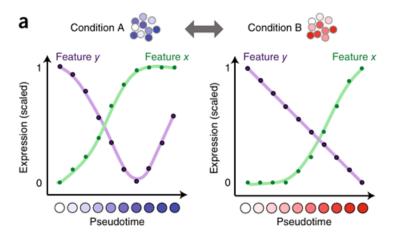
y ~ pseudotime

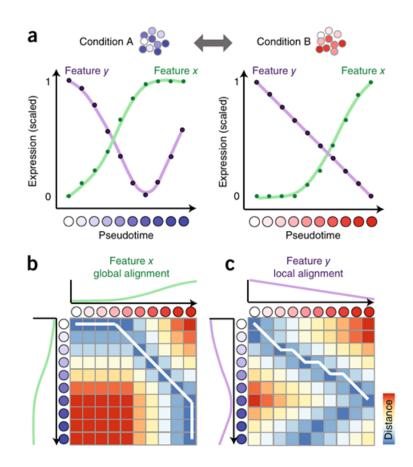
Alternative model:

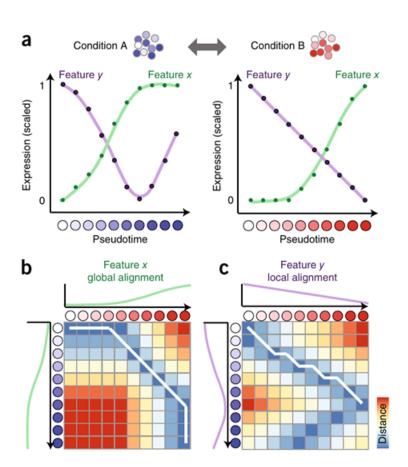
y ~ pseudotime + branch + pseudotime:branch

Likelihood ratio test:

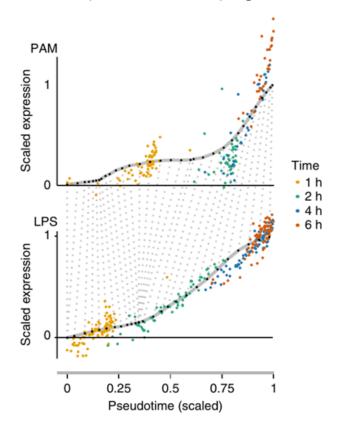
ratio = L(alternative) / L(null) if ratio >= 0 -> branch-dependent expression



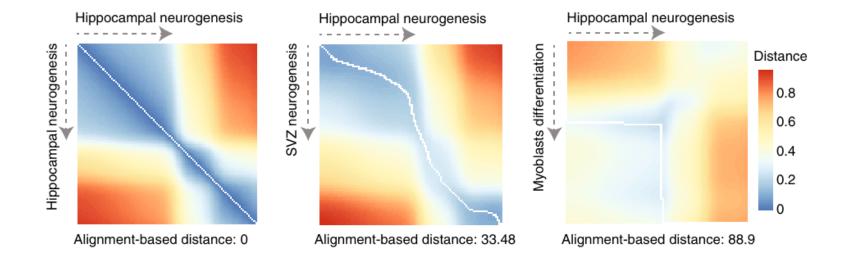




Dynamic time warping

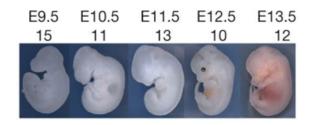


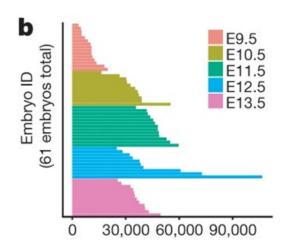
"CellAlign", Alpert et al., 2018

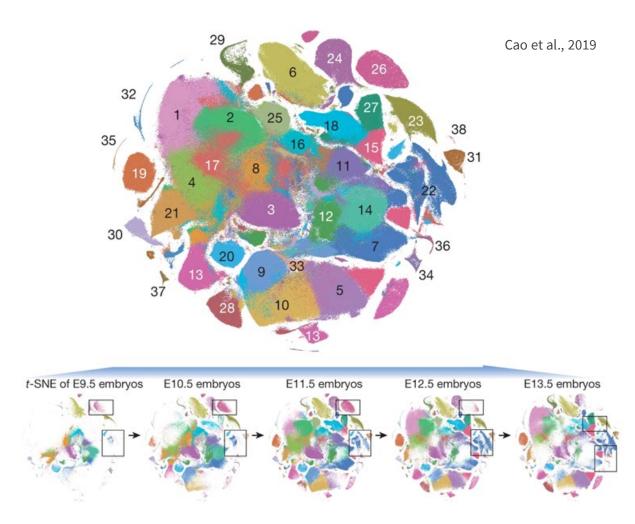


Applications

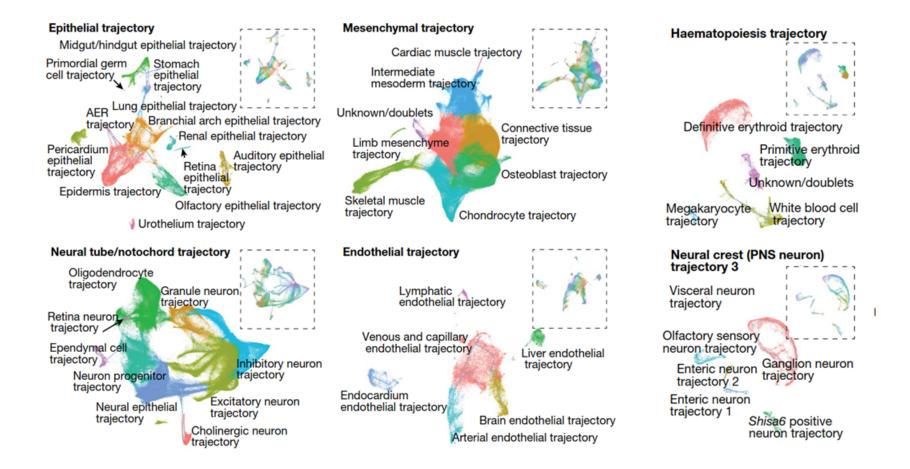
Mouse embryogenesis



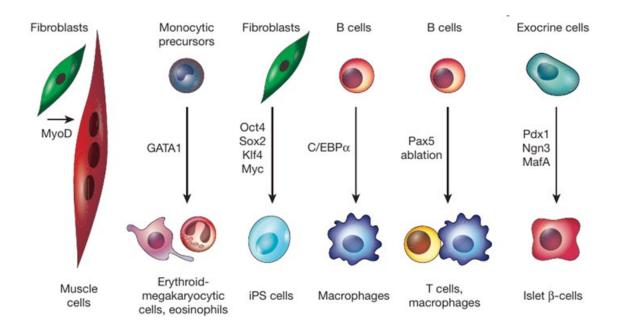




Mouse embryogenesis

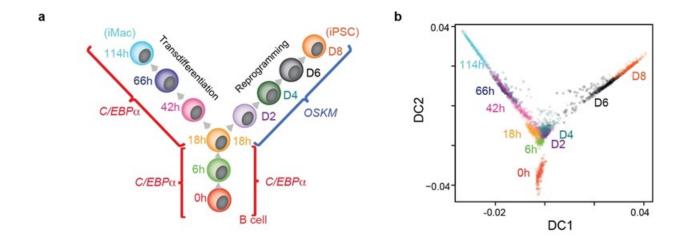


Transcription factors overexpression / silencing results in transdifferentiation:

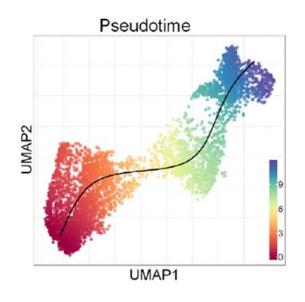


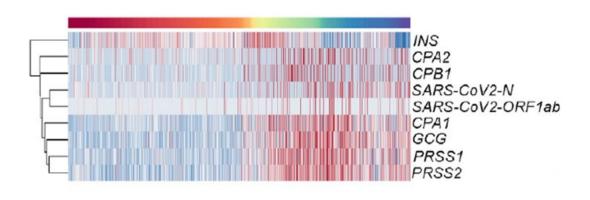
Efficiency of transdifferentiation

- Overexpression of C/EBPa (macrophages) and OSKM (iPSC) in B cells
- Homogenous final cell population, but variability in speed of differentiation
- Linked to Myc expression in initial state of the B cells



• COVID infected patients show a beta-to-alpha cell trans-differentiation in pancreatic islets





Thank You!

- a.mahfouz@lumc.nl
- mahfouzlab.org
- @ahmedElkoussy

