Emergence: A platform for modeling the simultaneous emergence of ecological patterns

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Introduction

The discovery, explanation, and prediction of patterns is foundational to the field of ecology. The study of ecological patterns across the tree of life has inspired ecological theories and paradigms for over a century (e.g., Watson 1859). Given enough time and resources, an army of ecologists could uncover many of these patterns in an environment of sufficient diversity and space. Yet historically, ecologists have focused little on how patterns that are predicted by different theories and explained by different paradigms, or studied within different subfields can emerge within a single system.

Within a given ecological community, one could test the predictions of any number of ecological theories. One could test the allometric predictions of metabolic theory, the growth related predictions of resource limitation theory, trade-offs predicted by life history theory, and the many predictions of commonness and rarity from any number of ecological theories of community ecology, macroecology, and biodiversity. However, the field of ecology has devoted little effort to understanding of how the predictions and patterns from various ecological theories can emerge in the same system. For example, metabolic theory of ecology (MTE) predicts many scaling patterns related to body size, the most powerful of which is the 3/4 scaling of metabolic rate with body size (Brown et al. 2004). However, MTE does not predict intensively studied patterns of commonness and rarity such as the species abundance distribution (SAD) and species-area relationship (SAR). Another general ecological theory, the maximum entropy theory of ecology (METE) predicts the SAD, SAR, and several other patterns of commonness and rarity (Harte 2011). However, despite their generality, METE and MTE do not predict any of the same patterns and use few, if any, of the same variables.

Ecologists have so far, not developed the computational tools to study the predictions of combined ecological theories and the simultaneous emergence of ecological patterns. However, one form of ecological modeling is amenable to this task, individual-based modeling (IBM). IBMs encode rules of how individual particles (e.g., organisms, resource particles) behave according to theories, principles, mechanisms, and processes (e.g., Rosindell et al. 2015). IBMs allow population to ecosystem-level dynamics to emerge over time and space, and provide degrees of ecological realism, individual variability, and spatial complexity that are untenable with other modeling approaches (Grimm and Railsback 2005). IBMs

allow realistic and unanticipated patterns and dynamics to emerge from otherwise simple individual-level interactions and multiple dimensions of ecological complexity (e.g., Locey et al. 2017). Finally, IBMs can allow researchers to track, record, and analyze an immense amount of information. However, ecological IBMs are typically used to examine highly specific questions and often require consider computational complexity (DeAngelis and Gross 1992, Rosindell et al. 2015, Grimm and Raidlsback 2005).

Here, we leverage the power of ecological IBMs with a relatively simple platform that encodes the first principles of several ecological theories. This platform, called 'Emergence', allows the user to run thousands of IBMs to study the simultaneous emergence of no less than 20 ecological patterns. Below, we provide a detailed explanation of how Emergence works, the data it quantifies and tracks, the theories and principles that Emergence integrates, and the analyses and tests that can be conducted using the Emergence source code.

Methods

Platform description

Here, we describe Emergence largely according to the ODD protocol (Overview, Design concepts, Details), which is standard for describing IBMs (Grimm et al. 2006). Emergence, however, is not one IBM intended for use with a specific system. Emergence is distributable software and a platform for simulating unlimited numbers of IBMs and for studying the simultaneous emergence of ecological patterns predicted by multiple theories. A detailed descriptions of Emergence source files, functions, and analysis code can be found on the public GitHub repository (https://github.com/LennonLab/Emergence).

Purpose

Emergence is intended to combine aspects of ecological paradigms and allow the user to study how patterns from each of these paradigms can simultaneously emerge. These paradigms include metabolic scaling, community ecology, life history, neutral theory, resource limitation, and ecological energetics. Emergence accomplishes three proximate objectives. First, Emergence assembles and runs IBMs from random combinations of system variables and species traits. Second, Emergence stores the outputs of IBMs including animations. Third, Emergence provides R and python code for analyzing simulation data.

Entities & their state variables

Individual organisms – Emergence simulates life history processes of growth, dispersal, reproduction, and basal respiration at the individual level. Individuals are distinguished by collections of elements within dictionaries, i.e., data objects

that hold key-value pairs. For example, the dictionary holding information on individual organisms is structured as follows:

where 'ind1' is the key and the variables following the colon are the values for the species ID, x-coordinate, y-coordinate, body size, amount of endogenous resources, and metabolic state (active or dormant). Individuals undergo changes when randomly sampled from the dictionary.

Species – Each species is characterized by the individuals that share a common set of traits, such as maximum growth rate, metabolic maintenance cost. Species information is stored in dictionaries, again as key-value pairs.

where the species with ID of '1' has an intrinsic growth rate of 0.8, an active dispersal rate of 0.5, a 0.3 probability of randomly resuscitating from a metabolically dormant state, a basal mass specific metabolic rate of 0.2, and resource specific use efficiencies of 0.1, 0.2, and 0.3.

When sampling individuals, the information about their species is gained by accessing the species dictionary.

Resource particles – Emergence simulates the movement and consumption of individual resource particles. These particles can vary over several orders of magnitude in size and belong to three resource types. As with individual organisms and species, information about individual resource particles is stored in dictionaries.

where 't' is the resource type, 'v' is the size of the particle, and 'x' and 'y' are the x and y coordinates.

System level state variables

Each Emergence model begins with random choices for the values of:

- width in arbitrary units
- height in arbitrary units
- flow through rate in units of distance moved per time step by the environmental matrix; a minimum of 0.

Spatial and temporal scales

Spatial extent – The environment of Emergence is square and two dimensional, and can vary along each axis from 1 to any number of arbitrary units. All particles move in decimal units, the limit of which is determined by Python's decimal precision. This means that individual particles can occupy practically infinite locations.

Temporal extent – Emergence models can run for any number of time steps and record data at any number of time steps.

Process overview and scheduling

Model assembly – The Emergence user runs the main python program (i.e., main.py). The main program chooses random values for system-level state variables including whether disturbance, immigration, speciation, fluid dynamics, etc. will occur and at what rates. The main program also imports modules (i.e., groups of functions) for diversity metrics, spatial analysis, the initiation of output files, and for simulating life history processes (immigration, maintenance, death, growth, consumption, disturbance, passive dispersal, active dispersal, resource flow, resource inflow, and metabolic state transitions).

Simulating life history – Emergence models begin simulation immediately after assembly. The order of life history processes is randomized at each time step to prevent scheduling bias.

Immigration: By default, individuals enter at any point in the environment. This can can be adjusted in the 'bide.py' file. Species identities of inflowing propagules are chosen at random from a uniform distribution rather than an ecologically realistic source pool (e.g., log-series or lognormal distribution). The reason for this is two-fold. First, pulling immigrants from a uniform distribution maximizes the starting diversity of each model. Second, beginning with a uniform distribution allows more realistic distributions of species abundances to emerge.

Dispersal: Active dispersal: Individuals can actively move against a force of flow, at random, or in specified directions. Preferences for particular modes of active dispersal can be specified or modified in the 'active_dispersal.py' file. Passive dispersal: Individuals can be moved passively (e.g., as planktonic organisms) through the system at rates determined by the rate of flow through. or by the combination of flow rate and active dispersal.

Consumption: Sampled individuals increase their levels of endogenous resources by feeding on resource particles. These endogenous resources (a.k.a. cell quotas) can be used to add structural biomass and to pay the energetic costs of life history processes. Individual consume resources according to their species specific consumption rates for three resource types. The number of simulated resource types can be changes in the source code files (consume.py, immigration.py, and resource_inflow.py). The simulation of consumption can be modified in the 'consume.py' file.

Growth: Sampled individuals grow in size by integrating endogenous resources as structural biomass. Individuals grow according to species specific rates of growth ranging between 0.1% and 100% increase in size per time step. Individuals' endogenous resources are decreased in direct proportion.

Reproduction: Individuals reproduce clonally with a probability determined by their endogenous resources. The endogenous resources of the mother individual is evenly divided between two daughter individuals. Unless in the case of speciation, the daughters are given a unique individual ID and the species ID of the mother.

Speciation: Speciation is simulated within Emergence as a discrete event, i.e., where clonal reproduction produces a new species. Speciation is accompanied by mutations in the values of one or more species traits. This approach allows for diversity to arise within the system, which the environment can then select on.

Death: Individuals sampled at random will die if their levels of endogenous resources or ability to draw resources from structural biomass falls below the minimum metabolic requirements. Dead individuals are removed from the system, i.e., scavenging and recycling do not currently occur in Emergence.

Emigration: Individuals are considered to have emigrated when they pass beyond edges of the environment. That is, individuals do not reenter.

Simulating resource processes

Supply/inflow: Resource particles can be allowed to enter at any point in the environment, which can be adjusted in the 'bide.py' file. The size and type of each inflowing resource particle is chosen at random from a uniform distribution, and can be modified in the same 'bide.py' file.

Resource dispersal: Resource particles can be moved passively through the system at rates determined by the rate of flow through. Resource dispersal can be turned off in the 'main.py' file.

Resource depletion: Resource particles are depleted through consumption, which can be partial or complete.

Design concepts

Basic principles Ecological selection on random variation: Emergence operates according to a basic principle of evolution, i.e., natural selection on random variation. Emergence assembles models from random combinations of system-level, species-level, and individual-level variables. Emergence then allows the environmental characteristics (e.g., flow rate, resource supply, spatial extent) to select on these random trait combinations.

Energy-limited life history: Emergence imposes energetic costs to growth and activity. These energetic costs are directly proportional to life history parameters. For example, the energetic cost of dispersal is the product of dispersal rate and dispersal distance. This intuitively means that the energetic cost of dispersal is multiplied (or compounded) across distance such that moving a distance of x in a specific direction requires half the energy as moving a distance of x in the same direction. In the same way, growing at a rate of x is half as costly as growing at a rate of x.

Lognormal dynamics: Multiplicative interactions of random variables underpin one of the most successful models of complex systems, i.e., the lognormal (Crow et al. 1988). The lognormal was introduced to ecologists by Preston (1962) as a description of how abundance varies among species. The lognormal has been one of the two most successful models of species abundance for macroscopic plants and animals, and was recently used to form a macroecological theory of microbial diversity (Shoemaker et al. 2017). By "multiplicative interactions" one simply means that two or more variables interact in a multiplicative or synergistic way. Such interactions are common in ecology and include population growth and energetic costs multiplied across distance and time (Putnam 1993). By "random variables" one simply means two independent processes or constraints with degrees of stochastic change. Emergence explicitly simulates lognormal dynamics. For example, energetic costs are multiplied across dispersal distance and magnitudes of growth and the frequency of transition between metabolic states. These energetic costs are determined by the values of randomly chosen species traits (i.e., random variables).

Simultaneous emergence: A popular advantage of IBMs is the potential to study the emergence of complex patterns from the individual level. Emergence is aimed at allowing emergence in three ways that IBMs are rarely employed. First, Emergence allows patterns to emerge from random combinations of traits and state variables. This allows realistic trait syndromes and patterns to emerge without being forced. Second, Emergence allows several orders of magnitude in random variation of starting conditions and species traits. This highly unconstrained approach allows the user of Emergence to explore a broad spectrum of trait combinations and ecological solutions. Third, Emergence allows for the

study of simultaneous emergence across a practically unlimited number of IBMs. In this way, Emergence initiates with unrealistic ecological communities and unrealistic combinations of species traits, and then allows for realism to develop over time in response to environmental conditions and according to energetic costs. This approach allows the user of Emergence to avoid one of the greatest challenges to ecological modeling, i.e., the circularity of documenting outcomes that are obviously forced to occur. The code made available for the analysis of Emergence data is intended to examine the variation and central limiting behavior of ecological patterns among thousands of models.

Other design concepts *Hypotheses*: These are entirely up to the user to formulate and test according to the capabilities and analytical tools of Emergence source code.

Learning: Currently, there is no aspect of individual-based learning in Emergence.

Prediction: Individuals in Emergence do not have the ability to anticipate conditions.

Sensing: Individuals can sense and move towards resource particles.

Interaction: Individuals interact through excluding each other from resources, i.e., preemption. There is no explicit communication.

Observation: An unlimited number of Emergence models can be run to examine trends and variation in ecological patterns.

Output data

Emergence generates three files of output data. Each Emergence model quantifies and writes output data for every n^{th} time step, where n can be designated by the user. The three are:

SimData.csv – Each column of this file corresponds to a piece of data about the system that was modeled (e.g., flow rate, total abundance, species richness, species turnover, resource supply and diversity, rate of disturbance, etc.). Most analyses in Emergence source code are conducted on the data in this file. The following is recorded for each Emergence model and stored in SimData.csv:

- Values of randomly chosen input variables
 - length
 - width
 - flow rate
 - maximum resource particle size
 - maximum number of inflowing resource particles
 - number of inflowing resource types
 - initial community size

- Total individual abundance (N) of the dormant and active fractions of ecological communities
- Species richness (S) of the dormant and active fractions of ecological communities
- Mean abundance-weighted specific growth rate for the dormant and active fractions of ecological communities
- Mean abundance-weighted species-specific dispersal rate for the dormant and active fractions of ecological communities
- Mean abundance-weighted species-specific resource consumption rates for the dormant and active fractions of ecological communities
- Mean abundance-weighted species-specific rate of random metabolic state transitions (dormant to active) for the dormant and active fractions of ecological communities
- Mean abundance-weighted species-specific rate of decrease in basal metabolic rate accomplished by transitioning to a dormant state, for the dormant and active fractions of ecological communities
- Species turnover
 - Whittaker's β
- Species evenness
 - Smith and Wilson's evenness, E_{var}
 - Simpson's evenness, $E_{1/D}$
- Species diversity
 - Shannon's diversity, H'
 - Simpson's diversity, $D_{1/D}$
- Dominance
 - Absolute, N_{max}
 - Relative, N_{max}/N
- Productivity of
 - Individuals
 - Biomass

SAR.csv – A file holding species-area relationships (SARs) from Emergence models. SARs quantify the rate at which species are encountered with increasing area of a sample, study, landscape, etc. The SAR is among the most intensively and long-studied patterns in ecology and is one of two patterns commonly predicted by biodiversity theories (Lomolino 2000, Hubbell 2001, Harte 2011).

RADs.csv – A file holding rank-abundance distributions (RADs) from Emergence models. Also referred to as species-abundance distributions (SADs), rank-abundance curves (RACs), and Whittaker plots, RADs are vectors of the abundances of species in a community. Along with the SAR, RADs are one of the most intensively studied and commonly predicted ecological patterns (Hubbell 2001, McGill et al. 2007, Harte 2011).

Patterns generated by Emergence

Emergence includes python code to analyze the simultaneous emergence of ecological patterns.

Species abundance distribution (SAD) The SAD is the vector of species abundance in an ecological community and is one of ecology's fundamental patterns of commonness and rarity. SAD's almost universally reflect that few species in ecological communities are highly abundant while most species are relatively rare (McGill *et al.* 2007). The SAD is predicted by more than 20 ecological models, the two most successful of which are the Poisson-lognormal and the log-series distributions (White et al. 2012, Baldridge et al. 2015, Shoemaker et al. 2017).

Species-area relationship (SAR) Also referred to as the species-area curve, the SAR describes the rate at which increasing numbers of species are observed with increasing area, and is also one of ecology's most intensively studied patterns (Lomolino 2000, Rosenzweig 2000). There four basic types of SARs pertaining to types of biotas and four general sampling schemes (Rosensweig 2000). Here, we consider SARs for single biotas (i.e., not crossing ecoregions or biogeographical provinces) and generate them using two sampling schemes (i.e., nested design, random aggregation of subplots).

Metabolic scaling The scaling of basal metabolic rate (B) with body size (M) is one of the strongest patterns of ecology (Brown et al. 2004). Taking the form $B \propto B_0 * M^z$, the scaling exponent z is most often observed to approach 3/4. However, this scaling exponent has long been argued to be closer to 2/3 and in some cases can approach 1.0 (Glazier 2006). The metabolic theory of ecology (MTE) predicts that z = 3/4 and, from this, predicts several other relationships that scale to quarter powers of body size. These include a -1/4 scaling of mass-specific metabolic rate and a -3/4 scaling of population density.

Diversity-abundance scaling relationships Aspects of species-level diversity have been shown to scale with the total abundance (N) of individuals in a sample at rates that are often similar for microorganisms and macroscopic plants and animals (Locey and Lennon 2016). These aspects include:

- Richness (S); the number of species in a community.
- Rarity; the concentration of species at low abundances can be quantified as the a measure of the skewness of the histogram of species abundances.
- Absolute dominance (N_{max}) ; the greatest species abundance.
- Evenness (E); the variation in abundance among species and often quantified as a transformation or reflection of the sample variance.

Taylor's Law The variance (σ^2) in population abundance often scales with the average population abundance (N/S) across space and through time at a rate between 1 and 2, i.e., $\sigma^2 = (N/S)^{1 < z < 2}$. Named after Taylor (1961), Taylor's Law is observed in many ecological and non-ecological systems. In ecology, the scaling exponent of this relationship is sometimes as high as 3 (ref).

Results

Species abundance distribution (SAD) Despite the IBMs being initialized with random samples from uniform distributions, the resulting SADs of Emergence are well-fit by the Poisson-lognormal and the log-series distributions (Fig 1).

Figure 1. Species abundance distributions for 1,000 Emergence models are well-explained by species abundance models. Kernel density curves of r-square values for the Poisson lognormal (PLN) distribution and the log-series predicted by the Maximum Entropy Theory of Ecology (METE). As commonly observed in ecological communities, both models predicted >75% variation in abundance among species.

Species-area relationship (SAR) Emergence produced realistic forms of the SAR according to several sampling schemes (Fig 2).

Figure 2. Species-area relationships from 1,000 Emergence models take realistic forms. Kernel density curves of slopes (z-values) of the species-area relationship (SAR) for both two sampling schemes, i.e., nested and random aggregation (R.A.)

Metabolic scaling Emergence closely reproduced the 3/4 power scaling of basal metabolic rate to body size, the -1/4 power scaling of mass-specific basal metabolic rate to body size, and the -3/4 scaling of population density to body size (Fig 3).

Figure 3. Patterns of metabolic scaling produced by 1,000 Emergence models. Each blue data point represent the mean for values across a binned x-axis, to prevent statistical bias due to the large number of data points of intermediate body sizes. The dashed blue line is the regression line and the light blue hull is the 95% prediction interval.

Diversity-abundance relationships Emergence closely reproduced diversity-abundance scaling relationships (Fig 4). The relationships for rarity, dominance, and evenness are close to the overall results from Locey and Lennon (2016). The relationship of richness to total abundance was similar to that for some microbial and animal datasets analyzed by Locey and Lennon (2016).

Figure 4. Diversity-abundance scaling relationships produced by 1,000 Emergence models are similar to those reported by Locey and Lennon (2016). Each blue data point represents the mean for values across a binned x-axis. This prevents statistical bias due to the large number of data points of high total abundance (N). The dashed blue line is the regression line and the light blue hull is the 95% prediction interval.

Taylor's Law Emergence reproduced Taylor's Law, with the scaling exponent just below 2.0 (Fig 5).

Figure 5. The population abundance variance-mean relationship from 1,000 Emergence models closely reproduces Taylor's Law.

Discussion

The Emergence platform allows patterns from different ecological paradigms to emerge simultaneously across thousands of individual-based models (IBMs). In doing so, primary patterns of community ecology, macroecology, metabolic theory, and biodiversity science all emerge from individual-level changes, relatively few explicit constraints, and selection on initially random variation.

The degree of emergence in Emergence is unique and difficult to fully appreciate. For example, realistically uneven SADs resulted from initially even SADs where almost every individual belonged to a different species. This starting condition is contrary to the criticism that all successful theories of biodiversity begin with the assumption that the SAD is a hollow-curve (McGill 2010). Additionally, the 3/4 scaling of metabolic rate to body size emerged despite the lack of any explicit constraints on body size and without enforcing any power-law mechanism. Likewise, realistic SARs emerged despite no hard constraints on area and realistic diversity-abundance scaling relationships emerged despite no hard constraints on total abundance. Finally, all of these patterns simultaneously emerged across thousands of IBMs.

The benefits of the Emergence platform are manifold. First, Emergence allows exploration of novel questions and patterns while ensuring realistic ecological structure and dynamics. Second, Emergence implicitly unifies major ecological patterns under three general mechanisms: lognormal dynamics (i.e., multiplicative interactions of stochastic variables), energetic constraints, ecological selection. To our knowledge, the entire set of patterns produced by Emergence have never been predicted by any single ecological theory, nor by any synthesis of theories. Third, many other ecological patterns could also be produced by the Emergence platform, as is. Examples are distance decay relationships, growth curves, spatial abundance distributions, body-size distributions, and speciestime relationships. Fourth, with additional modifications Emergence could produce countless other ecological patterns or even patterns that transcend biological fields, i.e., by simulating evolutionary processes, landscape dynamics, and by attributing genome sequences to individuals.

To our knowledge, Emergence offers the first IBM approach for testing metabolic scaling theory (Brown et al. 2004). Metabolic scaling predicts that the magnitude of basal metabolic rate (B) increases with the $^3/_4$ power of body mass (M), i.e., $B = M^{3/4}$. Studies have used the $^3/_4$ scaling law to predict aspects of metabolic power, population dynamics, community ecology, ecosystem function, and trophic interactions (Brown et al. 2004, Hechinger et al. 2011, Schramski et al. 2015). The reasoning behind the $^3/_4$ power rests on fractal geometry of tissues (West et al. 1997, West et al. 1999). While this fractal-based reasoning may hold, we not aware of any mechanistic tests, and it remains unresolved whether the argument is necessary. In Emergence, there are no such networks and the $^3/_4$ power law appears to emerge as a central tendency.

Emergence is well-positioned for testing the predictions of metabolic scaling.

Some scientists still argue whether a $^2/_3$ scaling based on surface area to volume ratios is more accurate and appropriate (White and Seymour 2003) and even whether a $^3/_4$ and $^2/_3$ scaling can arise from the same mechanism (Zhao 2015). Finally, some have shown that the scaling of metabolic rate to body size is nearly isometric (z=1) for some taxa (Glazier 2006). While Emergence most often produces a scaling exponent near $^3/_4$, it can produce each of these alternative outcomes by varying the constraints on the range of initial conditions of basal metabolic rate, resource inputs, and resource use efficiency.

Emergence is unique in several ways. First, Emergence is built to study the simultaneous emergence of ecological patterns across paradigms. Second, patterns in Emergence emerge as a consequence of ecological selection on initially random conditions. Third, patterns of Emergence emerge as robust central tendencies across hundreds to thousands of independent IBMs. Fourth, Emergence is agnostic in that it does not place primary importance on stochasticity, ecological selection, or energetic constraints, and does not place any explicit constraints on body size and life history trade-offs. Instead, we designed Emergence with relatively few rules to allow all patterns to emerge from conditions that would have been difficult to anticipate from examining the source code. Finally, Emergence can be freely distributed and modified, and will continue growing to give individuals evolvable genome sequences and to include new ecological dynamics (e.g., predator-prey, mutualism, parasitism) and the aspects of mass balance, stoichiometry, biocomplexity included in sister platforms (i.e., Locey et al. 2017).

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