

15-210: Parallel and Sequential Data Structures and Algorithms

Costs for Sequences, Sets and Tables

1 Function Costs

ArraySequence	<i>Work</i>	<i>Span</i>
<code>append(S_1, S_2)</code>	$ S_1 + S_2 $	1
<code>argmax f S</code>	$ S $	$\log S $
<code>collate f (S_1, S_2)</code>	$ S_1 + S_2 $	$\log(\min(S_1 , S_2))$
<code>collect f S</code>	$ S \log S $	$\log^2 S $
<code>drop(S, n)</code>	1	1
<code>empty ()</code>	1	1
<code>enum S</code>	$ S $	1
<code>filter f S</code>	$\sum_{s \in S} W(f(s))$	$\log S + \max_{s \in S} S(f(s))$
<code>flatten S</code>	$ S + \sum_{e \in S} e $	$\log S $
<code>fromList S</code>	$ S $	$ S $
<code>inject I S</code>	$ I + S $	1
<code>iter f b_0 S</code>	$O\left(\sum_{i=0}^{ S -1} W(f(b_i, S_i))\right)$	$\sum_{i=0}^{ S -1} S(f(b_i, S_i))$
<code>iterh f b_0 S</code>	$O\left(\sum_{i=0}^{ S -1} W(f(b_i, S_i))\right)$	$\sum_{i=0}^{ S -1} S(f(b_i, S_i))$
<code>length S</code>	1	1
<code>map f S</code>	$\sum_{e \in S} W(f(e))$	$\max_{e \in S} S(f(e))$
<code>map2 f S_1 S_2</code>	$\sum_{i=0}^{\min(S_1 , S_2)-1} W(f(S_{1i}, S_{2i}))$	$\max_{i=0}^{\min(S_1 , S_2)-1} S(f(S_{1i}, S_{2i}))$
<code>merge f S_1 S_2</code>	$ S_1 + S_2 $	$\log(S_1 + S_2)$
<code>nth S i</code>	1	1
<code>reduce f b S</code>	$O\left(S + \sum_{f(x,y) \in \mathcal{O}_r(f,b,S)} W(f(x,y))\right)$	$\log S \max_{f(x,y) \in \mathcal{O}_r(f,b,S)} S(f(x,y))$

ArraySequence	Work	Span
rev S	$ S $	1
scan $f \ b \ S$	$ S + \sum_{f(x,y) \in \mathcal{O}_s(f,b,S)} W(f(x,y))$	$\log S \max_{f(x,y) \in \mathcal{O}_s(f,b,S)} S(f(x,y))$
scani $f \ b \ S$	$ S + \sum_{f(x,y) \in \mathcal{O}_s(f,b,S)} W(f(x,y))$	$\log S \max_{f(x,y) \in \mathcal{O}_s(f,b,S)} S(f(x,y))$
showl S	1	1
showt S	1	1
singleton e	1	1
sort $f \ S$	$ S \log S $	$\log^2 S $
subseq(S, n)	1	1
tabulate $f \ n$	$\sum_{i=0}^{n-1} W(f(i))$	$\max_{i=0}^{n-1} S(f(i))$
take(S, n)	1	1
toString $f \ S$	$\sum_{e \in S} W(f(e))$	$\sum_{e \in S} S(f(e))$
unzip S	$ S $	1
upmap2 $f \ S$	$\sum_{e \in S} W(f(e))$	$\max_{e \in S} S(f(e))$
zip $S_1 \ S_2$	$\max(S_1 , S_2)$	1

For reduce, $\mathcal{O}_r(f, i, S)$ represents the set of applications of f as defined in the documentation. For scan, $\mathcal{O}_s(f, i, S)$ represents the applications of f defined by the implementation of scan in the lecture notes. For iter and iterh, $b_i = f(b_{i-1}, S_{i-1})$. For showti, argmax, merge, sort, collate, collect, fields, and tokens the given costs assume that the work and span of the application of f is constant.