Electron coupling to a waveguide mode

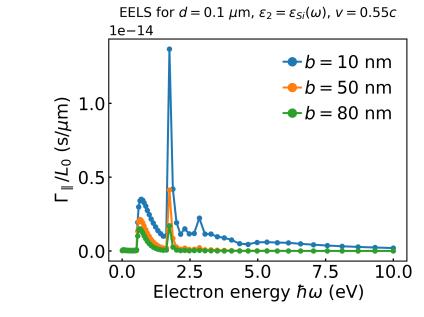
$$\frac{d\Gamma}{dy}(\mathbf{r},\omega) = \frac{2e^2}{\pi\hbar v^2} \int_0^\infty \frac{\mathrm{d}k_x}{k_\parallel^2} \mathrm{Re} \left\{ k_{z1} \mathrm{e}^{2\mathrm{i}k_{z1}z_\mathrm{e}(\mathbf{r})} \left[\left(\frac{k_x v}{k_{z1} c} \right)^2 r_{123}^\mathrm{s}(k_\parallel) - \frac{1}{\epsilon_1} r_{123}^\mathrm{p}(k_\parallel) \right] \right\}, \text{ \#paper149 Eq. (25)}$$

$$\Gamma(\omega) = \frac{2e^2}{\pi\hbar v^2} \int_0^\infty \frac{dk_x}{k_{\parallel}^2} \text{Re} \left\{ \int_{-\infty}^\infty dy \, e^{2ik_{z_1} z_e(y)} \, k_{z_1} \left[\left(\frac{k_x v}{k_{z_1} c} \right)^2 r_{123}^{\text{s}}(k_{\parallel}) - \frac{1}{\epsilon_1} r_{123}^{\text{p}}(k_{\parallel}) \right] \right\},\,$$

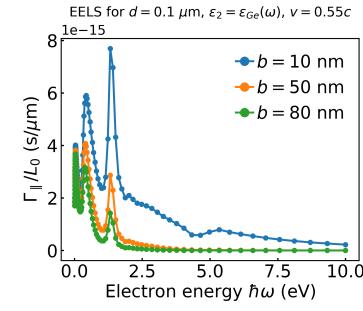
$$L^{\text{eff}}(k_{\parallel}) \approx L_0 e^{2ik_{z1}b} \sqrt{\frac{\beta q_0}{k_{\parallel}}},$$

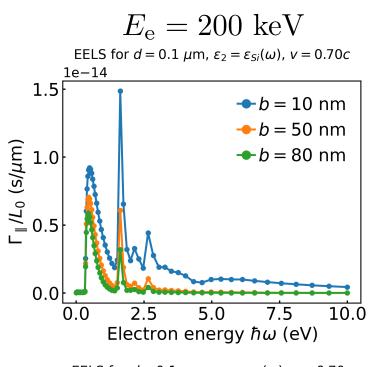
Si

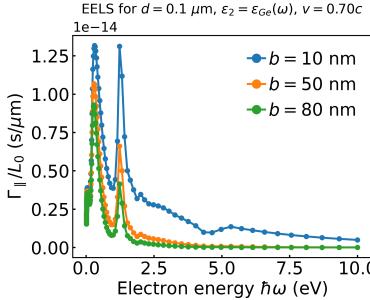
Ge

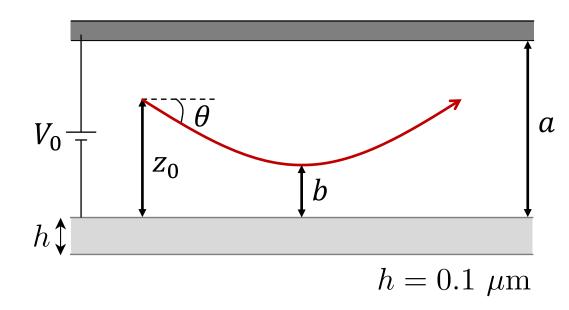


 $E_{\rm e} = 100 \, {\rm keV}$









 $L_0 = \sqrt{\hbar \pi a c / e V_0},$

$$q_0 = m_e v \gamma / \hbar, \ \beta = v / c.$$

