Malibiran, Mark Van Doren E. ME- 4203

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ASSIGNMENT 1

I. Solve for the laplace transform of the

following

1. L [3 - e^{-3t} + 5 sin 2t] =
$$\Gamma(s)$$

(a) 3 L (1) = $\frac{1}{s}$ = $\frac{3}{s}$

(a)
$$\int_{0}^{4} \left(e^{-3t}\right)^{2} = \frac{1}{s+a} = \frac{1}{s+3}$$

$$F(s) = \frac{3}{s} - \frac{1}{s+3} + \frac{10}{s^2+4}$$

2.
$$L[3 + 12t + 42t^3 - 3e^{2t}] = F(s)$$

6 12
$$\mathcal{L} + t = \frac{1}{S^2} = \frac{12}{S^2}$$

© 42 £ {
$$t^3$$
} = $\frac{n!}{s^{n+1}} = \frac{3!}{s^{3+1}} = \frac{c}{s^4} = \frac{252}{s^4}$

$$FCS) = \frac{3}{S} + \frac{12}{S^2} + \frac{252}{S^4} - \frac{3}{S^2}$$

3.
$$L[(t + 1)(t + 2)] = F(s)$$

 $t^2 + 3t + 2$

$$0 \ 3 \ \mathcal{L} \{t\} = \frac{1}{s^2} = \frac{3}{s^2}$$

$$F(s) = \frac{2}{s^3} + \frac{3}{s^2} + \frac{2}{s}$$

II. Solve for inverse laplace of the following 1. $L = \left[\frac{8 - 3s + s^2}{s^3}\right] = f(t) = \frac{8}{s^3} - \frac{3s}{s^3} + \frac{s^2}{s^3}$ $= 8 L = \left(\frac{1}{s^3}\right)^3 - 3 L = \left(\frac{s}{s^3}\right)^3 + L = \left(\frac{s^2}{s^3}\right)^3$ $= 8 L = \left(\frac{1}{s^3}\right)^3 = \frac{8}{s^3}$; $4L = \left(\frac{2}{s^3}\right)^3$; $\frac{2}{s^3} = \frac{n!}{s^{n+1}}$; t^n

$$\textcircled{5} \ 3 \ \mathcal{L}^{-} \left\{ \ \frac{s}{s^{3}} \ \right\} \ , \ 3 \ \mathcal{L}^{-} \left\{ \ \frac{1}{s^{2}} \ \right\} \ , \ \frac{1}{s^{2}} \ - t$$

$$\emptyset \stackrel{=}{\mathcal{L}} \frac{3t}{\left(\frac{s^2}{s^3}\right)} = \mathcal{L} \left(\frac{1}{s}\right) = 1$$

$$f(t) = 4t^2 - 3t + 1$$

2.
$$L^{-1} \left[\frac{5}{s^{-2}} - \frac{4s}{s^2 + 9} \right] = f(t)$$

 $\emptyset L^{-} \left\{ \frac{5}{s^{-2}} \right\} = 5 L^{-} \left\{ \frac{1}{s^{-2}} \right\}; \frac{1}{s^{-2}} = e^{qt}; a = 2$

$$\begin{array}{ll}
= 5e^{2t} \\
6 & 4s \\
= 3 & 5e^{2t}
\end{array}, \quad \sin \omega = \frac{\omega}{s^2 + \omega^2}, \quad \omega = 3$$

$$\frac{1}{s^{2} + w^{2}} \left(\frac{4s}{s^{2} + 9}\right) = \frac{4}{3} \sin 3t ; \frac{d}{dt} \left(\frac{4}{3} \sin 3t\right) = 4\cos 3t$$

$$f(t) = 5e^{2t} + 4\cos 3t$$

3.
$$L^{-1}\left[\frac{7}{s^2+6}\right] = f(t)$$

 $7 \mathcal{L}^{-}\left\{\frac{1}{s^2+6}\right\} = 7 \mathcal{L}^{-}\left\{\frac{\sqrt{6}}{s^2+6}\right\}$; $sin\sqrt{6}$
 $=\left(\frac{7}{\sqrt{6}}sin\sqrt{6}t\right) \cdot \frac{\sqrt{6}}{\sqrt{6}}$
 $f(t) = \frac{7\sqrt{6}}{6}sin\sqrt{6}t$