

# Topic 7: Electric & Magnetic Fields

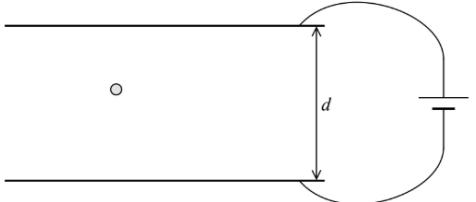
## 0.7 Specification notice:

In order to develop their practical skills, students should be encouraged to carry out a range of practical experiments related to this topic. Possible experiments include using a coulomb meter to measure charge stored and using an electronic balance to measure the force between two charges.

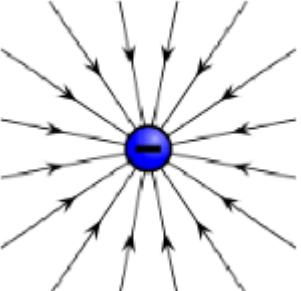
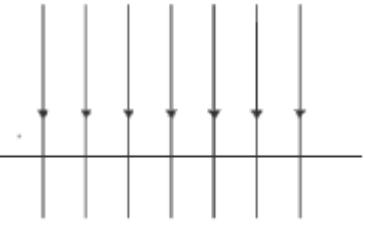
Mathematical skills that could be developed in this topic include sketching relationships which are modelled by  $y = k/x$ , and  $y = k/x^2$ , using logarithmic plots to test exponential and power law variations, interpreting logarithmic plots and sketching relationships that are modelled by  $y = e^{-x}$ .

This topic may be studied using applications that relate to fields, for example, communications and display techniques.

## 7.Q Exam questions

<p>In an experiment to determine the charge on an electron, negatively charged oil drops are allowed to fall between two parallel metal plates separated by a distance <math>d</math>. A potential difference (p.d.) is applied across the plates. The diagram shows one oil drop between the plates.</p>  <p>When the p.d. is 0 V the oil drop accelerates to terminal velocity. The p.d. is increased. It is observed that at a particular p.d. <math>V</math> the oil drop stops falling and remains stationary between the plates.</p> <p>(a) Explain the motion of the oil drop in terms of the forces acting on it as the p.d. is increased from 0 to <math>V</math>. (6)</p>	<p><b>Indicative content</b></p> <ul style="list-style-type: none"><li>At terminal velocity the forces on the drop are balanced <b>OR</b> weight = drag</li><li>The p.d. creates an electrostatic force acting upwards on the drop</li><li>The electrostatic force increases as p.d. increases</li><li>The net upward force causes the drop to have a negative acceleration</li><li>As speed decreases the drag decreases</li><li>The drop remains stationary when the forces are balanced <b>OR</b> until the drop remains stationary when weight = electrostatic force</li></ul>
--	--

## 7.108 Understand that an electric field (force field) is defined as a region where a charged particle experiences a force

Define Electric Field?	A region of space in which a charged particle experiences a force
What are the 2 types of electric fields?	<ul style="list-style-type: none"> <li>● Radial fields:</li>  <li>● Uniform fields:</li>  <p><i>This is approximately what it looks like at the Earth's surface</i></p> </ul>

## 7.109 understand that electric field strength is defined as $E=F/Q$ and be able to use this equation

Define Electric Field Strength and what are its 2 units and its equation?	<ul style="list-style-type: none"> <li>● The force per unit positive charge (thus, its direction is the direction a positive charge would move)</li> <li>● NC<sup>-1</sup> or Vm<sup>-1</sup></li> <li>● <math>E=F/Q</math></li> </ul> $E = \frac{F}{Q}$ <p><i>If the charge given is negative and thus the field strength too then the field points are going in the opposite direction</i></p>
---	--

**7.110 be able to use the equation  $F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2}$ , for the force between two charges**

<b>What is permittivity? <math>\epsilon_0</math></b>	<ul style="list-style-type: none"> <li>How difficult it is to generate an electric field in a medium</li> <li>The higher the permittivity of a material, the more charge is needed to generate an electric field of a given size</li> </ul>
What is Coulomb's law and the quantities that are proportional to each other?	<p>The force on a charged particle is directly proportional to the product of the two charges and inversely proportional to the distance of separation squared</p> <p>(Force between two point charges where attractive is negative and repulsive is positive).</p> $F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}$ $F = k_e \frac{q_1 q_2}{r^2}$ <p>Air can be treated as a vacuum thus use <math>\epsilon_0</math></p>

**7.111 be able to use the equation  $F = \frac{Q}{4\pi\epsilon_0 r^2}$  for the electric field due to a point charge**

What are the 3 Coulomb's law equation variants for an electric field due to a point charge?	$E = \frac{KQ}{r^2}$ where... $K = \frac{1}{4\pi\epsilon_0}$ Then $E = F/Q$
---	--

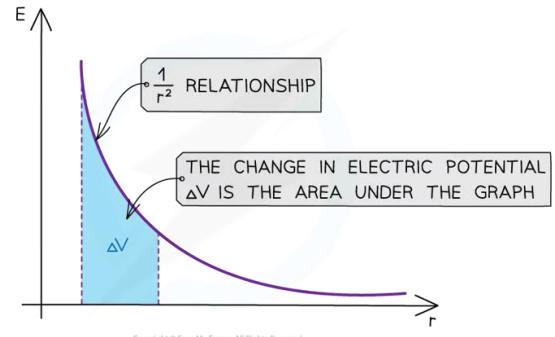
$$F = \frac{KQ}{r^2}$$

*Tip:*

If the charge is negative, the E field strength is negative and points towards the centre of the charge

If the charge is positive, the E field strength is positive and points away from the centre of the charge

What is the graph of E against radius (and F against r) for an electric field due to a point charge and its features?



- The values for E are all positive
- As r increases, E against r follows a  $1/r^2$  relation due to the inverse squared law
- The area under this graph is the change in electric potential  $\Delta V$
- The graph has a steep decline as r increases

## 7.112 know and understand the relation between electric field and electric potential

Derive the distance of closest approach formula?

$E_p = Q_1 V$  (this is the electrical energy of the alpha particle when it is stationary where Q is the charge on the alpha particle) and is equal to the kinetic energy of the alpha particle.

$V = \frac{kQ_2}{r}$  (this is the electrical potential at the distance of closest approach, r, where  $Q_2$  is the charge on the nucleus)

Therefore  $EP = \frac{kQ_1 Q_2}{r} = KE$  as well as

$$W = \frac{kQ_1 Q_2}{r}$$

$$\text{To which } r = \frac{kQ_1 Q_2}{E_k}$$

	<p><math>EP</math> is also Workdone (<math>W</math>)</p> $E_K = E_P$ $E_K = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_\alpha Q_n}{r}$ $r = \frac{1}{4\pi\epsilon_0} \cdot \frac{Q_\alpha Q_n}{E_K}$ <p><math>W</math> is the work done needed to remove a particle from 2 point charges. The KE of an electron relies of <math>v</math> being <math>\ll c</math> in <math>E_k = \frac{1}{2}mv^2</math></p> <p>Mr Adams: The equation is not given in formula booklet but is a good one to know</p>
Draw the electric potential graph of potential $V$ against distance ( $r$ ) for a POSITIVE charge	
Draw the electric potential graph of potential $V$ against distance ( $r$ ) for a NEGATIVE charge	

### 7.113 be able to use the equation $E=V/d$ for an electric field between parallel plates

How does the electric field strength vary in a uniform field (with parallel plates) and what is its equation?	<p>It is constant throughout the field (<math>E = Vm^{-1}</math>)</p> $E = \frac{V}{d}$ <p>Where <math>V</math> is the potential difference between the plates and <math>d</math> is their separation</p>
---	---

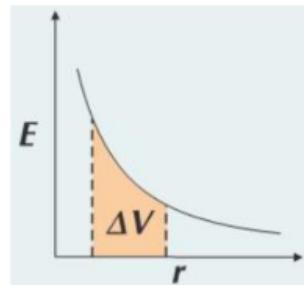
### 7.114 be able to user $V = \frac{Q}{4\pi\epsilon_0 r}$ for a radial field

What is Electric Potential and its equation?

The work required to move a unit charge from infinity to a point against the electric field.

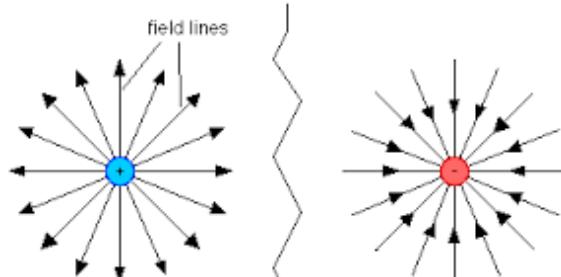
$$V=KQ/r$$

Its change is given by the area under a graph of electric field strength against radius.

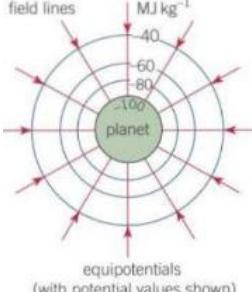


### 7.115 be able to draw and interpret diagrams using field lines and equipotentials to describe radial and uniform electric fields

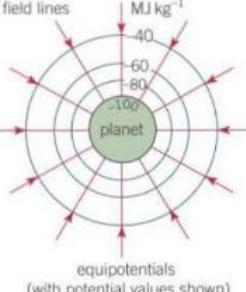
Draw an electric field + equipotential line for a point positive and negative charge?



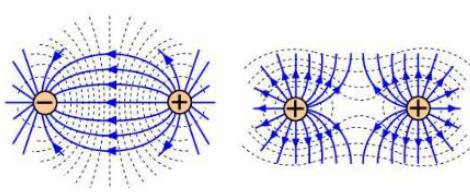
The electric field from an isolated positive charge



The electric field from an isolated negative charge

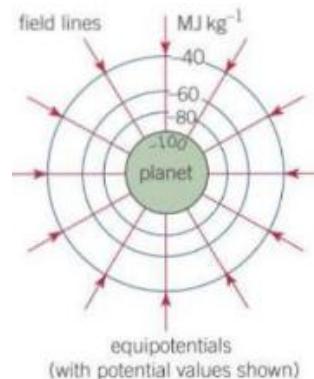


Draw an electric field + equipotential lines for two-like Point charges and between two-opposite Point charges?



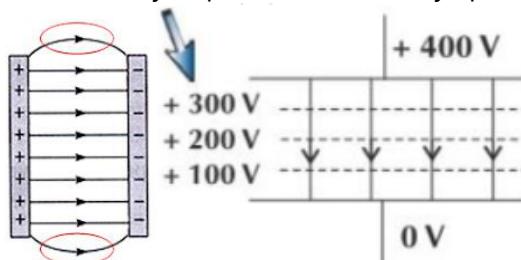
What is an equipotential?  
How are they positioned for radial fields?

- They're points at which gravitational potential or electric potential is constant (you can travel along one with it changing).
- Equipotential are spaced further apart equally as the field strength decreases so you can move further with the same work done



Draw a uniform Electric Field + Equipotential lines and How are the equipotentials different in a uniform field?

- A field produced by connecting two parallel plates to opposite poles of a battery
- They're parallel and evenly spaced



*The electric field strength is constant throughout, the distance decreases so must the potential difference*

Draw an electric field + equipotential lines for a point charge with a parallel plate

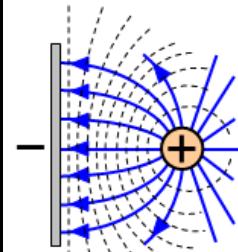
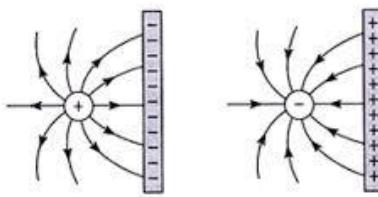
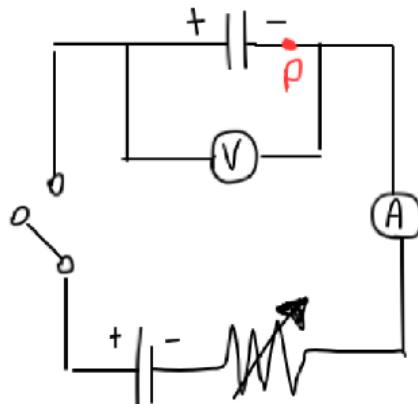


Figure 3

### 7.116 understand that capacitance is defined as $C=Q/V$ and be able to use this equation

What is Capacitance defined as and its equation?	The charge transferred per unit voltage and $C=Q/V$
What is a Farad defined as?	The capacitance where 1 coulomb of charge is transferred per volt of PD
How does a capacitor become charged?	<ul style="list-style-type: none"> <li>Electrons move from the cell to the capacitor -&gt; making one side negatively charged</li> <li>This side repels electrons on the other side making that positive.</li> </ul>

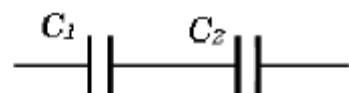
How can you maintain a constant current in a circuit with a capacitor?



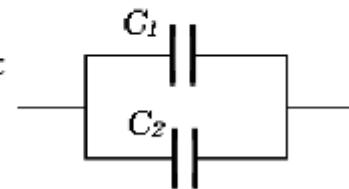
- Without a variable resistor, the current would increase over time as when enough negative charge builds up at P, it will repel incoming.
- With a variable resistor, you can have a high resistance at the start  $\rightarrow$  low current. Yet, when current begins to lower, you decrease resistor to bring it back up

What is the equation for capacitors for when there is 2 in series and in parallel

Series circuit



Parallel circuit



*This is due to conservation of charge.*

For series:

$$V_T = V_1 + V_2$$

$$\frac{Q}{C_T} = \frac{Q}{C_1} + \frac{Q}{C_2}$$

$$\frac{1}{C_T} = \frac{1}{C_1} + \frac{1}{C_2}$$

For parallel:

$$Q = VC$$

$$Q_T = Q_1 + Q_2$$

$$VC_T = VC_1 + VC_2$$

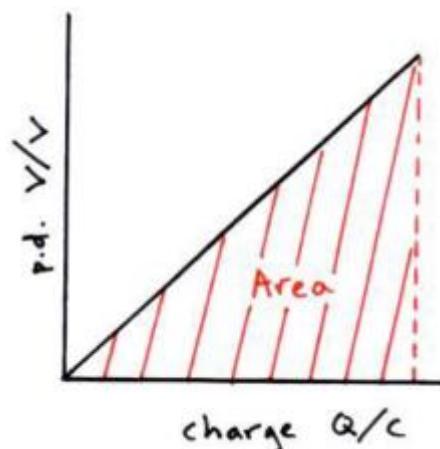
$$C_T = C_1 + C_2$$

You don't need to know derivation for both just the final equations

**7.117 be able to use the equation  $W= 0.5QV$  for the energy stored by a capacitor, be able to derive the equation from the area under a graph of potential difference against charge stored and be able to derive and use the equations  $W=0.5CV^2$**

and  $W = \frac{\frac{1}{2}Q^2}{C}$

Derive the 3 equations for the energy stored in a capacitor? From using a V against Q graph



- $W = \frac{1}{2}QV$
- $V = \frac{Q}{C}$
- $W = \frac{1}{2} \times \frac{Q}{C} \times Q$
- $W = \frac{Q^2}{2C}$
- $Q = CV$
- $W = \frac{1}{2}(CV) \times V$
- $W = \frac{1}{2}CV^2$

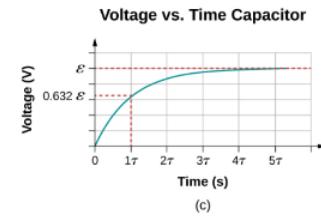
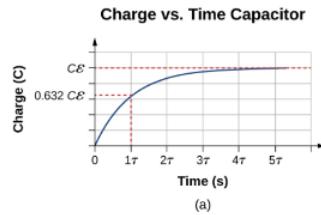
$$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2}\frac{Q^2}{C}$$

Half the energy is 'lost' under resistance.

*There is no way around this.  
It the same derivation for a Charge against Voltage graph too.*

## 7.118 be able to draw and interpret charge and discharge curves for resistor capacitor circuits and understand the significance of the time constant = $RC$

What is the charging graph of a capacitor with its equation and label how to find time constant ?



$$Q = Q_0(1 - e^{-\frac{t}{RC}})$$

*The same can be written replacing Q and  $Q_0$  with V and  $V_0$  respectively.*

$$T = V_0/63\%$$

$$\text{As } Q/C = V$$

$$V = V_0(1 - e^{-t/RC})$$

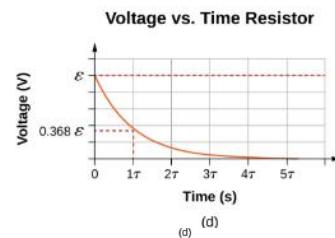
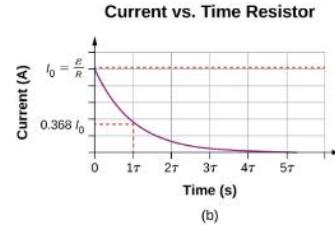
$$\text{As } I = V/R$$

$$I = I_0(1 - e^{-t/RC})$$

It tapers off to the emf of the battery because the rate at which charge comes in decreases. (The shape is the same as  $V = QC$  where C is a constant).

*It's considered fully charged after 5 time constants in this case*

What is the discharging graph of a capacitor with its equation and label how to find time constant ?



$$Q = Q_0 e^{-\frac{t}{RC}}$$

$$T = V_0 / 37\%$$

$$\text{As } Q/C = V$$

$$V = V_0 e^{-t/RC}$$

$$\text{As } I = V/R$$

$$I = I_0 e^{-t/RC}$$

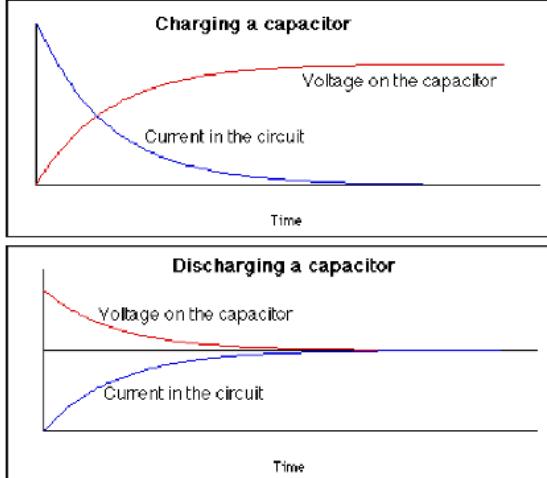
*It's considered fully discharged after 5 time constants in this case*

What is the time constant equation of a capacitor

$$\tau = RC$$

- Where R is the resistance and C is the capacitance of the circuit.
- Increasing T increases the time taken to charge and discharge so current flows for a longer time.

How does the (dis-) charging current circuit graph compare with the (dis-) charging charge capacitor graph? Why?



- The charging-current is the derivative of the charging-charge or proportional to charging-voltage

### 7.119 CORE PRACTICAL 11: Use an oscilloscope or data logger to display and analyse the potential difference (p.d.) across a capacitor as it charges and discharges through a resistor.

--	--

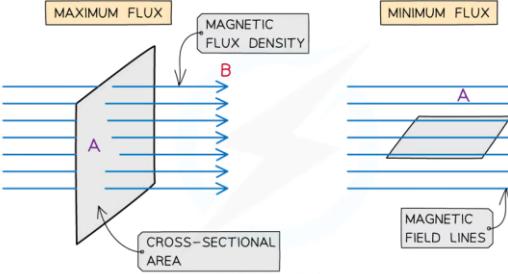
**7.120 be able to use the equation  $Q = Q_0 e^{-t/RC}$  and derive and use related equations for exponential discharge in a resistor-capacitor circuit,  $I = I_0 e^{-t/RC}$ , and  $V = V_0 e^{-t/RC}$  and the corresponding log equations  $\ln Q = \ln Q_0 - \frac{t}{RC}$ ,  $\ln I = \ln I_0 - \frac{t}{RC}$  and  $\ln V = \ln V_0 - \frac{t}{RC}$**

Derive  $\ln Q = \ln Q_0 - t/RC$  from  $Q = Q_0 e^{-t/RC}$

- $Q = Q_0 e^{-t/RC}$
- $\ln Q = \ln(Q_0 e^{-t/RC})$
- $\ln Q = \ln Q_0 + \ln(e^{-t/RC})$
- $\ln Q = \ln Q_0 - t/RC$

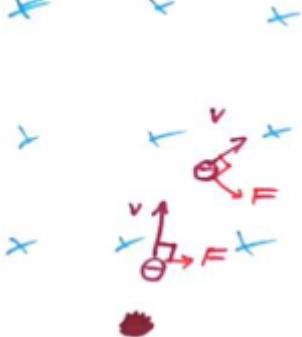
# MAGNETIC FIELDS

**7.121 understand and use the terms *magnetic flux density B* (also referred to as magnetic field strength), *flux φ* (magnetic flux) and *flux linkage Nφ***

Definition of a magnetic field?	A region of space where a magnetic material experiences a magnetic force
Definition, units and equation of magnetic flux $\phi$ (lines of magnetic flux) ?	<ul style="list-style-type: none"> <li>• The product of tesla (B) and cross sectional area (A)</li> <li>• Measured in Weber/Wb</li> <li>• <math>\phi = BA</math></li> <li>• <math>\phi = BAsin\Theta</math></li> </ul> <p>Referred to as “magnetic field lines” at GCSE</p>
When is the magnetic flux $\phi$ through some cross sectional area at a maximum or minimum?	 <ul style="list-style-type: none"> <li>• Its at a maximum when perpendicular to the cross sectional area (as <math>\Theta = 90</math> degrees to the horizontal)</li> <li>• Its at a minimum when parallel to the cross sectional area (as <math>\Theta = 0</math> degrees to the horizontal)</li> </ul>
What does closer B field lines mean?	Greater flux density -> greater force on object here

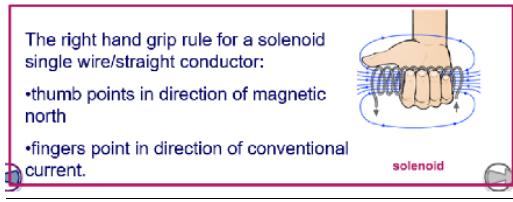
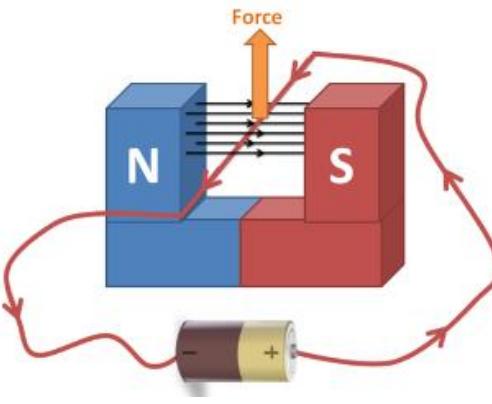
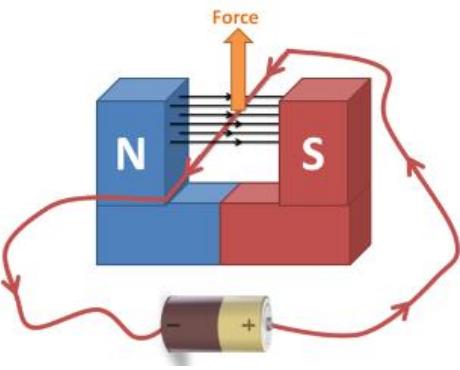
**7.122 be able to use the equation  $F = Bqv \sin\theta$  and apply Fleming's left-hand rule to charged particles moving in a magnetic field**

What is the equation for the force on a moving charge?	$F = BQv$
	Where the particle is travelling perpendicular to the direction of the magnetic field and the

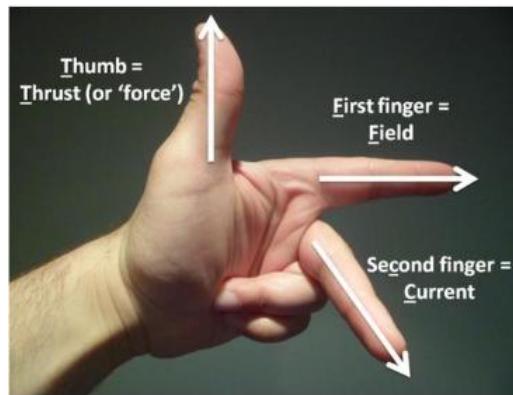
	B field is perpendicular to the velocity of the charge.
How does Fleming's Left Hand Rule apply to a charge moving in a magnetic field?	<p>The force is perpendicular to the direction of motion -&gt; circular motion.</p>  <p>You have to be careful, current is conventional current - the direction in which a positive charge moves</p> <p>And only one component of velocity will be affected (the component within the perpendicular plane).</p>

### 7.123 be able to use the equation $F = BIL \sin\theta$ and apply Fleming's left-hand rule to current carrying conductors in a magnetic field

What is the magnetic flux density B equation and units?	<ul style="list-style-type: none"> <li>• <math>F=BIL\sin\theta</math></li> <li>• Measure in Tesla (T) or <math>\text{Wbm}^{-2}</math></li> </ul> $B = \frac{F}{Il}$ <p>Defined as the force per unit length per unit current on a current carrying conductor at right angles to the magnetic field.</p>
What is the right-hand grip rules and in what 2 cases it used?	<p><b>Current-carrying conductor:</b></p>  <p>The right hand grip rule for a single wire/straight conductor:</p> <ul style="list-style-type: none"> <li>• thumb points in direction of conventional current</li> <li>• fingers point in direction of magnetic field lines.</li> </ul>

	<p><b>Solenoid:</b></p>  <p>The right hand grip rule for a solenoid single wire/straight conductor:      •thumb points in direction of magnetic north      •fingers point in direction of conventional current.</p>
What is the motor effect?	<p>The force exerted on a wire when a current passes along a wire <b>in a magnetic field</b></p> 
What does the force exerted in the motor effect depend on?	<ol style="list-style-type: none"> <li>1. The current in the wire and its direction</li> <li>2. Strength of the magnetic field</li> <li>3. Length of the wire</li> <li>4. Angle of the wire/current relative to the magnetic field lines.</li> </ol>  <p><i>The greatest force is experienced when the wire is perpendicular to the field. No force is experienced when parallel</i></p>

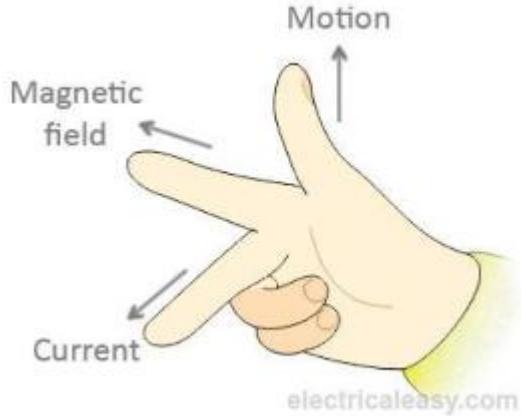
What is Fleming's Left Hand rule? What is it used for?



- Thumb = thrust/force
- First finger = field (going north to south)
- Second finger = conventional current
- Used to determine the **direction of the force** in the **motor effect** (where current and field are known).

*Motor cars drive on left so we remember it as Fleming's left hand rule for motor effect*

What is Flemming's Right hand rule? What is it used for?



- Thumb = thrust / force
- First finger = field (going north to south)
- Second finger = conventional current
- Used for generators (gene**RIGHT**ors).
- Used to determine the **direction of current** in the movement of the wire due to induction from Lenz's law (where force and field are known)

Describe the context for where to use Flemming's left and right hand rules?

- FLHR- This is where charge is moving (either as charged particles or a current in a wire) perpendicular to a B field and creates a force that is perpendicular to both the current and the B field (e.g. motor effect)
- FRHR- This is where a conductor is moving with a velocity perpendicular to the B field and therefore there is a change in the magnetic flux which would induce an EMF

How can the magnetic flux density be measured?	<ol style="list-style-type: none"> <li>1. Place magnet on balance</li> <li>2. Clamp wire in position so magnet can push down</li> <li>3. With no current passing through, set balance to zero</li> </ol> <ul style="list-style-type: none"> <li>● We know <math>mg = BIL</math></li> </ul>
Explain the script to how a magnetic field acts a force on a current carrying conductor?	<ul style="list-style-type: none"> <li>● The current in the wire produces a magnetic field around the wire</li> <li>● This magnetic field interacts with the magnetic field from the permanent magnet</li> <li>● Due to Flemming's Left hand rule there is force acted upon the wire (either into/out of the plane or upwards/downwards)</li> <li>● As the current and magnetic field are 90 degrees to each other</li> <li>● The force is at 90 degrees to the magnetic field and current</li> </ul>

### **7.124 understand the factors affecting the e.m.f. induced in a coil when there is relative motion between the coil and a permanent magnet**

What are the 4 factors that affect induced EMF?	<ul style="list-style-type: none"> <li>● The faster the object/motion (this reduces the time and increases the rate of change of flux)</li> <li>● The higher the magnetic field strength (this increases the flux and hence increases the rate of change of flux)</li> <li>● The higher the number of turns on the coil (this increases the flux linkage and rate of flux linkage)</li> <li>● The more area of coil within the magnetic field (Increases the rate of change of flux)</li> </ul>
---	---

### **7.125 understand the factors affecting the e.m.f. induced in a coil when there is a change of current in another coil linked with this coil**

--	--

## 7.126 understand how to use Lenz's law to predict the direction of an induced e.m.f. and how the prediction relates to energy conservation

What is Lenz's Law? And its equation?

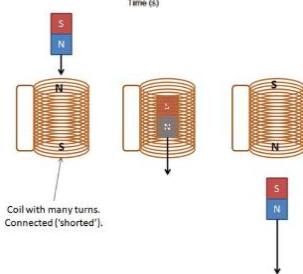
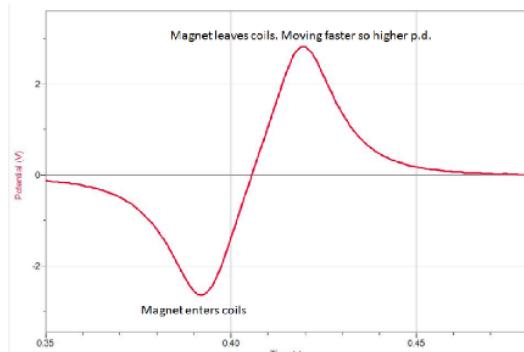
An induced EMF will cause a current to flow that creates a magnetic field that will oppose the change in flux which caused it (this is a consequence of conservation of energy)

$$\varepsilon = - \frac{d(N\Phi)}{dt}$$

- The **negative sign** represents Lenz's Law
  - This is because it shows the induced e.m.f  $\varepsilon$  is set up in an '**opposite direction**' to oppose the changing flux linkage

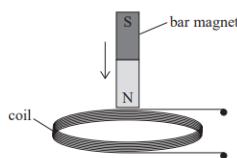
*The explanation of this comes from the conservation of energy. Induced current can never be in a direction to help the change that causes it otherwise you're producing electrical energy from nowhere*

Explain the shape of the graph of EMF against time as a Magnet falls through a coil?



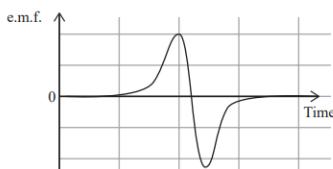
- When the magnet is at a distance there is small flux at the coil
- As the magnet gets closer to the coil the magnetic flux increases at the coil
- This causes a change in flux
- The change in flux causes an induced EMF due to Faraday's law as there is a rate of change of flux
- At the point the magnet enters the coil there is a very large rate of change of flux therefore a large induced EMF
- As the magnet passes through the coil there is the largest flux at the coil but there is no change of flux and therefore no induced EMF
- As the magnet exits the coil the flux starts to decrease and therefore there is a large change in flux and a large negative EMF
- The induced EMF as the magnet leaves the coil is greater than when it entered the coil as the magnet has accelerated as it moved downwards and therefore increased the rate of change of flux and therefore increased the induced EMF

\*16 A bar magnet was dropped vertically through a small coil, as shown.



The coil was attached to a data logger. The data logger recorded the variation of e.m.f. across the coil with time.

The output from the data logger is shown below.



Explain the variation of e.m.f. with time.

#### Indicative content

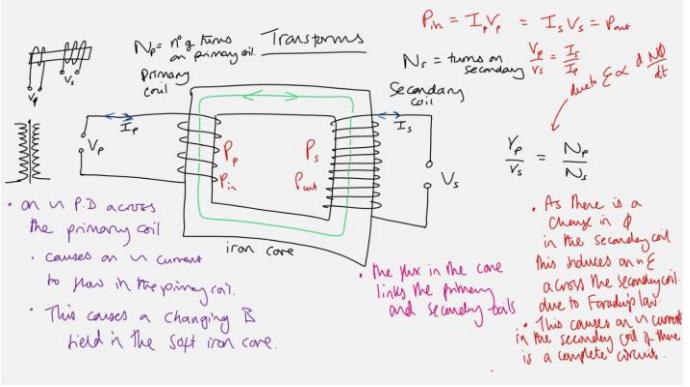
- IC1 There is a change in flux linkage (with the coil)  
**Or** the wires cut the magnetic field (lines) ignore magnet cuts lines no marks, but doesn't prevent subsequent marks, e.g. for change in flux linkage.
- IC2 The greater the rate of change of flux linkage the larger the induced e.m.f.
- IC3 After the south pole reaches the coil the flux linkage (starts to) decrease  
**Or** When the south pole reaches the coil, by Lenz's law the polarity of the coil changes to continue to resist the motion of the magnet  
**Or** As the south pole reaches the coil the rate of change of flux linkage is zero  
(Not direction of field lines opposite)(reference to wires move along field lines for no change in flux linkage)
- IC4 As the south pole of the magnet passes through the coil the (induced) e.m.f. is negative
- IC5 The (downwards) speed of the magnet increases
- IC6 Emf is zero before magnet enters coil  
**Or** Emf is zero when midpoint of magnet in coil  
**Or** Maximum negative value is greater than maximum positive value  
**Or** Time for which emf is negative is greater than time for which emf is positive  
**Or** emf is zero when magnet totally leaves coil

## 7.127 understand how to use Faraday's law to determine the magnitude of an induced e.m.f. and be able to use the equation that combines Faraday's and Lenz's laws $\varepsilon = \frac{-d(N\phi)}{dt}$

What is Faraday's Law? And its equation	The induced EMF is directly proportional to the rate of change of flux (linkage) $\varepsilon = \frac{\Delta(N\Phi)}{\Delta t}$
Describe the script for explaining how step up or step down transformers work?	<ul style="list-style-type: none"> <li>● An alternating PD runs across the primary coil</li> <li>● This causes an alternating current to flow in the primary coil</li> <li>● This causes an alternating magnetic field in the soft iron core as it cuts through it</li> <li>● The magnetic flux in the core links the primary and secondary coils</li> <li>● As there is a change in flux in the secondary coil this induces a EMF across the secondary coil due to faraday's law</li> <li>● This causes an alternating current in the</li> </ul>

secondary coil if there is a complete circuit

- If the transformer is a step up then the number of turns on the secondary coil is greater than the primary and therefore the flux linkage is greater on the secondary than the primary and a greater EMF is induced across the secondary coil as there is greater rate of change of flux linkage



Why does a transformer not work if a DC current flows through it?

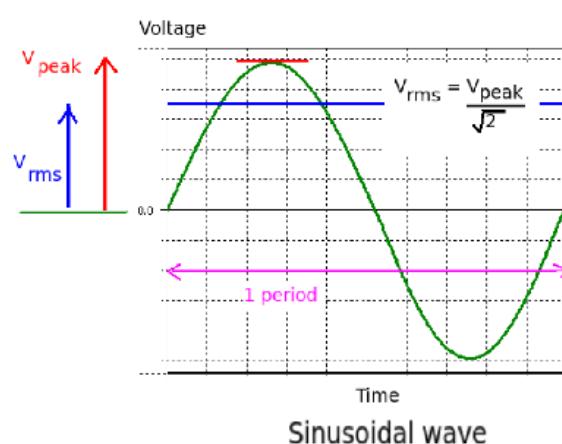
The rate of change of flux through the iron core is constant and so an EMF can not be induced in the secondary coil

### 7.128 understand what is meant by the terms *frequency*, *period*, *peak value* and *root-mean-square value* when applied to alternating currents and potential differences



### 7.129 be able to use the equations $V_{rms} = \frac{V_0}{\sqrt{2}}$ and $I_{rms} = \frac{I_0}{\sqrt{2}}$

What is RMS Voltage?



- This is the DC Equivalent of the AC voltage

	<ul style="list-style-type: none"><li>● The sine wave in the UK is 50 Hz</li></ul>
What are the 2 equations for rms	<ul style="list-style-type: none"><li>● <math>V_{rms} = V_0/\sqrt{2}</math></li><li>● <math>I_{rms} = I_0/\sqrt{2}</math></li></ul>