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Introduction

- 1.1 Radiative transform equation
- 1.2 Bayes Theorem
- 1.3 GMRF
- 1.4 Inverse Rosenblatt transform

2

Linear Forward model

- algorithmic box ? or in section?
- define posterior

2.1 Sampling

2.1.1 two hyperparameter DAG

Marginal – Gibbs-MH

Conditional – RTO

2.1.2 four hyperparameter DAG

Marginal – t-walk

Conditional – RTO

2.2 Extending Model to Temperature and Pressure

- algorithmic box ? updating scheme
- write down DAG
- define posterior

2.2.1 Squared Inverse Rosenblatt transform

3

Nonlinear Forward model

- algorithmic box? updating scheme

3.1 Sampling

3.1.1 two or four hyperparameter DAG

MTC or t-walk

4

Nonlinear to Linear Forward model

4.1 Strategie

- scheme image

4.2 local linear Map

4.2.1 Machine learning vs Gaussian elimination