

R Code

2025-06-05

#Load Packages

```
pacman::p_load("tidyverse", "lme4", "lmerTest", "mlmhelpr", "haven", "sjPlot", "quest", "mlmhelpr", "lattice", "interaction", "ggeffects", "lmtest", "sandwich", "multiwayvcov", "stargazer", "psych", "scales", "merTools", "emmeans", "HLMdiag", "sjPlot", "stringr", "mice", "nanian", "car", "patchwork")
```

#Load Data

```
soep <- readRDS("C:/Users/lenn0/AppData/Local/Temp/834af560-b32b-440a-afdf-938e22b26caa_SOEP-CORE.v39eu_R_EN.zip.caa/R_EN/soepdata/pequiv.rds")
```

#Data Wrangling

#Select variables that will be used in the subsequent analyses

```
soep_sub <- soep %>%
  dplyr::select(x1110111, x11102, d11101, d1110211, d11104, i11110, syer, d11108) %>%
  arrange(x1110111)
```

#Assign meaningful names to the variables

```
soep_sub <- soep_sub %>%
  rename(id_id = x1110111) %>%
  rename(hh_id = x11102) %>%
  rename(age = d11101) %>%
  rename(gender = d1110211) %>%
  rename(marital_status_unfinished = d11104) %>%
  rename(income = i11110) %>%
  rename(year = syer) %>%
  rename(education = d11108)
```

#Count units on each level

```
data.frame(
  level1_observations = nrow(soep_sub),
  level2_individuals = length(unique(soep_sub$id_id)),
  level3_households = length(unique(soep_sub$hh_id))
)
```

```
##   level1_observations level2_individuals level3_households
## 1             1148926             179412             66909
```

```

#Data Wrangling

#Code variables as numeric
soep_sub$income <- as.numeric(soep_sub$income)
soep_sub$age <- as.numeric(soep_sub$age)
soep_sub$gender <- as.numeric(soep_sub$gender)
soep_sub$marital_status_unfinished <- as.numeric(soep_sub$marital_status_unfinished)
soep_sub$education <- as.numeric(soep_sub$education)

#Filter the dataset for NAs and values that are relevant for the subsequent analyses
soep_fil <- soep_sub %>%
  filter(income >= 0) %>%
  filter(age >= 25 & age <= 60) %>%
  filter(gender > 0) %>%
  filter(marital_status_unfinished > 0) %>%
  filter(education != -1)

#Filter individuals between 25 and 60
soep_fil1 <- soep_sub %>%
  filter(age >= 25 & age <= 60)

#Recode gender so that male = 1 and female = 0
soep_fil <- soep_fil %>%
  mutate(male = case_when(
    gender == 1 ~ 1,
    gender == 2 ~ 0,
    TRUE ~ NA_real_))

#Recode marital status so that single = 0 and married = 1
soep_fil <- soep_fil %>%
  mutate(marital_status = marital_status_unfinished - 1) %>%
  mutate(marital_status = case_when(
    marital_status == 0 ~ 1,
    marital_status == 1 ~ 0,
    TRUE ~ marital_status ))

#Recode marital status so that single = 0 and married = 1
soep_fil <- soep_fil %>%
  mutate(education = education - 1)

soep_fil$education <- as.character(soep_fil$education)

#Create a new variable for which single = 0, married = 1, and other = 2
soep_fil <- soep_fil %>%
  mutate(marital_status_reduced = case_when(
    marital_status == 0 ~ 0,
    marital_status == 1 ~ 1,
    marital_status > 1 ~ 2
  ))

#Create a quadratic polynomial of age
soep_fil <- soep_fil %>%
  mutate(age_squared = age^2)

#Create a variable representing the logarithm of income
soep_fil <- soep_fil %>%
  mutate(log_income = case_when(
    income > 0 ~ log(income),
    income == 0 ~ 0,
    TRUE ~ NA_real_))

```

```

#Data Wrangling

#Center age and age-squared
soep_fil <- soep_fil %>%
  mutate(age_c = age - mean(age, na.rm = T)) %>%
  mutate(age_squared_c = age_squared - mean(age_squared, na.rm = T))

```

```
#Data Wrangling

#Compute mean income for each age group (by years)
soep_summary1 <- soep_fil %>%
  group_by(age) %>%
  summarise(mean_income_age = mean(income, na.rm = T), .groups = "drop")

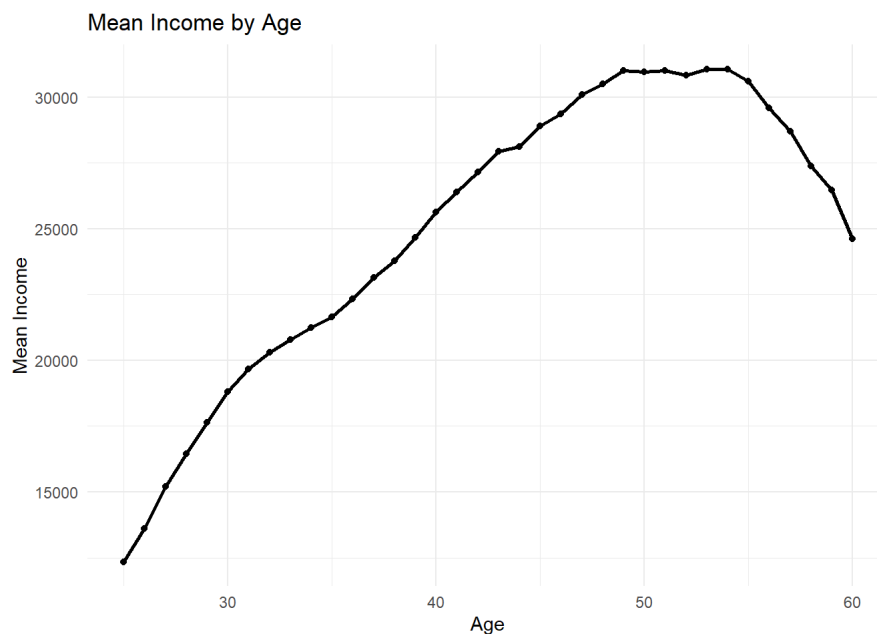
#Compute mean income for each age group conditioned on gender
soep_summary3 <- soep_fil %>%
  group_by(age, male) %>%
  summarise(mean_income_age = mean(income, na.rm = TRUE), .groups = "drop")

#Compute mean income for each age group conditioned on gender and marital status
soep_summary5 <- soep_fil %>%
  mutate(gender_marital_status = case_when(
    male == 0 & marital_status_reduced == 0 ~ "female_single",
    male == 0 & marital_status_reduced == 1 ~ "female_married",
    male == 0 & marital_status_reduced == 2 ~ "female_other",
    male == 1 & marital_status_reduced == 0 ~ "male_single",
    male == 1 & marital_status_reduced == 1 ~ "male_married",
    male == 1 & marital_status_reduced == 2 ~ "male_other")) %>%
  group_by(age, gender_marital_status) %>%
  summarise(mean_income_age_marital_status_gender = mean(income, na.rm = TRUE), .groups = "drop")
```

#Graphical Analysis

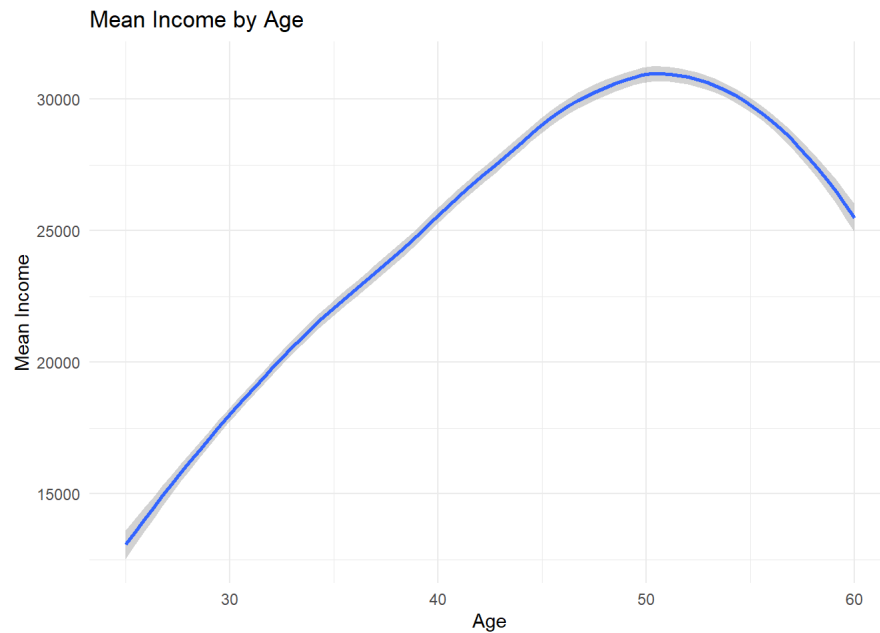
```
#Mean income
ggplot(soep_summary1, aes(x = age, y = mean_income_age))+
  geom_line(size =1) +
  geom_point() +
  labs(
    title = "Mean Income by Age",
    x = "Age",
    y = "Mean Income") +
  theme_minimal()
```

```
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
```

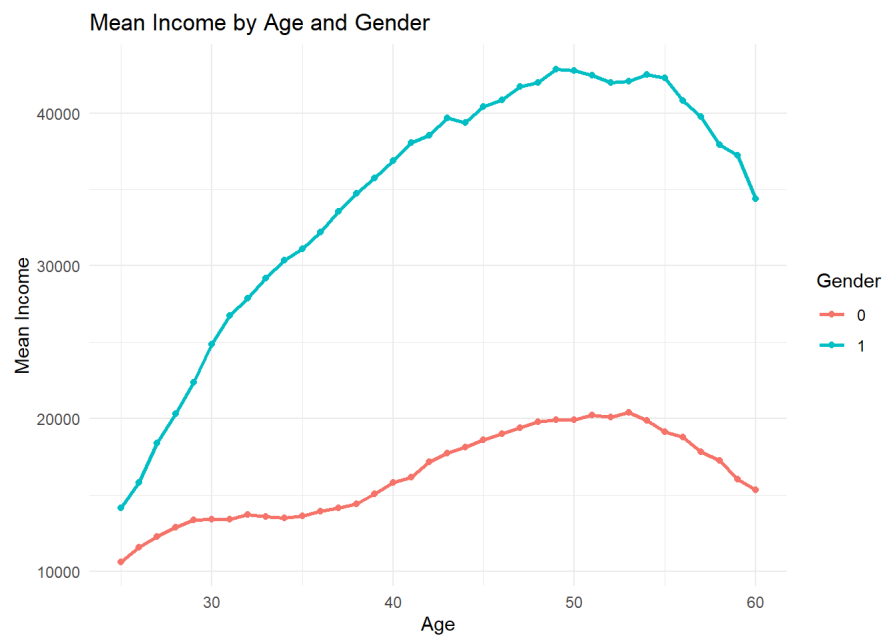


```
ggplot(soep_summary1, aes(x = age, y = mean_income_age))+
  geom_smooth(size =1) +
  labs(
    title = "Mean Income by Age",
    x = "Age",
    y = "Mean Income") +
  theme_minimal()
```

```
## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'
```



```
#Mean income by age and gender
ggplot(soep_summary3, aes(x = age, y = mean_income_age, color = as.factor(male))) +
  geom_line(size = 1) +
  geom_point() +
  labs(
    title = "Mean Income by Age and Gender",
    x = "Age",
    y = "Mean Income",
    color = "Gender") +
  theme_minimal()
```

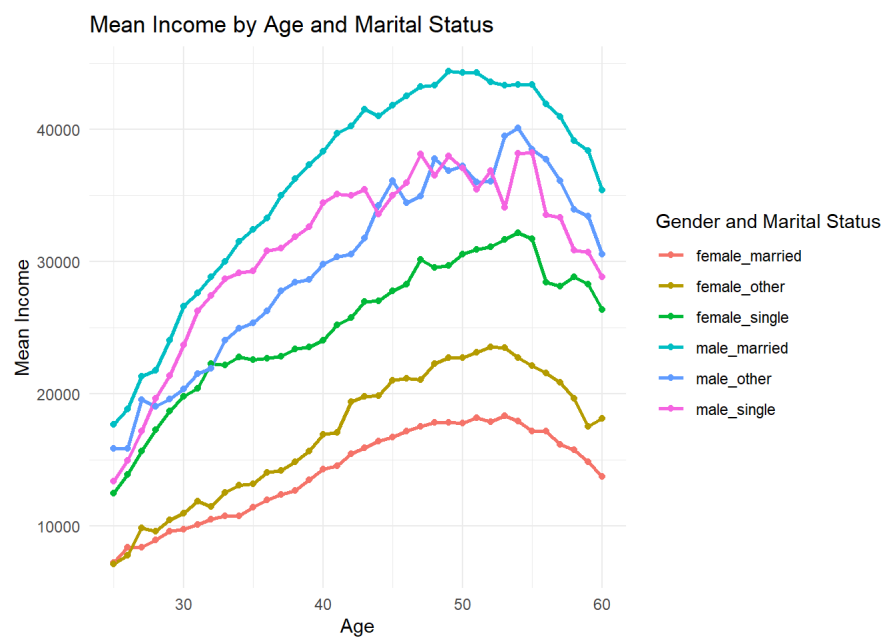


```
ggplot(soep_summary3, aes(x = age, y = mean_income_age, color = as.factor(male))) +
  geom_smooth(size = 1) +
  labs(
    title = "Mean Income by Age and Gender",
    x = "Age",
    y = "Mean Income",
    color = "Gender") +
  theme_minimal()
```

```
## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'
```

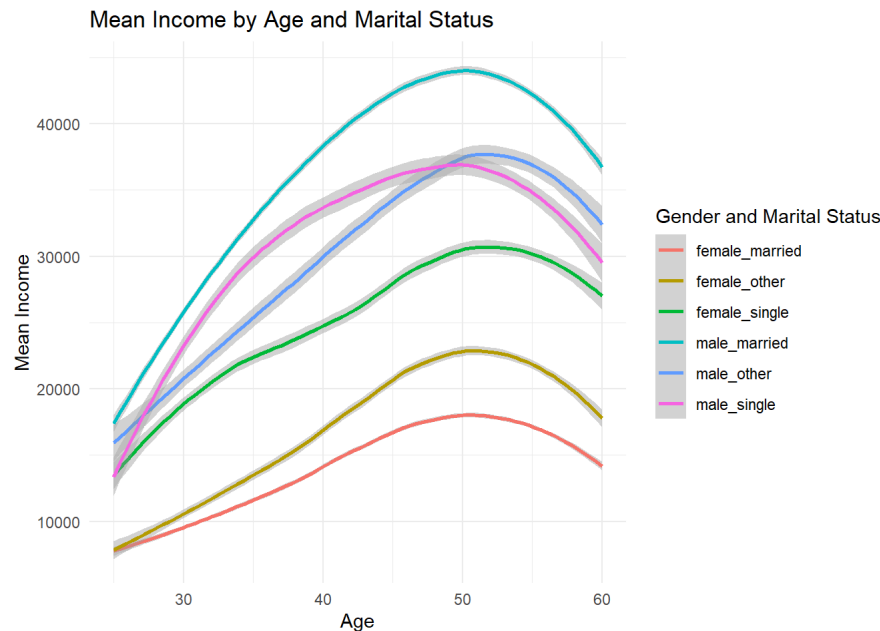


```
#Mean income by age, gender, and marital status
ggplot(soep_summary5, aes(x = age, y = mean_income_age_marital_status_gender, color = as.factor(gender_marital_status))) +
  geom_line(size = 1) +
  geom_point() +
  labs(
    title = "Mean Income by Age and Marital Status",
    x = "Age",
    y = "Mean Income",
    color = "Gender and Marital Status") +
  theme_minimal()
```



```
ggplot(soep_summary5, aes(x = age, y = mean_income_age_marital_status_gender, color = as.factor(gender_marital_status))) +
  geom_smooth(size = 1) +
  labs(
    title = "Mean Income by Age and Marital Status",
    x = "Age",
    y = "Mean Income",
    color = "Gender and Marital Status") +
  theme_minimal()
```

```
## `geom_smooth()` using method = 'loess' and formula = 'y ~ x'
```



```
#Filter the dataset for individuals that went from unmarried to married during the course of the panel
ids_changed <- soep_fil %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(prev_marital_status = lag(marital_status_reduced)) %>%
  filter(prev_marital_status == 0 & marital_status_reduced == 1) %>%
  distinct(id_id)

soep_changed <- soep_fil %>%
  filter(id_id %in% ids_changed$id_id)
```

```
#Determine the year in which the individual got married
soep_d <- soep_fil %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(prev_marital_status = lag(marital_status_reduced),
         transition = prev_marital_status == 0 & marital_status_reduced == 1) %>%
  filter(transition) %>%
  slice(1) %>%
  dplyr::select(id_id, transition_year = year)
```

```
#Center the variable so that 0 = year of marriage
soep_final <- soep_fil %>%
  inner_join(soep_d, by = "id_id") %>%
  mutate(relative_year = year - transition_year)
```

```
#Once married individuals are permanently coded as married
soep_final <- soep_final %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(married = cummax(marital_status_reduced %in% c(1, 2)))
```

```
#Count observations on each Level
data.frame(
  level1_observations = nrow(soep_final),
  level2_individuals = length(unique(soep_final$id_id)),
  level3_households = length(unique(soep_final$hh_id)))
```

```
##   level1_observations level2_individuals level3_households
## 1             64997             4885             4730
```

```
#Check skew
describe(soep_final$income)
```

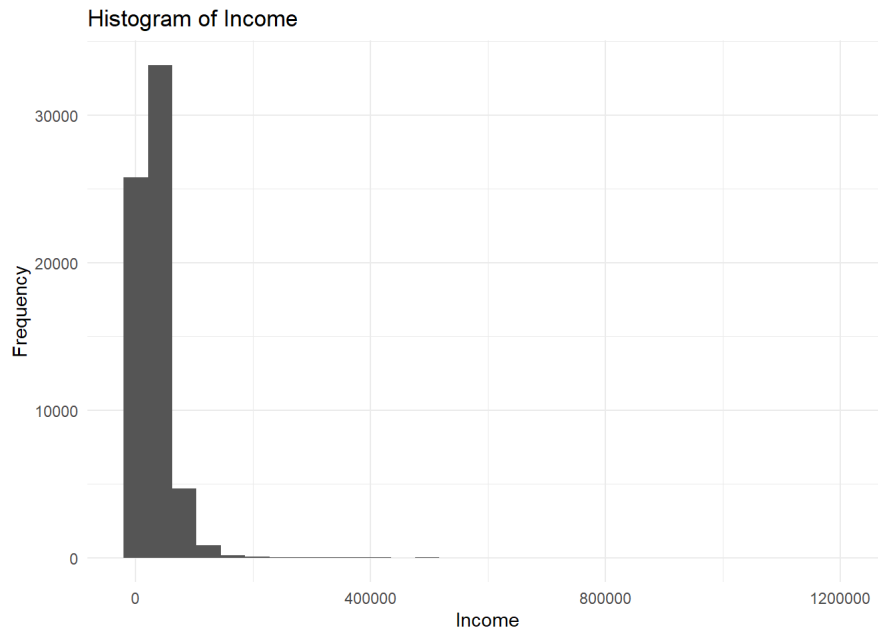
```
##   vars    n    mean    sd median trimmed   mad min    max range
## X1      1 64997 29828.82 27721.38  25695 26405.71 21032.16   0 1199988 1199988
##   skew kurtosis    se
## X1  4.7    94.07 108.73
```

```
describe(soep_final$log_income)
```

```
##      vars      n mean  sd median trimmed mad min max range skew kurtosis  se
## X1      1 64997 9.07 3.15 10.15    9.92 0.8  0 14   14 -2.3    3.9 0.01
```

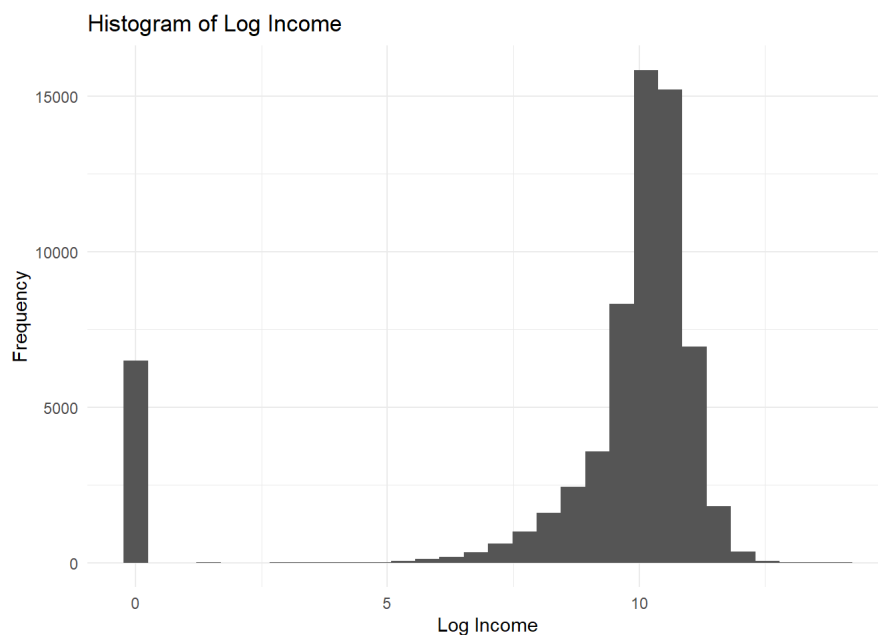
```
#Histogram of income
ggplot(soep_final, aes(x = income)) +
  geom_histogram() +
  labs(
    title = "Histogram of Income",
    x = "Income",
    y = "Frequency"
  ) +
  theme_minimal()
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```
#Histogram of Log income
ggplot(soep_final, aes(x = log_income)) +
  geom_histogram() +
  labs(
    title = "Histogram of Log Income",
    x = "Log Income",
    y = "Frequency"
  ) +
  theme_minimal()
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



```

soep_final <- soep_final %>%
  mutate(relative_year_squared = relative_year^2)

#Standardize variables
soep_final <- soep_final %>%
  mutate(
    age_sd = (age_c) / sd(age_c, na.rm = TRUE),
    age_squared_sd = (age_squared_c) / sd(age_squared_c, na.rm = TRUE),
    married_sd = (married - mean(married, na.rm = TRUE)) / sd(married, na.rm = TRUE),
    male_sd = (male - mean(male, na.rm = TRUE)) / sd(male, na.rm = TRUE),
    relative_year_sd = (relative_year - mean(relative_year, na.rm = TRUE)) / sd(relative_year, na.rm = TRUE),
    relative_year_squared_sd = (relative_year_squared - mean(relative_year_squared, na.rm = TRUE)) / sd(relative_year_squared, na.rm = TRUE))

#Center transition_year
soep_final <- soep_final %>%
  mutate(transition_year = transition_year - 1985)

#Convert the variables "male" and "married" to factors
soep_final <- soep_final %>%
  ungroup() %>%
  mutate(
    male = factor(male, levels = c(0, 1), labels = c("Female", "Male")),
    married = factor(married, levels = c(0, 1), labels = c("No", "Yes"))
  )

#Create a new time variable with 0 = start of the panel
soep_final <- soep_final %>%
  mutate(year_1984 = year - 1984)

soep_final$education <- factor(soep_final$education)

```

```

# Compute mean Log income and CIs
soep_k <- soep_final %>%
  group_by(male, married) %>%
  summarise(
    mean_log_income = mean(log_income, na.rm = TRUE),
    se_log = sd(log_income, na.rm = TRUE) / sqrt(n()),
    ci_lower_log = mean_log_income - 1.96 * se_log,
    ci_upper_log = mean_log_income + 1.96 * se_log,
    .groups = "drop"
  )

# Plot with CIs
p1 <- ggplot(soep_k, aes(x = as.factor(married), y = mean_log_income, fill = as.factor(male))) +
  geom_bar(stat = "identity", position = position_dodge(width = 0.7), width = 0.6) +
  geom_errorbar(
    aes(ymin = ci_lower_log, ymax = ci_upper_log),
    position = position_dodge(width = 0.7),
    width = 0.25,
    color = "black",
    linewidth = 0.5
  ) +
  scale_x_discrete(labels = c("0" = "Not Married", "1" = "Married")) +
  scale_fill_manual(
    values = c("Female" = "red", "Male" = "blue"),
    labels = c("Female", "Male")
  ) +
  labs(
    title = "Mean Log-Income by Marital Status and Gender (with 95% CIs)",
    x = "Married",
    y = "Log-Income",
    fill = "Gender"
  ) +
  theme_minimal()

soep_l <- soep_final %>%
  group_by(relative_year, male) %>%
  summarise(
    log_mean_income = mean(log_income, na.rm = TRUE),
    sd_log_income = sd(log_income, na.rm = TRUE),
    n = sum(!is.na(log_income)),
    se = sd_log_income / sqrt(n),
    ci_lower = log_mean_income - 1.96 * se,
    ci_upper = log_mean_income + 1.96 * se
  ) %>%
  ungroup()

```



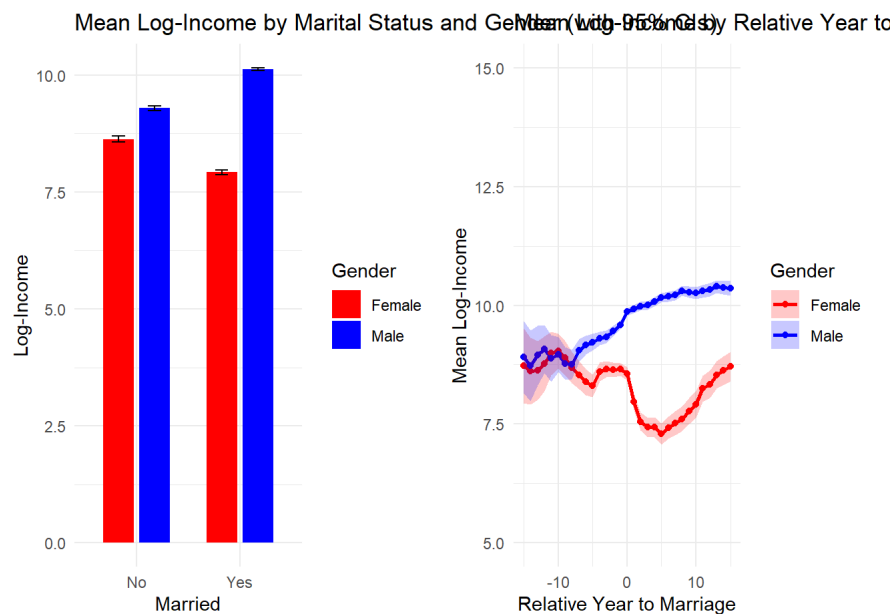
```
## `summarise()` has grouped output by 'relative_year'. You can override using the
## `.groups` argument.
```

```
p2 <- ggplot(soep_l, aes(x = relative_year, y = log_mean_income, color = as.factor(male))) +
  geom_line(size = 1) +
  geom_point() +
  geom_ribbon(
    aes(ymin = ci_lower, ymax = ci_upper, fill = as.factor(male)),
    alpha = 0.2,
    color = NA) +
  scale_x_continuous(limits = c(-15, 15)) +
  scale_y_continuous(limits = c(5, 15)) +
  scale_color_manual(
    values = c("Female" = "red", "Male" = "blue"),
    labels = c("Female", "Male")) +
  scale_fill_manual(
    values = c("Female" = "red", "Male" = "blue"),
    labels = c("Female", "Male")) +
  labs(
    title = "Mean Log-Income by Relative Year to Marriage (95% CIs)",
    x = "Relative Year to Marriage",
    y = "Mean Log-Income",
    color = "Gender",
    fill = "Gender") +
  theme_minimal()

#Combine and plot the plots for the graphical analysis
combined_plot <- p1 + p2
combined_plot
```

```
## Warning: Removed 65 rows containing missing values or values outside the scale range
## (`geom_line()`).
```

```
## Warning: Removed 65 rows containing missing values or values outside the scale range
## (`geom_point()`).
```



```
#OLS baseline model
ols0 <- lm(log_income ~ year_1984, data = soep_final)
summary(ols0)
```

```
##
## Call:
## lm(formula = log_income ~ year_1984, data = soep_final)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.4699  0.3131  1.1270  1.5306  4.6215
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  8.435119   0.033732   250.06  <2e-16 ***
## year_1984    0.027232   0.001346    20.23  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.145 on 64995 degrees of freedom
## Multiple R-squared:  0.006257, Adjusted R-squared:  0.006242
## F-statistic: 409.2 on 1 and 64995 DF, p-value: < 2.2e-16
```

```
#OLS final Model 1
ols1 <- lm(log_income ~ year_1984 + age_sd + age_squared_sd + education + married*male + transition_year, data = soep_final)
summary(ols1)
```

```
##
## Call:
## lm(formula = log_income ~ year_1984 + age_sd + age_squared_sd +
##      education + married * male + transition_year, data = soep_final)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.3323  0.0012  0.6928  1.5314  5.1979
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)      6.506856   0.064039  101.608  <2e-16 ***
## year_1984         0.031226   0.002292   13.624  <2e-16 ***
## age_sd            0.080388   0.035021    2.295   0.0217 *
## age_squared_sd   -0.022182   0.026647   -0.832   0.4052
## education1        1.544496   0.048540   31.819  <2e-16 ***
## education2        2.326532   0.050337   46.219  <2e-16 ***
## marriedYes       -1.033450   0.042951  -24.061  <2e-16 ***
## maleMale          0.720245   0.040921   17.601  <2e-16 ***
## transition_year   -0.002289   0.002124   -1.078   0.2812
## marriedYes:maleMale 1.541858   0.049539   31.124  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.938 on 64987 degrees of freedom
## Multiple R-squared:  0.1326, Adjusted R-squared:  0.1325
## F-statistic: 1104 on 9 and 64987 DF, p-value: < 2.2e-16
```

```
clustered_se <- cluster.vcov(ols1, cluster = soep_final[, c("id_id", "hh_id")])

#OLS final Model 1 with clustered se
ols1_clustered_se <- coeftest(ols1, vcov = clustered_se)
summary(ols1_clustered_se)
```

```
##      Estimate      Std. Error      t value      Pr(>|t|)
## Min.      :-1.03345 Min.      :0.005548 Min.      :-12.72343 Min.      :0.0000
## 1st Qu.:  0.00609 1st Qu.:0.066494 1st Qu.:  -0.02927 1st Qu.:0.0000
## Median :  0.40032 Median :0.084783 Median :   7.27671 Median :0.0000
## Mean   :  1.16937 Mean   :0.096361 Mean   :   7.36450 Mean   :0.1786
## 3rd Qu.:  1.54384 3rd Qu.:0.154412 3rd Qu.:  12.44133 3rd Qu.:0.2721
## Max.    :  6.50686 Max.    :0.199016 Max.    :  32.69512 Max.    :0.7321
```

```
stargazer(ols1, ols1_clustered_se, type = "text")
```

```
##
## =====
##                               Dependent variable:
##                               -----
##                               log_income
##                               OLS                coefficient
##                               test
##                               (1)                (2)
## -----
## year_1984                0.031***                0.031***
##                               (0.002)                (0.006)
##
## age_sd                0.080**                0.080
##                               (0.035)                (0.088)
##
## age_squared_sd                -0.022                -0.022
##                               (0.027)                (0.065)
##
## education1                1.544***                1.544***
##                               (0.049)                (0.173)
##
## education2                2.327***                2.327***
##                               (0.050)                (0.176)
##
## marriedYes                -1.033***                -1.033***
##                               (0.043)                (0.081)
##
## maleMale                0.720***                0.720***
##                               (0.041)                (0.072)
##
## transition_year                -0.002                -0.002
##                               (0.002)                (0.006)
##
## marriedYes:maleMale                1.542***                1.542***
##                               (0.050)                (0.098)
##
## Constant                6.507***                6.507***
##                               (0.064)                (0.199)
##
## -----
## Observations                64,997
## R2                0.133
## Adjusted R2                0.132
## Residual Std. Error                2.938 (df = 64987)
## F Statistic                1,103.850*** (df = 9; 64987)
## =====
## Note:                *p<0.1; **p<0.05; ***p<0.01
```

```
#OLS final Model 2
ols2 <- lm(log_income ~ year_1984 + education + relative_year_sd*male + relative_year_squared_sd*male , data = soep_final)
summary(ols2)
```

```
##
## Call:
## lm(formula = log_income ~ year_1984 + education + relative_year_sd *
##     male + relative_year_squared_sd * male, data = soep_final)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -11.6723   0.0088   0.7186   1.6041   5.6926
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.837556   0.060972   95.74 < 2e-16 ***
## year_1984       0.023592   0.001589   14.85 < 2e-16 ***
## education1     1.552302   0.048618   31.93 < 2e-16 ***
## education2     2.331263   0.050410   46.25 < 2e-16 ***
## relative_year_sd -0.072211   0.021301   -3.39 0.000699 ***
## maleMale       1.781322   0.023385   76.17 < 2e-16 ***
## relative_year_squared_sd  0.066745   0.019691    3.39 0.000700 ***
## relative_year_sd:maleMale  0.412033   0.026733   15.41 < 2e-16 ***
## maleMale:relative_year_squared_sd -0.320318   0.026727  -11.98 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.955 on 64988 degrees of freedom
## Multiple R-squared:  0.1228, Adjusted R-squared:  0.1227
## F-statistic: 1137 on 8 and 64988 DF, p-value: < 2.2e-16
```

```
clustered_se2 <- cluster.vcov(ols2, cluster = soep_final[, c("id_id", "hh_id")])

#OLS final Model 2 with clustered se
ols2_clustered_se <- coeftest(ols2, vcov = clustered_se2)
summary(ols2_clustered_se)
```

```
##      Estimate      Std. Error      t value      Pr(>|t|)
## Min.      :-0.32032   Min.      :0.004017   Min.      :-8.266   Min.      :0.000e+00
## 1st Qu.: 0.02359   1st Qu.:0.038752   1st Qu.: 2.166   1st Qu.:0.000e+00
## Median : 0.41203   Median :0.043932   Median : 9.026   Median :0.000e+00
## Mean    : 1.29025   Mean    :0.085640   Mean     : 9.656   Mean    :1.418e-02
## 3rd Qu.: 1.78132   3rd Qu.:0.171975   3rd Qu.:13.381   3rd Qu.:4.000e-09
## Max.    : 5.83756   Max.    :0.199184   Max.     :29.307   Max.    :9.728e-02
```

```
stargazer(ols2, ols2_clustered_se, type = "text")
```

```
##
## =====
##                               Dependent variable:
##                               -----
##                               log_income
##                               OLS          coefficient
##                               test
##                               (1)          (2)
## -----
## year_1984                      0.024***      0.024***
##                               (0.002)      (0.004)
##
## education1                     1.552***      1.552***
##                               (0.049)      (0.172)
##
## education2                     2.331***      2.331***
##                               (0.050)      (0.174)
##
## relative_year_sd              -0.072***      -0.072*
##                               (0.021)      (0.044)
##
## maleMale                      1.781***      1.781***
##                               (0.023)      (0.064)
##
## relative_year_squared_sd       0.067***      0.067**
##                               (0.020)      (0.031)
##
## relative_year_sd:maleMale      0.412***      0.412***
##                               (0.027)      (0.044)
##
## maleMale:relative_year_squared_sd -0.320***      -0.320***
##                               (0.027)      (0.039)
##
## Constant                      5.838***      5.838***
##                               (0.061)      (0.199)
##
## -----
## Observations                   64,997
## R2                             0.123
## Adjusted R2                   0.123
## Residual Std. Error           2.955 (df = 64988)
## F Statistic                   1,137.052*** (df = 8; 64988)
## =====
## Note:                          *p<0.1; **p<0.05; ***p<0.01
```

```
#Random Intercept
m11 <- lmer(log_income ~ year_1984 + (1|hh_id) + (1|id_id), data = soep_final, REML = F)
summary(m11)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 305272.6 305318.0 -152631.3 305262.6      64992
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8936 -0.0280  0.0887  0.2887  4.0013
##
## Random effects:
## Groups   Name      Variance Std.Dev.
## id_id    (Intercept) 3.318    1.821
## hh_id    (Intercept) 2.587    1.608
## Residual                    5.200    2.280
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept) 8.048e+00  5.282e-02 1.412e+04 152.37  <2e-16 ***
## year_1984   3.540e-02  1.529e-03 6.155e+04 23.16  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr)
## year_1984 -0.692
```

```
icc(ml1)
```

```
##              grps   icc
## 1 id_id (Intercept) 0.299
## 2 hh_id (Intercept) 0.233
## 3      Residual 0.468
```

```
##+key level 1 predictor
ml2 <- lmer(log_income ~ year_1984 + married + (1|hh_id) + (1|id_id), data = soep_final, REML = F)
summary(ml2)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + married + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 305255.3 305309.8 -152621.6 305243.3      64991
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8843 -0.0313  0.0897  0.2907  4.0285
##
## Random effects:
## Groups   Name      Variance Std.Dev.
## id_id    (Intercept) 3.321    1.822
## hh_id    (Intercept) 2.606    1.614
## Residual                    5.196    2.280
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept) 8.023e+00  5.316e-02 1.389e+04 150.921 < 2e-16 ***
## year_1984   3.944e-02  1.782e-03 5.798e+04 22.125 < 2e-16 ***
## marriedYes -1.205e-01  2.736e-02 6.414e+04 -4.404 1.06e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984
## year_1984   -0.644
## marriedYes  0.105 -0.514
```

```
##+ Level 1 control variables
ml3 <- lmer(log_income ~ year_1984 + age_sd + age_squared_sd + education + married + (1|hh_id) + (1|id_id), data = soep_fina
l, REML = F)
summary(ml3)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + age_sd + age_squared_sd + education +
## married + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 304149.2  304240.1 -152064.6  304129.2    64987
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8412 -0.0429  0.0909  0.2964  4.0239
##
## Random effects:
## Groups      Name                Variance Std.Dev.
## id_id      (Intercept)          3.355    1.832
## hh_id      (Intercept)          2.256    1.502
## Residual                    5.125    2.264
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)  7.789e+00  1.134e-01  1.355e+04  68.685 < 2e-16 ***
## year_1984    1.737e-02  2.436e-03  1.992e+04   7.128 1.05e-12 ***
## age_sd       3.641e-01  5.839e-02  1.310e+04   6.235 4.66e-10 ***
## age_squared_sd -2.217e-01  4.479e-02  1.215e+04  -4.951 7.50e-07 ***
## education1    6.084e-01  9.121e-02  2.051e+04   6.670 2.62e-11 ***
## education2    2.136e+00  9.969e-02  1.849e+04  21.427 < 2e-16 ***
## marriedYes   -2.885e-01  2.994e-02  6.219e+04  -9.637 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 age_sd ag_sq_ edctn1 edctn2
## year_1984    -0.491
## age_sd        0.314 -0.635
## age_sqrd_sd  -0.248  0.593 -0.990
## education1   -0.715 -0.040  0.025 -0.033
## education2   -0.670 -0.069  0.010 -0.018  0.861
## marriedYes   -0.145 -0.044 -0.378  0.347 -0.008 -0.029
```

```
##key level 2 predictor
m14 <- lmer(log_income ~ year_1984 + age_sd + age_squared_sd + education + married + male + (1|hh_id) + (1|id_id), data = soep_final, REML = F)
summary(m14)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + age_sd + age_squared_sd + education +
## married + male + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 303309.8 303409.7 -151643.9 303287.8    64986
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8583 -0.0510  0.0866  0.3069  4.0339
##
## Random effects:
## Groups   Name                Variance Std.Dev.
## id_id    (Intercept)         2.350    1.533
## hh_id    (Intercept)         2.345    1.531
## Residual                            5.132    2.265
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)  6.602e+00  1.139e-01  1.151e+04  57.965 < 2e-16 ***
## year_1984    2.283e-02  2.352e-03  1.874e+04   9.707 < 2e-16 ***
## age_sd       2.764e-01  5.549e-02  1.260e+04   4.981 6.42e-07 ***
## age_squared_sd -1.734e-01  4.243e-02  1.185e+04  -4.086 4.42e-05 ***
## education1    7.006e-01  8.715e-02  1.746e+04   8.039 9.65e-16 ***
## education2    2.171e+00  9.508e-02  1.585e+04  22.832 < 2e-16 ***
## marriedYes   -2.611e-01  2.966e-02  6.136e+04  -8.804 < 2e-16 ***
## maleMale     1.698e+00  5.452e-02  3.215e+03  31.140 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 age_sd ag_sq_ edctn1 edctn2 mrrdYs
## year_1984    -0.488
## age_sd       0.314 -0.623
## age_sqrd_sd  -0.249  0.583 -0.990
## education1   -0.682 -0.039  0.025 -0.033
## education2   -0.642 -0.068  0.011 -0.020  0.859
## marriedYes   -0.143 -0.062 -0.370  0.340 -0.008 -0.027
## maleMale     -0.329  0.079 -0.050  0.034  0.010  0.020  0.025
```

```
#+ Level 2 control variables
```

```
m14a <- lmer(log_income ~ year_1984 + age_sd + age_squared_sd + education + married + male + transition_year + (1|hh_id) +
(1|id_id), data = soep_final, REML = F)
summary(m14a)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + age_sd + age_squared_sd + education +
## married + male + transition_year + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 303299.8 303408.8 -151637.9 303275.8    64985
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8828 -0.0518  0.0873  0.3076  4.0473
##
## Random effects:
## Groups   Name                Variance Std.Dev.
## id_id    (Intercept)         2.345    1.531
## hh_id    (Intercept)         2.338    1.529
## Residual                    5.132    2.265
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)   6.783e+00  1.254e-01  8.453e+03  54.088 < 2e-16 ***
## year_1984     2.726e-02  2.677e-03  3.413e+04  10.183 < 2e-16 ***
## age_sd        2.440e-01  5.624e-02  1.297e+04   4.339 1.45e-05 ***
## age_squared_sd -1.559e-01  4.270e-02  1.212e+04  -3.652 0.000261 ***
## education1     6.928e-01  8.714e-02  1.746e+04   7.951 1.97e-15 ***
## education2     2.170e+00  9.503e-02  1.584e+04  22.833 < 2e-16 ***
## marriedYes    -2.783e-01  3.008e-02  6.446e+04  -9.254 < 2e-16 ***
## maleMale       1.693e+00  5.448e-02  3.215e+03  31.079 < 2e-16 ***
## transition_year -1.388e-02  4.021e-03  7.127e+03  -3.453 0.000558 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 age_sd ag_sq_ edctn1 edctn2 mrrdYs maleM1
## year_1984    -0.188
## age_sd        0.211 -0.618
## age_sqrd_sd  -0.175  0.564 -0.989
## education1    -0.631 -0.047  0.029 -0.036
## education2    -0.584 -0.062  0.012 -0.021  0.859
## marriedYes    -0.198 -0.134 -0.332  0.313 -0.003 -0.026
## maleMale      -0.309  0.058 -0.045  0.031  0.011  0.020  0.028
## transitn_yr  -0.420 -0.478  0.166 -0.118  0.028  0.004  0.167  0.024
```

```
#random slope
m15 <- lmer(log_income ~ year_1984 + age_sd + age_squared_sd + education + married + male + transition_year + (1| hh_id) +
(1 + married | id_id), data = soep_final, REML = FALSE)
summary(m15)
```



```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + age_sd + age_squared_sd + education +
## married + male + transition_year + (1 | hh_id) + (1 + married | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 299617.9 299745.0 -149794.9 299589.9      64983
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.2342 -0.0477  0.0752  0.2689  4.4872
##
## Random effects:
## Groups      Name                Variance Std.Dev. Corr
## id_id      (Intercept)          2.910    1.706
## marriedYes  marriedYes          3.961    1.990   -0.54
## hh_id      (Intercept)          1.907    1.381
## Residual                    4.533    2.129
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)  6.762e+00  1.221e-01  8.062e+03  55.373 < 2e-16 ***
## year_1984    3.234e-02  2.677e-03  2.965e+04  12.077 < 2e-16 ***
## age_sd       2.208e-01  5.384e-02  1.142e+04  4.100 4.16e-05 ***
## age_squared_sd -1.416e-01  4.070e-02  1.085e+04 -3.479 0.000504 ***
## education1    9.001e-01  8.630e-02  1.409e+04  10.430 < 2e-16 ***
## education2    2.194e+00  9.396e-02  1.297e+04  23.353 < 2e-16 ***
## marriedYes   -2.519e-01  4.144e-02  7.085e+03 -6.080 1.27e-09 ***
## maleMale     1.516e+00  5.200e-02  2.967e+03  29.157 < 2e-16 ***
## transition_year -2.005e-02  3.854e-03  7.223e+03 -5.202 2.02e-07 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 age_sd ag_sq_ edctn1 edctn2 mrrdYs maleM1
## year_1984    -0.199
## age_sd        0.218 -0.637
## age_sqrd_sd  -0.183  0.583 -0.989
## education1   -0.641 -0.042  0.029 -0.037
## education2   -0.593 -0.057  0.011 -0.021  0.852
## marriedYes   -0.236 -0.047 -0.245  0.232 -0.001 -0.017
## maleMale     -0.305  0.062 -0.048  0.035  0.011  0.022  0.023
## transitn_yr -0.383 -0.510  0.200 -0.150  0.027  0.001  0.103  0.021
```

```
##cross-level interaction
ml6 <- lmer(log_income ~ year_1984 + age_sd + age_squared_sd + education + married*male + transition_year + (1| hh_id) + (1
+ married | id_id), data = soep_final, REML = F)
summary(ml6)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + age_sd + age_squared_sd + education +
## married * male + transition_year + (1 | hh_id) + (1 + married | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 299350.9 299487.1 -149660.4 299320.9      64982
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.2362 -0.0517  0.0728  0.2742  4.4812
##
## Random effects:
## Groups Name Variance Std.Dev. Corr
## id_id (Intercept) 2.803 1.674
## marriedYes 3.621 1.903 -0.53
## hh_id (Intercept) 1.888 1.374
## Residual 4.535 2.130
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept) 7.104e+00 1.233e-01 8.205e+03 57.634 < 2e-16 ***
## year_1984 3.182e-02 2.669e-03 2.977e+04 11.921 < 2e-16 ***
## age_sd 2.253e-01 5.367e-02 1.146e+04 4.197 2.73e-05 ***
## age_squared_sd -1.444e-01 4.058e-02 1.089e+04 -3.559 0.000374 ***
## education1 9.021e-01 8.597e-02 1.407e+04 10.493 < 2e-16 ***
## education2 2.193e+00 9.360e-02 1.296e+04 23.435 < 2e-16 ***
## marriedYes -8.886e-01 5.572e-02 5.817e+03 -15.948 < 2e-16 ***
## maleMale 8.753e-01 6.467e-02 3.118e+03 13.535 < 2e-16 ***
## transition_year -1.959e-02 3.838e-03 7.253e+03 -5.103 3.42e-07 ***
## marriedYes:maleMale 1.209e+00 7.272e-02 4.678e+03 16.625 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 age_sd ag_sq_ edctn1 edctn2 mrrdYs maleM1 trnst_
## year_1984 -0.197
## age_sd 0.216 -0.635
## age_sqrd_sd -0.181 0.582 -0.989
## education1 -0.632 -0.042 0.029 -0.037
## education2 -0.585 -0.057 0.011 -0.021 0.852
## marriedYes -0.282 -0.031 -0.185 0.174 -0.004 -0.012
## maleMale -0.341 0.055 -0.042 0.031 0.006 0.018 0.425
## transitn_yr -0.377 -0.510 0.199 -0.150 0.027 0.001 0.074 0.013
## mrrdYs:m1M1 0.167 -0.009 0.005 -0.004 0.004 -0.001 -0.686 -0.599 0.005
```

```
#Safe estimated marginal effects
emm <- emmeans(m16, ~ married * male)
```

```
## Note: D.f. calculations have been disabled because the number of observations exceeds 3000.
## To enable adjustments, add the argument 'pbkrtest.limit = 64997' (or larger)
## [or, globally, 'set emm_options(pbkrtest.limit = 64997)' or larger];
## but be warned that this may result in large computation time and memory use.
```

```
## Note: D.f. calculations have been disabled because the number of observations exceeds 3000.
## To enable adjustments, add the argument 'lmerTest.limit = 64997' (or larger)
## [or, globally, 'set emm_options(lmerTest.limit = 64997)' or larger];
## but be warned that this may result in large computation time and memory use.
```

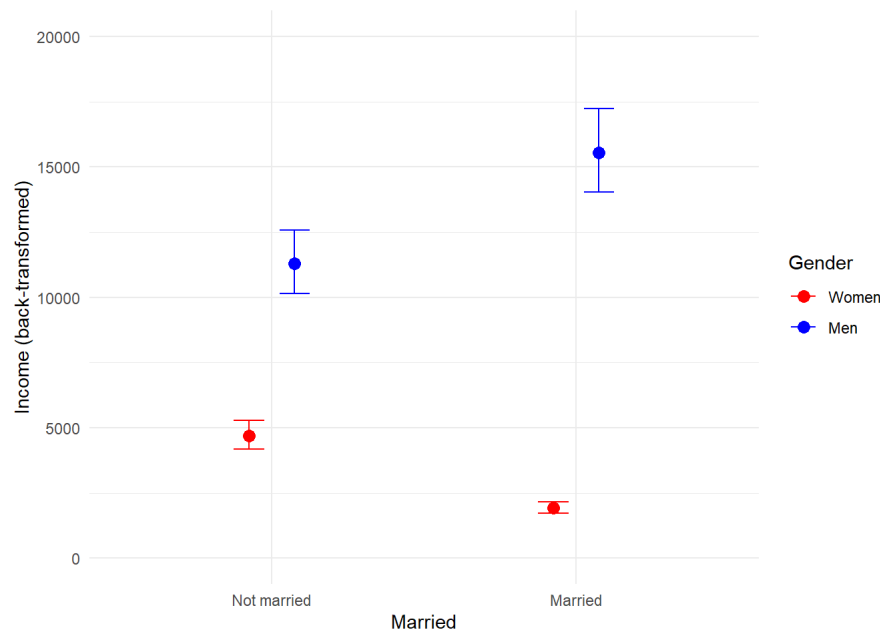
```
# Get married effect within each gender:
contrast(emm, method = "pairwise", by = "male")
```

```
## male = Female:
## contrast estimate      SE df z.ratio p.value
## No - Yes      0.889 0.0557 Inf 15.948 <.0001
##
## male = Male:
## contrast estimate      SE df z.ratio p.value
## No - Yes     -0.320 0.0532 Inf -6.021 <.0001
##
## Results are averaged over the levels of: education
## Degrees-of-freedom method: asymptotic
```

```
#Safe as dataframe
emm_df <- as.data.frame(emm)

#Back-transformed the log-transformed income (and confidence intervals)
emm_df <- emm_df %>%
  mutate(
    emmean_expo = exp(emmean),
    lower_expo = exp(asymp.LCL),
    upper_expo = exp(asymp.UCL)
  )

#Plot the EMM
ggplot(emm_df, aes(x = factor(married), y = emmean_expo, color = factor(male))) +
  geom_point(position = position_dodge(0.3), size = 3) +
  geom_errorbar(aes(ymin = lower_expo, ymax = upper_expo),
    position = position_dodge(0.3), width = 0.2) +
  scale_y_continuous(limits = c(0, 20000)) +
  labs(
    x = "Married",
    y = "Income (back-transformed)",
    color = "Gender"
  ) +
  scale_color_manual(
    values = c("Female" = "red", "Male" = "blue"),
    labels = c("Women", "Men")
  ) +
  scale_x_discrete(labels = c("Not married", "Married")) +
  theme_minimal()
```



```
#+ key level 1 predictors
rm1 <- lmer(log_income ~ year_1984 + relative_year_sd + relative_year_squared_sd + (1|hh_id) + (1|id_id), data = soep_final,
  REML = F)
summary(rm1)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + relative_year_sd + relative_year_squared_sd +
## (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 305144.1  305207.7 -152565.1  305130.1    64990
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.9129 -0.0316  0.0862  0.2905  3.9826
##
## Random effects:
## Groups   Name                Variance Std.Dev.
## id_id    (Intercept)  3.305      1.818
## hh_id    (Intercept)  2.515      1.586
## Residual                    5.195      2.279
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)      8.486e+00  8.460e-02  1.497e+04 100.300 < 2e-16 ***
## year_1984         1.777e-02  3.117e-03  2.187e+04  5.701 1.20e-08 ***
## relative_year_sd   1.794e-01  1.963e-02  3.584e+04  9.137 < 2e-16 ***
## relative_year_squared_sd -8.440e-02  1.100e-02  6.277e+04 -7.671 1.74e-14 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 rltv__
## year_1984      -0.894
## reltv_yr_sd    0.747 -0.829
## rltv_yr_sq_    0.181 -0.212 -0.071
```

```
#+level 1 control variables
```

```
rm1a <- lmer(log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd + (1|hh_id) + (1|id_id), data
= soep_final, REML = F)
summary(rm1a)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
## (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 304226.6  304308.4 -152104.3  304208.6    64988
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.8932 -0.0342  0.0883  0.2925  3.9481
##
## Random effects:
## Groups   Name                Variance Std.Dev.
## id_id    (Intercept)  3.380      1.839
## hh_id    (Intercept)  2.190      1.480
## Residual                    5.135      2.266
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)      7.573e+00  1.166e-01  1.750e+04  64.958 < 2e-16 ***
## year_1984         1.200e-02  3.083e-03  2.111e+04  3.893 9.94e-05 ***
## education1        6.213e-01  9.100e-02  2.032e+04  6.828 8.85e-12 ***
## education2        2.103e+00  9.958e-02  1.823e+04  21.123 < 2e-16 ***
## relative_year_sd   1.415e-01  1.946e-02  3.486e+04  7.273 3.59e-13 ***
## relative_year_squared_sd -5.305e-02  1.097e-02  6.283e+04 -4.834 1.34e-06 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 edctn1 edctn2 rltv__
## year_1984      -0.623
## education1     -0.691 -0.015
## education2     -0.647 -0.045  0.860
## reltv_yr_sd    0.556 -0.820 -0.022 -0.051
## rltv_yr_sq_    0.118 -0.215  0.000  0.051 -0.078
```

```
##key Level 2 predictor
rm2 <- lmer(log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd + male + (1|hh_id) + (1|id_id), data = soep_final, REML = F)
summary(rm2)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
## male + (1 | hh_id) + (1 | id_id)
## Data: soep_final
##
##           AIC          BIC       logLik -2*log(L)  df.resid
## 303351.6  303442.4 -151665.8  303331.6      64987
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -4.9318 -0.0444  0.0837  0.3031  3.9661
##
## Random effects:
## Groups Name Variance Std.Dev.
## id_id (Intercept) 2.342 1.530
## hh_id (Intercept) 2.296 1.515
## Residual 5.140 2.267
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept) 6.463e+00 1.164e-01 1.423e+04 55.528 < 2e-16 ***
## year_1984 1.725e-02 2.976e-03 1.841e+04 5.796 6.89e-09 ***
## education1 7.092e-01 8.682e-02 1.731e+04 8.168 3.34e-16 ***
## education2 2.133e+00 9.482e-02 1.563e+04 22.497 < 2e-16 ***
## relative_year_sd 1.143e-01 1.900e-02 3.232e+04 6.017 1.80e-09 ***
## relative_year_squared_sd -5.675e-02 1.096e-02 6.301e+04 -5.179 2.24e-07 ***
## maleMale 1.724e+00 5.413e-02 3.208e+03 31.859 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 edctn1 edctn2 rltv__ rlt__
## year_1984 -0.618
## education1 -0.662 -0.013
## education2 -0.621 -0.043 0.858
## reltv_yr_sd 0.544 -0.811 -0.023 -0.050
## rltv_yr_sq_ 0.113 -0.208 -0.002 0.048 -0.092
## maleMale -0.297 0.066 0.007 0.016 -0.058 -0.009
```

```
##random slope
rm3 <- lmer(log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd + male + (1| hh_id) + (1 + relative_year_sd | id_id), data = soep_final, REML = FALSE)
summary(rm3)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
## male + (1 | hh_id) + (1 + relative_year_sd | id_id)
## Data: soep_final
##
##      AIC      BIC    logLik -2*log(L)  df.resid
## 296056.6 296165.6 -148016.3 296032.6    64985
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.7466 -0.0522  0.0649  0.2614  5.0445
##
## Random effects:
## Groups Name Variance Std.Dev. Corr
## id_id (Intercept) 2.509 1.584
## relative_year_sd 1.187 1.089 0.12
## hh_id (Intercept) 1.858 1.363
## Residual 4.113 2.028
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
## Estimate Std. Error df t value Pr(>|t|)
## (Intercept) 6.428e+00 1.310e-01 8.434e+03 49.084 < 2e-16 ***
## year_1984 1.425e-02 3.629e-03 6.839e+03 3.926 8.73e-05 ***
## education1 9.154e-01 9.215e-02 1.249e+04 9.935 < 2e-16 ***
## education2 2.198e+00 9.931e-02 1.178e+04 22.131 < 2e-16 ***
## relative_year_sd 1.317e-01 2.512e-02 1.009e+04 5.242 1.62e-07 ***
## relative_year_squared_sd -5.183e-02 1.322e-02 4.095e+04 -3.921 8.83e-05 ***
## maleMale 1.669e+00 5.384e-02 3.205e+03 30.993 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
## (Intr) y_1984 edctn1 edctn2 rltv__ rlt__
## year_1984 -0.689
## education1 -0.636 0.010
## education2 -0.589 -0.028 0.856
## reltv_yr_sd 0.480 -0.637 -0.028 -0.046
## rltv_yr_sq_ 0.048 -0.103 0.003 0.060 -0.111
## maleMale -0.286 0.085 0.010 0.019 -0.057 -0.005
```

```
##+random slope
```

```
rm4 <- lmer(log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd + male + (1 | hh_id) + (1 + relative_year_squared_sd | id_id), data = soep_final, REML = FALSE)
summary(rm4)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_squared_sd | id_id)
## Data: soep_final
##
##      AIC      BIC    logLik -2*log(L)  df.resid
## 298523.3 298632.3 -149249.7 298499.3    64985
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.3383 -0.0504  0.0702  0.2631  4.3546
##
## Random effects:
## Groups   Name                Variance Std.Dev. Corr
## id_id    (Intercept)          2.4425   1.5628
##           relative_year_squared_sd 0.8475   0.9206   0.12
## hh_id    (Intercept)          2.1781   1.4758
## Residual                    4.3474   2.0850
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)    6.638e+00  1.246e-01  1.115e+04  53.257 < 2e-16 ***
## year_1984      9.869e-03  3.356e-03  1.082e+04   2.940  0.00329 **
## education1     7.271e-01  9.022e-02  1.444e+04   8.060  8.26e-16 ***
## education2     2.129e+00  9.764e-02  1.337e+04  21.806 < 2e-16 ***
## relative_year_sd 6.544e-02  2.097e-02  2.271e+04   3.121  0.00181 **
## relative_year_squared_sd -5.208e-02  1.739e-02  5.308e+03  -2.994  0.00276 **
## maleMale       1.717e+00  5.397e-02  3.208e+03  31.811 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##      (Intr) y_1984 edctn1 edctn2 rltv__ rlt__
## year_1984    -0.658
## education1   -0.646 -0.005
## education2   -0.600 -0.041  0.860
## reltv_yr_sd   0.542 -0.768 -0.023 -0.047
## rltv_yr_sq_   0.086 -0.118 -0.003  0.030 -0.068
## maleMale     -0.289  0.076  0.008  0.017 -0.063 -0.006
```

```
#+random slope
```

```
rm4b <- lmer(log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd + male + (1 | hh_id) + (1 + relative_year_sd + relative_year_squared_sd | id_id), data = soep_final, REML = F)
```

```
## Warning in checkConv(attr(opt, "derivs"), opt$par, ctrl = control$checkConv, :
## Model failed to converge with max|grad| = 0.00378561 (tol = 0.002, component 1)
```

```
summary(rm4b)
```

```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula:
## log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_sd + relative_year_squared_sd |
##   id_id)
## Data: soep_final
##
##           AIC          BIC      logLik -2*log(L)  df.resid
## 293856.5    293992.7 -146913.2   293826.5     64982
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.3671 -0.0568  0.0547  0.2327  4.5175
##
## Random effects:
## Groups   Name                Variance Std.Dev. Corr
## id_id    (Intercept)          2.546    1.596
##           relative_year_sd    1.945    1.395    0.26
##           relative_year_squared_sd 1.291    1.136   -0.21 -0.55
## hh_id    (Intercept)          1.699    1.303
## Residual                    3.642    1.908
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value Pr(>|t|)
## (Intercept)    6.471e+00  1.303e-01  7.811e+03  49.675 < 2e-16 ***
## year_1984      1.184e-02  3.597e-03  6.255e+03   3.293 0.000996 ***
## education1     1.079e+00  9.211e-02  1.121e+04  11.715 < 2e-16 ***
## education2     2.201e+00  9.921e-02  1.062e+04  22.188 < 2e-16 ***
## relative_year_sd  4.987e-02  2.931e-02  6.041e+03   1.701 0.088906 .
## relative_year_squared_sd -5.172e-03  2.186e-02  3.217e+03  -0.237 0.813013
## maleMale       1.525e+00  5.269e-02  3.072e+03  28.936 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##      (Intr) y_1984 edctn1 edctn2 rltv__ rlt__
## year_1984    -0.689
## education1   -0.640  0.013
## education2   -0.591 -0.027  0.851
## reltv_yr_sd  0.429 -0.539 -0.027 -0.043
## rltv_yr_sq_  0.009 -0.071  0.002  0.034 -0.393
## maleMale     -0.284  0.087  0.009  0.021 -0.049 -0.006
## optimizer (nloptwrap) convergence code: 0 (OK)
## Model failed to converge with max|grad| = 0.00378561 (tol = 0.002, component 1)
```

#+cross-level interaction

```
rm5 <- lmer(log_income ~ year_1984 + education + relative_year_sd*male + relative_year_squared_sd*male + (1| hh_id) + (1 + r
relative_year_sd + relative_year_squared_sd| id_id), data = soep_final, REML = F)
summary(rm5)
```



```
## Linear mixed model fit by maximum likelihood . t-tests use Satterthwaite's
## method [lmerModLmerTest]
## Formula: log_income ~ year_1984 + education + relative_year_sd * male +
##   relative_year_squared_sd * male + (1 | hh_id) + (1 + relative_year_sd +
##   relative_year_squared_sd | id_id)
## Data: soep_final
##
##      AIC      BIC    logLik -2*log(L)  df.resid
## 293576.7 293731.1 -146771.4 293542.7    64980
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -5.3683 -0.0621  0.0545  0.2380  4.4786
##
## Random effects:
##   Groups      Name                Variance Std.Dev. Corr
##   id_id      (Intercept)          2.544    1.595
##              relative_year_sd      1.804    1.343    0.26
##              relative_year_squared_sd 1.229    1.109   -0.21 -0.52
##   hh_id      (Intercept)          1.683    1.297
##   Residual                3.641    1.908
## Number of obs: 64997, groups: id_id, 4885; hh_id, 4730
##
## Fixed effects:
##              Estimate Std. Error      df t value
## (Intercept)    6.407e+00  1.299e-01  7.876e+03  49.325
## year_1984      1.091e-02  3.584e-03  6.291e+03   3.045
## education1     1.078e+00  9.180e-02  1.125e+04  11.744
## education2     2.197e+00  9.889e-02  1.066e+04  22.219
## relative_year_sd -3.448e-01  3.807e-02  4.719e+03  -9.056
## maleMale       1.695e+00  5.364e-02  3.221e+03  31.602
## relative_year_squared_sd 2.923e-01  3.125e-02  3.266e+03   9.356
## relative_year_sd:maleMale 7.568e-01  4.784e-02  3.412e+03  15.818
## maleMale:relative_year_squared_sd -5.647e-01  4.282e-02  3.213e+03 -13.190
##              Pr(>|t|)
## (Intercept)    < 2e-16 ***
## year_1984      0.00233 **
## education1     < 2e-16 ***
## education2     < 2e-16 ***
## relative_year_sd < 2e-16 ***
## maleMale       < 2e-16 ***
## relative_year_squared_sd < 2e-16 ***
## relative_year_sd:maleMale < 2e-16 ***
## maleMale:relative_year_squared_sd < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Correlation of Fixed Effects:
##              (Intr) y_1984 edctn1 edctn2 rltv__ maleM1 rlt__ rl__:M
## year_1984    -0.688
## education1   -0.640  0.013
## education2   -0.591 -0.027  0.851
## reltv_yr_sd  0.347 -0.402 -0.023 -0.032
## maleMale     -0.285  0.083  0.010  0.020 -0.159
## rltv_yr_sq_  -0.019 -0.047  0.005  0.024 -0.432  0.096
## rltv_yr_s:M  -0.029 -0.018  0.004 -0.002 -0.656  0.186  0.357
## m1M1:rlt__   0.035 -0.004 -0.006 -0.001  0.328 -0.137 -0.726 -0.488
```

```
#SD for relative year
sd(soep_final$relative_year)
```

```
## [1] 8.059238
```

```

## Create prediction data
new_data <- expand.grid(
  relative_year_sd = seq(-1.5, 1.5, by = 0.1),
  male = factor(c("Female", "Male")),
  year_1984 = c(0),
  education = "0"
)

new_data$relative_year_squared_sd <- new_data$relative_year_sd^2

## Ensure factors match model
new_data$male <- factor(new_data$male, levels = levels(soep_final$male))
new_data$education <- factor(new_data$education, levels = levels(soep_final$education))

## Predict with standard errors
pred <- predict(rms, newdata = new_data, re.form = NA, se.fit = TRUE)

## Add predicted values and 95% CI
new_data$predicted_log_income <- pred$fit
new_data$se <- pred$se.fit
new_data$lower <- new_data$predicted_log_income - 1.96 * new_data$se
new_data$upper <- new_data$predicted_log_income + 1.96 * new_data$se

## Back-transform log-transformed income variable (and confidence intervals)
new_data$predicted_income <- exp(new_data$predicted_log_income)
new_data$lower_income <- exp(new_data$lower)
new_data$upper_income <- exp(new_data$upper)

## Plot the trajectories (back-transformed logged income)
ggplot(new_data, aes(x = relative_year_sd, y = predicted_income, color = male, fill = male)) +
  geom_line(size = 1.2) +
  geom_ribbon(aes(ymin = lower_income, ymax = upper_income), alpha = 0.2, color = NA) +
  labs(
    title = "Predicted Income Trajectories Over Time",
    x = "Standardized Relative Year",
    y = "Predicted Income",
    color = "Gender",
    fill = "Gender"
  ) +
  scale_color_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  scale_fill_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  theme_minimal(base_size = 14) +
  theme(
    axis.text.y = element_blank(),
    axis.ticks.y = element_blank()
  )

## Predict the trajectories (logged income)
ggplot(new_data, aes(x = relative_year_sd, y = predicted_log_income, color = male, fill = male)) +
  geom_line(size = 1.2) +
  geom_ribbon(aes(ymin = lower, ymax = upper), alpha = 0.2, color = NA) +
  labs(
    title = "Predicted Log Income Trajectories Over Time",
    x = "Standardized Relative Year",
    y = "Predicted Log Income",
    color = "Gender",
    fill = "Gender"
  ) +
  scale_color_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  scale_fill_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  theme_minimal(base_size = 14)

ggplot(new_data, aes(x = relative_year_sd, y = predicted_income, color = male, fill = male)) +
  geom_line(size = 1.2) +
  geom_ribbon(aes(ymin = lower_income, ymax = upper_income), alpha = 0.2, color = NA) +
  labs(
    title = "Predicted Income Trajectories Over Time",
    x = "Standardized Relative Year",
    y = "Predicted Income",
    color = "Gender",
    fill = "Gender"
  ) +
  scale_color_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  scale_fill_manual(values = c("red", "blue"), labels = c("Women", "Men")) +
  theme_minimal(base_size = 14) +
  theme_minimal(base_size = 14)

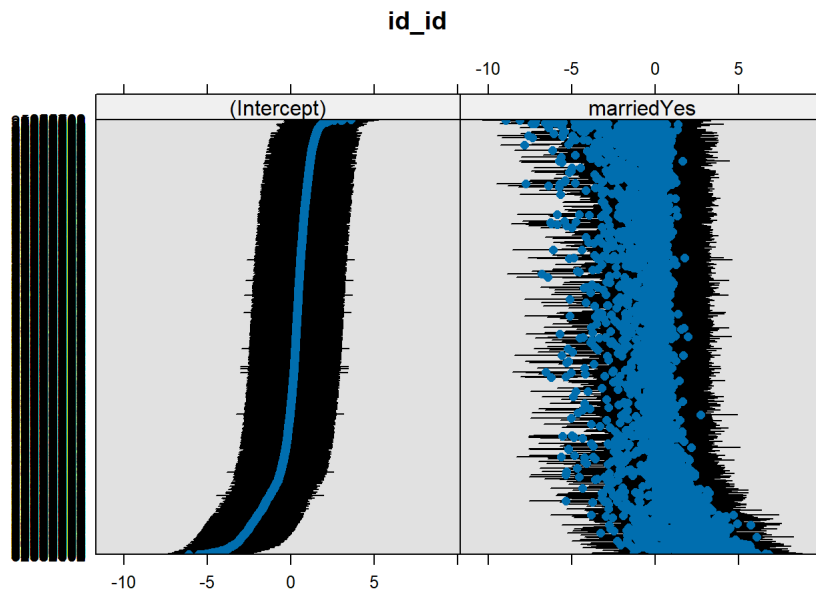
```

```

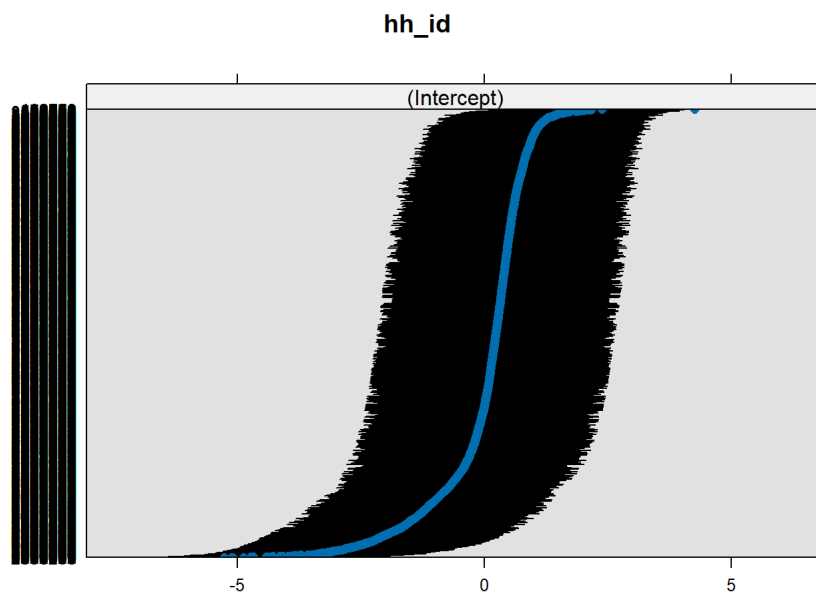
#Inspect variance components
dotplot(ranef(m15))

```

```
## $id_id
```

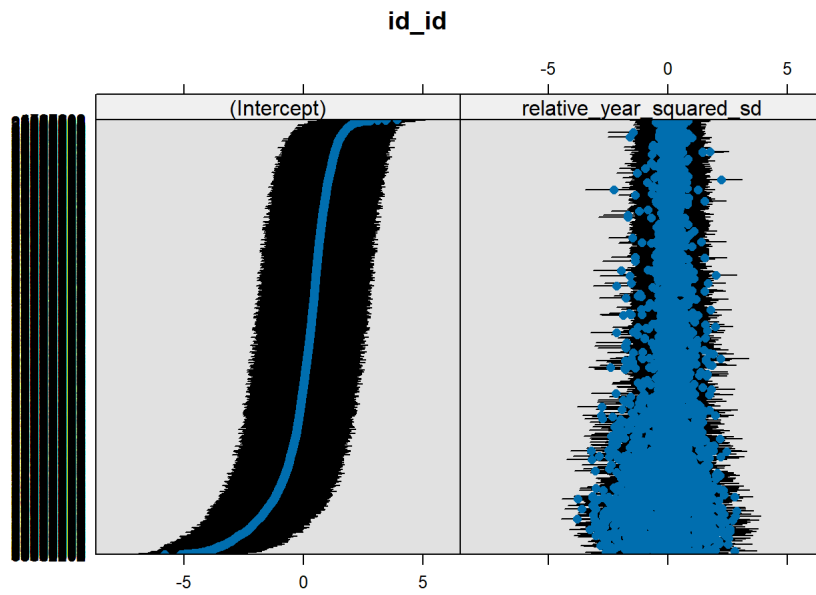


```
##  
## $hh_id
```

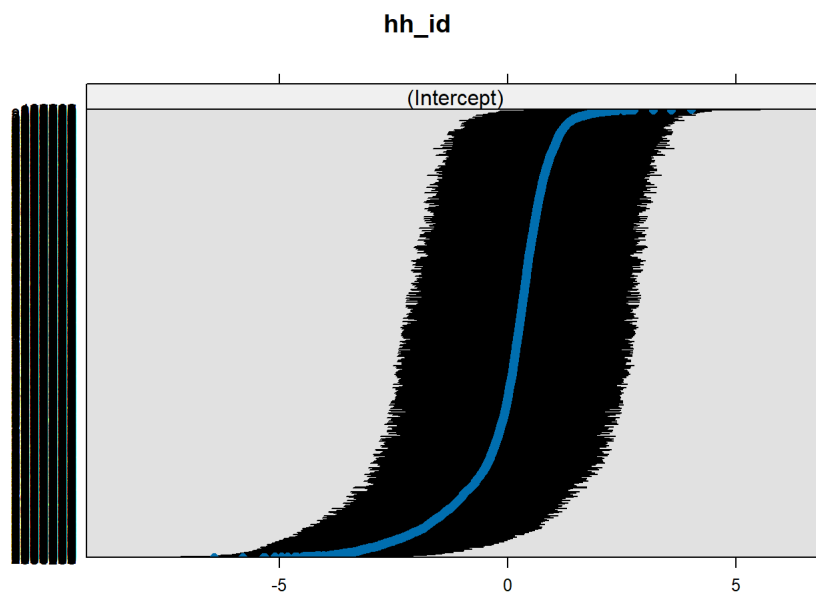


```
dotplot(ranef(rm4))
```

```
## $id_id
```

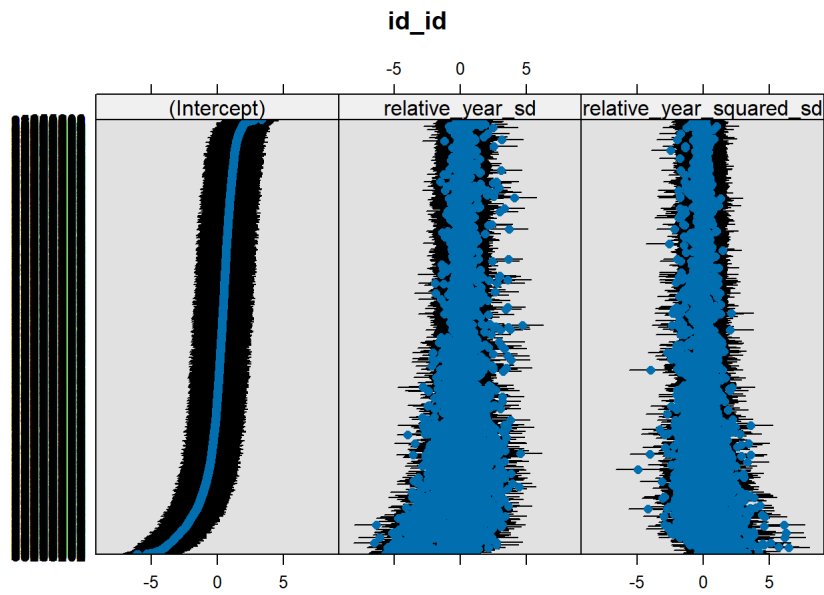


```
##
## $hh_id
```

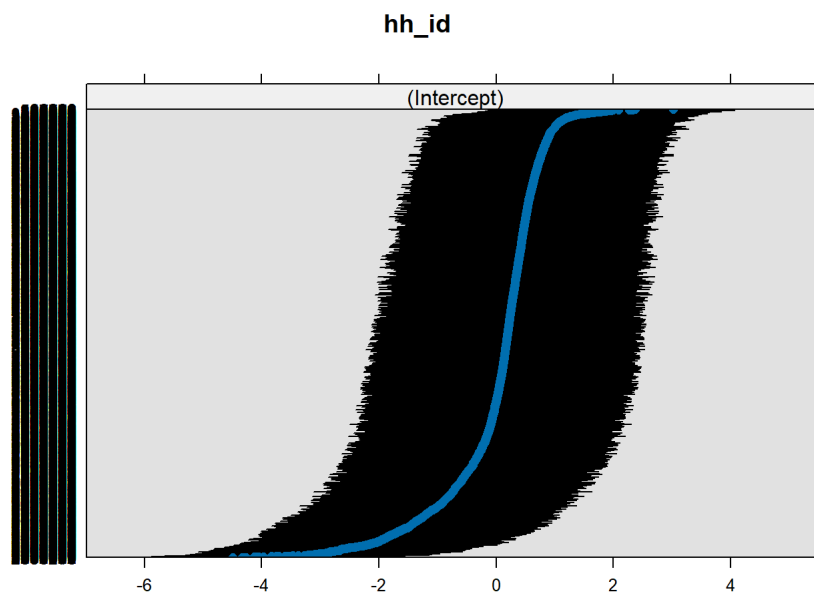


```
dotplot(ranef(rm4b))
```

```
## $id_id
```



```
##
## $hh_id
```



```
#Likelihood-Ratio Tests to compare the models with and without the random slopes
lrtest(m15, m14a)
```

```
## Likelihood ratio test
##
## Model 1: log_income ~ year_1984 + age_sd + age_squared_sd + education +
##   married + male + transition_year + (1 | hh_id) + (1 + married |
##   id_id)
## Model 2: log_income ~ year_1984 + age_sd + age_squared_sd + education +
##   married + male + transition_year + (1 | hh_id) + (1 | id_id)
##   #Df  LogLik Df Chisq Pr(>Chisq)
## 1   14 -149795
## 2   12 -151638 -2   3686 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
lrtest(rm2, rm3)
```

```
## Likelihood ratio test
##
## Model 1: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 | id_id)
## Model 2: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_sd | id_id)
##   #Df  LogLik Df  Chisq Pr(>Chisq)
## 1   10 -151666
## 2   12 -148016   2   7299  < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
lrtest(rm2, rm4)
```

```
## Likelihood ratio test
##
## Model 1: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 | id_id)
## Model 2: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_squared_sd | id_id)
##   #Df  LogLik Df  Chisq Pr(>Chisq)
## 1   10 -151666
## 2   12 -149250   2 4832.3  < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
lrtest(rm3, rm4b)
```

```
## Likelihood ratio test
##
## Model 1: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_sd | id_id)
## Model 2: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_sd + relative_year_squared_sd |
##   id_id)
##   #Df  LogLik Df  Chisq Pr(>Chisq)
## 1   12 -148016
## 2   15 -146913   3 2206.1  < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
lrtest(rm4, rm4b)
```

```
## Likelihood ratio test
##
## Model 1: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_squared_sd | id_id)
## Model 2: log_income ~ year_1984 + education + relative_year_sd + relative_year_squared_sd +
##   male + (1 | hh_id) + (1 + relative_year_sd + relative_year_squared_sd |
##   id_id)
##   #Df  LogLik Df  Chisq Pr(>Chisq)
## 1   12 -149250
## 2   15 -146913   3 4672.8  < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#Variance in the effect of marriage status on income explained by gender
((as.data.frame(VarCorr(m15))[2,4])-(as.data.frame(VarCorr(m16))[2,4])) /
(as.data.frame(VarCorr(m15))[2,4])
```

```
## [1] 0.08591941
```

```
# Extract variance components as data frames
vc_m15a <- as.data.frame(VarCorr(m15))
vc_m16 <- as.data.frame(VarCorr(m16))

# Extract the random slope variance for 'marriedYes' at the individual level ("id_id")
slope_var_m15a <- vc_m15a[vc_m15a$grp == "id_id" & vc_m15a$var1 == "marriedYes" & is.na(vc_m15a$var2), "vcov"]
slope_var_m16 <- vc_m16[vc_m16$grp == "id_id" & vc_m16$var1 == "marriedYes" & is.na(vc_m16$var2), "vcov"]

# Calculate proportional reduction in variance
reduction_married <- (slope_var_m15a - slope_var_m16) / slope_var_m15a

# Show result
reduction_married
```

```
## [1] 0.08591941
```

```
# Extract random effect variance components as data frames
vc_rm4b <- as.data.frame(VarCorr(rm4b))
vc_rm5 <- as.data.frame(VarCorr(rm5))

# Filter to individual-level random slopes (usually group = "id_id")
slope_var_ry <- vc_rm4b[vc_rm4b$grp == "id_id" & vc_rm4b$var1 == "relative_year_sd" & is.na(vc_rm4b$var2), "vcov"]
slope_var_ry2 <- vc_rm4b[vc_rm4b$grp == "id_id" & vc_rm4b$var1 == "relative_year_squared_sd" & is.na(vc_rm4b$var2), "vcov"]

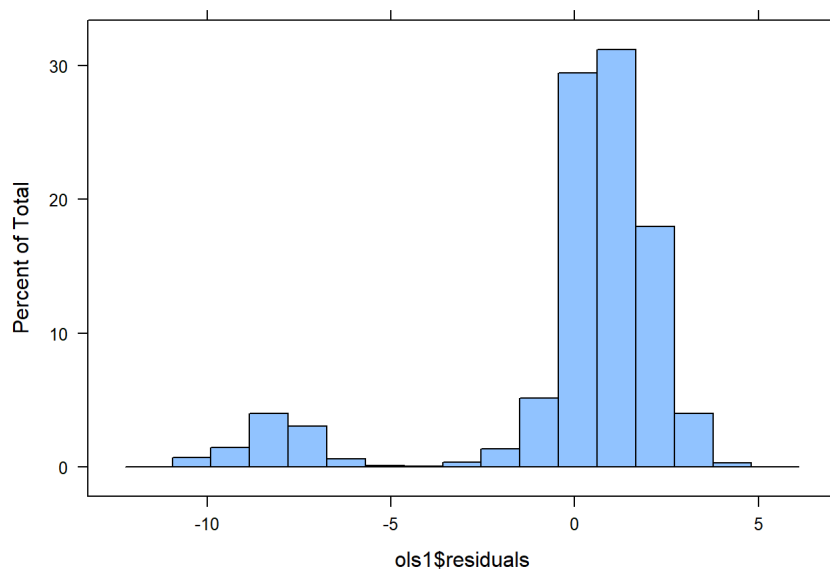
slope_var_ry_new <- vc_rm5[vc_rm5$grp == "id_id" & vc_rm5$var1 == "relative_year_sd" & is.na(vc_rm5$var2), "vcov"]
slope_var_ry2_new <- vc_rm5[vc_rm5$grp == "id_id" & vc_rm5$var1 == "relative_year_squared_sd" & is.na(vc_rm5$var2), "vcov"]

# Compute proportional reduction in variance for both slopes
reduction_ry <- (slope_var_ry - slope_var_ry_new) / slope_var_ry
reduction_ry2 <- (slope_var_ry2 - slope_var_ry2_new) / slope_var_ry2

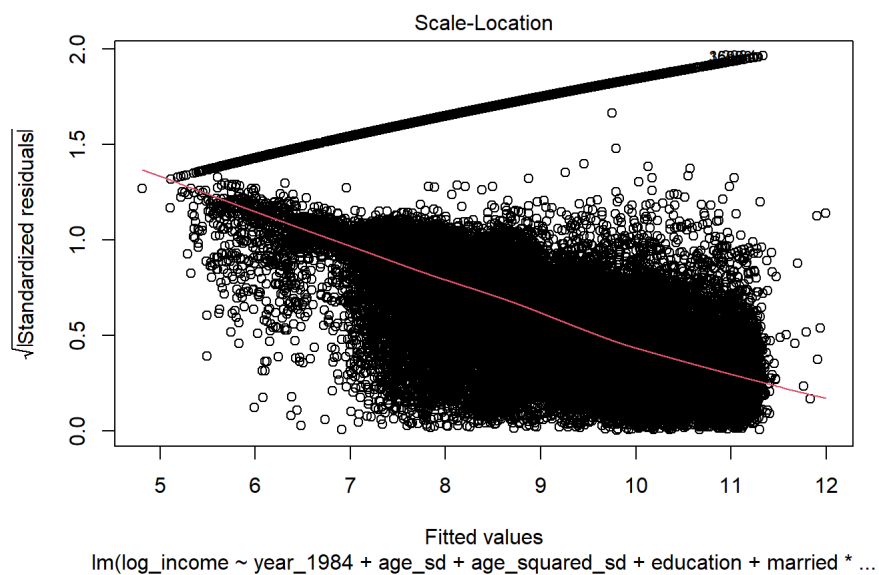
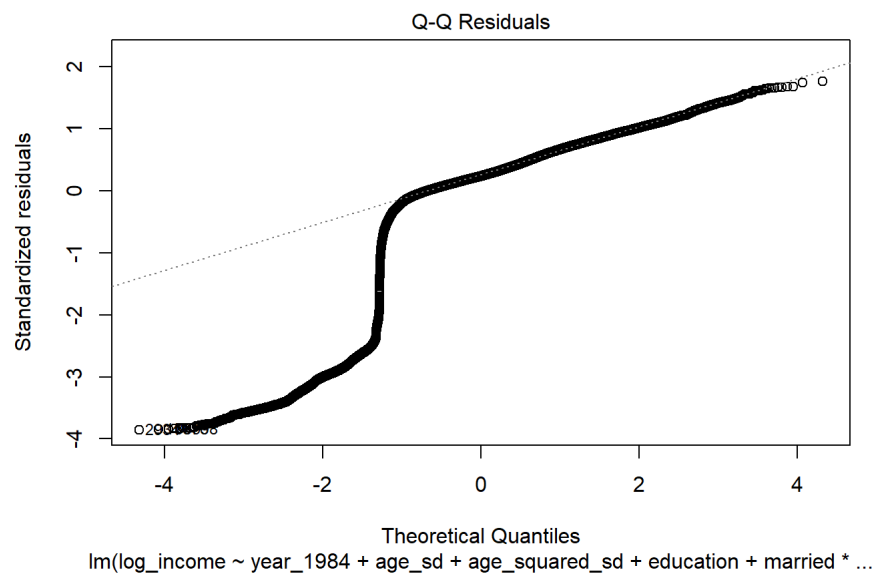
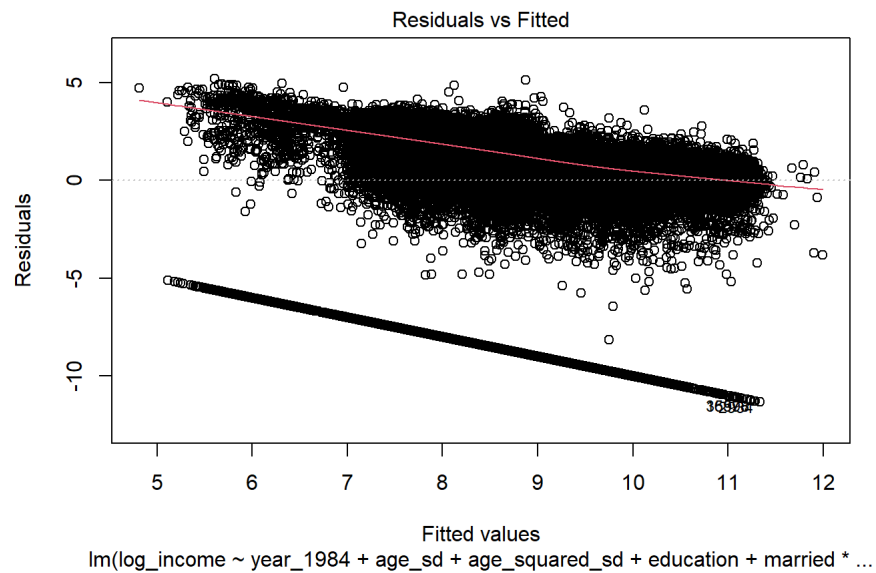
reduction_ry + reduction_ry2
```

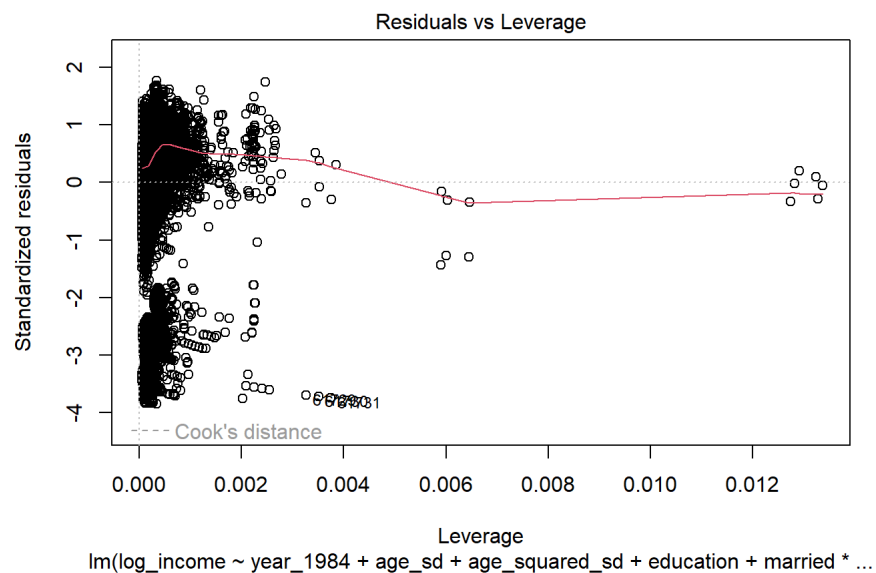
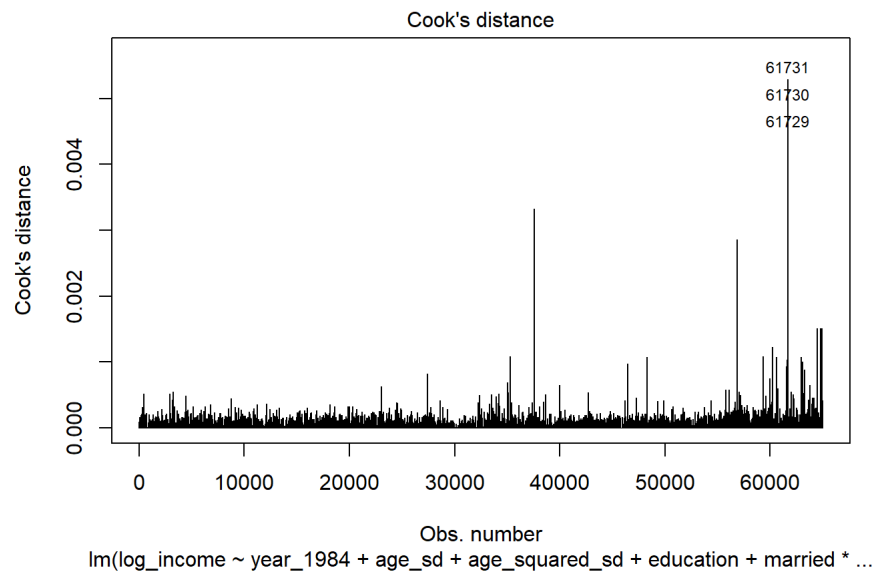
```
## [1] 0.1204257
```

```
#Assumptions OLS
histogram(ols1$residuals)
```



```
plot(ols1, which = 1:5)
```





```
#Assumptions multilevel models
```

```
#Model 1
```

```
#Level 1
```

```
#Normality
```

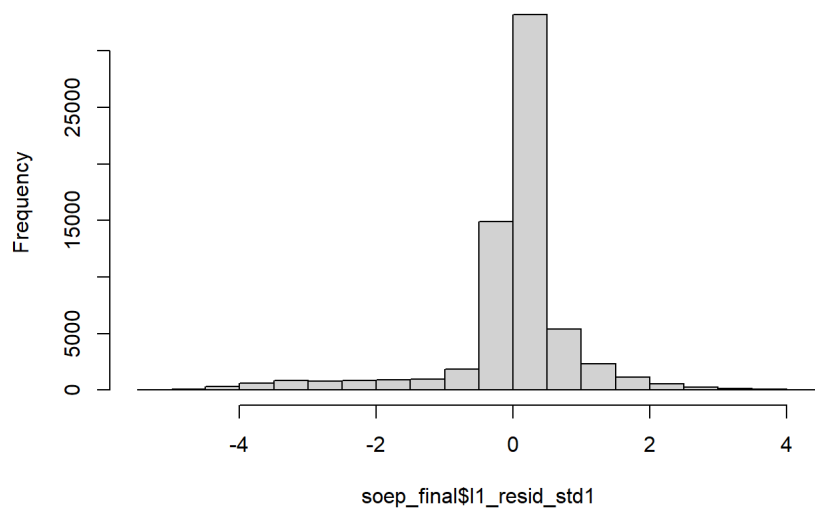
```
#Level 1 residuals

#Extract L1 residuals
soep_final$l1resid <- residuals(ml6)

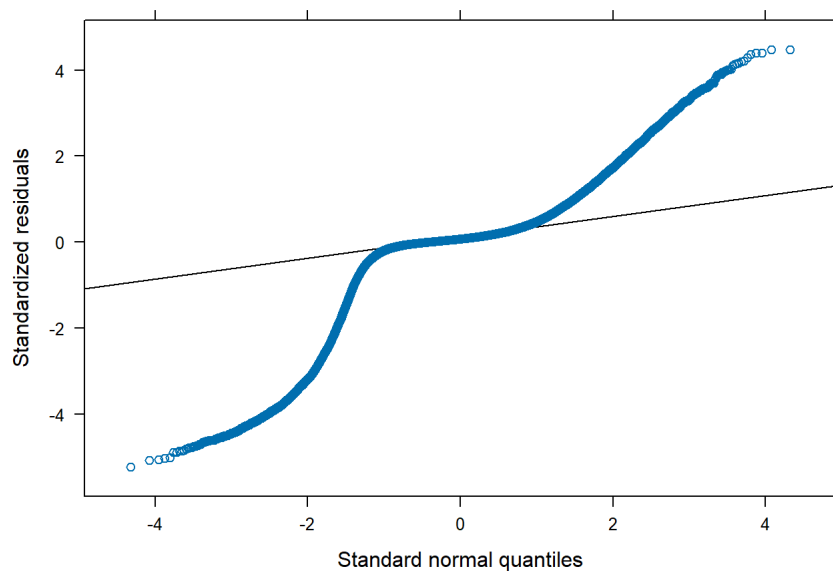
#Extract standardized residuals
soep_final$l1_resid_std1 <- resid(ml6, type = "pearson", scale = TRUE)

#Histogram L1 residuals
hist(soep_final$l1_resid_std1)
```

Histogram of soep_final\$I1_resid_std1

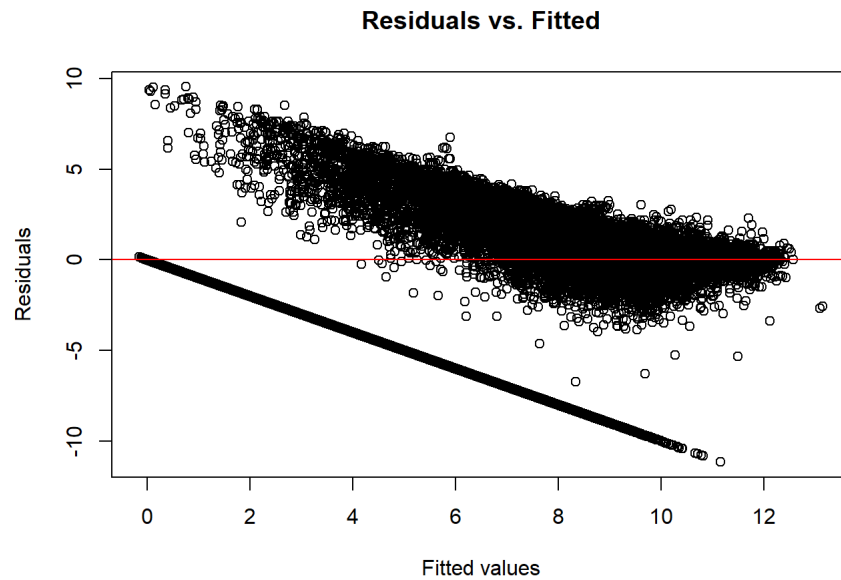


```
#QQ Plot
qqmath(m16)
```



```
#Homoskedasticity
```

```
plot(fitted(m16), resid(m16),
     xlab = "Fitted values", ylab = "Residuals",
     main = "Residuals vs. Fitted")
abline(h = 0, col = "red")
```



#Level 2

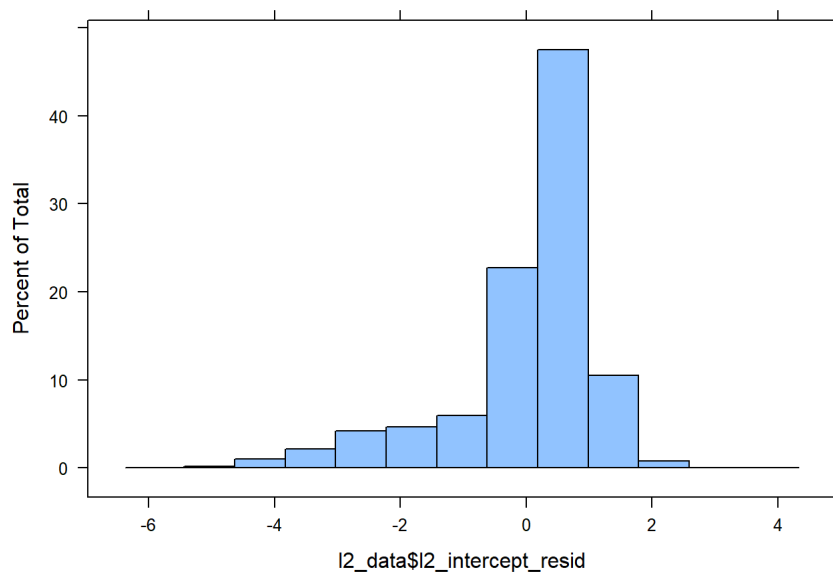
```
#Level 2 residuals

l2_data <- soep_final %>%
  group_by(id_id) %>%
  mutate(log_income_mean = mean(log_income, na.rm = T)) %>%
  dplyr::select(id_id, log_income_mean, male) %>%
  unique()

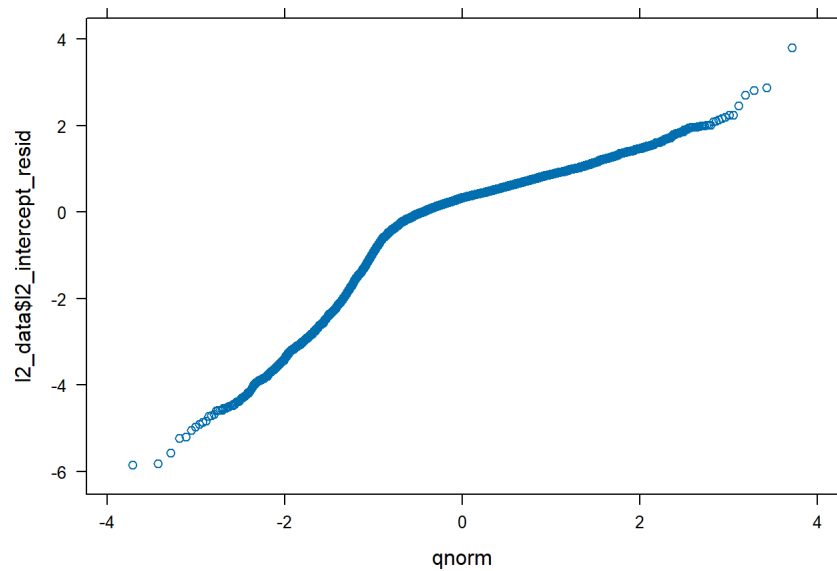
#Random Intercept and Random Slope residuals
l2_data$l2_intercept_resid = ranef(ml6)$id_id [, 1]
l2_data$l2_slope_resid = ranef(ml6)$id_id [, 2]
```

#Normality

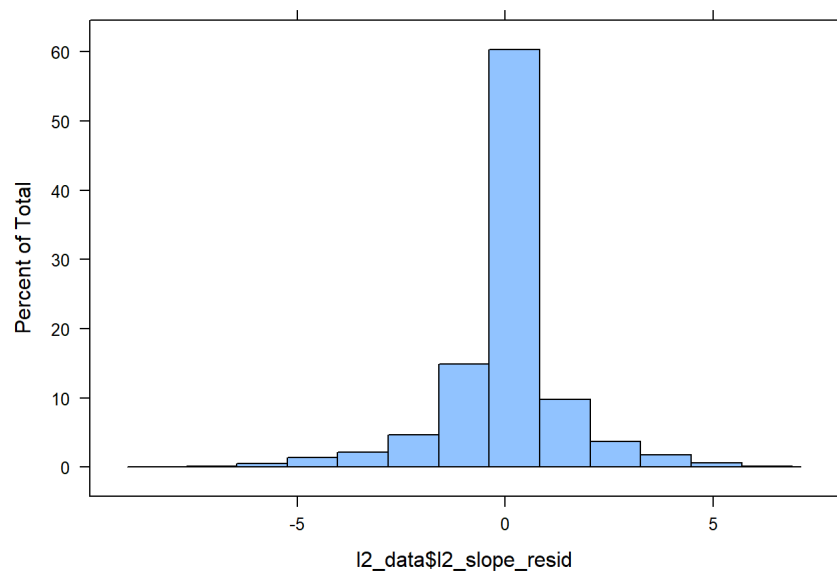
```
#Histogram
histogram(l2_data$l2_intercept_resid)
```



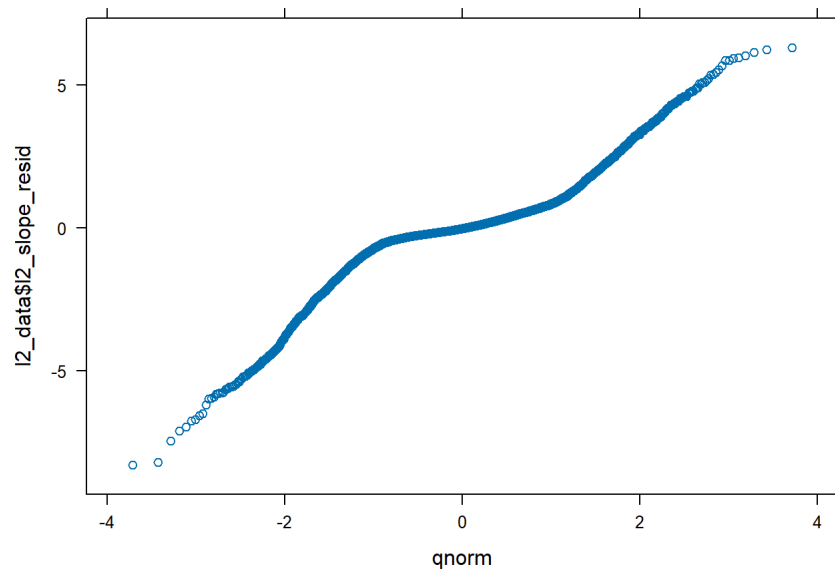
```
#QQ Plot
qqmath(l2_data$l2_intercept_resid)
```



```
#Histogram  
histogram(l2_data$l2_slope_resid)
```



```
#QQ Plot  
qqmath(l2_data$l2_slope_resid)
```

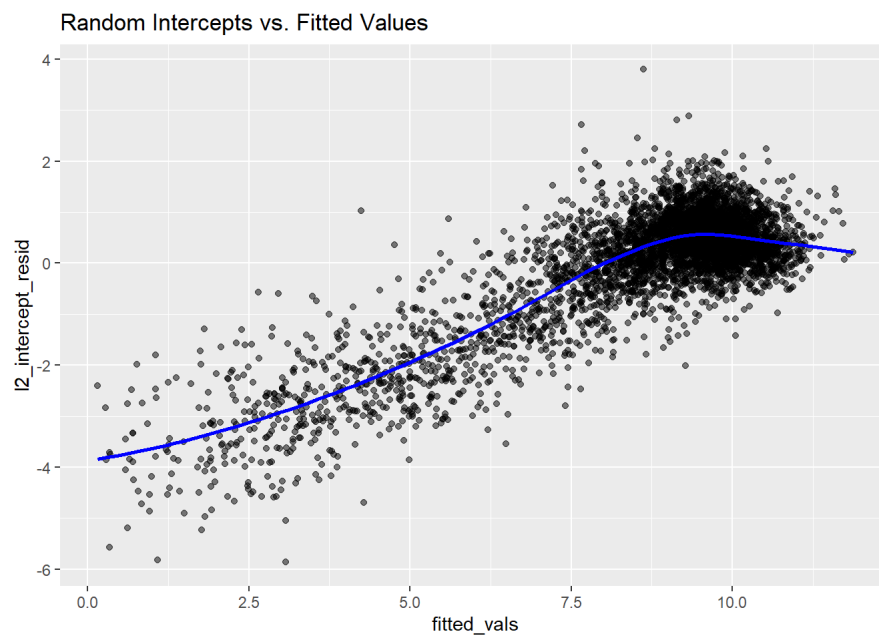


#Homoskedasticity

```
# Random intercepts
l2_data$fitted_vals <- fitted(ml6)[match(l2_data$id_id, soep_final$id_id)]

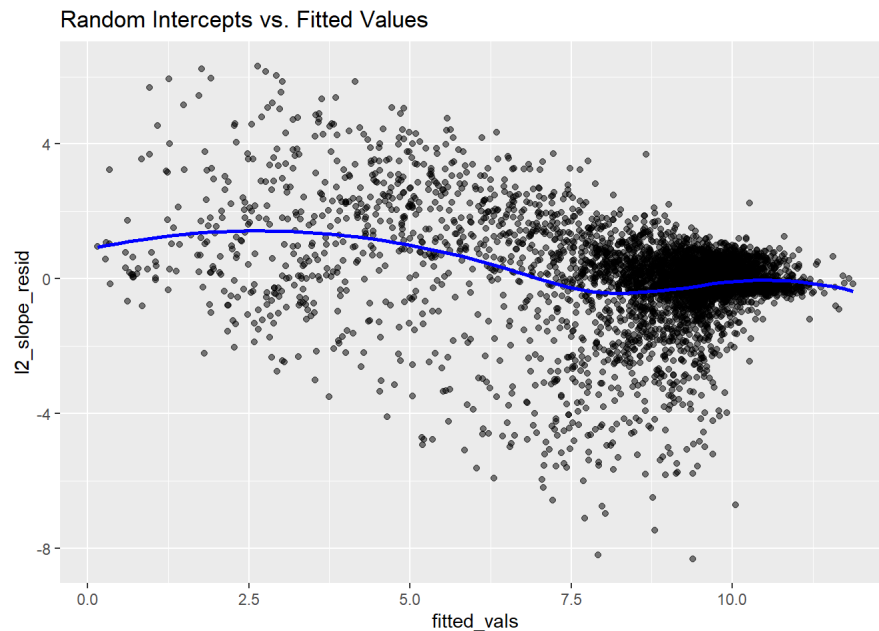
ggplot(l2_data, aes(x = fitted_vals, y = l2_intercept_resid)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```



```
# Random slopes
ggplot(l2_data, aes(x = fitted_vals, y = l2_slope_resid)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```



```
#Check whether the variance of the L1 residual errors is the same in all groups
soep_final$abs.l1resid<-soep_final$l1residuals
```

```
## Warning: Unknown or uninitialised column: `l1residuals`.
```

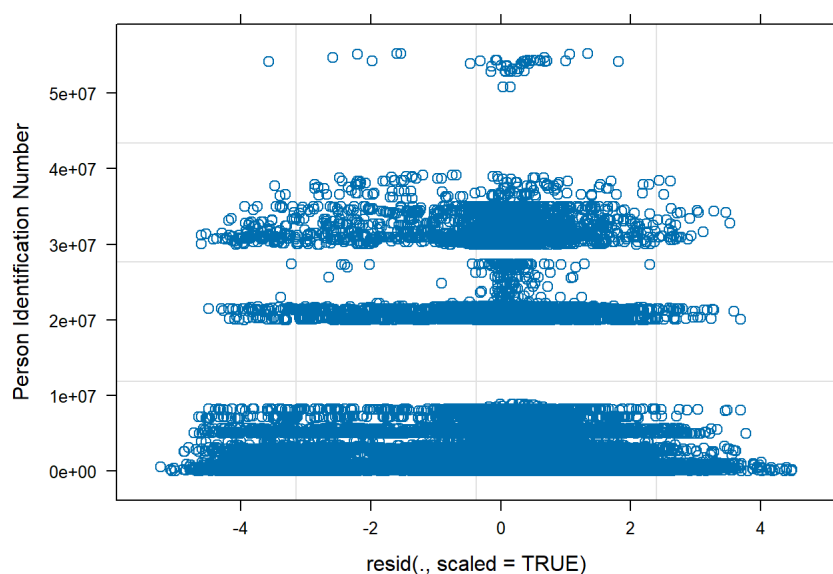
```
soep_final$abs.l1resid <- abs(soep_final$l1resid)
soep_final$abs.l1resid2 <- soep_final$abs.l1resid^2

soep_final$abs.l1resid2<-soep_final$abs.l1resid^2

Levene.Model.F <- lm(abs.l1resid2 ~ id_id, data=soep_final)
#ANOVA of the squared residuals
anova(Levene.Model.F) #displays the results
```

```
## Analysis of Variance Table
##
## Response: abs.l1resid2
##           Df Sum Sq Mean Sq F value Pr(>F)
## id_id      1      9    9.196   0.0663 0.7968
## Residuals 64995 9014157 138.690
```

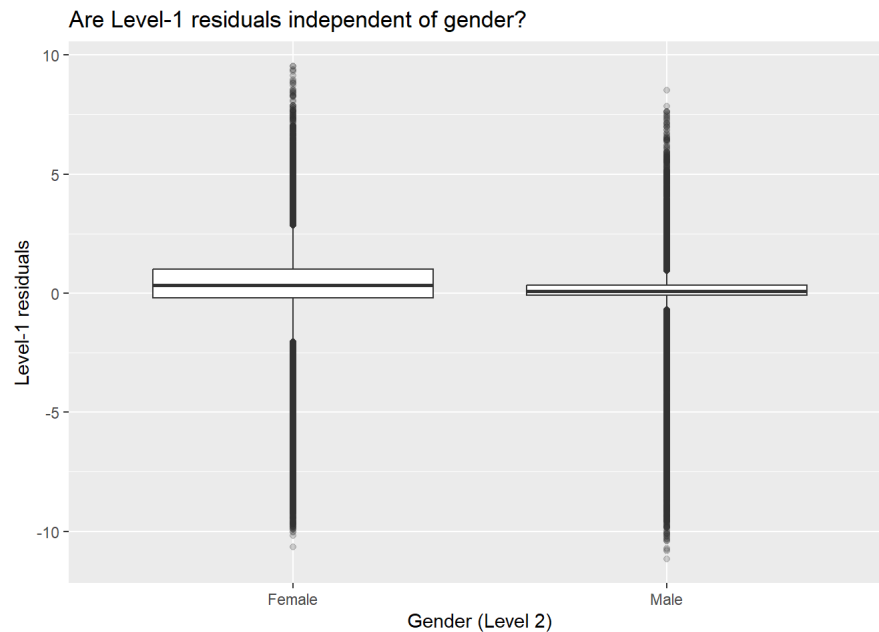
```
plot(ml6, id_id ~ resid(., scaled=TRUE))
```



```
# Independence of L1 residuals from Level 2 predictors

soep_final$llresid <- resid(ml6)

ggplot(soep_final, aes(x = male, y = llresid)) +
  geom_boxplot(outlier.alpha = 0.2) +
  labs(x = "Gender (Level 2)",
       y = "Level-1 residuals",
       title = "Are Level-1 residuals independent of gender?")
```



```
leveneTest(llresid ~ male, data = soep_final)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value    Pr(>F)
## group   1 4384.9 < 2.2e-16 ***
##      64995
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

#Model 2

#Level 1

#Normality

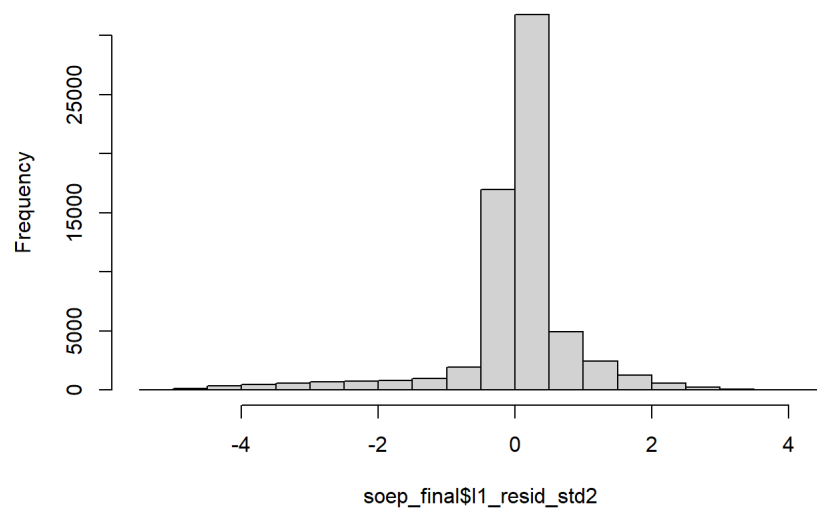
```
#Level 1 residuals

#Extract L1 residuals
soep_final$llresid1 <- residuals(rm5)

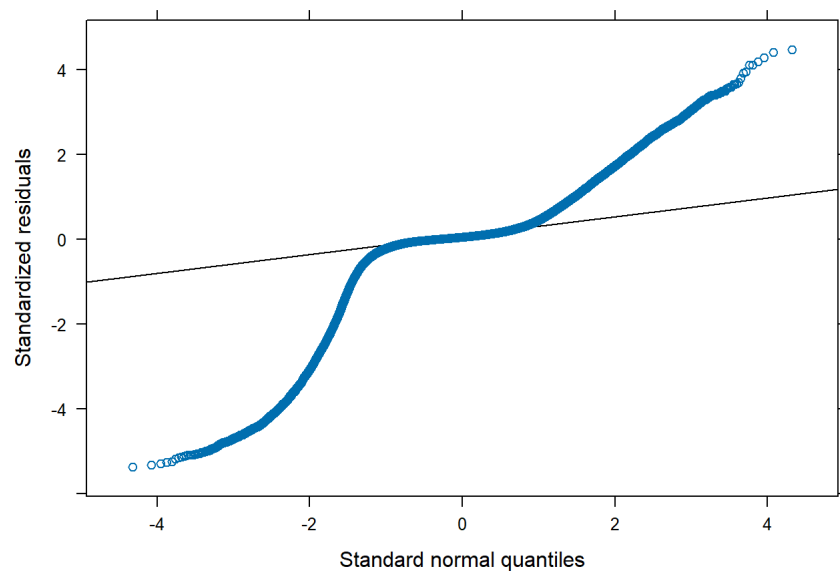
#Extract standardized residuals
soep_final$ll_resid_std2 <- resid(rm5, type = "pearson", scale = TRUE)

#Histogram L1 residuals
hist(soep_final$ll_resid_std2)
```

Histogram of soep_final\$I1_resid_std2

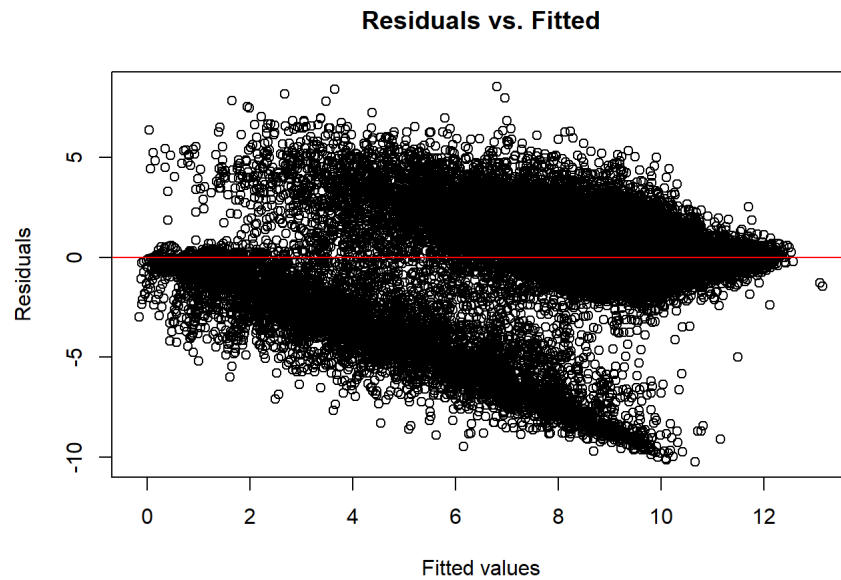


```
#QQ Plot
qqmath(rm5)
```



```
#Homoskedasticity
```

```
plot(fitted(m16), resid(rm5),
     xlab = "Fitted values", ylab = "Residuals",
     main = "Residuals vs. Fitted")
abline(h = 0, col = "red")
```

#Level 2

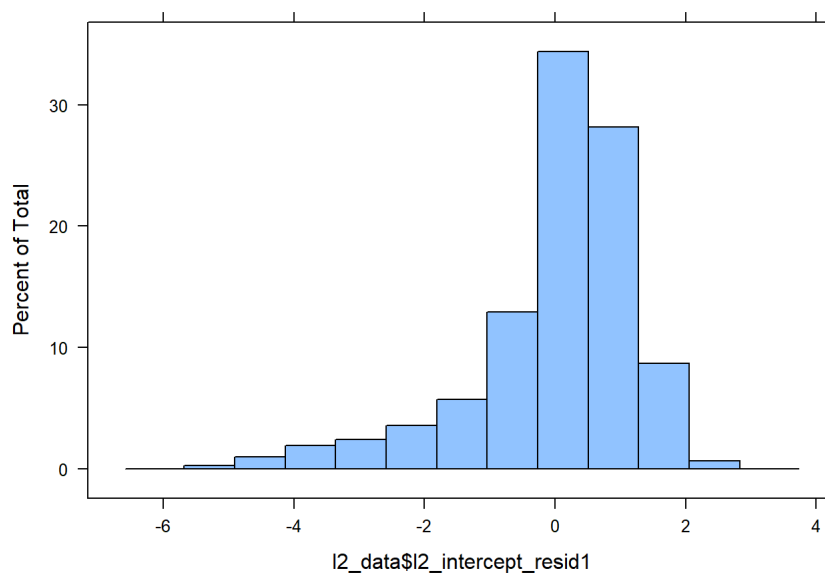
```
#Level 2 residuals

l2_data <- soep_final %>%
  group_by(id_id) %>%
  mutate(log_income_mean = mean(log_income, na.rm = T)) %>%
  dplyr::select(id_id, log_income_mean, male) %>%
  unique()

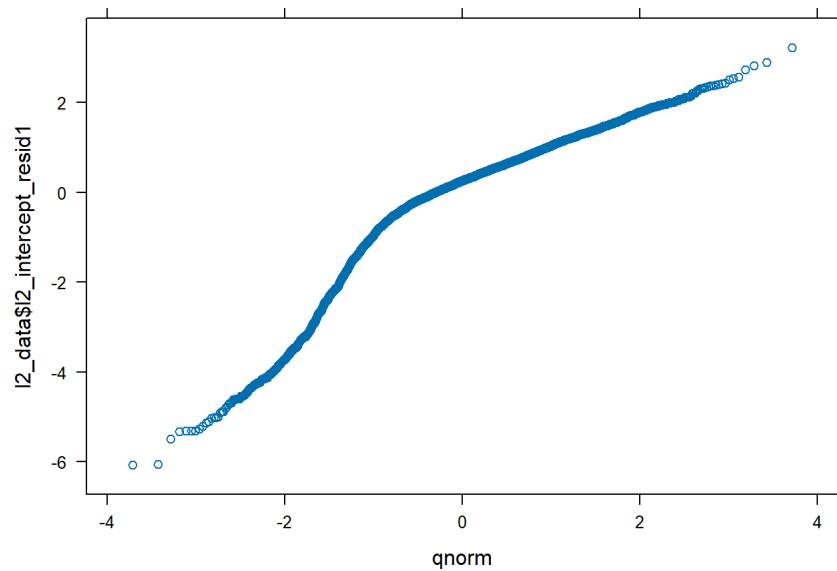
#Random Intercept and Random Slope residuals
l2_data$l2_intercept_resid1 = ranef(rm5)$id_id [, 1]
l2_data$l2_slope_resid1 = ranef(rm5)$id_id [, 2]
l2_data$l2_slope_resid2 = ranef(rm5)$id_id[, 3]
```

#Normality

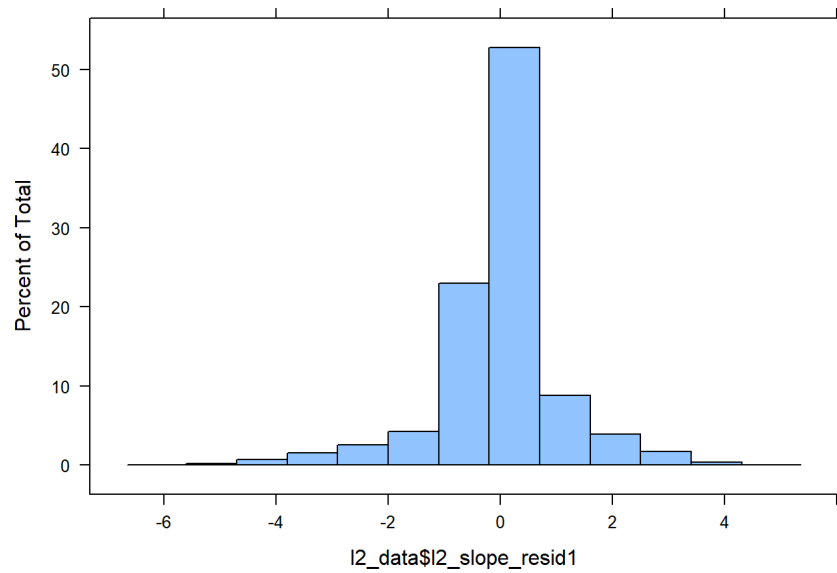
```
#Histogram
histogram(l2_data$l2_intercept_resid1)
```



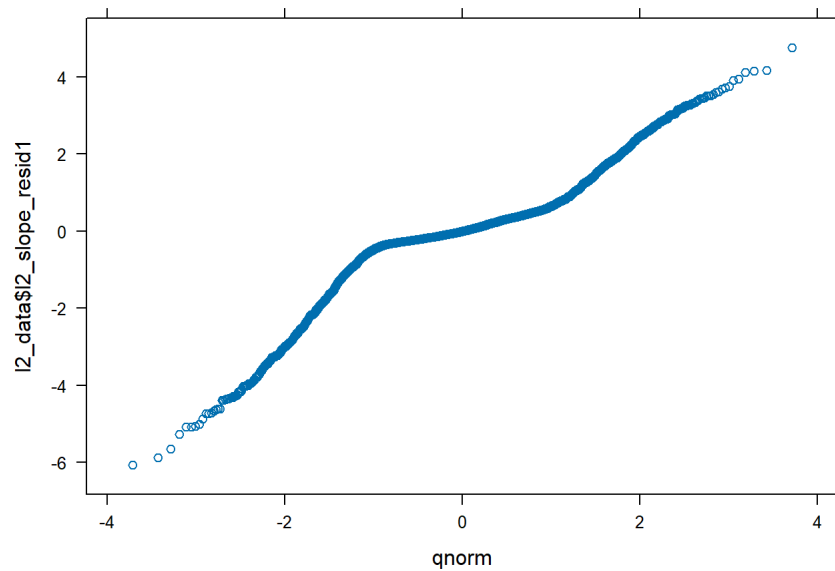
```
#QQ Plot
qqmath(l2_data$l2_intercept_resid1)
```



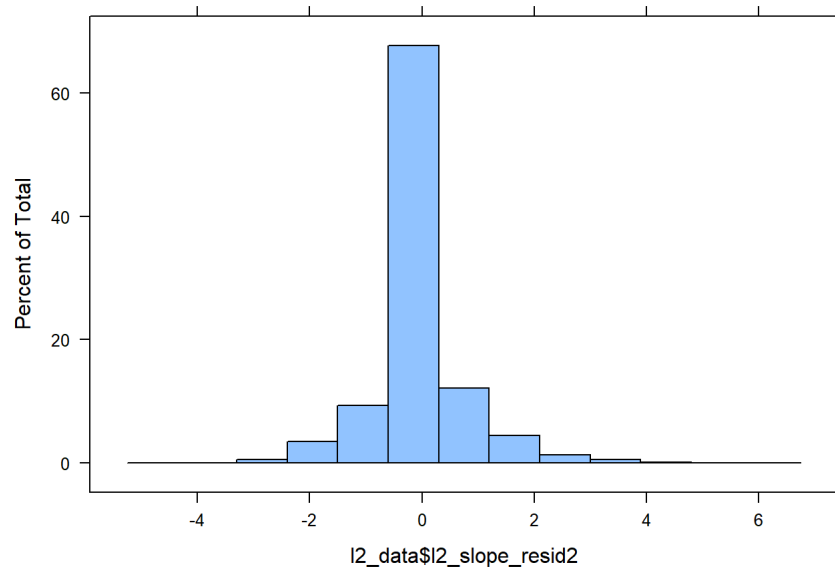
```
#Histogram  
histogram(l2_data$l2_slope_resid1)
```



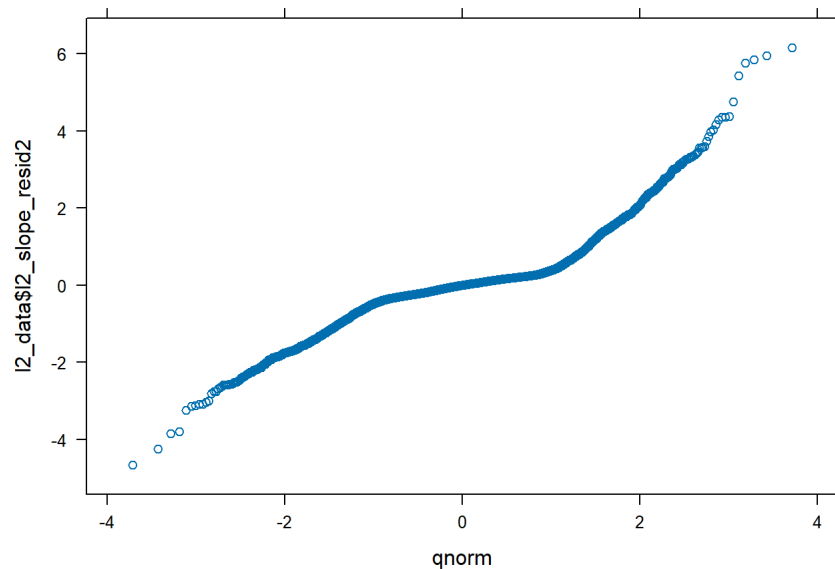
```
#QQ Plot  
qqmath(l2_data$l2_slope_resid1)
```



```
#Histogram  
histogram(l2_data$l2_slope_resid2)
```



```
#QQ Plot  
qqmath(l2_data$l2_slope_resid2)
```



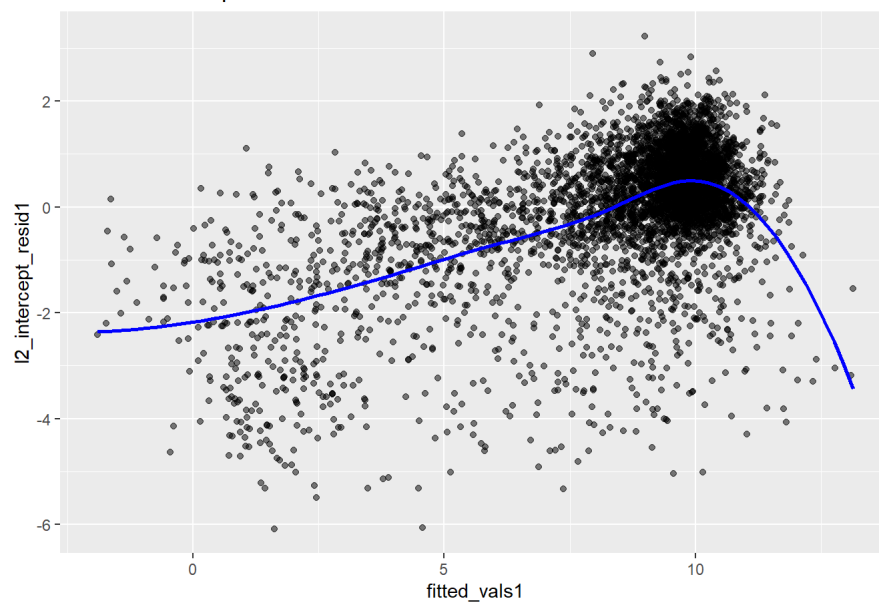
#Homoskedasticity

```
# Random intercepts
l2_data$fitted_vals1 <- fitted(rm5)[match(l2_data$id_id, soep_final$id_id)]

ggplot(l2_data, aes(x = fitted_vals1, y = l2_intercept_resid1)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

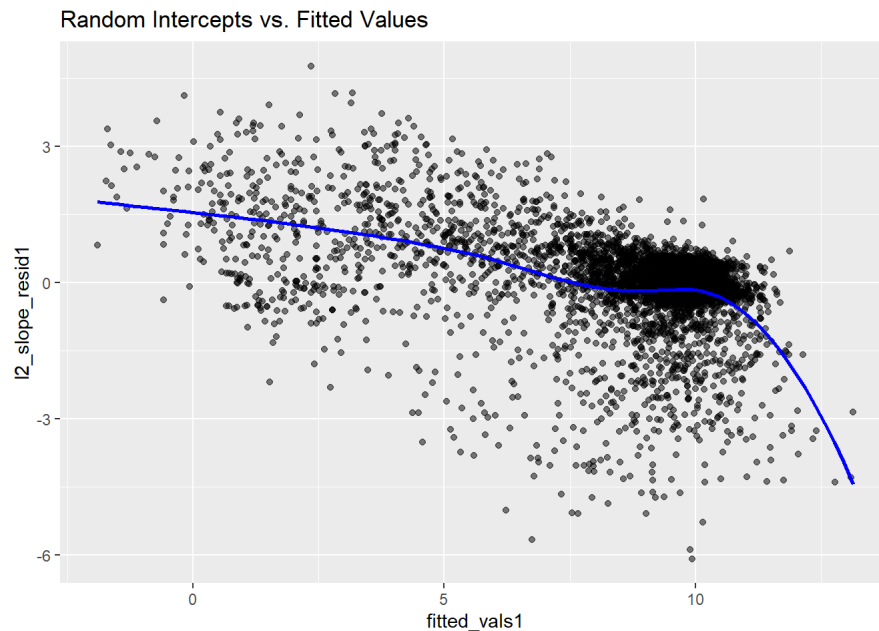
```
## `geom_smooth()` using formula = 'y ~ x'
```

Random Intercepts vs. Fitted Values



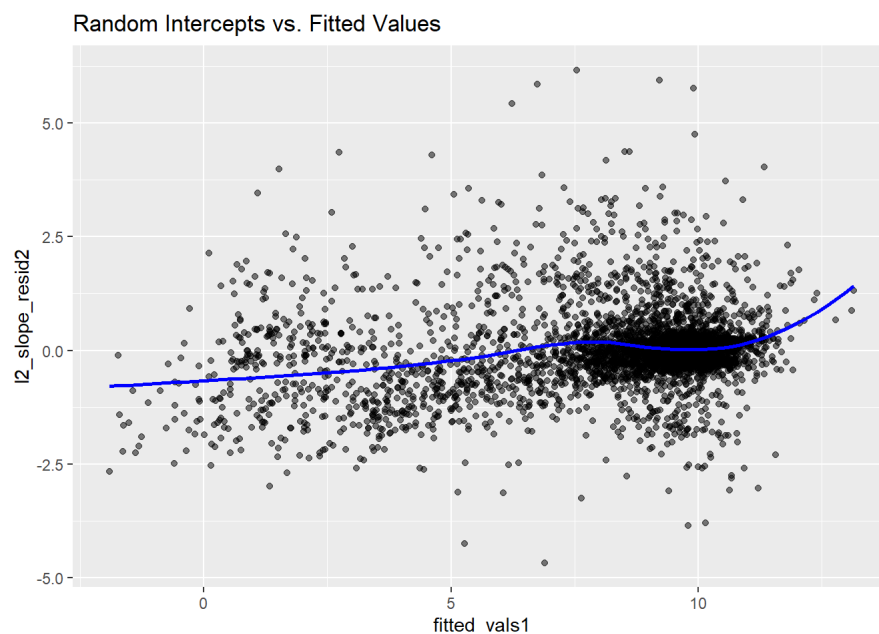
```
# Random slopes
ggplot(l2_data, aes(x = fitted_vals1, y = l2_slope_resid1)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```



```
# Random slopes
ggplot(l2_data, aes(x = fitted_vals1, y = l2_slope_resid2)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```



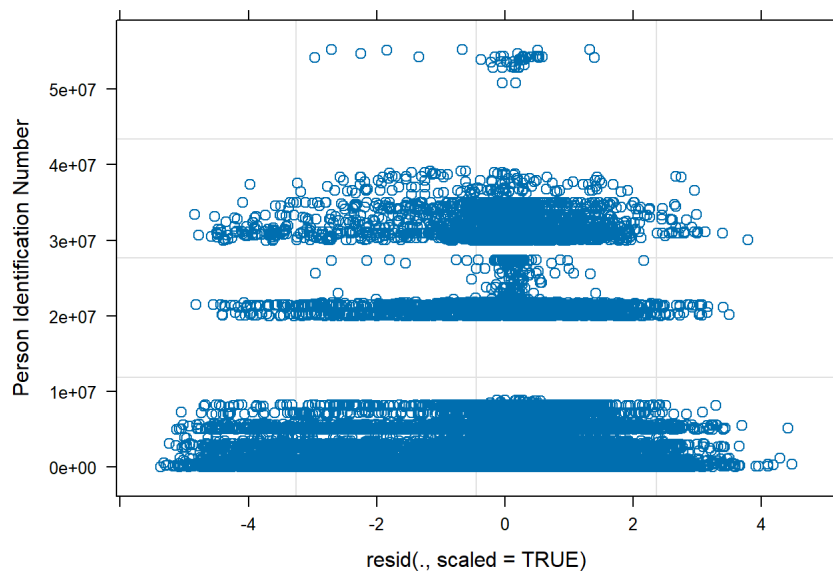
```
#Check whether the variance of the L1 residual errors is the same in all groups
soep_final$l1resid123 <- resid(rm5)

soep_final$abs_l1resid1 <- abs(soep_final$l1resid123)
soep_final$sq_l1resid <- soep_final$abs_l1resid1^2

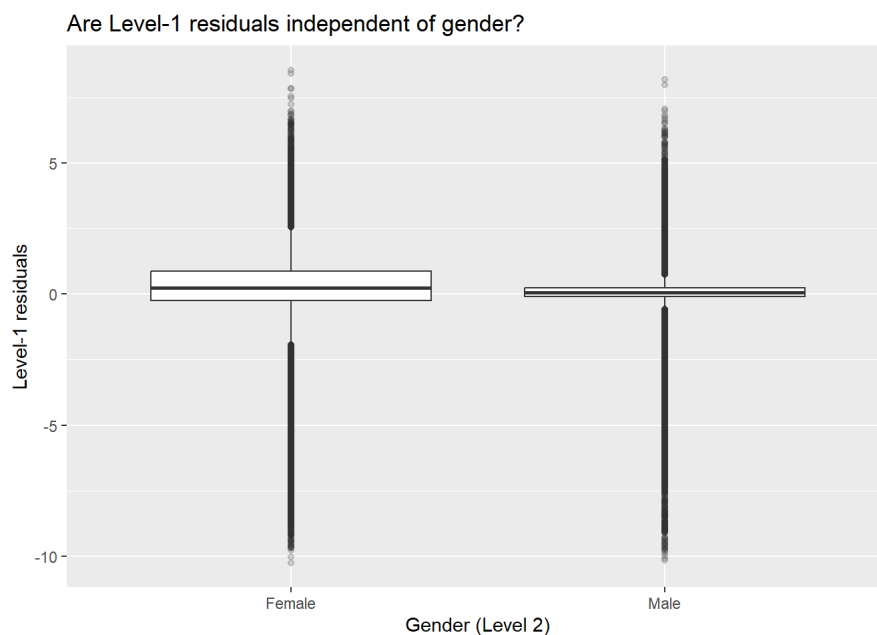
Levene.Model.F1 <- lm(sq_l1resid ~ id_id, data=soep_final)
#ANOVA of the squared residuals
anova(Levene.Model.F1) #displays the results
```

```
## Analysis of Variance Table
##
## Response: sq_l1resid
##           Df Sum Sq Mean Sq F value Pr(>F)
## id_id      1     2.286    0.0254  0.8734
## Residuals 64995 5846838   89.958
```

```
plot(rm5, id_id ~ resid(., scaled=TRUE))
```



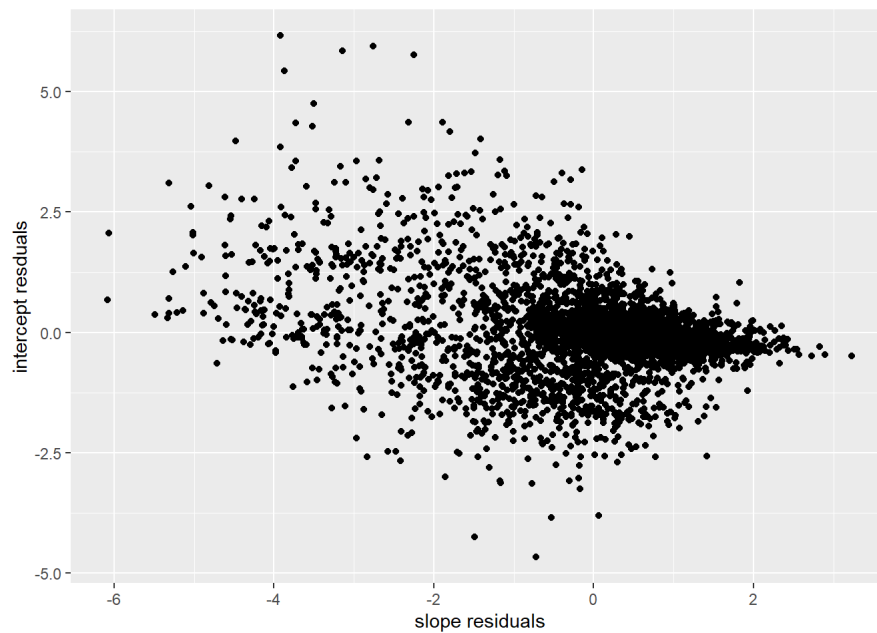
```
# Independence of L1 residuals from Level 2 predictors
ggplot(soep_final, aes(x = male, y = l1resid123)) +
  geom_boxplot(outlier.alpha = 0.2) +
  labs(x = "Gender (Level 2)",
       y = "Level-1 residuals",
       title = "Are Level-1 residuals independent of gender?")
```



```
leveneTest(l1resid123 ~ male, data = soep_final)
```

```
## Levene's Test for Homogeneity of Variance (center = median)
##      Df F value    Pr(>F)
## group  1 4582.6 < 2.2e-16 ***
##      64995
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
#Intercept residuals and Slope residuals relation
l2_data %>%
  ggplot(mapping = aes(x = l2_intercept_resid1, y = l2_slope_resid2)) +
  geom_point() +
  labs(x = "slope residuals", y = "intercept residuals")
```



```
cor.test(l2_data$l2_slope_resid2, as.numeric(l2_data$l2_intercept_resid1))
```

```
##
## Pearson's product-moment correlation
##
## data: l2_data$l2_slope_resid2 and as.numeric(l2_data$l2_intercept_resid1)
## t = -21.195, df = 4883, p-value < 2.2e-16
## alternative hypothesis: true correlation is not equal to 0
## 95 percent confidence interval:
## -0.3157268 -0.2643612
## sample estimates:
## cor
## -0.290253
```

#Level 3

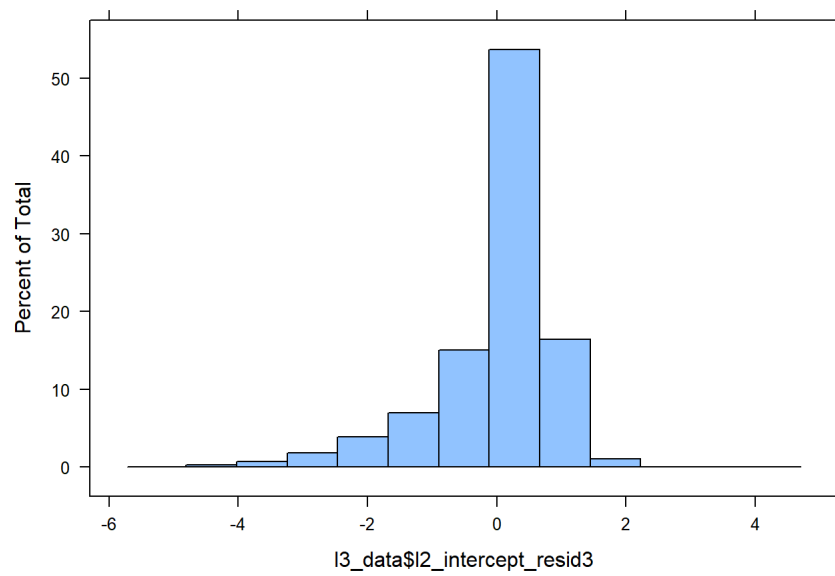
```
#Level 2 residuals

l3_data <- soep_final %>%
  group_by(hh_id) %>%
  mutate(log_income_mean = mean(log_income, na.rm = T)) %>%
  dplyr::select(hh_id, log_income_mean) %>%
  unique()

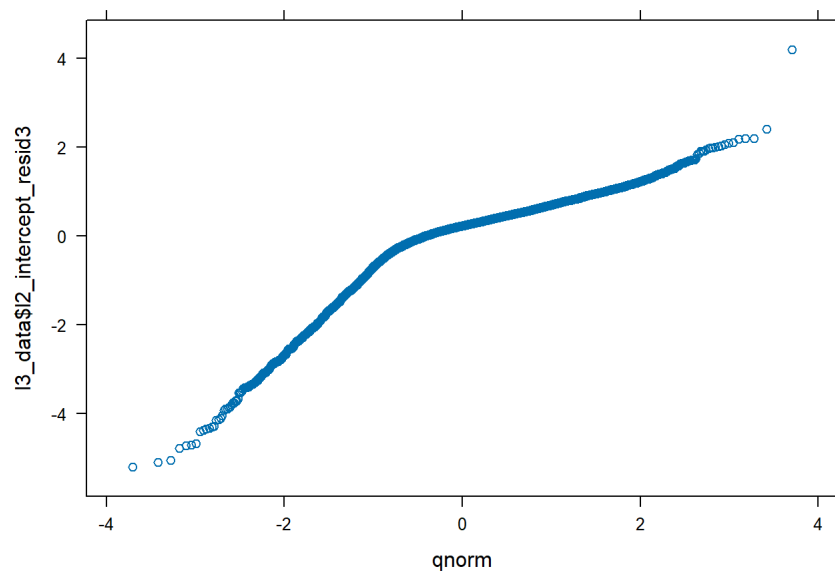
#Random Intercept and Random Slope residuals
l3_data$l2_intercept_resid3 = ranef(ml6)$hh_id [, 1]
l3_data$l2_intercept_resid4 = ranef(rm5)$hh_id [, 1]
```

#Normality

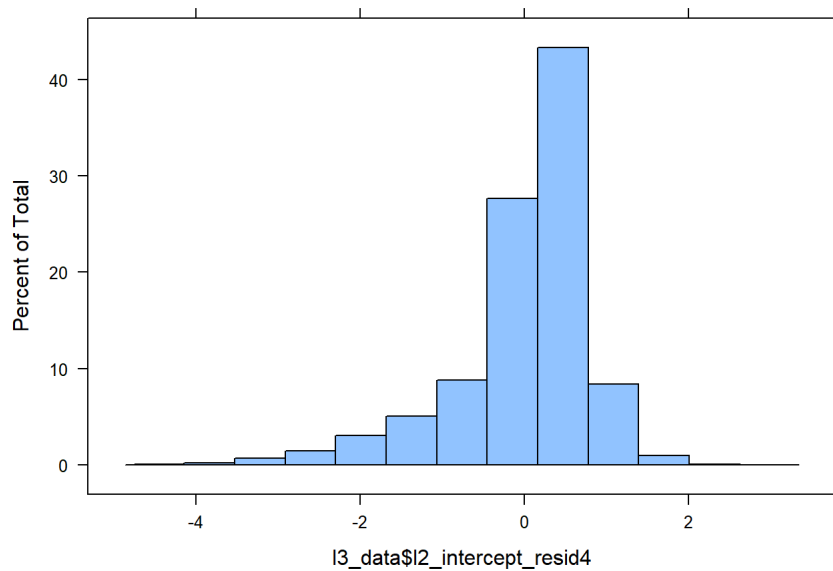
```
#Histogram
histogram(l3_data$l2_intercept_resid3)
```



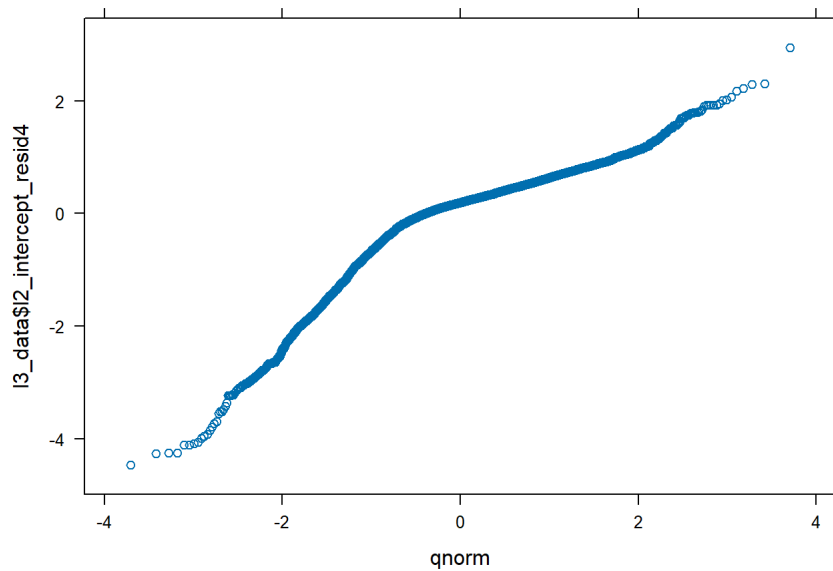
```
#QQ Plot  
qqmath(l3_data$l2_intercept_resid3)
```



```
#Histogram  
histogram(l3_data$l2_intercept_resid4)
```

```
#QQ Plot
qqmath(l3_data$l2_intercept_resid4)
```



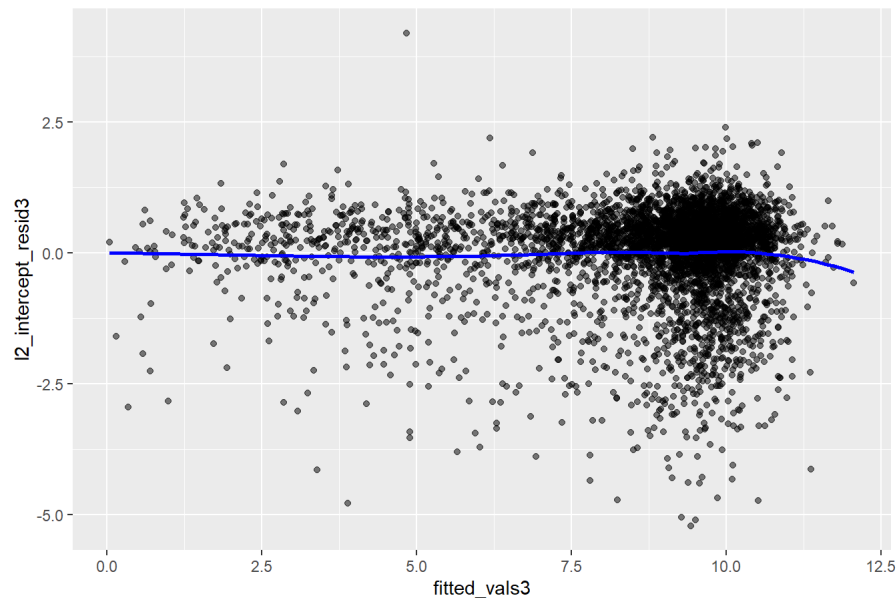
#Homoskedasticity

```
# Random intercepts
l3_data$fitted_vals3 <- fitted(ml6)[match(l3_data$hh_id, soep_final$hh_id)]
l3_data$fitted_vals4 <- fitted(rm5)[match(l3_data$hh_id, soep_final$hh_id)]

ggplot(l3_data, aes(x = fitted_vals3, y = l2_intercept_resid3)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```

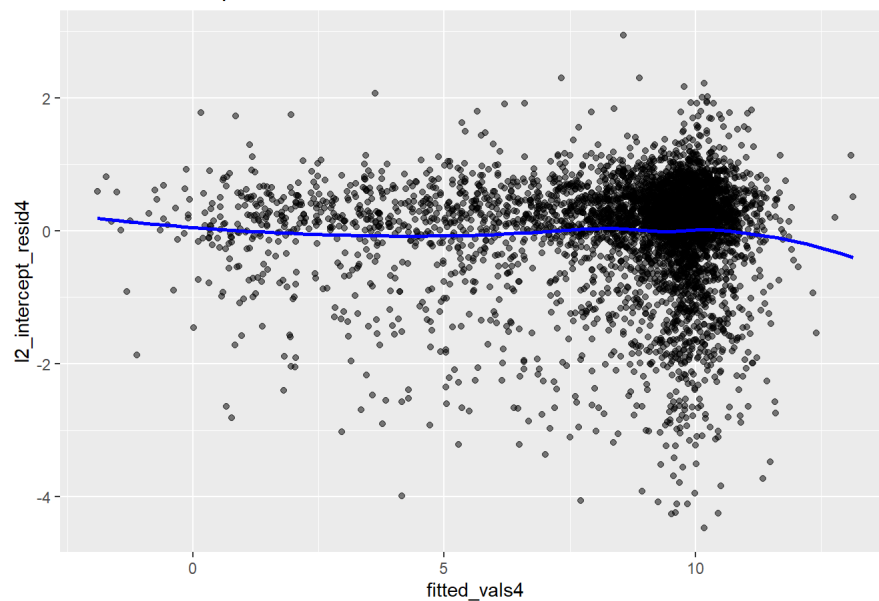
Random Intercepts vs. Fitted Values



```
ggplot(l3_data, aes(x = fitted_vals4, y = l2_intercept_resid4)) +
  geom_point(alpha = 0.5) +
  geom_smooth(method = "loess", color = "blue", se = FALSE) +
  labs(title = "Random Intercepts vs. Fitted Values")
```

```
## `geom_smooth()` using formula = 'y ~ x'
```

Random Intercepts vs. Fitted Values



```
#Check whether the variance of the L1 residual errors is the same in all groups
soep_final$l1resid3 <- resid(ml6)
soep_final$l1resid4 <- resid(rm5)

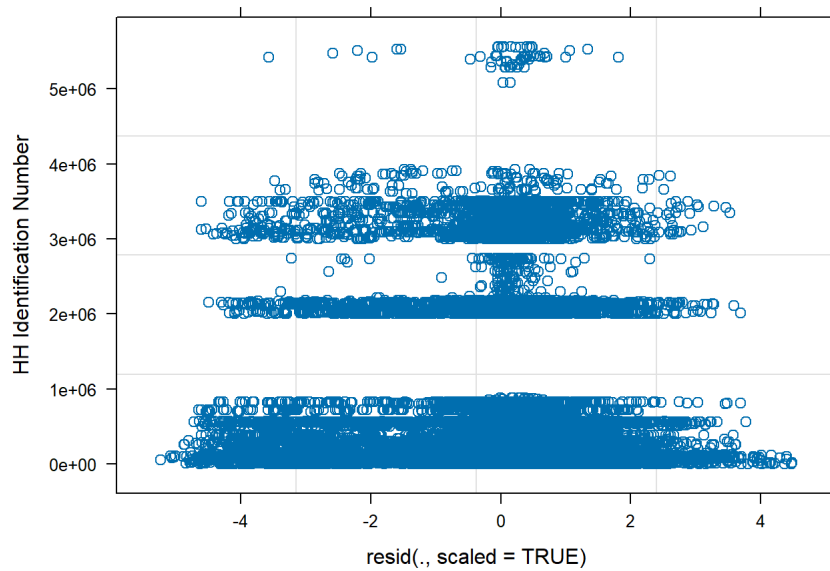
soep_final$abs_l1resid3 <- abs(soep_final$l1resid3)
soep_final$sq_l1resid3 <- soep_final$abs_l1resid3^2

soep_final$abs_l1resid4 <- abs(soep_final$l1resid4)
soep_final$sq_l1resid4 <- soep_final$abs_l1resid4^2

Levene.Model.F3 <- lm(sq_l1resid3 ~ hh_id, data=soep_final)
#ANOVA of the squared residuals
anova(Levene.Model.F3) #displays the results
```

```
## Analysis of Variance Table
##
## Response: sq_llresid3
##           Df Sum Sq Mean Sq F value Pr(>F)
## hh_id      1     44  44.103    0.318 0.5728
## Residuals 64995 9014122 138.689
```

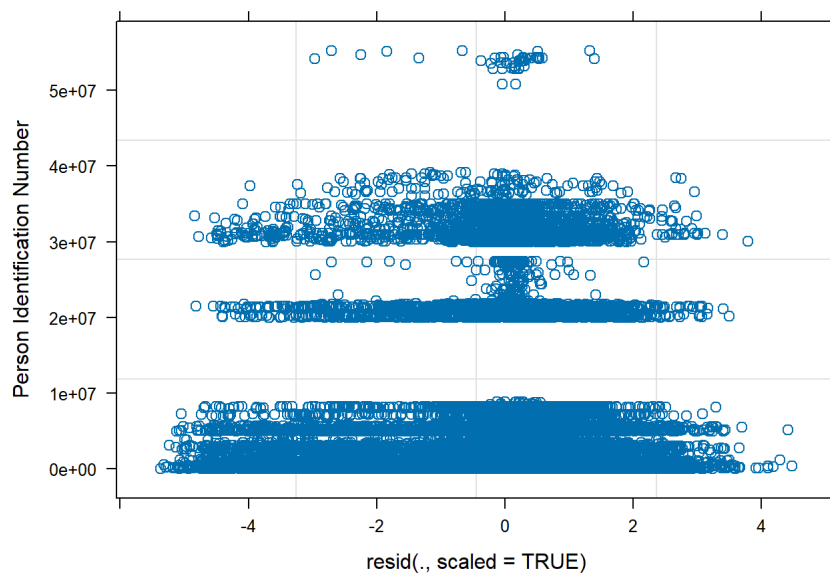
```
plot(m16, hh_id ~ resid(., scaled=TRUE))
```



```
Levene.Model.F4 <- lm(sq_llresid4 ~ hh_id, data=soep_final)
#ANOVA of the squared residuals
anova(Levene.Model.F4) #displays the results
```

```
## Analysis of Variance Table
##
## Response: sq_llresid4
##           Df Sum Sq Mean Sq F value Pr(>F)
## hh_id      1      0   0.206   0.0023 0.9618
## Residuals 64995 5846840  89.958
```

```
plot(rm5, id_id ~ resid(., scaled=TRUE))
```



```
##Missing Data
```

```

soep_fill1 <- soep_sub %>%
  filter(age >= 25 & age <= 60)

#Recode gender so that male = 1 and female = 0
soep_fill1 <- soep_fill1 %>%
  mutate(male = case_when(
    gender == 1 ~ 1,
    gender == 2 ~ 0,
    TRUE ~ NA_real_))

#Recode marital status so that single = 0 and married = 1
soep_fill1 <- soep_fill1 %>%
  mutate(marital_status = marital_status_unfinished - 1) %>%
  mutate(marital_status = case_when(
    marital_status == 0 ~ 1,
    marital_status == 1 ~ 0,
    TRUE ~ marital_status ))

#Create a new variable for which single = 0, married = 1, and other = 2
soep_fill1 <- soep_fill1 %>%
  mutate(marital_status_reduced = case_when(
    marital_status == 0 ~ 0,
    marital_status == 1 ~ 1,
    marital_status > 1 ~ 2
  ))

```

```

#Filter the dataset for individuals that went from unmarried to married during the course of the panel
ids_changed1 <- soep_fill1 %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(prev_marital_status = lag(marital_status_reduced)) %>%
  filter(prev_marital_status == 0 & marital_status_reduced == 1) %>%
  distinct(id_id)

soep_changed1 <- soep_fill1 %>%
  filter(id_id %in% ids_changed1$id_id)

```

```

#Determine the year in which the individual got married
soep_d1 <- soep_fill1 %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(prev_marital_status = lag(marital_status_reduced),
    transition = prev_marital_status == 0 & marital_status_reduced == 1) %>%
  filter(transition) %>%
  slice(1) %>%
  dplyr::select(id_id, transition_year = year)

#Center the variable so that 0 = year of marriage
soep_final1 <- soep_fill1 %>%
  inner_join(soep_d1, by = "id_id") %>%
  mutate(relative_year = year - transition_year)

soep_final1 <- soep_final1 %>%
  arrange(id_id, year) %>%
  group_by(id_id) %>%
  mutate(married = cummax(marital_status_reduced %in% c(1, 2)))

soep_final_NA <- soep_final1 %>%
  dplyr::select(id_id, hh_id, income, age, year, education, gender, married, transition_year, relative_year)

soep_final_NA <- soep_final_NA %>%
  mutate(
    income = ifelse(income < 0, NA, income),
    gender = ifelse(gender < 0, NA, gender),
    age = ifelse(age < 0, NA, age),
    education = ifelse(education < 0, NA, education))

```

```

#Count observations on each Level
data.frame(
  level1_observations = nrow(soep_final_NA),
  level2_individuals = length(unique(soep_final_NA$id_id)),
  level3_households = length(unique(soep_final_NA$hh_id))
)

```

```

##   level1_observations level2_individuals level3_households
## 1             66523             4885             4759

```

```

#Total number of missings
sum(is.na(soep_final_NA))

```

```
## [1] 1514
```

```
#Number of missings per variable
colSums(is.na(soep_final_NA))
```

```
##          id_id          hh_id          income          age          year
##           0           0           132           0           0
##    education          gender    married transition_year    relative_year
##       1382           0           0           0           0
```

```
#Pattern of missing values
md.pattern(soep_final_NA, plot = F)
```

```
##          id_id hh_id age year gender married transition_year relative_year income
## 65016      1    1  1  1  1    1    1    1    1    1
## 1375      1    1  1  1  1    1    1    1    1    1
## 125       1    1  1  1  1    1    1    1    1    0
## 7         1    1  1  1  1    1    1    1    1    0
##          0    0  0  0  0    0    0    0    0    132
##    education
## 65016      1    0
## 1375      0    1
## 125       1    1
## 7         0    2
##       1382 1514
```

```
#Proportion of missing values
sum(is.na(soep_final_NA)) / (nrow(soep_final_NA) * ncol(soep_final_NA)) * 100
```

```
## [1] 0.2275905
```

```
#Number of missings on income variable
sum(is.na(soep_final_NA$income))
```

```
## [1] 132
```

```
#Number of missings on education variable
sum(is.na(soep_final_NA$education))
```

```
## [1] 1382
```

```
#Proportion of missings on income variable
sum(is.na(soep_final_NA$income)) / nrow(soep_final_NA) * 100
```

```
## [1] 0.1984276
```

```
#Proportion of missings on education variable
sum(is.na(soep_final_NA$education)) / nrow(soep_final_NA) * 100
```

```
## [1] 2.077477
```

```
#Missings on income by gender
soep_final_NA %>%
  mutate(income_missing = is.na(income)) %>%
  group_by(gender) %>%
  summarise(
    percent_missing_income = mean(income_missing) * 100,
    n = n())
```

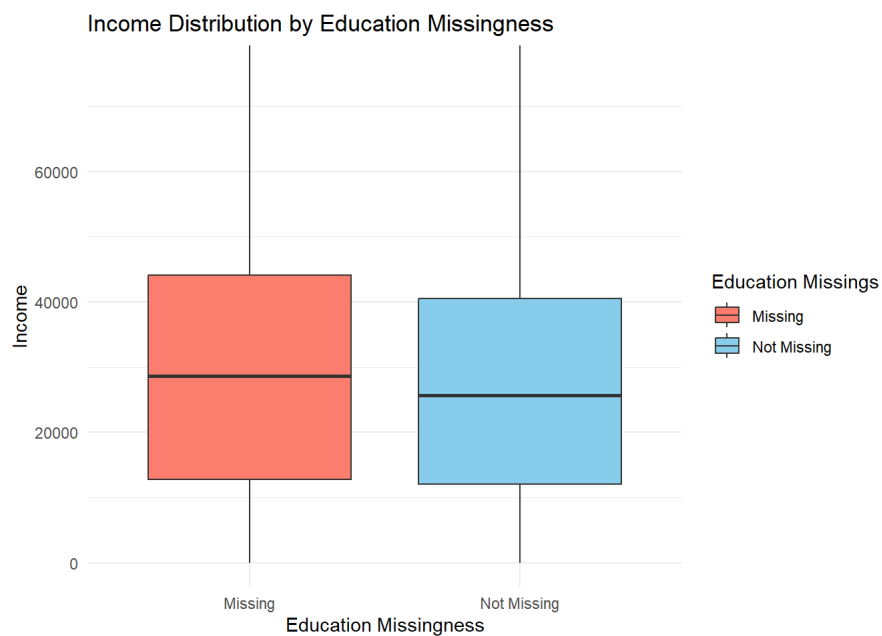
```
## # A tibble: 2 × 3
##   gender percent_missing_income    n
##   <dbl>             <dbl> <int>
## 1     1             0.247 36040
## 2     2             0.141 30483
```

```
#Missings on education by gender
soep_final_NA %>%
  mutate(education_missing = is.na(education)) %>%
  group_by(gender) %>%
  summarise(
    percent_missing_education = mean(education_missing) * 100,
    n = n())
```

```
## # A tibble: 2 × 3
##   gender percent_missing_education    n
##   <dbl>      <dbl>      <dbl> <int>
## 1     1         1         2.60 36040
## 2     2         2         1.46 30483
```

```
#Income of observations with NA on education vs no NA
soep_final_NA %>%
  mutate(
    education_missing = ifelse(is.na(education), "Missing", "Not Missing")
  ) %>%
  ggplot(aes(x = education_missing, y = income, fill = education_missing)) +
  geom_boxplot(outlier.shape = NA) +
  coord_cartesian(ylim = c(0, quantile(soep_final_NA$income, 0.95, na.rm = TRUE))) +
  labs(
    x = "Education Missingness",
    y = "Income",
    title = "Income Distribution by Education Missingness",
    fill = "Education Missings"
  ) +
  scale_fill_manual(values = c("Not Missing" = "skyblue", "Missing" = "salmon")) +
  theme_minimal()
```

```
## Warning: Removed 132 rows containing non-finite outside the scale range
## (`stat_boxplot()`).
```



```
#Little's MCAR test
soep_final_NA_test <- soep_final_NA %>%
  dplyr::select(education, income, id_id, age, relative_year)

mcar_test(soep_final_NA_test)
```

```
## # A tibble: 1 × 4
##   statistic    df p.value missing.patterns
##   <dbl> <dbl> <dbl>      <int>
## 1    380.    11      0         4
```

```
##Tables
```

```

#Descriptive Statistics

soep_desc <- soep_final %>%
  dplyr::select(log_income, married, relative_year, male, age, age_squared, transition_year, education)

soep_desc <- as.data.frame(soep_desc)

soep_desc$married <- as.numeric(soep_desc$married)
soep_desc$male <- as.numeric(soep_desc$male)
soep_desc$education <- as.numeric(soep_desc$education)

soep_desc <- soep_desc %>%
  mutate(married = case_when(
    married == 1 ~ 0,
    married == 2 ~ 1,
    TRUE ~ NA_real_)) %>%
  mutate(male = case_when(
    male == 1 ~ 0,
    male == 2 ~ 1,
    TRUE ~ NA_real_))

soep_desc <- soep_desc %>%
  mutate(education0 = case_when(
    education == 1 ~ 1,
    education == 2 ~ 0,
    education == 3 ~ 0,
    TRUE ~ NA_real_))

soep_desc <- soep_desc %>%
  mutate(education1 = case_when(
    education == 1 ~ 0,
    education == 2 ~ 1,
    education == 3 ~ 0,
    TRUE ~ NA_real_))

soep_desc <- soep_desc %>%
  mutate(education2 = case_when(
    education == 1 ~ 0,
    education == 2 ~ 0,
    education == 3 ~ 1,
    TRUE ~ NA_real_))

soep_desc <- soep_desc %>%
  dplyr::select(-c(education))

#USE LATEX AND CHANGE N MANUALLY
stargazer(soep_desc, style = "asr", digits=1, title = "Table 1 Descriptives", out = "table1.html", covariate.labels =
  c("log Income", "Marital Status", "Relative Year to Marriage", "Gender", "Age", "Age Squared", "Year of Marriage",
  "Less than High School", "High School", "More than High School"))

```

```

##
## % Table created by stargazer v.5.2.3 by Marek Hlavac, Social Policy Institute. E-mail: marek.hlavac at gmail.com
## % Date and time: Thu, Jun 26, 2025 - 10:28:22 PM
## \begin{table}[!htbp] \centering
## \caption{Table 1 Descriptives}
## \label{}
## \begin{tabular}{@{\extracolsep{5pt}}lcccc}
## \hline \hline \hline \hline \hline
## Statistic & \multicolumn{1}{c}{N} & \multicolumn{1}{c}{Mean} & \multicolumn{1}{c}{St. Dev.} & \multicolumn{1}{c}{Min} & \multicolumn{1}{c}{Max} \\
## \hline \hline \hline \hline \hline
## log Income & 64,997 & 9.1 & 3.2 & 0.0 & 14.0 \\
## Marital Status & 64,997 & 0.7 & 0.5 & 0 & 1 \\
## Relative Year to Marriage & 64,997 & 3.5 & 8.1 & $-30 & 34 \\
## Gender & 64,997 & 0.5 & 0.5 & 0 & 1 \\
## Age & 64,997 & 36.8 & 8.1 & 25 & 60 \\
## Age Squared & 64,997 & 1,417.6 & 645.4 & 625 & 3,600 \\
## Year of Marriage & 64,997 & 18.8 & 9.9 & 0 & 37 \\
## Less than High School & 64,997 & 0.1 & 0.2 & 0 & 1 \\
## High School & 64,997 & 0.6 & 0.5 & 0 & 1 \\
## More than High School & 64,997 & 0.3 & 0.5 & 0 & 1 \\
## \hline \hline \hline \hline \hline
## \end{tabular}
## \end{table}

```

```
#Presentation
```

```
tab_model(
  m11, m12, m13, m14, m14a, m15, m16,
  dv.labels = "Log Income",
  show.re.var = TRUE,
  show.ci = FALSE,
  file = "M1.html",
  pred.labels = c("Intercept", "Year", "Age", "Age Squared",
    "High School", "More Than High School",
    "Married", "Male",
    "Year of Marriage", "Married:Male"))
```

| Log Income | | | | | | | | | | | | | | | |
|--|---------------|--------|---------------|--------|---------------|--------|---------------|--------|---------------|--------|------------------|--------|------------------|--------|--|
| Predictors | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | |
| Intercept | 8.05 | <0.001 | 8.02 | <0.001 | 7.79 | <0.001 | 6.60 | <0.001 | 6.78 | <0.001 | 6.76 | <0.001 | 7.10 | <0.001 | |
| Year | 0.04 | <0.001 | 0.04 | <0.001 | 0.02 | <0.001 | 0.02 | <0.001 | 0.03 | <0.001 | 0.03 | <0.001 | 0.03 | <0.001 | |
| Age | | | -0.12 | <0.001 | -0.29 | <0.001 | -0.26 | <0.001 | -0.28 | <0.001 | -0.25 | <0.001 | -0.89 | <0.001 | |
| Age Squared | | | | | 0.36 | <0.001 | 0.28 | <0.001 | 0.24 | <0.001 | 0.22 | <0.001 | 0.23 | <0.001 | |
| High School | | | | | -0.22 | <0.001 | -0.17 | <0.001 | -0.16 | <0.001 | -0.14 | 0.001 | -0.14 | <0.001 | |
| More Than High School | | | | | 0.61 | <0.001 | 0.70 | <0.001 | 0.69 | <0.001 | 0.90 | <0.001 | 0.90 | <0.001 | |
| Married | | | | | 2.14 | <0.001 | 2.17 | <0.001 | 2.17 | <0.001 | 2.19 | <0.001 | 2.19 | <0.001 | |
| Male | | | | | | | 1.70 | <0.001 | 1.69 | <0.001 | 1.52 | <0.001 | 0.88 | <0.001 | |
| Year of Marriage | | | | | | | | | -0.01 | 0.001 | -0.02 | <0.001 | -0.02 | <0.001 | |
| Married:Male | | | | | | | | | | | | | 1.21 | <0.001 | |
| Random Effects | | | | | | | | | | | | | | | |
| σ^2 | 5.20 | | 5.20 | | 5.12 | | 5.13 | | 5.13 | | 4.53 | | 4.53 | | |
| τ_{00} | 3.32 | id_id | 3.32 | id_id | 3.36 | id_id | 2.35 | id_id | 2.34 | id_id | 2.91 | id_id | 2.80 | id_id | |
| | 2.59 | hh_id | 2.61 | hh_id | 2.26 | hh_id | 2.34 | hh_id | 2.34 | hh_id | 1.91 | hh_id | 1.89 | hh_id | |
| τ_{11} | | | | | | | | | | | 3.96 | | 3.62 | | |
| | | | | | | | | | | | id_id.marriedYes | | id_id.marriedYes | | |
| ρ_{01} | | | | | | | | | | | -0.54 | id_id | -0.53 | id_id | |
| ICC | 0.53 | | 0.53 | | 0.52 | | 0.48 | | 0.48 | | 0.52 | | 0.52 | | |
| N | 4730 | hh_id | 4730 | hh_id | 4730 | hh_id | 4730 | hh_id | 4730 | hh_id | 4730 | hh_id | 4730 | hh_id | |
| | 4885 | id_id | 4885 | id_id | 4885 | id_id | 4885 | id_id | 4885 | id_id | 4885 | id_id | 4885 | id_id | |
| Observations | 64997 | | 64997 | | 64997 | | 64997 | | 64997 | | 64997 | | 64997 | | |
| Marginal R ² / Conditional R ² | 0.009 / 0.536 | | 0.011 / 0.538 | | 0.063 / 0.553 | | 0.121 / 0.541 | | 0.120 / 0.540 | | 0.105 / 0.574 | | 0.125 / 0.578 | | |

```
tab_model(
  m11, rm1, rm1a, rm2, rm3, rm4, rm4b, rm5,
  dv.labels = "Log Income",
  show.re.var = TRUE,
  show.ci = FALSE,
  file = "M2.html",
  pred.labels = c("Intercept", "Year",
    "High School", "More Than High School",
    "Relative Year to Marriage", "Male", "Relative Year to Marriage Squared",
    "Relative Year to Marriage:Male", "Relative Year to Marriage Squared:Male"))
```

| Log Income | | | | | | | | | | | | | | | |
|-----------------------|-----------|--------|-----------|--------|-----------|--------|-----------|--------|-----------|--------|-----------|--------|-----------|--------|--|
| Predictors | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | Estimates | p | |
| Intercept | 8.05 | <0.001 | 8.49 | <0.001 | 7.57 | <0.001 | 6.46 | <0.001 | 6.43 | <0.001 | 6.64 | <0.001 | 6.47 | <0.001 | |
| Year | 0.04 | <0.001 | 0.02 | <0.001 | 0.01 | <0.001 | 0.02 | <0.001 | 0.01 | <0.001 | 0.01 | 0.003 | 0.01 | 0.003 | |
| High School | | | 0.18 | <0.001 | 0.14 | <0.001 | 0.11 | <0.001 | 0.13 | <0.001 | 0.07 | 0.002 | 0.05 | 0.002 | |
| More Than High School | | | -0.08 | <0.001 | -0.05 | <0.001 | -0.06 | <0.001 | -0.05 | <0.001 | -0.05 | 0.003 | -0.01 | 0.81 | |

| | | | | | | | | | | | | |
|--|---------------------------|---------------------------|---------------------------|---------------------------|---------------------------------------|---|------|--------|------|--------|---|--------|
| Relative Year to Marriage | | | 0.62 | <0.001 | 0.71 | <0.001 | 0.92 | <0.001 | 0.73 | <0.001 | 1.08 | <0.001 |
| Male | | | 2.10 | <0.001 | 2.13 | <0.001 | 2.20 | <0.001 | 2.13 | <0.001 | 2.20 | <0.001 |
| Relative Year to Marriage Squared | | | | | 1.72 | <0.001 | 1.67 | <0.001 | 1.72 | <0.001 | 1.52 | <0.001 |
| Relative Year to Marriage:Male | | | | | | | | | | | | |
| Relative Year to Marriage Squared:Male | | | | | | | | | | | | |
| Random Effects | | | | | | | | | | | | |
| σ^2 | 5.20 | 5.19 | 5.14 | 5.14 | 4.11 | 4.35 | | | | | 3.64 | |
| τ_{00} | 3.32 <small>id_id</small> | 3.30 <small>id_id</small> | 3.38 <small>id_id</small> | 2.34 <small>id_id</small> | 2.51 <small>id_id</small> | 2.44 <small>id_id</small> | | | | | 2.55 <small>id_id</small> | |
| | 2.59 <small>hh_id</small> | 2.51 <small>hh_id</small> | 2.19 <small>hh_id</small> | 2.30 <small>hh_id</small> | 1.86 <small>hh_id</small> | 2.18 <small>hh_id</small> | | | | | 1.70 <small>hh_id</small> | |
| τ_{11} | | | | | 1.19 | 0.85 | | | | | 1.94 <small>id_id.relative_year_</small> | |
| | | | | | <small>id_id.relative_year_sd</small> | <small>id_id.relative_year_squared_sd</small> | | | | | 1.29 | |
| | | | | | | | | | | | <small>id_id.relative_year_square</small> | |
| ρ_{01} | | | | | 0.12 <small>id_id</small> | 0.12 <small>id_id</small> | | | | | 0.26 <small>id_id.relative_year_</small> | |
| | | | | | | | | | | | -0.21 | |
| | | | | | | | | | | | <small>id_id.relative_year_square</small> | |
| ICC | 0.53 | 0.53 | 0.52 | 0.47 | 0.57 | 0.55 | | | | | 0.64 | |
| N | 4730 <small>hh_id</small> | 4730 <small>hh_id</small> | 4730 <small>hh_id</small> | 4730 <small>hh_id</small> | 4730 <small>hh_id</small> | 4730 <small>hh_id</small> | | | | | 4730 <small>hh_id</small> | |
| | 4885 <small>id_id</small> | 4885 <small>id_id</small> | 4885 <small>id_id</small> | 4885 <small>id_id</small> | 4885 <small>id_id</small> | 4885 <small>id_id</small> | | | | | 4885 <small>id_id</small> | |
| Observations | 64997 | 64997 | 64997 | 64997 | 64997 | 64997 | | | | | 64997 | |
| Marginal R ² / Conditional R ² | 0.009 / 0.536 | 0.007 / 0.532 | 0.056 / 0.547 | 0.117 / 0.536 | 0.110 / 0.618 | 0.113 / 0.604 | | | | | 0.088 / 0.674 | |