

**Name:** \_\_\_\_\_

**Directions:** Complete the following quiz on paper. Show all work necessary to receive full credit.

1. Consider the matrix  $A = \begin{pmatrix} 2 & 0 & 0 \\ 1 & 2 & 1 \\ -1 & 0 & 1 \end{pmatrix}$

- (a) Find the characteristic polynomial of  $A$ .
- (b) Find all eigenvalues of  $A$ .
- (c) For each eigenvalue, find a basis for the corresponding eigenspace.
- (d) If possible, diagonalize  $A$ .

2. Let  $\vec{u} = \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}$  and  $\vec{v} = \begin{bmatrix} 2 \\ 0 \\ 1 \\ 3 \end{bmatrix}$ , find  $\langle \vec{u}, \vec{v} \rangle$ .