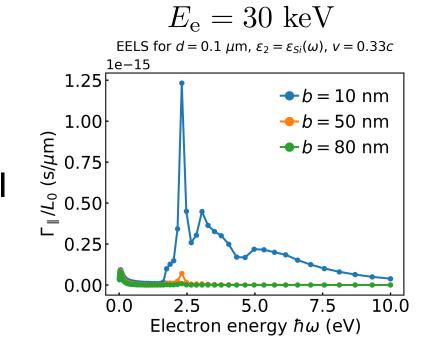
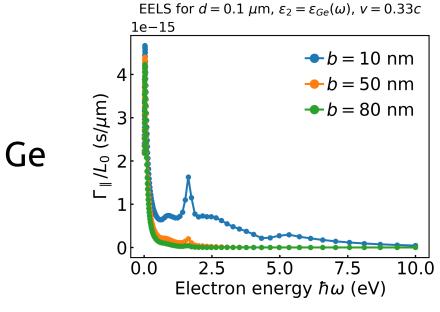
## Electron coupling to a waveguide mode

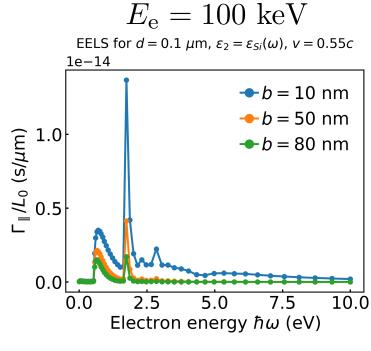
$$\frac{d\Gamma}{dy}(\mathbf{r},\omega) = \frac{2e^2}{\pi\hbar v^2} \int_0^\infty \frac{\mathrm{d}k_x}{k_{\parallel}^2} \mathrm{Re} \left\{ k_{z1} \mathrm{e}^{2\mathrm{i}k_{z1}z_{\mathrm{e}}(\mathbf{r})} \left[ \left( \frac{k_x v}{k_{z1} c} \right)^2 r_{123}^{\mathrm{s}}(k_{\parallel}) - \frac{1}{\epsilon_1} r_{123}^{\mathrm{p}}(k_{\parallel}) \right] \right\}, \text{\#paper149 Eq. (25)}$$

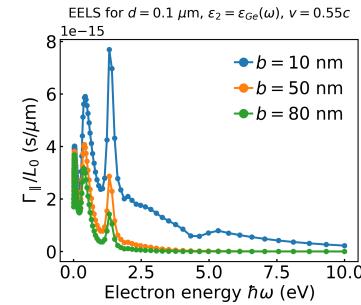
$$\Gamma(\omega) = \frac{2e^2}{\pi\hbar v^2} \int_0^\infty \frac{dk_x}{k_{\parallel}^2} \text{Re} \left\{ \underbrace{\int_{-\infty}^\infty dy \, e^{2ik_{z_1} z_e(y)}}_{\text{---}} k_{z_1} \left[ \left( \frac{k_x v}{k_{z_1} c} \right)^2 r_{123}^{\text{s}}(k_{\parallel}) - \frac{1}{\epsilon_1} r_{123}^{\text{p}}(k_{\parallel}) \right] \right\},\,$$

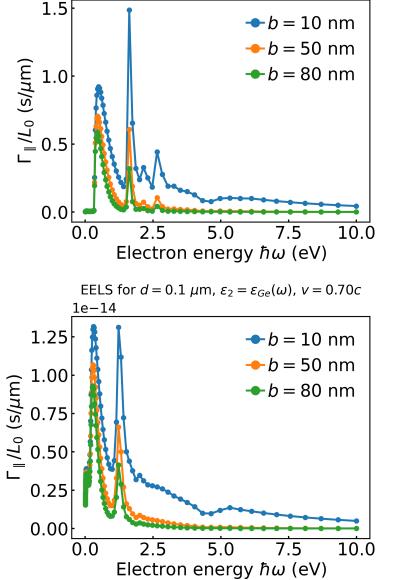
$$L^{\text{eff}}(k_{\parallel}) \approx L_0 e^{-2k_{\parallel}b} \sqrt{\frac{\beta q_0}{k_{\parallel}}},$$





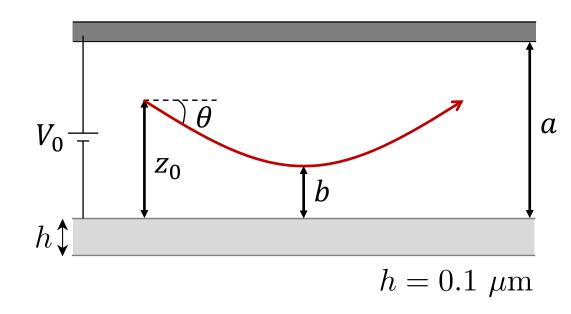






 $E_{\rm e} = 200 \; {\rm keV}$ 

EELS for  $d = 0.1 \mu \text{m}$ ,  $\varepsilon_2 = \varepsilon_{Si}(\omega)$ , v = 0.70c



$$L_0 = \sqrt{\hbar \pi a c / e V_0},$$
  $q_0 = m_{\rm e} v \gamma / \hbar, \ \beta = v / c.$ 

