

❄️ Curva de Rotação ESO 116-G12 ❄️

Utilitários

Tabelas

```
In[2]:= data =  
    Import["C:\\\\Users\\Leoleo\\Desktop\\TCC\\Mathematica\\Fitting\\116.dat"];  
    _importa _constante  
RCtotal = Table[{data[[i, 1]], data[[i, 3]]}, {i, 1, 15}];  
    _tabela  
RCgas = Table[{data[[i, 1]], data[[i, 4]]}, {i, 1, 15}];  
    _tabela  
Erro = Table[data[[i, 5]], {i, 1, 15}];  
    _tabela  
radii = Part[Transpose[data], 1];  
    _parte _transposição  
Vel = Part[Transpose[data], 3];  
    _parte _transposição  
err = Part[Transpose[data], 5];  
    _parte _transposição  
  
TableForm[data, TableHeadings -> {{""}, {"Raio", "", "Vtotal", "Vgas", "Erro"}}]  
_forma de tabela _cabeçalhos de tabela
```

Out[9]/TableForm=

	Raio		Vtotal	Vgas	Erro
	0.295522	7.58904	20.94	-0.234178	3.4
	0.985821	7.79329	39.95	-1.95065	3.29
	1.62537	8.47973	51.54	-1.68024	2.96
	2.18881	9.15955	67.92	5.43454	3.45
	3.17687	9.76846	80.22	13.5993	2.93
	3.76791	9.48569	83.33	18.0705	3.08
	4.35896	8.74732	91.38	21.8567	2.83
	4.8903	7.95629	101.65	24.2219	5.4
	6.19403	6.20847	104.77	27.7912	4.21
	7.16418	5.25717	108.62	29.5757	2.1
	8.0597	4.68539	108.48	30.9882	2.1
	8.95522	4.27244	108.73	33.3072	2.1
	9.85075	3.43065	110.24	36.6602	2.1
	10.7463	1.87414	110.63	38.4926	2.33
	11.6418	0.66706	111.52	36.585	4.74

Valores de Parâmetros

Conversor de Unidades

Equações

Interpolação do Gás

Gráfico Velocidade das estrelas no disco

Gráfico Velocidade Matéria Escura

Modelo de Burket ESO 116-G12

Ajuste Linear

Ajuste Não Linear

```
In[57]:= Clear[f]
         apaga

VDisk[r_, M_] :=  $\frac{1}{2 R_d} \left( G (M * 10^9) \left( \frac{r}{R_d} \right)^2 \right.$ 
                 $\left. \left( \text{BesselI}\left[0, \frac{r}{2 R_d}\right] \text{BesselK}\left[0, \frac{r}{2 R_d}\right] - \text{BesselI}\left[1, \frac{r}{2 R_d}\right] \text{BesselK}\left[1, \frac{r}{2 R_d}\right] \right) \right];$ 
                função I de Bessel função K de Bessel função I de Bessel função K de Bessel

VDark[r_, R_, P_] :=  $\frac{1}{r} 6.4 G \left( (P * 10^7) R^3 \right.$ 
                     $\left. \left( \frac{1}{2} \text{Log}\left[\left(\frac{r}{R}\right)^2 + 1\right] + \text{Log}\left[\frac{r}{R} + 1\right] - \text{ArcTan}\left[\frac{r}{R}\right] \right) \right];$ 
                    logaritmo logaritmo arco tangente

h[r_, R_, P_, M_] := Sqrt[VDisk[r, M] + VDark[r, R, P]];
                    raiz quadrada

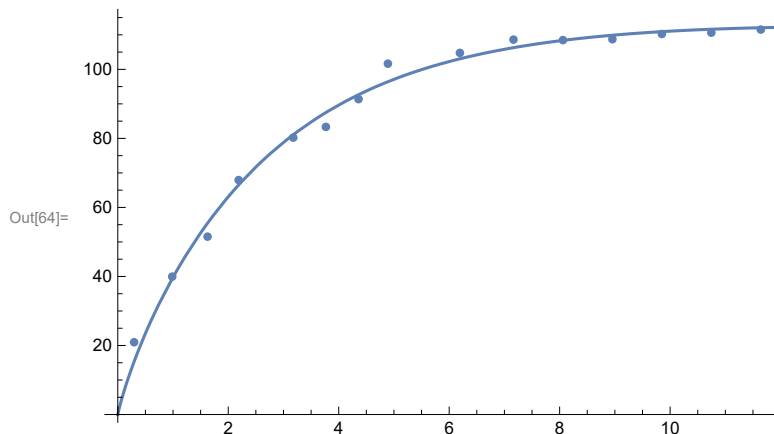
Rd := 1.7;

Fit2 = NonlinearModelFit[RCtotal,
    ajusta a um modelo não linear
    h[r, R, P, M], {{M, 0.1, 10}, {P, 0.1, 10}, {R, 1, 10}}, r]
Fit2["ParameterTable"]
Show[ListPlot[RCtotal], Plot[Fit2[r], {r, 0, 100}, AxesOrigin -> {0, 0}]]
    gráfico de uma lista de v gráfico origem dos eixos
```

Out[62]= FittedModel[$\sqrt{905.618 r^2 \langle\langle 1 \rangle\rangle + \frac{129439. \langle\langle 1 \rangle\rangle}{r}}$]

Out[63]=

	Estimate	Standard Error	t-Statistic	P-Value
M	2.06848	0.687315	3.00951	0.0108728
P	4.63667	1.15787	4.00447	0.00174759
R	4.66305	0.626713	7.44048	7.83508×10^{-6}



In[65]:=

```

j[r_, R_, P_, M_] := Sqrt[VDisk[r, M] + VDark[r, R, P] + Igas[r]^2]
                        raiz quadrada
Fit3 = NonlinearModelFit[RCtotal, j[r, R, P, M],
                        ajusta a um modelo não linear
                        {{M, 0.1, 10}, {P, 0.1, 10}, {R, 1, 10}}, r, Weights -> 1/err^2]
                        pesos
Fit3["ParameterTable"]
Show[ListPlot[RCtotal], Plot[Fit3[r], {r, 0, 100}, AxesOrigin -> {0, 0}]]
mostra gráfico de uma lista de v... gráfico origem dos eixos

```

Out[66]= FittedModel[

$$\sqrt{\left(911.561 r^2 \langle\langle 1 \rangle\rangle + \frac{\langle\langle 19 \rangle\rangle \langle\langle 1 \rangle\rangle}{r} + \text{InterpolatingFunction}\left[\begin{array}{c} \text{Domain: } \{\{0.296, 11.6\}\} \\ \text{Output: scalar} \end{array}\right][r]^2\right)}$$

Out[67]=

	Estimate	Standard Error	t-Statistic	P-Value
M	2.08205	0.735815	2.82959	0.0151873
P	4.51678	1.32533	3.40803	0.0051921
R	4.40809	0.670834	6.57106	0.0000264688

InterpolatingFunction::dmval :

Input value {0.00204286} lies outside the range of data in the interpolating function. Extrapolation will be used. >>

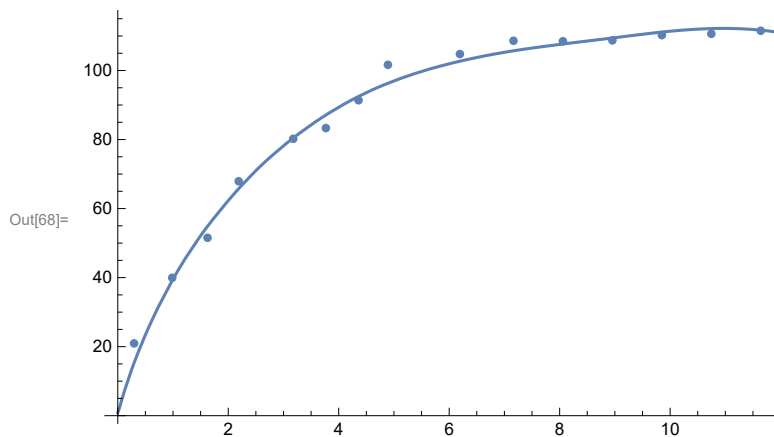
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Input value {0.00204286} lies outside the range of data in the interpolating function. Extrapolation will be used. >>

General::stop : Further output of InterpolatingFunction::dmval will be suppressed during this calculation. >>



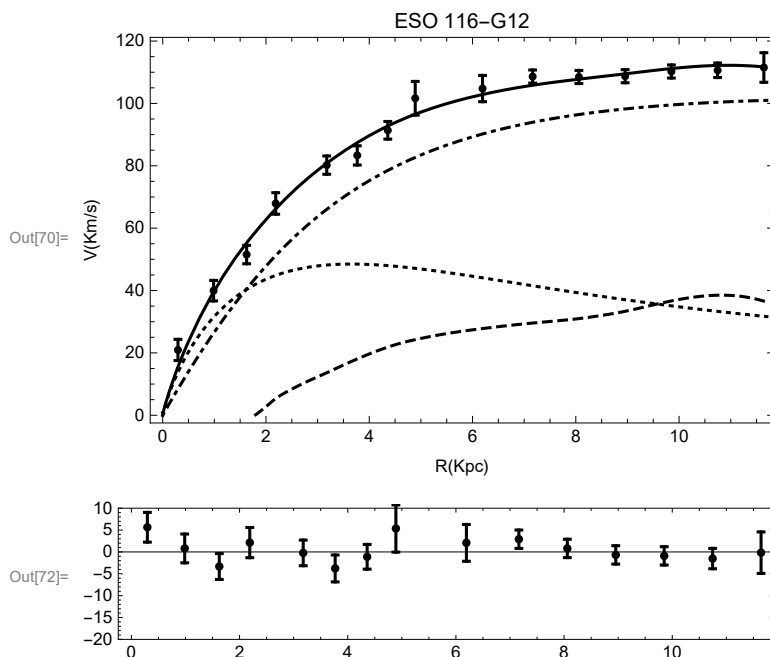
Gráficos do Ajuste

In[69]:=

```
FINAL = Plot[Vt[r] /. {Md -> 2.17 * 10^9, Rd -> 1.7, Ro -> 4.42, Po -> 4.48 * 10^7},
  {r, 0, 11.6}, PlotStyle -> Black, PlotRange -> Automatic];
Show[CRtot, RCstars, RChalo, FINAL, Gas, Frame -> True,
  PlotRange -> {{0, 11.6}, {0, 115}}, PlotLabel -> "ESO 116-G12",
  FrameLabel -> {"R(Kpc)", "V(Km/s)"}]
FITERRO = Table[{data[[i, 1]], Fit3["FitResiduals"][[i]]}, {i, 15}];
ErrorListPlot[{Table[{FITERRO[[i]], ErrorBar[Erro[[i]]]}, {i, 15}]}],
  PlotStyle -> Black, MeshStyle -> PointSize[Large],
  PlotRange -> {-20, 10}, Frame -> True, AspectRatio -> 0.2]
```

InterpolatingFunction::dmval :

Input value {0.000236971} lies outside the range of data in the interpolating function. Extrapolation will be used. >>



```
In[73]:= chi2[P_, R_, M_] :=
  N[Plus@@Table[(Vel[[i]] - j[radii[[i]], M, P, R])^2 / (err[[i]])^2,
    ...[soma [tabela
      {i, Dimensions[radii][[1]]}]]
    [dimensões
  BestFit = Timing[NMinimize[{chi2[M, P, R],
    [cronome [minimiza numericamente
      M > 1 && M < 50 && P > 1 && P < 10 && R > 1 && R < 10}, {M, P, R}]]]
```

```
Out[74]= {1.04688, {10.129, {M → 4.51677, P → 2.08206, R → 4.40809}}}
```

```
In[75]:=
  10.129/12
```

```
Out[75]= 0.844083
```