## Statistical analysis

## 1 Project Summary

#### Collaborators

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### Project questions

- 1. Does resource stoichiometry affect the growth rate of Synechococcus?
- 2. How does resource stoichiometry alter ecological dynamics?
- 3. Does stoichiometry alter phenotypic (co)evolution in cyanobacteria and phage?

#### Data collection

Briefly, all data for this project was collected during a long term continuous culture experimental evolution study with *Synechococcus* and SRIM-8 cyanomyophage.

For a complete description of the materials and methods for this repository, see Larsen et al. 2016.

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# 2 Physiological growth: Does nutrient stoichiometry affect the growth rate of *Synechococcus*?

Overview: In this experiment, we tested for growth enhancement with the addition of N or P to our stoichiometrically amended AN media (Lennon *et al.* 2007; see Larsen *et al.* 2016 Table S1).

### 2.1 Summary of Major Results

1. Addition of N or P to our N-limited or P-limited media increased *Synechococcus* in comparison to the control treatment (Figure 1, Table 1).

#### \*Analysis Notes:\*

- 1. Population growth curve data was collected on a Biotek Synergy Mx instrument loaded with softward version 2.01.12.
- 2. Growth rate calculations were completed using lab generated code for bacterial growth rate analysis for the above instrument and can be found at http://github.com/LennonLab/Growth\_Curves.

## ${\bf 2.2}\quad Synechococcus \ {\bf growth} \ {\bf rates} \ {\bf with} \ {\bf response} \ {\bf to} \ {\bf nutrient} \ {\bf addition}$

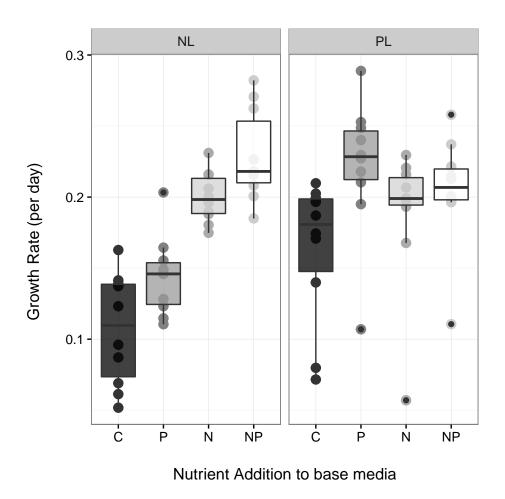


Figure 1: Nitrogen (N), phosphorus (P), or NP addition to the base N-limited and P-limited media used in the chemostat experiment. Culture controls (C) did not contain additional N or P.

### 2.2.1 Growth rate ANOVA tables

#### N-limited

Table 1: ANOVA table for NL nutrient addition

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
med.add	3	0.08993	0.02998	33.3	1.743e-10
Residuals	36	0.0324	0.0009001	NA	NA

Table 2: Posthoc comparisons using Tukey HSD

	diff	lwr	upr	p adj
N-C	0.0929	0.05677	0.129	2.426e-07
NP-C	0.1218	0.0857	0.158	$4.542\mathrm{e}\text{-}10$
P-C	0.03716	0.001027	0.0733	0.04188
NP-N	0.02893	-0.007204	0.06507	0.1551
P-N	-0.05574	-0.09188	-0.01961	0.001056
P-NP	-0.08467	-0.1208	-0.04854	1.564 e-06

### P-limited

Table 3: ANOVA table for PL nutrient addition

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
med.add	3	0.01865	0.006215	2.845	0.05117
Residuals	36	0.07864	0.002184	NA	NA

Table 4: Posthoc comparisons using Tukey HSD

	diff	lwr	upr	p adj
N-C	0.02548	-0.03081	0.08178	0.619
NP-C	0.04166	-0.01463	0.09796	0.2094
P-C	0.05857	0.002277	0.1149	0.03881
NP-N	0.01618	-0.04011	0.07247	0.8656
P-N	0.03309	-0.02321	0.08938	0.4008
P-NP	0.01691	-0.03939	0.0732	0.8498

## 2.3 Percent Change in Growth

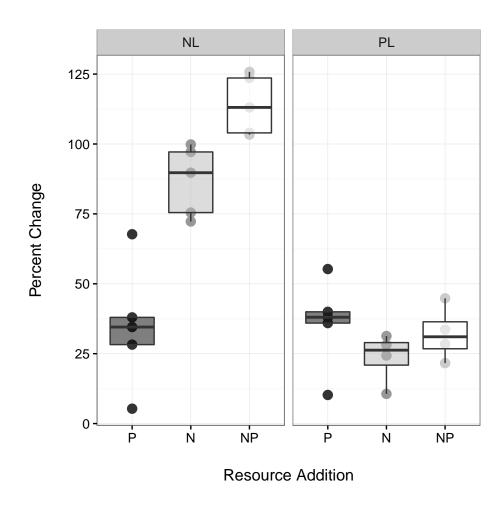


Figure 2: Percent change in growth rate between control and nutrient additions (N, P, or NP) cultures. NL = N-limited; PL = P-limited

### 2.3.1 Growth rate ANOVA tables

#### N-limited

Table 5: ANOVA table for NL nutrient addition

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
med.add	2	16206	8103	31.59	1.653e-05
Residuals	12	3078	256.5	NA	NA

Table 6: Posthoc comparisons using Tukey HSD

	diff	lwr	upr	p adj
NP-N	27.06	0.03951	54.08	0.04966
P-N	-52.14	-79.16	-25.12	0.0006541
P-NP	-79.2	-106.2	-52.18	$1.316\mathrm{e}\text{-}05$

### P-limited

Table 7: ANOVA table for PL nutrient addition

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
med.add Residuals	2 10	$343.4 \\ 1592$	171.7 $159.2$	1.079 NA	0.3765 NA

Table 8: Posthoc comparisons using Tukey HSD

	diff	lwr	upr	p adj
NP-N	8.522	-15.93	32.98	0.6197
P-N	12.29	-10.91	35.49	0.3532
P-NP	3.764	-19.44	26.96	0.8978

# 3 Population Dynamics: Does nutrient stoichiometry affect temporal dynamics?

Overview: In this experiment, whole samples were collected from each chemostat system three times per week for ~5 months. Each sample was processed, stained, and counted using epi-fluorescence on a Zeiss microscope and quantified using Axiovision software. Statistics for these data include repeated measures anova (RMANOVA), stability (1/CV), and cross-correlation analyses on whitened data.

### 3.1 Summary of Major Results

- 1. Stoichiometry significantly affected Synechococcus and phage densities. RMANOVA
- 2. Altered mean and stability of the populations
- 3. Modified the temporal coherence, or synchrony, of the *Synechococcus*-phage dynamics, suggesting ecological ramifications of stoichiometry.

### 3.2 Chemostat-level comparisons

### 3.2.1 Population dynamics

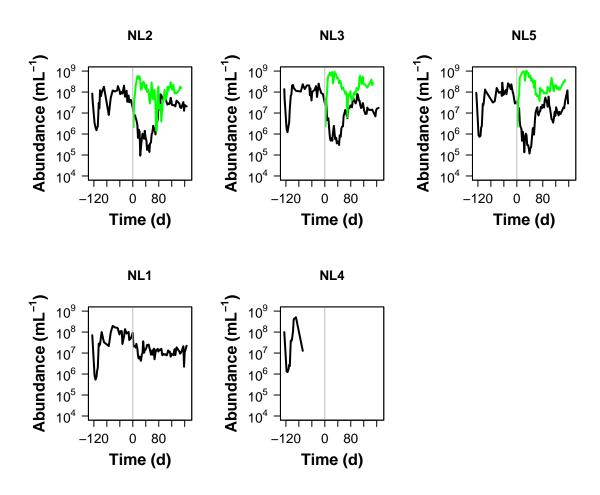


Figure 3: N-Limited Chemostats

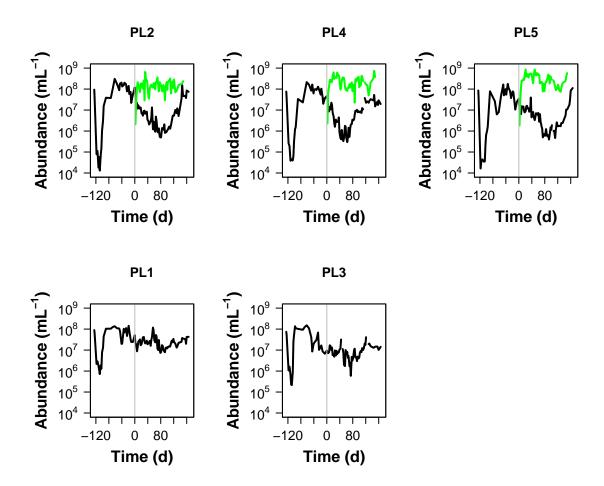
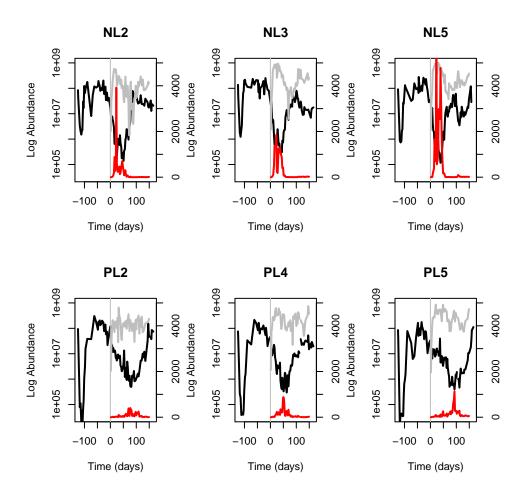


Figure 4: P-Limited Chemostats

### 3.2.2 Phage to bacteria ratio



### 3.3 Treatment-level comparisons

### 3.3.1 Controls

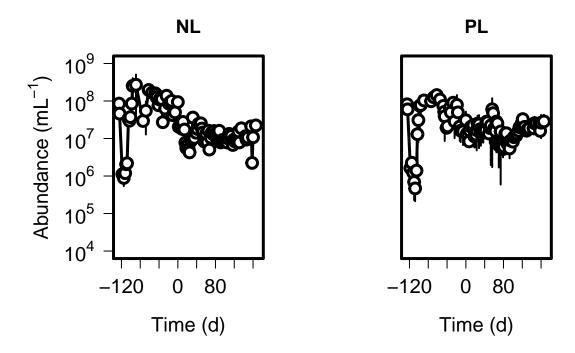


Figure 5: Control Chemostats

### 3.3.2 Treatment (i.e. Exposed) population abundances

RMANOVA for control cyanobacteria

RMANOVA for control vs exposed cyanobacteria densities

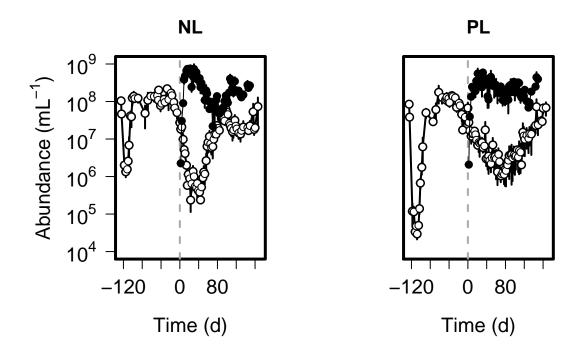
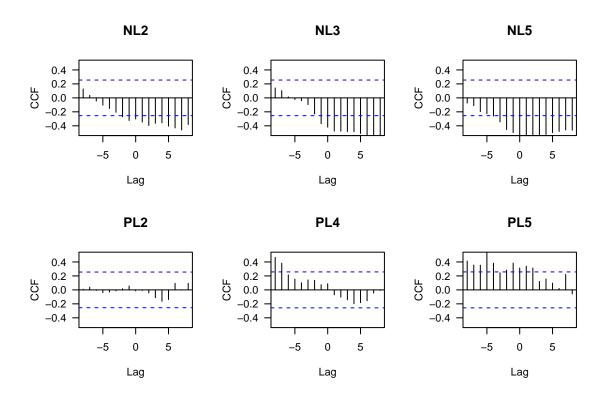


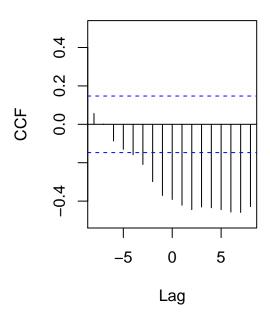
Figure 6: Treatment Chemostats

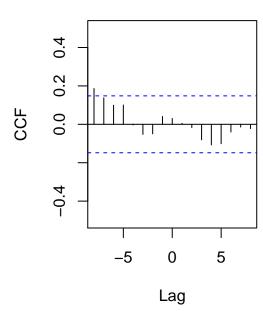
### 3.3.3 Temporal autocorrelation





## P-limited

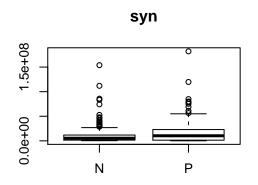


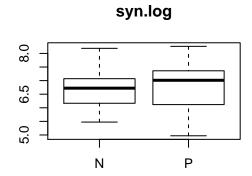


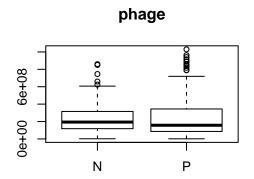
## 3.4 Statistical analyses

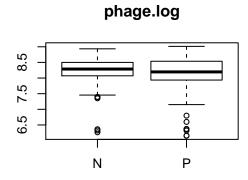
 $NOTE \hbox{:} Cross\hbox{-} correlation$  analyses and RMANOVA were also completed in SAS

## 3.4.1 Heteroskedaskicity (i.e skewness) with treatment data only









## 3.4.2 Reapeated Measures ANOVA (RMANOVA)

	numDF	denDF	F-value	p-value
(Intercept)	1	230	14010	0
$\lim$	1	4	0.3592	0.5812
day.fac	58	230	10.22	0
lim:day.fac	58	230	2.588	2.771e-07

```
numDF denDF F-value p-value
##
## (Intercept)
                     245 987.2110 <.0001
                 1
                           0.1869 0.6878
## lim
                 1
## day.fac
                 62
                      245
                           3.3834 <.0001
## lim:day.fac
                 62
                     245
                           2.4368 <.0001
```

	${\rm numDF}$	denDF	F-value	p-value
(Intercept)	1	245	12432	0
$\lim$	1	4	0.5225	0.5098
day.fac	62	245	3.354	1.14e-11
lim:day.fac	62	245	2.437	6.993 e-07

## 3.4.3 Despcriptive statistics

lim	$\operatorname{cID}$	microbe	mean	var	sem
N	NL2	Phage	151575375	1.881e + 16	79190498
N	NL3	Phage	292205382	6.38e + 16	145831435
N	NL5	Phage	312565642	7.765e + 16	160881119
P	PL2	Phage	161267374	1.047e + 16	59073946
P	PL4	Phage	243403403	2.342e + 16	88361764
Ρ	PL5	Phage	312523940	$3.66e{+}16$	110450827
N	NL2	$\operatorname{Syn}$	17594096	4.371e + 14	12070003
N	NL3	$\operatorname{Syn}$	16110168	3.023e + 14	10039048
N	NL5	$\operatorname{Syn}$	16985817	8.152e + 14	16484799
P	PL2	$\operatorname{Syn}$	12944893	6.116e + 14	14277915
P	PL4	$\operatorname{Syn}$	10812795	1.329e + 14	6655700
Р	PL5	$\operatorname{Syn}$	9399556	$3.232e{+14}$	10380093

Limitation	Treatment	Synechococcus mean densitiy (+/- SEM)	Synechococcus mean stability	Phage mean density (+/- SEM)	Phage mean stability
N	Control	1.3e+07(4e+06)	2.1	NaN(NA)	NA
N	Infect	1.7e + 07(1e + 07)	0.75	2.5e + 08(1.4e + 08)	1
P	Control	1.8e + 07(9e + 06)	1.1	NaN(NA)	NA
P	Infect	1.1e+07(1e+07)	0.59	2.4e + 08(9.5e + 07)	1.5

Chemostat	Treatment	Synechococcus mean densitiy (+/- SEM)	Synechococcus mean stability	Phage mean density (+/- SEM)	Phage mean stability
NL1	Control	1.3e + 07(4e + 06)	2.1	NaN(NA)	NA
NL2	Infect	1.8e + 07(1e + 07)	0.84	1.5e + 08(7.9e + 07)	1.1
NL3	Infect	1.6e + 07(1e + 07)	0.93	2.9e+08(1.5e+08)	1.2
NL5	Infect	1.7e + 07(2e + 07)	0.59	3.1e+08(1.6e+08)	1.1
PL1	Control	2.5e + 07(1e + 07)	1.4	NaN(NA)	NA
PL2	Infect	1.3e + 07(1e + 07)	0.52	1.6e + 08(5.9e + 07)	1.6
PL3	Control	9864044(4e+06)	1.4	NaN(NA)	NA
PL4	Infect	1.1e + 07(7e + 06)	0.94	2.4e + 08(8.8e + 07)	1.6
PL5	Infect	9399556(1e+07)	0.52	3.1e+08(1.1e+08)	1.6

## 3.4.4 Topographic statistics

Table 14: Table continues below

lim	cID	microbe	mean	var	sem	stab	start.abd
N	NL2	Phage	151575375	1.881e+16	79190498	1.105	2102121
N	NL3	Phage	292205382	6.38e + 16	145831435	1.157	2362910
N	NL5	Phage	312565642	7.765e + 16	160881119	1.122	2299688
P	PL2	Phage	161267374	1.047e + 16	59073946	1.576	2102121
P	PL4	Phage	243403403	2.342e + 16	88361764	1.59	2299688
Ρ	PL5	Phage	312523940	$3.66e{+}16$	110450827	1.634	1841331
N	NL2	$\operatorname{Syn}$	17594096	$4.371e{+14}$	12070003	0.8416	9599786
N	NL3	$\operatorname{Syn}$	16110168	$3.023e{+}14$	10039048	0.9265	22353787
N	NL5	$\operatorname{Syn}$	16985817	$8.152e{+14}$	16484799	0.5949	23186422
P	PL2	$\operatorname{Syn}$	12944893	6.116e + 14	14277915	0.5234	42190080
P	PL4	$\operatorname{Syn}$	10812795	$1.329e{+14}$	6655700	0.938	31571541
Р	PL5	$\operatorname{Syn}$	9399556	$3.232e{+14}$	10380093	0.5228	9874066

final.abd	min.day	min.abd	max.day	max.abd
157137459	72	1422488	16	573074216
261895765	2	2362910	30	940323547
378381691	2	2299688	30	1.029e+09
237940680	2	2102121	32	659870095
378302664	2	2299688	146	7.46e + 08
5.74e + 08	2	1841331	21	859404750
20629744	23	93339	98	84902597
17710626	44	300299	100	80035767
1.82e + 08	39	117089	166	1.82e + 08
74192632	79	496642	146	153895345
19439567	63	297912	146	52700866
111891383	93	393297	166	111891383

microbe	analysis	df	pvalue
syn	mean	2.68	0.01793
$\operatorname{syn}$	stability	3.63	0.5036
$_{ m phage}$	mean	3.92	0.855
$_{\mathrm{phage}}$	stability	3.94	4e-05

#### 3.4.5 Temporal Synchrony

# 4 Infection Dynamics: Does stoichiometry alter phenotypic (co)evolution in cyanobacteria and phage?

Overview: To examine how nutrient stoichiometry impact evolutionary interactions, I collected cross-infectivity data from 96 phage and  $\sim 200$  Synechococcus strains. Each challenge was recorded based on cellular growth where lysis = 1 (i.e. infectious interaction occured) or no lysis (i.e. no evidence of infection; cell line is resistant). This data was incorporated into network-based metrics.

### 4.1 Summary of Major Results

- 1. Are temporal infection dynamics affected by stoichiometry?
- 2. Do community infection networks change as a result of the environment?
- 3. How are the dynamics affected? Through changes in overall resistance/infectivity? Changes in compositional resistance?

## 4.2 Degree of interaction

## 4.3 RMANOVA

	AIC	BIC	logLik	L.Ratio	p-value
model.ar	254.3	329	-108.2	NA	NA
model.arma1	233.7	312.3	-96.86	22.59	2.003e-06
${f model.arma2}$	225.7	308.2	-91.84	10.05	0.001523

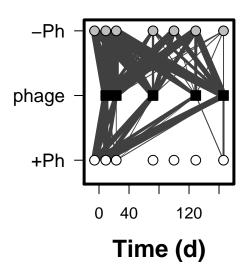
	Std.Error	t-value	p-value
(Intercept)	0.08346	9.123	4.674e-18
$\mathbf{trtT}$	0.1136	-2.871	0.004325
$\lim P$	0.1155	-3.857	0.01819
phage.time	0.0006714	-1.743	0.08219
bac.time	0.001086	0.0845	0.9327
trtT:limP	0.1588	1.295	0.196
trtT:phage.time	0.0009219	0.7362	0.4621
limP:phage.time	0.0009172	2.812	0.005188
trtT:bac.time	0.001379	-2.373	0.01815
limP:bac.time	0.001367	-0.06095	0.9514
phage.time:bac.time	9.204 e-06	-1.641	0.1016
trtT:limP:phage.time	0.001273	-0.6152	0.5388
trtT:limP:bac.time	0.001816	1.275	0.2029
trtT:phage.time:bac.time	1.15e-05	1.662	0.09738
limP:phage.time:bac.time	1.145e-05	0.3174	0.7511
trtT:limP:phage.time:bac.time	1.498e-05	-1.448	0.1484

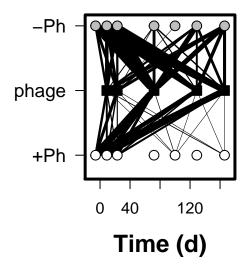
4.4 Infection dynamics by chemostat

## 4.5 Infection dynamics by treatment

## 4.5.1 Network plots

##		[,1]		[,3]		[,5]		[,7]			[,10]		[,12]	[,13]
##	[1,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[2,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[3,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[4,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[5,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[6,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[7,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[8,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[9,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[10,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[11,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[12,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[13,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[14,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[15,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[16,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[17,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[18,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	[19,]	0	0	0	0	0	0	0	0	0	0	0	0	0
##	5. 3	[,14]				,17]		[,19]						
##	[1,]	C			0	0	0	(						
##	[2,]	C			0	0	0	(						
##	[3,]	C			0	0	0	(						
##	[4,]	C			0	0	0	(						
##	[5,]	C			0	0	0	(						
##	[6,]	C			0	0	0	(						
##	[7,]	C			0	0	0	(						
##	[8,]	C			0	0	0	(						
##	[9,]	C			0	0	0	(						
##	[10,]	C			0	0	0	(						
##	[11,]	C			0	0	0	(						
##	[12,]	C			0	0	0	(						
##	[13,]	C			0	0	0	(						
##	[14,] [15,]	C			0	0	0	(						
##	-	C				0								
## ##	[16,] [17,]	C			0 0	0	0	(						
##	[18,]	C			0	0	0							
##	[19,]	C			0	0	0	(						
##	[19,]	C	,	,	U	U	U	(	,					





## null device
## 1

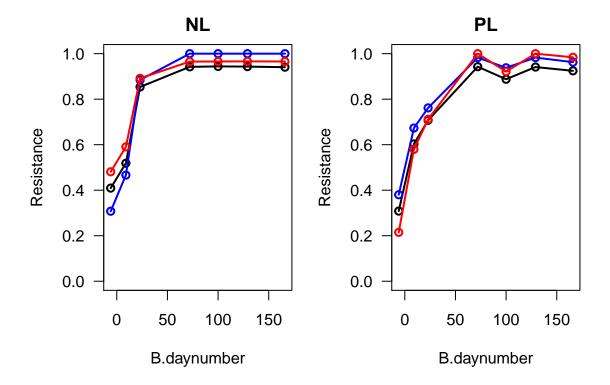
4.6 Community Networks

## 4.7 BiWeb estimates for nestedness and modularity

	statistic.t	parameter.df	p.value
connectance	1.456400410208	3.89610299683149	0.220826873899216
modularity.qb	-3.5488938188692	3.00184431086153	0.0380832752236465
modularity.qr	-0.337865126206578	3.62274149633006	0.754122338605035
$\operatorname{nodf}$	0.371973397721244	3.80924523421393	0.729674513225951
$\mathbf{ntc}$	-0.848020202172062	3.96441380258424	0.444591439999469

## 4.8 Synechococcus resistance

## 4.8.1 global; sympatric vs. allopatric resistance



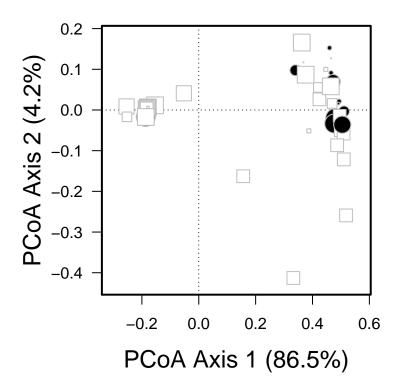
##		${\tt numDF}$	${\tt denDF}$	F-value	p-value
##	(Intercept)	1	97	43.84393	<.0001
##	B.trt	1	4	1.45906	0.2936
##	B.daynumber	6	97	14.27125	<.0001
##	B.trt:B.daynumber	6	97	0.51041	0.7992

	numDF	denDF	F-value	p-value
(Intercept)	1	97	2184	0
$\mathbf{B.trt}$	1	4	0.05589	0.8247
B.daynumber	6	97	31.82	0
B.trt:B.daynumber	6	97	0.5104	0.7992

	${\rm numDF}$	denDF	F-value	p-value
(Intercept)	1	97	1645	0
${f B.trt}$	1	4	1.962	0.2339
B.daynumber	6	97	27.78	0
B.trt:B.daynumber	6	97	0.7992	0.5729

	numDF	denDF	F-value	p-value
	$\operatorname{numDF}$	denDF	F-value	p-value
(Intercept)	1	97	2394	0
${f B.trt}$	1	4	0.4009	0.561
B.daynumber B.trt:B.daynumber	6 6	97 97	36.72 $1.557$	$0 \\ 0.168$

### 4.8.2 Compositional resistance



4.9

	Df	${\bf SumsOfSqs}$	MeanSqs	F.Model	R2	Pr(>F)
Time	1	4.242	4.242	71.5	0.39	0.001

 $\textbf{Limitation} \ 1 \ 0.03804 \ 0.03804 \ 0.6411 \ 0.003496 \ 0.017$ 

\*\*Time\*Limitation\*\* 1 0.07149 0.07149 1.205 0.006572 0.263

**Residuals**	110	6.527	0.05933	NA	0.6	NA
**Total**	113	10.88	NA	NA	1	NA

Table: Blocks: strata

- 4.10 Phage Host Range
- 4.10.1 global; sympatric vs. allopatric host range

## 4.10.2 Compositional infectivity

4.11 Treatement level degree of infection

## 5 Appendix

## 5.1 R and packages

All analyses were completed using R version 3.2.5 (2016-04-14)

## 5.2 References

## 5.3 Appendix

## 5.3.1 Key term definitions

Word	Abbreviation	Definition
Nitrogen	N	
Phosphorus	P	
Nitrogen Limited	NL	
Phosphorus Limited	$\operatorname{PL}$	
chemostat	$\operatorname{cID}$	