

$$\Gamma_{\text{EELS}} = \frac{2}{\hbar} |\alpha|^2 \frac{2K^3}{3} |\vec{E}^{\text{ext}}|^2$$

$$\alpha = \frac{i3}{2K^3}$$

$$\text{Im}\{1/\alpha\} = -\frac{2K^3}{3}$$

$$\Gamma_{\text{EELS}} = \frac{1}{4\pi} \left(\frac{2e\omega}{v^2 \gamma} \right) f\left(\frac{\omega b}{v\gamma}\right) \text{Im}\{\alpha_{sp}\}$$

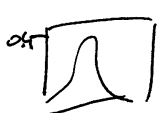
$$f(\gamma) = k_1^2(\gamma) + k_2^2(\gamma) / \gamma$$

$$\alpha_{sp} = a^3 \left(\frac{\epsilon - 1}{\epsilon + 2} \right)$$

$$\vec{k}_{\parallel} \cdot (\vec{R} - \vec{R}_0)$$

$$\frac{e^{iK|\vec{R} - \vec{R}_0|}}{|\vec{R} - \vec{R}_0|}$$

our derivation

$$\Gamma_{sp} =$$



$$\Gamma_{\text{EELS}} =$$

$$\Gamma_{sp} / \Gamma_{\text{EELS}} \approx 1$$

From #149 (dipole)

$$\Gamma_{sp} = \dots$$

$$\Gamma_{\text{EELS}} = \dots \text{Im}\{\alpha_{sp}\} f_{\gamma}(\gamma)$$

0.04  $\Gamma_{\text{EELS}} \ll \Gamma_{\text{sp}}$

$$(\vec{a} \otimes \vec{b}) \vec{c} = \vec{a} (\vec{b} \cdot \vec{c})$$

$$\vec{E}_p^+ (\vec{E}_p^+ \cdot \vec{p})$$

$$\vec{a} = (a_1, a_2, a_3)$$

$$\vec{b} = (b_1, b_2, b_3)$$

$$\begin{pmatrix} (a_1 b_1) & (a_1 b_2) & (a_1 b_3) \\ (a_2 b_1) & (a_2 b_2) & (a_2 b_3) \\ (a_3 b_1) & (a_3 b_2) & (a_3 b_3) \end{pmatrix} \begin{pmatrix} c_1 \\ c_2 \\ c_3 \end{pmatrix}$$

$$= \begin{pmatrix} a_1 (b_1 c_1 + b_2 c_2 + b_3 c_3) \\ a_2 (\dots) \\ a_3 (\dots) \end{pmatrix}$$

$$= \vec{a} (\vec{b} \cdot \vec{c})$$

$$(\vec{k}^2 + \vec{\nabla} \otimes \vec{\nabla}) \left(\begin{array}{c} - \\ \checkmark \\ i\vec{k} \end{array} \right)$$

$$E^{\text{ind}} = \textcircled{G} \vec{p}$$

$$k^2 (1 - \hat{k} \otimes \hat{k}) \left(\begin{array}{c} \\ \end{array} \right)$$