

COMP 302 A5

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Q.1.1

$$FV(e_1, e_2) = FV(e_1) \cup FV(e_2) \quad (\text{pair})$$

$$FV(\text{let } (x, y) = e_1 \text{ in } e_2 \text{ end}) = FV(e_1) \cup (FV(e_2) / \{x, y\}) \quad (\text{match})$$

Q1.3

$$[e'/x](e_1, e_2) = ([e'/x]e_1, [e'/x]e_2) \quad (\text{pair})$$

$$[e'/x](\text{let } (z, y) = e_1 \text{ in } e_2 \text{ end}) = \quad (\text{match})$$

$$\text{let } (z, y) = [e'/x]e_1 \text{ in } [e'/x]e_2 \text{ end}$$

$$\text{provided that } x \neq z, x \neq y, z \& y \notin FV(e')$$

$$z \notin FV(e'), y \notin FV(e')$$

Q1.5

$$\frac{\Gamma \vdash e_1 : T_1 \quad \Gamma \vdash e_2 : T_2}{\Gamma \vdash (e_1, e_2) : T_1 \times T_2} \quad (\text{pair})$$

$$\frac{\Gamma \vdash e_1 : T_1 \times T_2 \quad \Gamma, x : T_1, y : T_2 \vdash e_2 : T}{\Gamma \vdash \text{let } (x, y) = e_1 \text{ in } e_2 \text{ end} : T} \quad (\text{match})$$