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structure ArraySequence : SEQUENCE =
struct
 (* An array with starting index and length *)
 type 'a seq = { ary : 'a array, idx : int, len : int }
 type 'a ord = 'a * 'a -> order
 datatype 'a treeview = EMPTY | ELT of 'a | NODE of 'a seq * 'a \hookleftarrow
    seq
 datatype 'a listview = NIL | CONS of 'a * 'a seq
 exception Range
 exception Size
 val length : 'a seq -> int = #len
 fun empty _ = {ary=Array.fromList [], idx=0, len=0}
 fun singleton x = {ary=Array.fromList [x], idx=0, len=1}
 fun collate cmp (\{ary=x, \ldots\} : 'a seq, \{ary=y, \ldots\} : 'a seq) \leftarrow
     Array.collate cmp (x, y)
 fun tabulate f n =
     if n < 0 then raise Size
     else {ary=Array.tabulate (n, f), idx=0, len=n}
 fun nth {ary, idx, len} i =
     if i < 0 orelse i >= len then raise Range
     else Array.sub (ary, idx+i)
 fun toString f s =
      "<" ^ String.concatWith "," (List.tabulate (length s, f o \leftrightarrow
         nth s)) ^ ">"
 fun fromList l =
     let val ary = Array.fromList 1
     in {ary=ary, idx=0, len=Array.length ary}
 val % = fromList
 fun subseq {ary, idx, len} (i, len') =
     if len' < 0 then raise Size
     else if i < 0 orelse i+len' > len then raise Range
     else {ary=ary, idx=idx+i, len=len'}
 fun take (s, n) = subseq s (0, n)
 fun drop (s, n) = subseq s (n, length s - n)
 fun showt s =
     case length s
       of 0 => EMPTY
        | 1 => ELT (nth s 0)
        | n => let val half = n div 2
            in NODE (take (s, half), drop (s, half))
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end
fun rev s =
    let val n = length s
    in tabulate (fn i => nth s (n-1-i)) n
fun append (s, t) =
    let val (ns, nt) = (length s, length t)
      fun ith i = if i >= ns then nth t (i-ns) else nth s i
    in tabulate ith (ns+nt)
    end
fun iterh f b s =
    let
      fun iterh' s (old, cur) =
          case showl s
            of NIL => (rev (fromList old), cur)
              | CONS (x, xs) => iterh' xs (cur::old, f (cur, x))
    in iterh' s ([], b)
    end
fun iter f b s = #2 (iterh f b s)
fun toList s = iter (fn (1,x) \Rightarrow x::1) [] (rev s)
fun merge cmp s t =
    let
      (* Sequential merge. Pretend it's parallel! *)
      fun merge' s t =
          case (showl s, showl t)
            of (NIL, _) => toList t
              | (_, NIL) => toList s
              | (CONS (x, xs), CONS (y, ys)) =>
                if cmp (y, x) = LESS then y::merge' s ys
                else x::merge' xs t
    in fromList (merge' s t)
    end
fun sort cmp s =
    case showt s
      of EMPTY => s
       \mid ELT x => singleton x
       \mid NODE (1, r) \stackrel{-}{=} merge cmp (sort cmp 1) (sort cmp r)
fun enum s = tabulate (fn i => (i, nth s i)) (length s)
fun map f s = tabulate (f o (nth s)) (length s)
fun map2 f s t =
    tabulate (fn i => f (nth s i, nth t i)) (Int.min (length s, \leftarrow
         length t))
fun unmap2 (spl : 'a -> 'b * 'c) s =
    let
      val n = length s
      val s' = map spl s
    in (tabulate (#1 o nth s') n, tabulate (#2 o nth s') n)
    end
fun zip s t = map2 (fn x \Rightarrow x) s t
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fun unzip s = unmap2 (fn x => x) s
fun reduce f b s =
    if length s = 0 then b
    else let
      fun pp2 x n = if n \geq= x then n div 2 else pp2 x (2*n)
      fun prevPow2 x = pp2 x 1
      fun reduce' s =
           case length s
             of 1 \Rightarrow nth s 0
              | n => let val half = prevPow2 n
                     in f (reduce' (take (s, half)),
                           reduce' (drop (s, half)))
    in f (b, reduce' s)
    end
fun scan f b s =
    case length s
     of 0 => (empty (), b)
      | 1 \Rightarrow (singleton b, f (b, nth s 0))
      | n =>
        let
          fun contract i =
               if i = n div 2 then nth s (2*i)
               else f (nth s (2*i), nth s (2*i+1))
           val s' = tabulate contract (((n-1) div 2) + 1)
           val (r, res) = scan f b s'
           fun expand i =
               if i mod 2 = 0 then nth r (i div 2)
               else f (nth r (i div 2), nth s (i-1))
        in (tabulate expand n, res)
        end
fun scani f b s =
    let val (r, res) = scan f b s
    in append (r, singleton res)
    end
fun ({ary, ...} : 'a seq) >> (f : int * 'a -> unit) =
    Array.appi f ary
fun flatten ss =
    let
      val (starts, n) = scan op+0 (map length ss)
      val idxs = tabulate (fn _ => (0, 0)) n
      fun setIdxs (i, (start,s)) =
          s >> (fn (j,_) => Array.update (#ary idxs, start+j, (\hookleftarrow
              i,j)))
      val _ = zip starts ss >> setIdxs
      fun ith i =
          let val (j, k) = nth idxs i
          in nth (nth ss j) k
           end
    in tabulate ith n
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fun filter p s =
    flatten (map (fn x => if p x then singleton x else empty ()\leftarrow
        ) s)
fun argmax cmp s =
    case length s
      of 0 => raise Range
       | n =>
         let
            fun best (i, j) =
                case cmp (nth s j, nth s i)
                  of LESS => j
                   | _ => i
          in reduce best 0 (tabulate (fn i => i) n)
          end
fun inject idx s =
    let val s' as \{ary, \ldots\} = tabulate (nth s) (length s)
      val _ = idx >> (fn (_,(i,x)) => Array.update (ary, i, x))
    in s'
    end
local
  datatype 'a diff = RUN of int | SAME of int
  fun opdiff (_, RUN x) = RUN x
    | opdiff (RUN x, SAME y) = RUN (x+y)
    | opdiff (SAME x, SAME y) = SAME (x+y)
  fun collect cmp s =
      case length s
        of 0 => empty ()
         | n =>
            let
              val (ks, vs) = unzip (sort (fn ((x,_), (y,_)) => \leftrightarrow
                  cmp(x,y))s)
              (* SAME 1 indicates the next position has the same \hookleftarrow
                   key *)
              fun dk (x,y) = if cmp (x,y) = EQUAL then SAME 1 \leftrightarrow
                  else RUN 1
              val diffs = map2 dk (take (ks, n-1)) (drop (ks, 1)\leftarrow
              val runs = scani opdiff (RUN 1) diffs
              (* RUN 1 marks the starting position of each \hookleftarrow
                  sequence *)
              val flags = map (fn (i, RUN 1) => SOME i | _ => \hookleftarrow
                  NONE) (enum runs)
              val starts = map valOf (filter isSome flags)
              val lengths = map2 op- (drop (append (starts, %[n \leftarrow
                  ]), 1)) starts
              fun make (i, len) =
                  let val k = nth ks i
                  in (k, subseq vs (i, len))
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end
in map2 make starts lengths
end
end
end
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