

A Four-stage Heuristic Algorithm for Solving On-demand Meal Delivery Routing Problem

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Abstract—Meal delivery services provided by platforms with integrated delivery systems are becoming increasingly popular. This paper adopts a rolling horizon approach to solve the meal delivery routing problem (MDRP). To improve delivery efficiency in scenarios with high delivery demand, multiple orders are allowed to be combined into one bundle with orders from different restaurants. Following this strategy, an optimization-based four-stage heuristic algorithm is developed to generate an optimal routing plan at each decision point. The algorithm first generates bundles according to orders’ spatial and temporal distribution. Secondly, we find feasible bundle pairs. Then, routes for delivering any single bundle or multiple bundles are optimized, respectively. Finally, the routes are assigned to available couriers. In computational experiments using instances from open datasets, the system’s performance is evaluated in respect of average click-to-door time and ready-to-pickup time. We demonstrate that this algorithm can effectively process real-time information and assign optimal routes to the couriers. By comparing the proposed method with existing the-state-of-the-art algorithms, the results indicate that our method can generate solutions with higher service quality and shorter distance.

Keywords—Meal delivery problem, pickup and delivery problem, rolling horizon method, heuristic algorithm.

I. INTRODUCTION

As the digital economy enables a variety of convenient daily services, the mobile app-based on-demand meal delivery market is booming worldwide. According to Statista [1], revenue in the online meal delivery industry is expected to grow at an annual rate of 9.9 percent from 2019 to 2023, bringing the market size to \$53.786 billion. Grubhub, Deliveroo and Uber Eats are just a few examples of these online food delivery platforms, a business model that is rapidly gaining popularity around the world.

With the rapid expansion of the market, growing competition arises among meal delivery platforms for providing services with higher quality and lower costs. Meal delivery platforms often encounter the following challenges when dealing with a large number of orders in reality. On the one hand, orders cannot be picked up on time or even cancelled

by limited service capacity. On the other hand, due to limited information perceived by couriers, a delivery route without optimization results in a longer detour time and thus lowers the system’s service efficiency. Therefore, many strategies have been implemented to efficiently group the orders into bundles and then optimize the delivery routes accordingly. So that it can help improve the system’s efficiency and reduce the cost.

The service requests of meal delivery routing problem (MDRP) are often has two important characteristics — dynamism and urgency [2]. Dynamism is defined by the fact that requests and system decisions are placed over time. Urgency indicates the high time sensitivity of the orders, which should be assigned and delivered within a short time window. The precise definition of these important concepts keeps evolving. In this paper, we use the definition from van Lon et al. [3]. They found that there is a nonlinear relationship between dynamism, urgency, and “cost”. This matches the work of Lund et al. [4] suggesting that as long as the optimization system receives requests before actual service time, despite a large number of dynamic requests, it is still possible to get a good solution.

A common strategy for solving such dynamic problems is incorporating rolling horizon technique in time-dependent model, i.e., optimizing tasks periodically [2, 5, 6]. The purpose of this study is to develop a heuristic algorithm for solving MDRP with a rolling horizon technique. To improve the delivery efficiency in scenarios with high service demand, the algorithm allows multiple bundles from different restaurants to be combined into a bundle pair and delivered on one route. In this paper, we limit the restaurant number of bundle pairs to two for the simplicity of the model.

In the existing literature, this Meal Delivery Routing Problem (MDRP) generally belongs to the category of Dynamic Vehicle Routing Problem (DVRP) and is closely related to the Dynamic Delivery Problem (DDP) [7]. It is one of the important classes of Dynamic Pickup and Delivery Problems (DPDP) that have emerged recently. In DPDP, the input data is real-time user requests. The solution strategy uses the dynamic information of requests to specify what actions should be performed over time [8]. As requests for on-demand services grow, many researchers are devoted to investigating on-demand

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dynamic delivery systems, not only from a theoretical [9,10,11], but also from a practical perspective [12,13,14].

Our algorithm is developed based on the meal delivery model proposed by [7]. The paper aims to find an exact solution to the delivery problem to minimize total service time of all orders with all order information known before optimization, which is far from reality. Our method is inspired by the pivotal work of [2]. One of the differences between our works lies in the generation of bundles. The bundle generation in [2]’s model is the result of a single-step optimization. In our model, we optimize bundle generation by considering orders’ temporal and spatial distribution. In addition, our model focuses on minimizing the freshness loss and maximizing the delivery volume per unit of time, while their model concerns more about the cost of couriers.

The main contributions of this paper are threefold: i) We propose a heuristic algorithm to deal with bundle generation, bundle pairing, route optimization, and task assignment in MDRP; ii) A comparison with an existing algorithm and exact solution is conducted for assessing system efficiency; iii) Computational results of our algorithm are presented for evaluating algorithm performances.

The remainder of this paper is organized as follows: Section II describes the problem formulation. A heuristic algorithm is developed in Section III to find optimal solutions. Section IV conducts result analysis on algorithm performance and system performance. Section V draws conclusions and provides an outlook for future works.

II. PROBLEM FORMULATION

Consider an on-demand meal delivery system served by a fleet of couriers, who are crowd-sourced freelancers and tend to work for a shift voluntarily. As orders arrive throughout a service day and order information is revealed dynamically, instructions are sent to couriers based only on known requests. In order to solve this dynamic problem, a rolling-horizon approach is adopted in this paper. We separate the whole service time evenly into multiple small time intervals of f minutes. The system is then optimized at the decision point t_{opt} , which is the end of each time interval.

For time interval $T = \{t: t_{opt} - f < t \leq t_{opt}\}$, orders placed in T or unserved in previous interval are waiting to be assigned at t_{opt} . R is the set of restaurants in the system. Each restaurant $r \in R$ has an associated location. U_r is the set of orders to be assigned at restaurant r . Taking order $o \in U_r$ as an example, its information includes placement timestamp P_o , associated restaurant R_o (which is r here), drop-off position D_o , and ready timestamp r_o . For courier c , information includes the start-timestamp S_c and the off-timestamp O_c of the day, as well as the current location of the courier L_c .

Two strategies are adopted in our method for improving delivery efficiency. One is that orders from a same restaurant are allowed to be grouped into a bundle, denoted as b , and delivered on one route. Here we call the timestamp r_o of the

latest ready order o in the bundle b as the bundle’s ready timestamp r_b . Note that any bundle b can only be picked up after its ready timestamp r_b . The other one is that up to two bundles from two different restaurants can be seen as a bundle pair and be delivered on one route.

An available courier that we can give instructions to at t_{opt} should be the courier c on duty ($S_c \leq t_{opt} \leq O_c$). In addition, he is neither en route to pick up orders nor delivering orders at this decision point. Note that a courier c cannot receive new instructions after his off-timestamp O_c but can keep delivering orders which are assigned before. After receiving instructions, couriers must take the bundles according to the instruction and deliver orders along the optimized route. In this paper, we consider a fixed pick-up service time when a courier is picking up a bundle in a restaurant. This service time is independent of the number of orders in the bundle. Similarly, a drop-off service time is counted on a courier’s arrival at a drop-off location.

For clarity, a flow chart to represent the problem sequence at a decision point is shown in Fig. 1. Fig. 2 demonstrates the timeline of events to deliver an order.

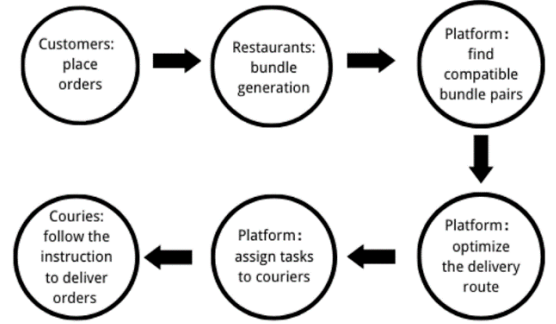


Fig. 1. Flow chart of problem sequence within one optimization

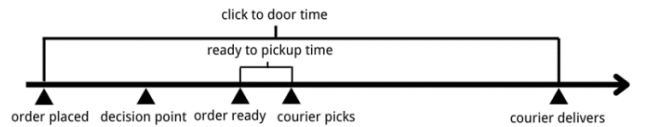


Fig. 2. Timeline of events to deliver an order

For the optimization at each decision point, we have two goals. The first is to improve delivery efficiency, which means that couriers can deliver more orders per unit time. The second is to reduce the freshness loss of orders.

Some important notations and related descriptions used in section III are listed below:

TABLE I. NOTATION AND DESCRIPTION

| Notation | Description |
|----------|--|
| U_r | Set of all orders which are placed in restaurant r |
| C | Set of all couriers available at this decision point |
| S | Set of bundles of all restaurants in the system |
| Q | Set of all single bundles and feasible bundle pairs |

| | |
|-------------|---|
| N_{total} | Total number of all orders placed in the system |
| $N_{o,r}$ | Total number of all orders placed in the restaurant r |
| N_d | Number of available couriers who are available at this decision point |
| $N_{d,r}$ | Number of available couriers who are available for restaurant r at this decision point |
| $N_{b,r}$ | Number of bundles in a restaurant |
| $N_{o,q}$ | Number of orders in a route q |
| r_b | Last ready timestamp of order in bundle b |
| r_o | Ready timestamp of order o |
| R_o | Associated restaurant of order o . |
| R_b | Associated restaurant of bundle b |
| R_q | Associated restaurant of route q |
| D_o | Drop-off position of order o . |
| $\Pi_{q,c}$ | Pick up timestamp if route q is assigned to courier c |
| β | Penalty parameter for the delivery delay |
| α | Pick up delay tolerance time |
| θ | Penalty parameter for freshness loss |
| o | Order |
| r | restaurant |
| c | Courier in set C |
| q | Single bundle or bundle pair in set Q with an optimized route (we also call it a "route" in this paper) |
| t | Deliver sequence number in the optimized route |

III. A HEURISTIC ALGORITHM FOR THE MEAL DELIVERY ROUTING PROBLEM

The algorithm for optimizing the delivery strategies can be divided into four steps. The first step is to combine unassigned orders into bundles for each restaurant. Secondly, the generated bundles are matched in pairs to find the feasible bundle pairs that can be picked up by one courier. Then, delivery routes of all generated bundles and bundle pairs are optimized to minimize delivery time. Finally, optimized routes are assigned to appropriate couriers.

A. Bundle Generation

To determine the number of bundles in restaurant r , we first give a rough estimation of the target bundle size K at t_{opt} as follows:

$$K = \frac{N_{total}}{N_d}$$

The value is then compared with the number of available couriers for this restaurant $N_{d,r}$ at this decision point. The smaller value is taken as the number of bundles $N_{b,r}$. This can help us avoid the situation that there are too many bundles to be taken by couriers. $N_{b,r}$ is defined as below:

$$N_{b,r} = \min \left\{ \frac{N_{o,r}}{K}, N_{d,r} \right\}$$

With a known target bundle number $N_{b,r}$ of restaurant r , we follow the steps below to get a bundle list for the restaurant.

1) Generating a Draft List of Bundles Considering Spatial Dimension

First, we set up a binary variable $B_{b,o}$. If and only if order $o \in U_r$ is in bundle b , $B_{b,o} = 1$. *Aggregation Cost* is defined below as the sum of the distance between the drop-off positions of any two orders in the bundle:

$$\begin{aligned} \text{Aggregation Cost}(b) &= \sum_{o_1 \in U_r} \sum_{o_2 \in U_r} \text{Distance}(D_{o_1}, D_{o_2}) * B_{b,o_1} \\ &\quad * B_{b,o_2} \end{aligned}$$

A draft list of bundles considering spatial dimension is generated when the sum of the aggregation cost of all bundles is minimized:

$$\text{Min } \sum_b \text{Aggregation Cost}(b) \quad (1a)$$

$$\text{s.t. } \sum_b B_{b,o} = 1, \forall o \in U_r \quad (1b)$$

Here (1b) indicates that each order can only appear in one bundle. According to the value of variables $B_{b,o}$, we can obtain a draft bundle list $B_{r,d}$ of the restaurant r . This list can tell us the order belonging to each bundle.

2) Further Optimizing Bundle List Considering Temporal Dimension

We have two objectives to consider in temporal dimension. One is to reduce the sum of delivery time of all bundles. The other is to reduce the sum of all orders' delay time. Combine these two objectives into one total objective function. Then we can optimize the draft bundle list $B_{r,d}$ in this Procedure 1.

Procedure 1: Further Optimization

Input: U_r , set of all orders which are placed in restaurant r .
 $B_{r,d}$, the draft bundle list which is generated above.

Output: $B_{r,new}$, improved list of bundles.

- 1: /* Initial construction
 - 2: $B_{r,new} \leftarrow B_{r,d}$
 - 3: $\text{Cost}(b) = \text{Sending_time}(b) + \beta * \sum_{o \in b} \text{Predict_delay}(o)$
 - 4: $\text{Temporal Cost} = \sum_{b \in B_r} \text{Cost}(b)$
 - 5: **For** $o \in U_r$ **do:**
 - 6: Remove o from its current bundle b_o
 - 7: List all bundles (which contains b_o), find a bundle b_{new} to re-insert o to achieve minimum *Temporal Cost*
 - 8: Update $B_{r,new}$ with inserting o into b_{new}
 - 9: **End**
 - 10: **return** $B_{r,new}$
-

3) Assign Priority Levels to Bundles

Based on the updated bundle list $B_{r,new}$, bundles are assigned priority levels according to the following rules:

- (1) The bundles with more orders have higher priority levels.
- (2) If two bundles with same number of orders, the one have earlier ready time has higher priority level.

When couriers are limited in the system, bundles with higher priority levels will be assigned first.

B. Combination of Feasible Bundle Pairs

Considering restaurants within the proximity, bundles of two restaurants are allowed to be grouped together for a higher delivery efficiency of a route. A bundle pair is regarded as feasible if its second bundle doesn't suffer an excessive detour on the route, i.e., the courier can get the second bundle within a tolerable delay time.

Procedure 2: Generate Feasible Bundle Pair

Input: S , set of all bundles in all restaurants,

α , pick up delay tolerance time ($\alpha \geq 0$)

Output: Set Q of singles bundles and bundle pairs to be assigned.

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1: /* Initial construction
2:  $P \leftarrow \emptyset$ 
3: For  $b1 \in S$  do:
4:   For  $b2 \in S \setminus \{b1\}$  do:
5:     If  $r_{b1} + \text{TravelTime}(R_{b1}, R_{b2}) \leq r_{b2} +$ 
        $\alpha$  then:
6:        $P \leftarrow P \cup \{b1, b2\}$ 
7:     End
8:   End
9: End
10:  $Q \leftarrow P \cup S$ 
11: return  $Q$ 

```

C. Calculation of Shortest Delivery Time of Bundles and Bundle Pairs

For $\forall q \in Q$, we follow the below steps to optimize the route. First, we define the variable:

$\gamma_{t,o} \in \{0, 1\}$, indicates whether the order o is delivered in sequence t in the route.

The optimization problem is formulated as:

$$\text{Min}(\sum_{o \in q} \text{Travel Time}(R_q, D_o) * \gamma_{1,o} + \sum_{t=1}^{N_{o,q}} \sum_{o2 \in q} \sum_{o1 \in q} \text{Travel Time}(D_{o1}, D_{o2}) * \gamma_{t,o1} * \gamma_{t,o2}) \quad (2a)$$

$$\text{s.t. } \sum_{o \in q} \gamma_{t,o} = 1, \forall t \in [1, Nq] \quad (2b)$$

$$\sum_{t=1}^{Nq} \gamma_{t,o} = 1, \forall o \in q \quad (2c)$$

Here constraints (2b) indicate that in each time sequence of delivery, the courier can deliver only one order. Constraints (2c) guarantee that each order can only be delivered once.

D. Assignment Model

Based on the set Q of available single bundles and bundle pairs and their optimized delivery route, tasks are assigned to available couriers. The goal of the assignment is to improve delivery efficiency and reduce the freshness loss of orders. We define the variable:

$X_{q,c} \in \{0, 1\}$, indicates whether route q is assigned to courier c .

The delivery efficiency E of courier c delivering route q is calculated as below:

$$E(q, c) = \frac{N_{o,q}}{(\Pi_{q,c} T_q - T_{optimize})}$$

It's important to note that the optimization time is ignored here, which means that all instructions are sent to couriers at the decision point immediately. We take the total time the courier needs to complete the task as the denominator.

Freshness loss FL is measured by the difference between the picks up timestamp of the final order and the last ready timestamp r_o of the latest ready order o in the route. It is given by:

$$FL(q, c) = \Pi_{q,c} - \max_{o \in q} \{r_o\}$$

Using these definitions, the optimization problem is formulated as:

$$\max \sum_c \sum_{q \in Q} [(E(q, c) - \theta * FL(q, c)) * X_{q,c}] \quad (3a)$$

$$\text{s.t. } \sum_{q \in Q} X_{q,c} \leq 1, \forall c \in C \quad (3b)$$

$$\sum_{c \in C} X_{q,c} \leq 1, \forall q \in Q \quad (3c)$$

$$\sum_{q \in Q(q)} X_{q,c} \leq 1, \forall q \in Q \quad (3d)$$

Constraints (3b) indicate that a courier can only choose one route. Constraints (3c) guarantee that a route can only be chosen by one courier. Constraints (3d) guarantee that the selected routes cannot contain the same bundles.

IV. COMPUTATIONAL STUDY

In this computational study section, two indexes are adopted to assess the algorithms and the dynamic system's performance:

- 1) The average click-to-door time (aCtD) of all orders assigned to couriers in the system. Click-to-door time (CtD) of an order indicates the difference between its drop-off timestamp and its placement timestamp.
- 2) The average ready-to-pickup time (aRtP) of all orders assigned to couriers in the system. Ready-to-pickup time (RtP) of an order indicates the difference between its pickup timestamp and its ready timestamp.

A. Algorithm Performance in Different Data Size Instances

We generate instances with order, restaurant and courier information based on open datasets provide by [15] to test the algorithm's performance. Table II shows the characteristics of the instances. Table III demonstrates the performance of the algorithm in different instances.

TABLE II. COMPARISON OF CHARACTERISTICS OF DIFFERENT INSTANCES

| Instance | Number of Orders | Number of Couriers | Number of Restaurants |
|----------|------------------|--------------------|-----------------------|
| S1 | 20 | 8 | 4 |
| S2 | 40 | 16 | 8 |
| S3 | 60 | 24 | 12 |
| S4 | 100 | 40 | 20 |
| S5 | 200 | 80 | 40 |

TABLE III. COMPARISON OF ALGORITHM PERFORMANCE OF DIFFERENT INSTANCES

| Instance | Optimization Time (s) | CtD (min) | RtP (min) |
|----------|-----------------------|-----------|-----------|
| S1 | 1.67 | 34.00 | 2.40 |
| S2 | 5.26 | 33.83 | 1.43 |
| S3 | 12.34 | 32.97 | 2.02 |
| S4 | 40.64 | 32.88 | 2.64 |
| S5 | 176.71 | 32.81 | 2.66 |

As can be seen from Table III, the optimization time do exponential growth as the number of orders increase. In the five instances, the CtD and RtP lie around 33 minutes and within 3 minutes, respectively. The problem scale has no obvious impacts on the two indexes. In addition, we found that CtD has a slight advantage in instances with more orders.

B. System Performance

Instances with service period of 900 minutes are selected for testing the algorithm in dynamic processes. The full introduction of the datasets can be found in [15]. For clarity, we list the key characteristics of the instances in Table IV.

TABLE IV. COMPARISON OF CHARACTERISTICS OF DIFFERENT INSTANCES

| Instance | Number of orders | Preparation time multifaction factor | Number of restaurants | Courier velocity (m/min) |
|----------|------------------|--------------------------------------|-----------------------|--------------------------|
| D1 | 252 | 1 | 93 | 320 |
| D2 | 252 | 1.25 | 93 | 320 |
| D3 | 252 | 1 | 93 | 427 |
| D4 | 242 | 1 | 54 | 320 |
| D5 | 242 | 1.25 | 54 | 320 |
| D6 | 505 | 1 | 116 | 320 |

In order to study the impact of different optimization time frequencies on the system, four instances are optimized with time intervals of 5 minutes, 10 minutes, and 15 minutes, respectively.

TABLE V. COMPARISON OF SYSTEM PERFORMANCE WITH VARIED OPTIMIZATION TIME INTERVALS

| Time interval | 5 minutes | | 10 minutes | | 15 minutes | |
|---------------|------------|------------|------------|------------|------------|------------|
| Instance | aCtD (min) | aRtP (min) | aCtD (min) | aRtP (min) | aCtD (min) | aRtP (min) |
| D1 | 30.83 | 1.94 | 31.43 | 2.65 | 32.65 | 3.87 |
| D2 | 33.94 | 1.93 | 34.57 | 2.64 | 35.72 | 4.25 |
| D3 | 27.94 | 1.50 | 29.81 | 2.29 | 29.91 | 2.83 |
| D6 | 31.83 | 2.43 | 32.35 | 2.89 | 32.74 | 3.58 |

From Table V, we can find that a decrease in optimization time interval leads to shorter aCtD and aRtP in all the instances. Therefore, we select 5 minutes as the default time interval hereinafter.

Fig. 3 and Fig. 4 present the distribution of CtD and RtP in four instances, respectively. Fig. 3 illustrates that in most time intervals, orders can be delivered to customers between 20 to 40 minutes. As depicted in Fig. 4, the RtP is within three minutes for most of the time intervals. However, orders in a few time intervals suffer from a severe freshness loss due to high demand and courier shortage in peak hours.

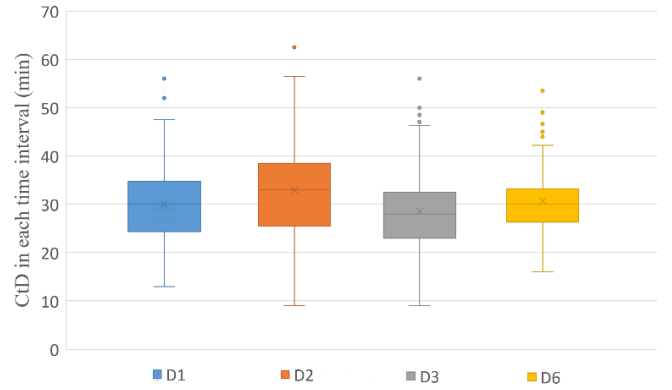


Fig. 3. Distribution of average click-to-door time in different time intervals in four instances

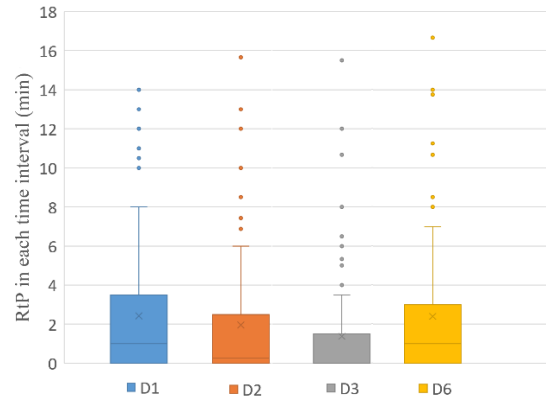


Fig. 4. Distribution of average ready-to-pickup time in different time intervals in all instances

C. Algorithm Comparison

A comparison of the solution obtained by our algorithm and an existing algorithm proposed by [2] is conducted. The results in Table VI indicate that our algorithm improves aCtD and aRtP of the system slightly. We also compare the solutions obtained by our algorithm and the exact solution proposed by [4]. The details are demonstrated in Table VII.

TABLE VI. COMPARISON OF SOLUTIONS OBTAINED BY OUR ALGORITHM AND EXISTING ALGORITHM

| Instance | Four-stage heuristic algorithm | | Algorithm in [3] | |
|---------------------|--------------------------------|------------|------------------|------------|
| | aCtD (min) | aRtP (min) | aCtD (min) | aRtP (min) |
| 0o50t100s1p100 (D1) | 30.83 | 1.94 | 31.19 | 2.52 |
| 0o50t100s1p125 (D2) | 33.94 | 1.93 | 34.67 | 2.27 |
| 0r50t100s1p100 (D4) | 31.41 | 2.11 | 32.46 | 2.14 |
| 0r50t100s1p125 (D5) | 35.88 | 1.41 | 36.75 | 2.16 |

TABLE VII. COMPARISON OF SOLUTIONS OBTAINED BY OUR ALGORITHM AND EXACT SOLUTION

| Instance | Four-stage heuristic algorithm | | Exact solution in [4] | |
|---------------------|--------------------------------|------------|-----------------------|------------|
| | aCtD (min) | aRtP (min) | aCtD (min) | aRtP (min) |
| 0o50t100s1p100 (D1) | 30.83 | 1.94 | 29.81 | 1.46 |
| 0o50t100s1p125 (D2) | 33.94 | 1.93 | 33.40 | 1.23 |
| 0r50t100s1p100 (D3) | 31.41 | 2.11 | 30.76 | 1.13 |
| 0r50t100s1p125 (D4) | 35.88 | 1.41 | 34.66 | 0.97 |

V. CONCLUSION

This paper proposed a four-stage rolling horizon optimization algorithm to solve MDRP. The method can be employed based on real-time order information. The algorithm first generates bundles according to orders' spatial and temporal distribution. For improving delivery efficiency, up to two bundles are allowed to be delivered on one route. Thus, secondly, we find feasible bundle pairs. Then, routes for delivering any single bundle or a bundle pair are optimized. Finally, the routes are assigned to available couriers.

Through result analysis, we can conclude that our algorithm is able to solve MDRP with up to 200 orders within about 3 minutes. Additionally, slightly improved service quality is observed in scenarios with higher demand. Through a comparison of the dynamic system solved with different optimization frequencies, smaller aCtD and aRtP are obtained when reducing the time interval. According to the distribution of aCtD and aRtP of orders, we find that orders in most time intervals can be picked up and delivered in time. A comparison of our algorithm with the existing algorithm and exact solutions is conducted as well. Our algorithm is able to produce more efficient and accurate solutions than the existing algorithm.

As limitations of this work, the heuristic algorithm currently doesn't consider the load capacity of couriers, which plays a great role when serving a huge number of orders in reality. Thus, we will include this constraint to improve the algorithm in the future.

REFERENCE

- [1] J. Wang, X. Shen, X. Huang, and Y. Liu, "Influencing Factors of the Continuous Usage Intention of Consumers of Online Food Delivery Platform Based on an Information System Success Model," *Frontiers in Psychology*, vol. 12, Aug. 2021.
- [2] D. Reyes, A. Erera, M. Savelsbergh, S. Sahasrabudhe, and R. O'Neil. The meal delivery routing problem. Optimization Online, 2018.
- [3] R. R. S. van Lon, E. Ferrante, A. E. Turgut, T. Wenseleers, G. Vanden Berghe, and T. Holvoet, "Measures of dynamism and urgency in logistics," *European Journal of Operational Research*, vol. 253, no. 3, pp. 614–624, Sep. 2016.
- [4] Karsten Lund, Oli B.G. Madsen, and Jens M. Rygaard. "Vehicle routing problems with varying degrees of dynamism." Technical Report IMM-REP-1996-1, Department of Mathematical Modeling, The Technical University of Denmark, May 1996.
- [5] M. Stiglic, N. Agatz, M. Savelsbergh, and M. Gradisar, "Making dynamic ride-sharing work: The impact of driver and rider flexibility," *Transportation Research Part E: Logistics and Transportation Review*, vol. 91, pp. 190 -- 207, Jul. 2016.
- [6] X. Wang, N. Agatz, and A. Erera, "Stable Matching for Dynamic Ride-Sharing Systems," SSRN Electronic Journal, 2014.
- [7] B. Yildiz and M. Savelsbergh, "Provably High-Quality Solutions for the Meal Delivery Routing Problem," *Transportation Science*, vol. 53, no. 5, pp. 1372–1388, Sep. 2019.
- [8] G. Berbeglia, J. Cordeau and G. Laporte, "Dynamic pickup and delivery problems," *European Journal of Operational Research*, vol. 202, (1), pp. 8-15, 2010.
- [9] C. Archetti, D. Feillet, and M. G. Speranza, "Complexity of routing problems with release dates," *European Journal of Operational Research*, vol. 247, no. 3, pp. 797–803, Dec. 2015.
- [10] M. W. Ulmer, B. W. Thomas, and D. C. Mattfeld, "Preemptive depot returns for dynamic same-day delivery," *EURO Journal on Transportation and Logistics*, Apr. 2018.
- [11] M. A. Klapp, A. L. Erera, and A. Toriello, "The One-Dimensional Dynamic Dispatch Waves Problem," *Transportation Science*, vol. 52, no. 2, pp. 402–415, Mar. 2018.
- [12] I. Dayarian and M. Savelsbergh, "Crowdshipping and Same-day Delivery: Employing In-store Customers to Deliver Online Orders," *Production and Operations Management*, vol. 29, no. 9, Jun. 2020.
- [13] S. A. Voccia, A. M. Campbell, and B. W. Thomas, "The Same-Day Delivery Problem for Online Purchases," *Transportation Science*, vol. 53, no. 1, pp. 167–184, Feb. 2019.
- [14] N. Azi, M. Gendreau, and J.-Y. Potvin, "A dynamic Vehicle routing problem with multiple delivery routes," *Annals of Operations Research*, vol. 199, no. 1, pp. 103–112, Oct. 2011.
- [15] "Meal Delivery Routing Problem Test Instances." GitHub. <https://github.com/grubhub/mdrplib> (accessed Nov. 11, 2022).