

Graphical Abstract

Self-tunable approximated explicit MPC: Heat exchanger implementation

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Highlights

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- Research highlight 1
- Research highlight 2

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Abstract

max 250 words!

Keywords:

1. Introduction

2. Preliminaries

2.1. Explicit model predictive control

TODO: remark, ze sme si vedomi aj delta-u formulacie, ale viedie na zlozitejsie eMPC

2.2. Tunable explicit model predictive control

2.3. Self-tunable explicit model predictive control

3. Methodology

3.1. Self-tunable technique for systems with asymmetric behavior

TODO: spomenut, ze to je vhodne celkovo aj pre klasicke online MPC

4. Results and discussion

In this section, the results of the proposed tuning method are presented. The plant on which the control was implemented is a laboratory liquid-to-liquid plate heat exchanger Armfield Process Plant Trainer PCT23 [1], see Fig. 1. The cold feed as well as heating medium are transported to the heat exchanger by two peristaltic pumps. The flow rate of the feed is constant,

while the aim is to track the reference value of its temperature. Therefore, the controlled variable is the feed temperature T at the outlet of the heat exchanger and the manipulated variable is the voltage U corresponding to the power of the heating medium pump. The voltage is set in percentage, while it is constrained from 20% to 100%. As the heat exchange is a nonlinear and non-symmetric process [2], this heat exchanger represents a suitable candidate for the presented controller tuning strategy.

The matrices of the linear state-space model of the plant, discretized with sampling time $T_s = 1\text{ s}$, are

$$A = [0.839], \quad (1a)$$

$$B = [0.039], \quad (1b)$$

$$C = [1], \quad (1c)$$

$$D = [0]. \quad (1d)$$

The constraints are considered in the terms of manipulated variable, i.e.

$$-15\% \leq u \leq 65\%. \quad (2)$$

Note, the variable u represents the manipulated variable in the deviation form. The values of feed temperature and voltage of the heating medium pump corresponding to zero steady state are respectively $T^s = 35\text{ }^\circ\text{C}$ and $U^s = 35\%$.

The penalty matrices of the problem TODO:ref were systematically tuned and the corresponding control was implemented on the laboratory heat exchanger for every MPC setup. The aim was to determine, which penalty matrix will be the tuned one. Based on observations, the most significant effect on the control trajectories had tuning the penalty matrix Q_y , while still preserving a satisfactory control performance, i.e., without steady-state control error and significant oscillations around the setpoint. The boundary values of matrix Q_y were tuned as $Q_{y,L} = 100$ and $Q_{y,U} = 1000$. The built-in integrator was penalized with $Q_{x2} = 1$ and the manipulated variable with $R = 10$. The prediction horizon N was 20 steps long. The explicit model predictive controllers were constructed in MATLAB R2020b using the Multi-Parametric Toolbox 3 [3]. The controllers were implemented to track a time-varying reference. For the first 200 seconds, the system was in the

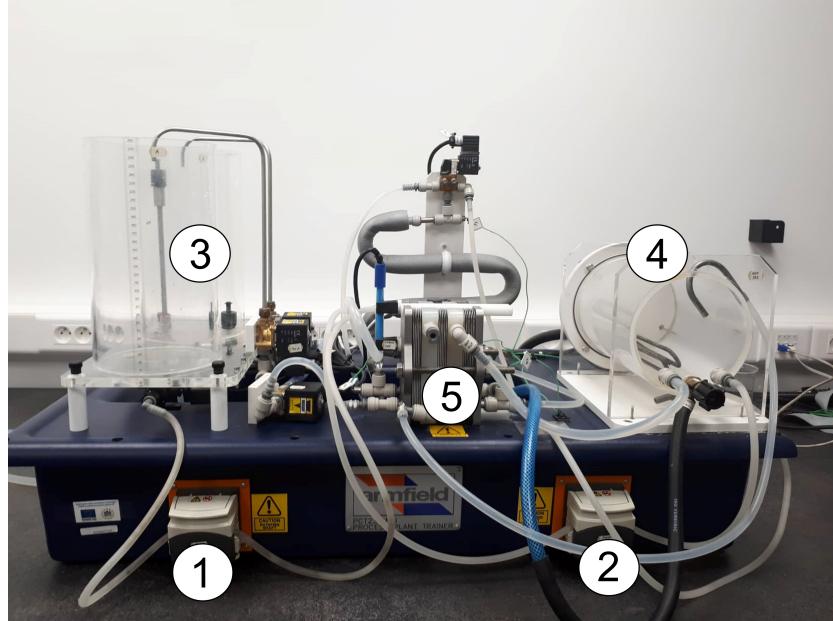


Figure 1: Laboratory heat exchanger Armfield Process Plant Trainer PCT23: feed pump (1), heating medium pump (2), feed tanks (3), heater for heating medium (4), heat exchanger (5).

steady state. After that the reference changed its value twice upwards and twice downwards. The reference changes also acquired different sizes in order to examine the proposed tuning method as it is dependent on the size of the reference step change. The control results for both control setups are compared in Fig. 2 for the controlled variable, and in Fig. 3 for the manipulated variable.

The trajectories in Fig. 2 show the non-symmetric nature of controlling the process of heat exchange mainly when observing the overshoots and undershoots. When applying the control associated with the lower bound $Q_{y,L}$, significant undershoots are present when tracking the reference downwards, i.e., when the reference change is negative. On the contrary, when implementing the controller associated with $Q_{y,U}$, the undershoots are negligible, but significant overshoots can be seen when tracking the reference upwards.

These observations form the base for the strategy of self-tuning the penalty matrix Q_y . The strategy follows the ideas summarized in Section 3.1.

TODO: dopisat strucne princip ladenia podla toho, ako bude spisana

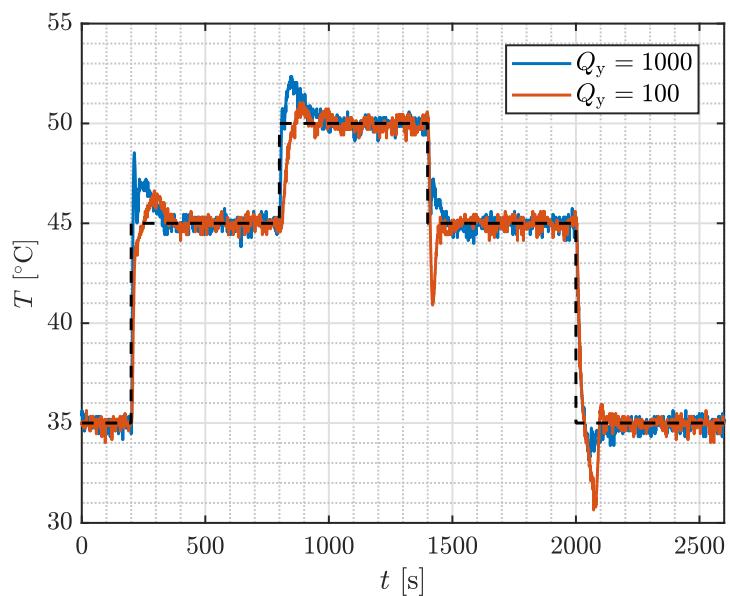


Figure 2: Controlled variable trajectory for two boundary controllers. The solid lines represent the controlled temperature and the dashed line represents the reference value.

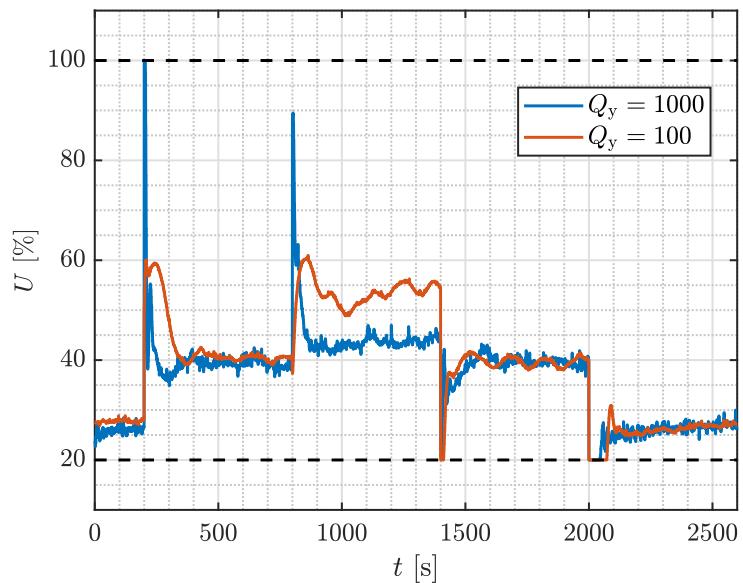


Figure 3: Manipulated variable trajectory for two boundary controllers. The solid lines represent the voltage and the dashed lines represent the constraints.

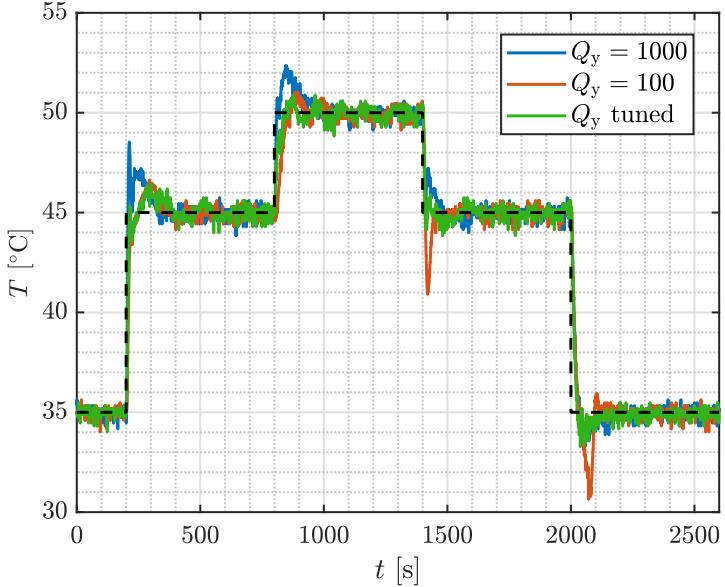


Figure 4: Controlled variable trajectory for two boundary controllers and the tuned one. The solid lines represent the controlled temperature and the dashed line represents the reference value.

teoria v 3.1. odkazat sa na rovnice atd...

The control results of the self-tunable technique compared to the boundary controllers can be seen in Fig. 4 for the controlled variable, and in Fig. 5 for the manipulated variable. It can be seen that the tuned controller combined the benefits of the two boundary controllers. The overshoots and undershoots were reduced, as in the first half of control the penalty matrix Q_y acquired value from the first half of the penalty interval. When tracking the reference with negative change, the penalty matrix acquired the values from the second half of the interval, i.e., closer to the upper bound $Q_{y,U}$. The similarity with the boundary controllers can be seen also on the manipulated variable trajectory. Note, the constraints on the input variable were satisfied as they were scaled based on the boundary controllers which are constructed considering the constraints.

TODO: what about state constraints?

The control performance was also investigated quantitatively. The Table 1 summarizes the evaluated control performance criteria for the tuned

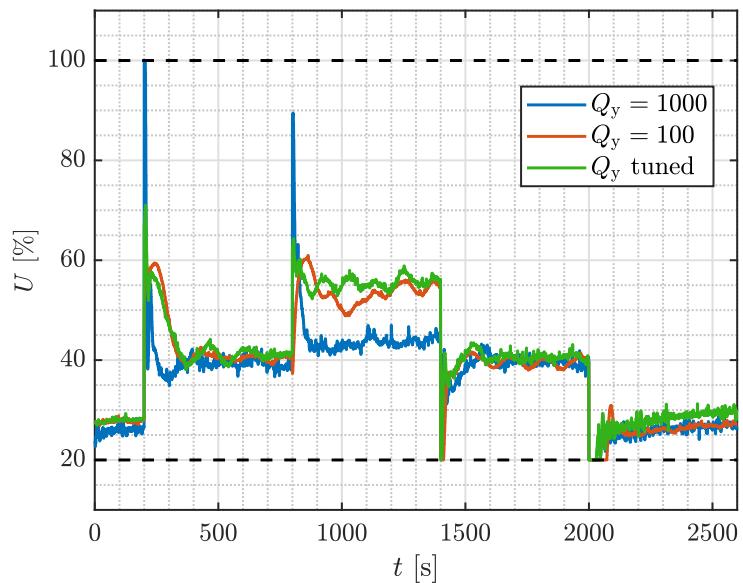


Figure 5: Manipulated variable trajectory for two boundary controllers and the tuned one. The solid lines represent the voltage and the dashed lines represent the constraints.

and two boundary controllers. The control performance is evaluated for every reference step change respectively. The criteria are integral square error ISE , maximal overshoot/undershoot σ_{\max} , settling time t_ϵ for 5%-neighbourhood of the reference value, and the volume of the heating medium utilized for the corresponding control. To provide better readability of the results, the best (i.e. minimal) values are written in bold.

Table 1: Control performance criteria.

Reference step change	Q_y	ISE [$^{\circ}\text{C}^2 \text{s}$]	σ_{\max} [%]	t_ϵ [s]	V [l]
1	1000	714	33.50	16.5	2.12
	100	867	16.65	12.5	2.36
	tuned	678	15.19	9.5	2.38
2	1000	365	47.20	5	2.49
	100	606	23.25	26.5	3.19
	tuned	248	19.13	9.5	3.35
3	1000	245	18.92	6.5	2.00
	100	398	79.64	31	2.00
	tuned	186	24.59	6.5	2.10
4	1000	1024	18.43	22.5	0.94
	100	1402	41.87	90	0.93
	tuned	967	16.49	18.5	1.10

It can be seen in Table 1, that real-time tuning of the controller helped to improve two to three criteria when tracking each reference value. The cost for this is the energy associated with control. Although the integral square error, maximal overshoot/undershoot and settling time decreased, the volume of consumed heating medium did not. Nevertheless, the average deterioration in the terms of consumed heating medium is approximately 17%.

The improvement or deterioration in percentage of using the tunable controller relative to the second best setup is summarized in Table 2 for every reference step change separately. The negative numbers represent deterioration compared to the best controller setup in the corresponding reference tracking.

It can be seen that implementing a tunable controller leads to improved control performance in many criteria. Utilizing a controller with a scalable aggressivity according to the operating conditions leads in general to higher

Table 2: Improvement or deterioration of the control performance in percentage.

Reference step change	ISE	σ_{\max}	t_ϵ	V
1	5.04	8.77	24.00	-12.26
2	32.05	17.72	-90.00	-34.54
3	24.08	-29.97	0	-4.48
4	5.57	10.53	17.78	-18.28

accuracy, lower overshoot and faster achieving the reference value. Although the volume of the heating medium is not saved in this control scenario, the improved control performance may lead to other benefits. TODO: krajsie skomentovať výhody zlepšenia kvality riadenia

5. Conclusion

References

- [1] Introduction Manual, PCT23-MkII Process Plant Trainer, Armfield, 2007.
- [2] B. G. Liptak, Instrument Engineers' Handbook, 4th Edition, Vol. 2: Process Control and Optimization, CRC Press, London, 2005.
- [3] M. Herceg, M. Kvasnica, C. Jones, M. Morari, Multi-parametric toolbox 3.0, in: European Control Conference, 2013, pp. 502–510.