

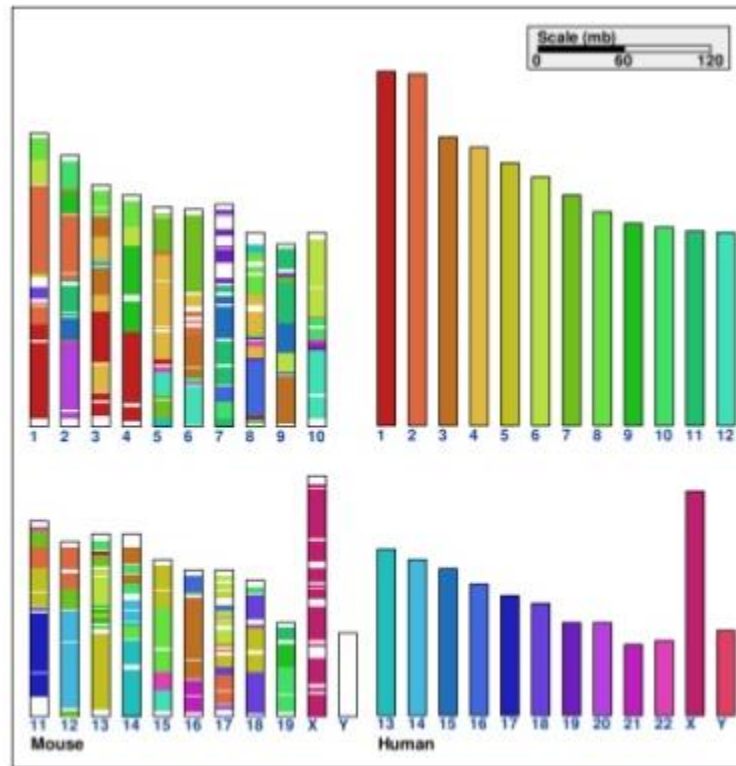
Synten Blocks

MPA-PRG: Programming in Bioinformatics

Exercise 8

Synteny Blocks

- a group of consecutive genes that do not have any structural aberrations (insertions, deletions, translocations of other genes)



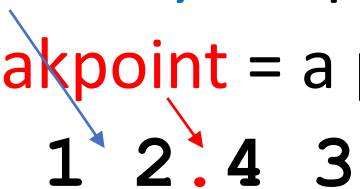
Comparison of Synteny Blocks

- compare the chromosome set of two organisms
- find the synteny blocks
- compare the positions of synteny blocks
- infer the possible steps of chromosomal aberrations leading from an unknown ancestor to the current descendants
- comparison of synteny blocks within several organisms can give a rough picture of the genome of their mutual ancestor

Sorting by reversals

- let $\pi = \pi_1 \pi_2 \dots \pi_n$ be a permutation of n distinct numbers and $1 \leq \pi_i \leq n$
- the reversal $\rho = \rho(i, j)$ for $1 \leq i < j \leq n$ applied to π reverses the values of $\pi_i \pi_{i+1} \dots \pi_{j-1} \pi_j$ and thus transforms π into a permutation
 $\pi \cdot \rho(i, j) = \pi_1 \dots \pi_j \pi_{j-1} \dots \pi_{i+1} \pi_i \dots \pi_n$
- for example: $\pi = 1 \ 2 \ 4 \ 3 \ 7 \ 5 \ 6$, then $\pi \cdot \rho(3, 6) = 1 \ 2 \ 5 \ 7 \ 3 \ 4 \ 6$
- the identity permutation I is the permutation where each $\pi_i = i$ for $1 \leq i \leq n$
- the distance $d(\pi, I)$ between π and I is the minimum number of reversals ρ that transform π to I

Breakpoint Sort

- greedy algorithm
 - minimize breakpoints between synteny blocks
 - **adjacency** = a pair of adjacent elements that are consecutive
 - **breakpoint** = a pair of adjacent elements that are not consecutive
- 1 2 . 4 3
- 
- block reversals are performed in such a way, that the number of breakpoints is reduced (or remains the same)
 - each reversal removes at most 2 breakpoints
 - number of reversals = hypothetical number of chromosomal changes

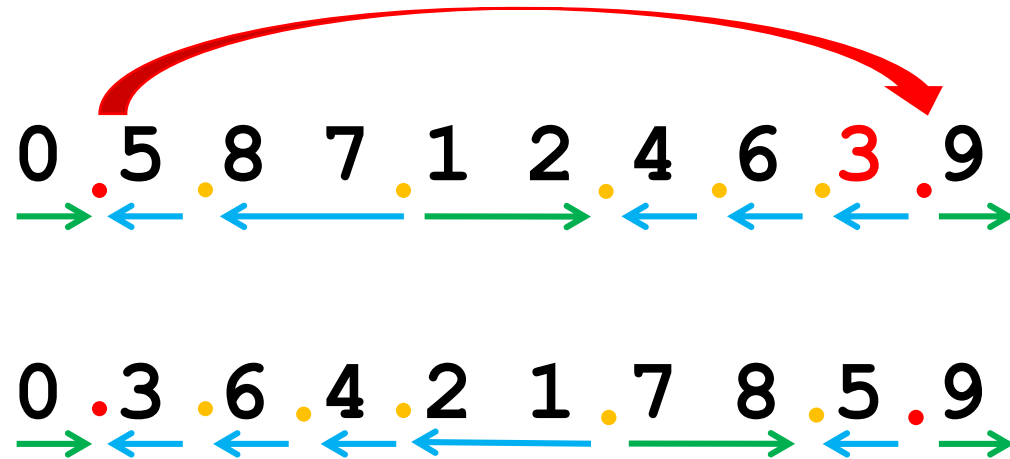
Breakpoint Sort – Steps

- extend the permutation $\pi_1 \dots \pi_n$ by $\pi_0 = 0$ and $\pi_{n+1} = n + 1$ on the ends, π_0 and π_{n+1} never change their positions
- mark the ascending and descending parts of the permutation
- reverse the descending part that will lead to the largest reduction in the number of breakpoints

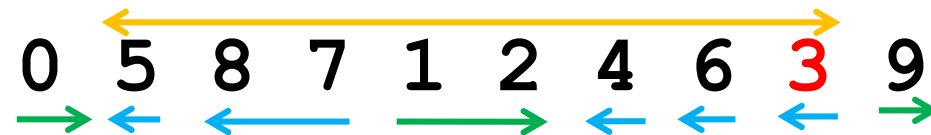


Reversal

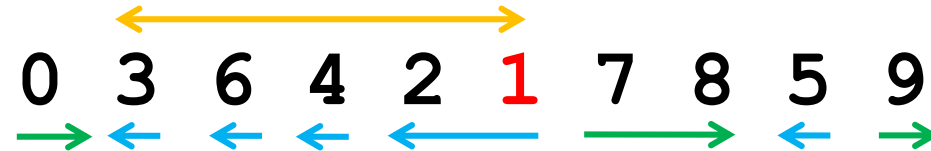
- find the descending part with the smallest value at the end
- reverse the region between the first breakpoint and the breakpoint following the selected descending part



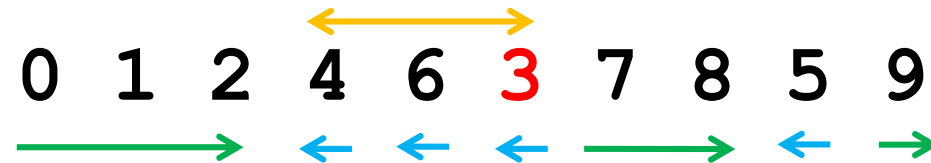
Example



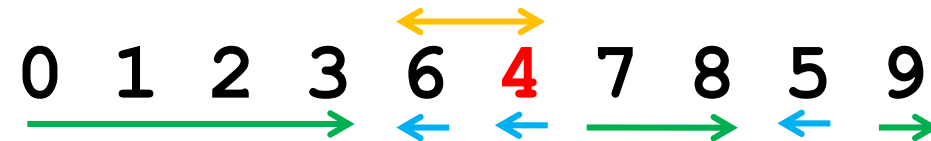
BP = 7



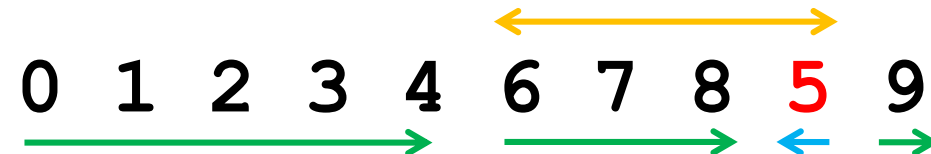
BP = 7



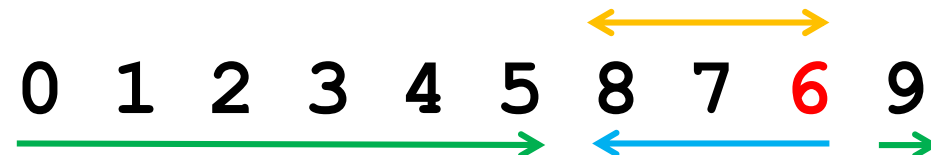
BP = 6



BP = 5



BP = 3



BP = 2

1 2 3 4 5 6 7 8

No Descending Part

- reverse the entire block between the first and last breakpoint
- or the ascending part that starts with the value "end of sorted part" + 1

0 1 2 5 6 3 4 7 8 9
→ → → →

0 1 2 4 3 6 5 7 8 9
→ ← ← →

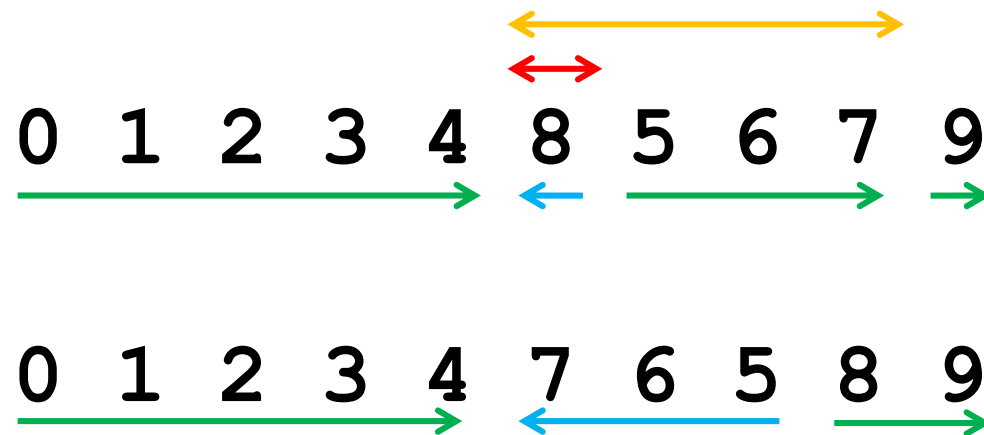
or

0 1 2 5 6 3 4 7 8 9
→ → → →

0 1 2 5 6 4 3 7 8 9
→ → ← →

One Descending Value in front of Sorted Part

- if the descending vector consists of one element and only the sorted part of the vector is in front of it, its reversal does not solve anything
- reverse the entire region between the first and last breakpoint



Example

- sort permutation $\pi = 5\ 3\ 2\ 1\ 8\ 7\ 4\ 6$ using the breakpoint sort

Tasks – The Breakpoint Sort

- implement function `FindSorted()`
- implement function `IndicateAscending()`
- implement function `BreakPointSort()`

Task 1

- In R, create a function `FindSorted()` to find an index, at which the unsorted part starts.
- Input:
 - a permutation of integers e.g. 0 1 2 3 6 7 4 5 8
- Output:
 - a position where the unsorted part starts at e.g. 5

Hint: Compare successively values of the permutation with an increasing number starting at zero (0, 1, 2, ...) and ending at length of the permutation - 1. The comparison ends when the value in permutation is not the same as the tested value or when the tested value is equal to the length of the permutation - 1.

Task 2

- In R, create a function `IndicateAscending()` to mark ascending and descending parts of the permutation.
- Input:
 - a permutation of integers e.g. 0 4 5 3 2 1 6 7 8
- Output:
 - a vector of zeros and ones, where ascending parts are marked by 1 and descending by 0 e.g. 1 1 1 0 0 0 1 1 1

Hint: Create an indication vector of the same length as the permutation containing only 0 values, and then set the first and last values to 1. The ascending parts of the permutation vector will be marked with 1 values in the indication vector. Create a loop that iterates through the permutation and if two values next to each other are ascending, i.e. the second is the first + 1, then the indication vector is set to 1 at the given indexes.

Task 3

- In R, create a function `BreakPointSort()` to sort a permutation using breakpoints.
- Input:
 - permutation of integers e.g. 5 1 4 3 7 8 9 2 6
- Output:
 - sorted permutation of integers e.g. 1 2 3 4 5 6 7 8 9

Hint: Add marginal values to the permutation and the following steps are repeated in the loop:

- find the start of the unsorted region,
- mark ascending/descending parts,
- find the smallest value that is marked as descending part,
- reversal between the start of unsorted region and the smallest value marked as descending.

The loop ends when the permutation vector is sorted. Watch out for collision situations.