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Decision Boundary

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In order to get our discrete 0 or 1 classification, we can translate the output of the hypothesis function as follows:

$$h_{ heta}(x) \geq 0.5
ightarrow y = 1 \ h_{ heta}(x) < 0.5
ightarrow y = 0$$

The way our logistic function g behaves is that when its input is greater than or equal to zero, its output is greater than or equal to 0.5:

$$g(z) \ge 0.5$$
 when $z > 0$

Remember.

$$egin{aligned} z = 0, e^0 = 1 &\Rightarrow g(z) = 1/2 \ z & o \infty, e^{-\infty} & o 0 \Rightarrow g(z) = 1 \ z & o -\infty, e^\infty & o \infty \Rightarrow g(z) = 0 \end{aligned}$$

So if our input to g is $\theta^T X$, then that means:

$$h_{ heta}(x) = g(heta^T x) \geq 0.5 \ when \ heta^T x \geq 0$$

From these statements we can now say:

$$\theta^T x \ge 0 \Rightarrow y = 1$$

 $\theta^T x < 0 \Rightarrow y = 0$

The **decision boundary** is the line that separates the area where y = 0 and where y = 1. It is created by our hypothesis function.

Example:

$$heta=egin{bmatrix} -1\ 0 \end{bmatrix}$$
 COURSEIG $y=1\ if\ 5+(-1)x_1+0x_2\geq 0 \ 5-x_1\geq 0 \ -x_1\geq -5 \ x_1\leq 5 \end{pmatrix}$

In this case, our decision boundary is a straight vertical line placed on the graph where $x_1=5$, and everything to the left of that denotes y = 1, while everything to the right denotes y = 0.

Again, the input to the sigmoid function g(z) (e.g. $\theta^T X$) doesn't need to be linear, and could be a function that describes a circle (e.g. $z=\theta_0+\theta_1x_1^2+\theta_2x_2^2$) or any shape to fit our data.

Mark as completed

