

# **Asymptote 范例教程**

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本文是基于 Asymptote 1.70 的一组教程。

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# 第一章 赵爽的弦图

赵爽博士是位老知识分子，研究兴趣是天文历法与算学，一生精研《周髀算经》。不过赵老爷子年轻的时候书籍都是手写，最近才紧跟时代潮流用上了电脑。现在他要修订他研究《周髀算经》的札记，决定使用  $\text{\LaTeX}$  来排版。

现在他遇到一个难题，就是他要画出笔记中讲解勾股定理的一幅弦图。听人介绍，几经比较之后，他决定使用现在炒得火热的 **Asymptote**。

赵博士的原图是手画的，线框多有不直不准的，图 1.1 就是旧年据手稿做的雕版图，赵博士并不满意。赵爽博士理想中的图，线条要平整美观，文字要清楚整齐，图形还要上色：朱实自然得用红色，黄实也该用黄色，以与注文一致——就是图 1.2 的样子。

计议已定，赵博士要开始正式的绘图了。

## 1.1 绘图环境

**Asymptote** 的安装并不复杂，在 Windows 下面就是下载运行那个安装包，在 Linux 下面一般也只需要下载对应的压缩包，解压就可以使用了。哦，赵博士用的就是 Windows。

点图标运行 **Asymptote**，就出现了交互式的命令行，提示符是一个 `>`。输入命令：

```
draw((0,0) -- (3cm,4cm)); // 一条直线
```

赵博士装的 **GSView** 立即弹了出来，里面已经画出一条倾斜的直线。再输入 **quit**，程序退出，并留下了一个叫做 **out.eps** 的图形文件，小菜一碟。

这里稍稍解释一下上面的一句代码。**draw** 是画线的命令，更准确地说，是 **Asymptote** 中的函数：它带有一个参数 `(0,0) -- (3cm,4cm)`，参数外面是圆括号，整个命令以分号结束。里面的 `(0,0) -- (3cm,4cm)` 是由两个

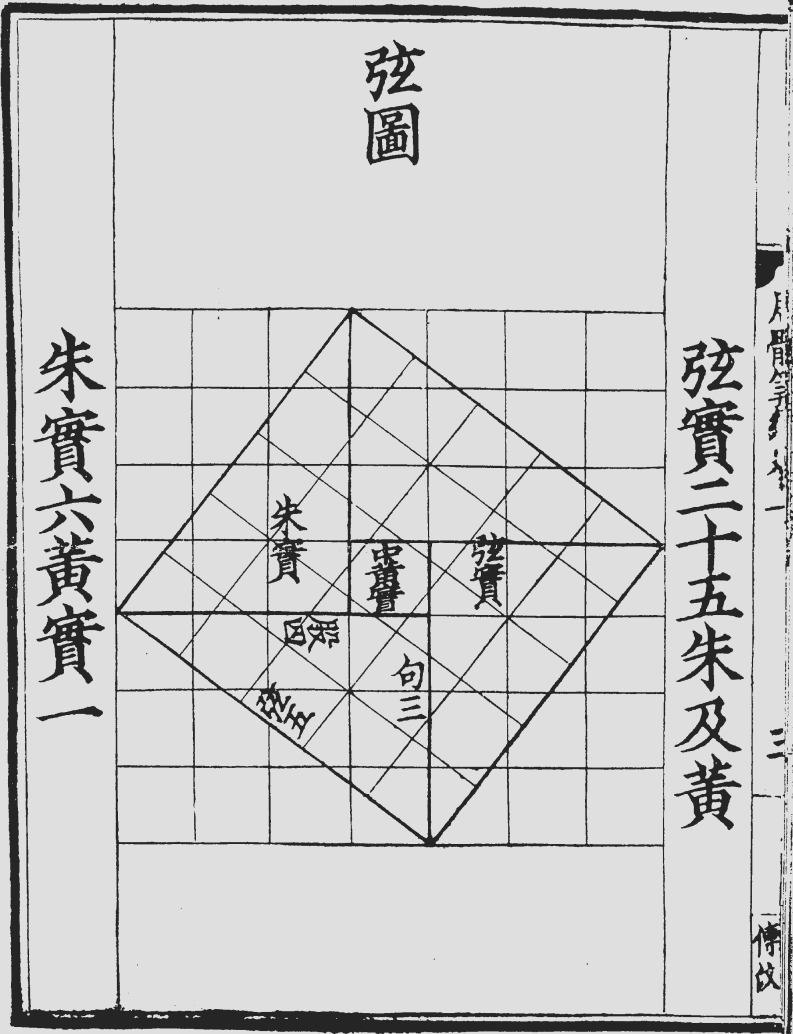
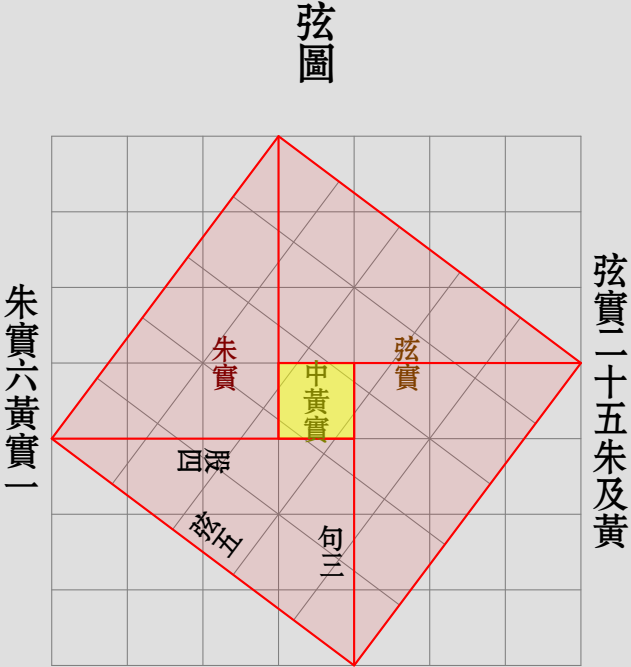


图 1.1: 旧年做的雕版



句股各自乘，併之為弦實，開方除之即弦。案：弦圖又可以句股相乘為朱實一，倍之為朱實四，以句股之差自相乘為中黃實，加差實亦成弦實。

图 1.2: 理想中的新版本

坐标连接而成的直线，坐标是在直角坐标系下的，可以带单位 `mm`, `cm`, `pt`, `bp`, `inch`, `inches`，其意义与在  $\text{\TeX}$  中的一样，如果不带单位，则默认为 `bp`。行末以 `//` 开头的是注释，另有一种在 `/* */` 之间的注释，与 C 语言相同。

不过赵博士写书讲求胸有成竹方才下笔，因此他更愿意使用更一种方式：打开一个文本编辑器，把上面的绘图命令都录入完毕，保存为一个名为 `line.asy` 的文件，最后把这个文件拖动到 **Asymptote** 的图标上面，就完成了整个作图。

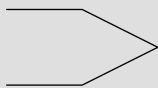
赵博士的小侄子不屑于这种快捷图标的编译方式，他直接进入命令行，输入 `asy`，就进入了 **Asymptote** 的交互环境；要是输入 `asy line`，就画出了刚才的保存的直线。

## 1.2 直线与绘图命令

弦图的图形其实很简单，都是直线、方块、三角形这些，而且为了计算的简便，所有长度也都是整数值。那么，首先就是在 **Asymptote** 中来画直线。

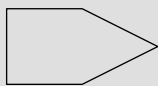
正如前面试验的时候做的那样，一条直线就是用 `--` 把坐标连起来，再使用 `draw` 命令，直线就画出来了。事实上，可以用 `--` 把坐标点连成折线：

```
draw( (0,0) -- (1cm,0) -- (2cm,0.5cm) -- (1cm,1cm) -- (0,1cm) );
```



像这样把坐标用 `--` 连结起来的，就成为一条路径。把直线而稍做修改，在后面连上一个特殊的坐标 `cycle`，就可以得到一条首尾相接的闭路径。如：

```
draw( (0,0) -- (1cm,0) -- (2cm,0.5cm) -- (1cm,1cm) -- (0,1cm) -- cycle );
```



画一条路径可以使用不同的颜色、粗细的笔，这只要给 `draw` 命令多加一个画笔 参数（多个参数用逗号分开）：

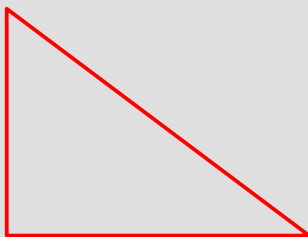
```
draw((0,0) -- (1cm,0) -- (2cm,0.5cm) -- (1cm,1cm) -- (0,1cm), darkblue+1mm);
```



这里 `darkblue` 是颜色，`1mm` 是线的粗细。`darkblue+1mm` 即指一毫米宽的深蓝色粗线。（可用的颜色名称可以参考 [1]）

赵博士画的是“勾三股四弦五”的红色三角形，这很容易：

```
draw( (0,0) -- (4cm,0) -- (0,3cm) -- cycle, red+0.5mm );
```



不过现在还需要的是实心的三角形，因此就需要一个新的绘图命令 `fill`，即填充。于是，红色三角形就成为

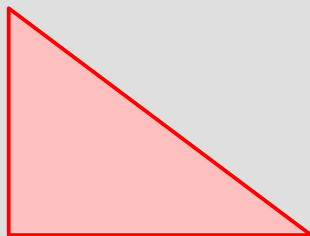
```
fill( (0,0) -- (4cm,0) -- (0,3cm) -- cycle, red );
```





但这样一来三角形的颜色就太重了，而且边界也不清楚。因此似乎应该先用浅红色填充一遍，然后再用深红色勾边。好在可以使用一个命令 `filldraw` 同时完成这两件事情，这样就不需要把一条路径写两遍了。即有：

```
filldraw((0,0) -- (4cm,0) -- (0,3cm) -- cycle,  
fillpen=palered, drawpen=red+0.5mm);
```



这里可以简单地直接写两个参数 `palered`, `red+0.5mm`，不过为了清晰起见还是使用“键 = 值”的写法，明确表示出填充的画笔和描线的画笔。

现在，赵博士的整个弦图的框架就呼之欲出了，就是画出四个三角形（图 1.3）：

```
filldraw( (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle,  
fillpen=palered, drawpen=red+0.5mm);  
filldraw( (7cm,4cm) -- (4cm,4cm) -- (4cm,0) -- cycle,  
fillpen=palered, drawpen=red+0.5mm);  
filldraw( (3cm,7cm) -- (3cm,4cm) -- (7cm,4cm) -- cycle,  
fillpen=palered, drawpen=red+0.5mm);  
filldraw( (0,3cm) -- (3cm,3cm) -- (3cm,7cm) -- cycle,  
fillpen=palered, drawpen=red+0.5mm);
```

还应该画出弦图的中间的“黄实”，用黄色填充。这部分是一个正方形，可以使用现成的 `box(角点, 角点)` 命令来产生矩形的路径，因而填充正中间的正方形就可以用：

```
fill( box((3cm,3cm), (4cm,4cm)), yellow );
```

这个填充的命令应该放在画线之前（以免覆盖描的红线）。

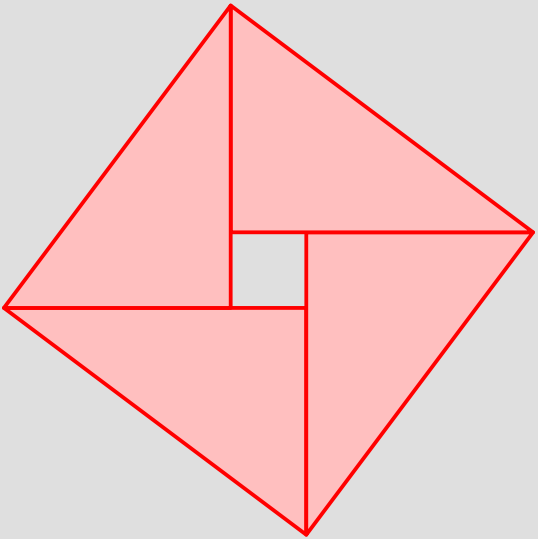


图 1.3: 弦图的初步框架

回顾前面的代码，赵博士觉得连续地写四个 `filldraw` 命令太重复了。他读了 **Asymptote** 的文档 [1]，才知道多条路径可以用符号 `^^` 连起来，一起使用，于是立即着手改进原来的代码。

而且，由于还打算在图的后面画出参考网格，图形的颜色还应该设置为半透明的。好在这并不难实现，只要稍稍改动一下填充的画笔，使用 `opacity(数值)` 来设定有一定不透明度（取值为 0 ~ 1）的画笔，并把它加在原来的画笔上。于是赵博士最后写出了这样的代码：

```
fill( box((3cm,3cm), (4cm,4cm)), opacity(0.5)+yellow );  
filldraw( (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle  
  ^^ (7cm,4cm) -- (4cm,4cm) -- (4cm,0) -- cycle  
  ^^ (3cm,7cm) -- (3cm,4cm) -- (7cm,4cm) -- cycle  
  ^^ (0,3cm) -- (3cm,3cm) -- (3cm,7cm) -- cycle,  
  fillpen=opacity(0.1)+red, drawpen=red+0.5mm );
```

至此，弦图的主要框架（图 1.4）就此完成。

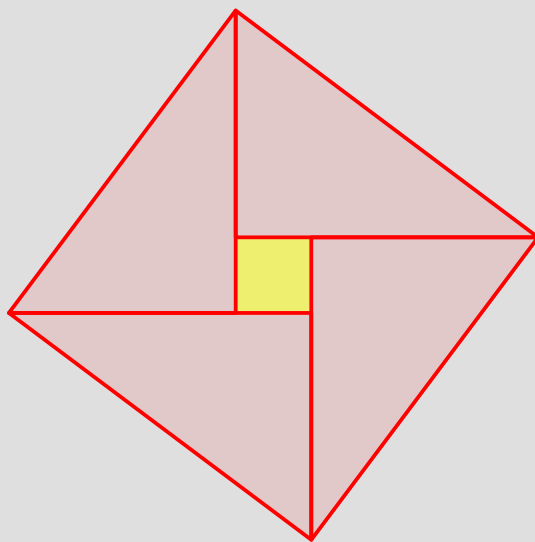


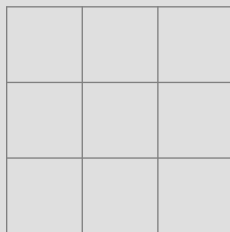
图 1.4: 弦图的进一步优化的框架

## 1.3 图形变换与功能模块的使用

然后是画作为长度参考的网格。其实网格一开始就该在图中画出来，这样后面画图准确与否才能看得清楚。不过现在赵博士是重作旧图，图样已定，网格就搁在弦图的主要图形后面才画了。

按说这个网格是十分简单的，无非就是画一些灰色的纵横细线。比如这个  $3 \times 3$  的网格：

```
draw( (0,0) -- (3cm,0)
      ^^ (0,1cm) -- (3cm,1cm)
      ^^ (0,2cm) -- (3cm,2cm)
      ^^ (0,3cm) -- (3cm,3cm),
      gray );
draw( (0,0) -- (0,3cm)
      ^^ (1cm,0) -- (1cm,3cm)
      ^^ (2cm,0) -- (2cm,3cm)
      ^^ (3cm,0) -- (3cm,3cm),
      gray );
```



可无疑这个办法显得太麻烦了，赵博士要画的是  $7 \times 7$  的网格，就要分别画出 16 条直线。这样的代码不仅不好写，而且容易出错，修改一下也很麻烦。

赵博士看到了手册 [1] 中讲循环语句的用法，似乎可以完成这件事。可是以赵博士的年龄，再去看什么编程什么变量的，命令不能一条一条执行下来，很不习惯，头脑就往往转不清楚。

于是赵博士就去论坛上咨询，一些人劝他去用几行循环语句，甚至有人已经把完整的函数做好了。但有一个结

果特别引人注目，有人指出，在 `math` 模块中已经定义好了一个 `grid` 函数，只要拿来用就可以了。赵博士立即精神大振，来看这个 `grid` 函数：

```
picture grid(int Nx, int Ny, pen p=currentpen)
```

这个是在 `math` 模块中 `grid` 函数的原型。它说明 `grid` 函数有 `Nx`, `Ny` 两个整数类型的必需参数，一个可选的画笔，并且返回一个 `picture`（图）类型的对象。

要使用模块的功能，需要在绘图之前导入这个模块，这只要使用

```
import 模块名;
```

因此，要使用 `math` 模块中的 `grid` 函数，只要在代码中写

```
import math;
```

就可以了。

`grid` 函数的行为看起来很奇怪，调用它会在一个单独的图上画出一个  $Nx \times Ny$  的网格，网格的左下角在 origin，间距为 1。要使用 `grid` 函数画的图形，要使用 `add(图)` 命令，把这个图形加在当前的图上：

```
import math;
add(grid(10,10,gray));
```



不过直接这样做的结果是只能得到一个小得已经看不清的网格。因此，必须对图形进行放缩。

`Asymptote` 提供了平移、旋转、放缩、倾斜、反射等各种的仿射变换，来对坐标、路径、图形等元素进行变换（严格的函数原型参考 [1]）：

<code>shift(坐标)</code>	// 按坐标平移
<code>shift(x, y)</code>	// 按 (x, y) 平移
<code>scale(倍数)</code>	// 按倍数放缩
<code>xscale(倍数)</code>	// $x$ 轴方向按倍数放缩
<code>yscale(倍数)</code>	// $y$ 轴方向按倍数放缩
<code>scale(x, y)</code>	// 在 $x$ 轴、 $y$ 轴方向分别按倍数 $x$ , $y$ 放缩

```
rotate(角度, z=(0,0)) // 按角度绕中心 z (默认为原点, 逆时针) 旋转  
slant(因子)           // 按一定因子向右倾斜  
reflect(a, b)         // 相对直线 a--b 反射
```

使用一个变换就是把这个变换乘在被变换对象的左边。例如一个放缩一个单位正方形：

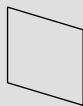
```
draw( scale(2cm) * box((0,0), (1,1)) );
```



这样的变换可以连续地做下去，例如

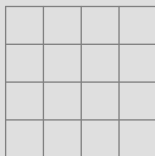
```
draw( rotate(90) * slant(0.3) * scale(1cm) * box((0,0), (1,1)) );
```

就是把一个单位正方形先放大，再倾斜，再旋转  $90^\circ$ ：



有了这些变换，画出一个合适大小的网格就不再是什么难事了：

```
import math;  
add( scale(5mm) * grid(4, 4, gray) );
```



赵博士的弦图有两个网格，不仅要大小合适，而且其中一个需要进行旋转和平移。平移的位置很明显，但旋转仍然需要一些计算。当然这难不倒精研天文算学多年的赵博士，这里弦实（ $5 \times 5$  的正方形）可以看作是顺时针旋转得到的，从朱实的三角形容易看出旋转的角度正好是  $\arctan(3/4)$ 。Asymptote 中也可以方便地调用返回角度的反三角函数 `aTan` 来计算这个角度。更详细的数学函数列表，参看 [1]。

于是，赵博士弦图中的网格，就可以这样方便地画出来了（图 1.5）：

```
// 网格
import math;
add( scale(1cm) * grid(7, 7, gray) );
add( shift(0,3cm) * rotate(-aTan(3/4)) * scale(1cm) * grid(5, 5, gray) );
// 弦图主体
fill( box((3cm,3cm), (4cm,4cm)), opacity(0.5)+yellow );
filldraw( (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle
  ^^ (7cm,4cm) -- (4cm,4cm) -- (4cm,0) -- cycle
  ^^ (3cm,7cm) -- (3cm,4cm) -- (7cm,4cm) -- cycle
  ^^ (0,3cm) -- (3cm,3cm) -- (3cm,7cm) -- cycle,
  fillpen=opacity(0.1)+red, drawpen=red+0.5mm );
```

## 1.4 标注文字

现在要进行的是文字的标注。按照勾股定理的约定，赵博士打算在一个红色三角形内标注“朱实”，在黄色矩形处标注“黄实”，并为拼得的整个大矩形标注“弦实”；在另一红色三角形的三边标注“勾三”、“股四”、“弦五”的尺寸；最后在图形两侧加上说明的文字。

在标注文字之前，对于中文标签，应该先定义好中文环境和字体。Asymptote 会调用  $\text{\LaTeX}$  来进行标签的处理，因而需要设置的就是  $\text{\LaTeX}$  的编译引擎与一般的中文  $\text{\LaTeX}$  文件导言区。在这里，赵博士决定使用  $\text{\XeLaTeX}$  引擎与 `xeCJK` 宏包来处理中文。为此，在 Asymptote 源文件中，他使用了下面的设置代码：

```
settings.tex = "xelatex";
usepackage("xeCJK");
```

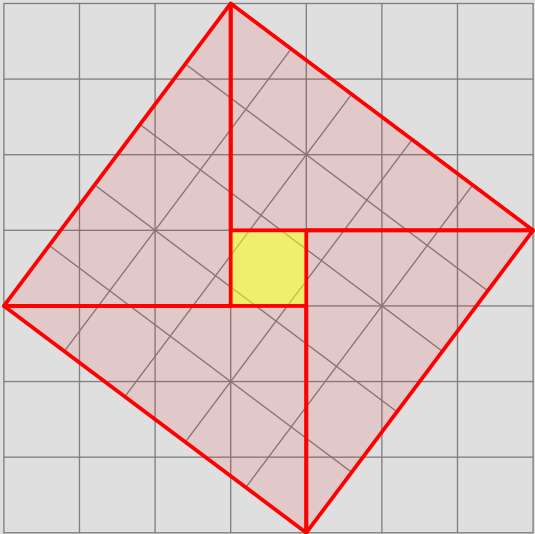


图 1.5: 带网格的弦图草图



```
tex preamble{"\setCJKmainfont{SimSun}");
```

这里第一行是设置编译时所用的  $\text{T}_{\text{E}}\text{X}$  引擎。后面 `usepackage` 命令就是  $\text{E}_{\text{T}}\text{X}$  中的 `\usepackage` 命令的一个包装形式，里面的字符串参数就是宏包名；而 `tex preamble` 命令则把接收的参数直接放进  $\text{E}_{\text{T}}\text{X}$  的导言区。

进行上述设置后，就可以正确使用中文标签了。标注的命令很简单，就是 `label`，参数正是标签文字和标签的位置。例如：

```
draw( (0,0) -- (1cm,1cm) -- (2cm,0) );
label( "中间", (1cm,0cm) );
```

就得到



可以在标签中使用任意的  $\text{E}_{\text{T}}\text{X}$  代码，包括数学公式，例如：

```
label("$x = \sin\alpha$", (0,0));
```

就会正确地得到  $x = \sin \alpha$  的标签。

现在，我们可以给弦图加上“朱实”、“黄实”和“弦实”的标签了。在前面的框架代码后面加上

```
label("朱实", (2cm,4cm));
label("黄实", (3.5cm,3.5cm));
label("弦实", (5cm,4cm));
```

以及设置字体的代码，就得到图 1.6 的结果。

下面则是要给三角形的三边进行标注。

与前面在一个点处标注不同，这里实际是给一条路径（直线）标注标签。因此，想要得到的是距离这条路径的中点一定方向距离加一个标签，而不是简单地取路径上的一点作为标签的位置。好在 `Asymptote` 确实也提供了这样的功能，仍然使用 `label` 命令，基本语法是：

```
label(标签, 路径)
```

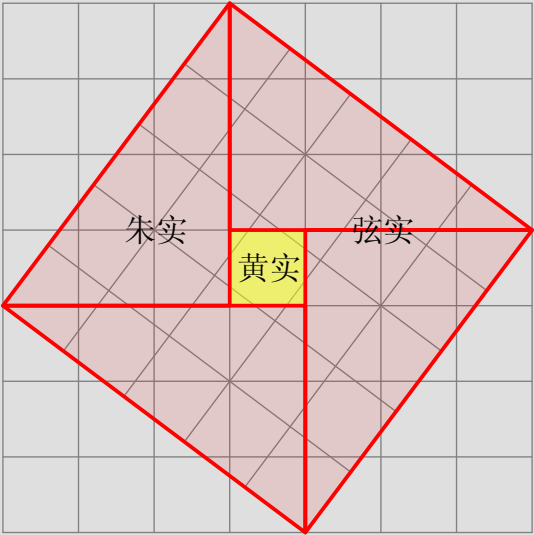


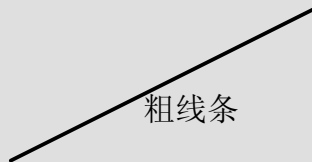
图 1.6: 带部分标注的弦图

## 1.4. 标注文字

这里默认会在路径中间的右侧（沿着路径行进方向）加标签。例如：

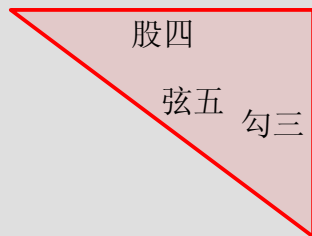
```
draw( (0,0) -- (4cm,2cm), linewidth(0.5mm) );
label("粗线条", (0,0) -- (4cm,2cm));
```

（其中的 `linewidth` 函数用来表示具有一定线宽的画笔）这段代码将得到



现在，赵博士就可以给三角形的三边加上“勾三”、“股四”、“弦五”的标签了，只要稍稍注意一下标签摆放的默认方向：

```
filldraw( (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle,
  fillpen=opacity(0.1)+red, drawpen=red+0.5mm );
label( "勾三", (4cm,3cm) -- (4cm,0) );
label( "股四", (0,3cm) -- (4cm,3cm) );
label( "弦五", (4cm,0) -- (0,3cm) );
```

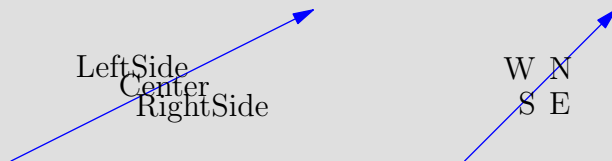


不过，为了得到正确的标签位置，不得不把原来逆时针画的线用顺时针方向重写，这多少让赵博士有些恼火：为什么不能在路径的左边标注标签呢？确实可以，很简单，只要给 `label` 命令再加上 `align=LeftSide` 选项（或

者简单地只用 `LeftSide` ) 就指定了在左边放置对齐。同理, 还有向右对齐的 `RightSide`, 在中间对齐的 `Center` 以及一般意义的相对方向 `Relative(方向)`。例如:

```
draw( (0,0) -- (4cm,2cm), blue, Arrow );
label( "LeftSide", (0,0) -- (4cm,2cm), align=LeftSide );
label( "RightSide", (0,0) -- (4cm,2cm), align=RightSide );
label( "Center", (0,0) -- (4cm,2cm), align=Center );

draw( (6cm,0)--(8cm,2cm), blue, Arrow );
label( "E", (6cm,0)--(8cm,2cm), Relative(E) );
label( "S", (6cm,0)--(8cm,2cm), Relative(S) );
label( "W", (6cm,0)--(8cm,2cm), Relative(W) );
label( "N", (6cm,0)--(8cm,2cm), Relative(N) );
```



E, S, W, N 分别是东南西北四个罗盘方向, 用在 `Relative` 函数里面就表示相对于路径方向的四个方向。为明确, 这里用 `Arrow` 选项在画线时加了箭头。

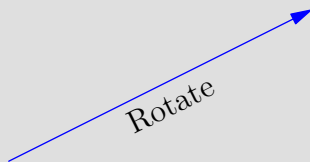
不过, 这样的标签还是不能令赵博士满意。赵博士给三角形加标签, 还希望标签随着三角形的边作旋转, 使标签沿着边排列。为此, 赵博士不得不又仔细查看了 [1], 在讲标注文字一节 (`label`) 他找到了一个构造标签的更高级的办法, 即不仅仅是使用一个简单的字符串, 而是使用

### `Label`(标签)

函数进行构造。里面的“标签”参数仍然可以是原来的字符串, 或是通过这个函数构造出来的高级的标签。这个函数可以带许多可选的其他参数, 如 `position=位置` 的参数就可以指定标签放在路径中点之外的其他地方; 而 `embed=嵌入变换方式` 的参数则可以解决标签自动旋转的问题。

这里暂且放下 **position** 参数。只来看 **embed** 参数的一个特例：**Rotate(方向)**。这个参数会让标签向着给定的方向旋转，如：

```
draw( (0,0)--(4cm,2cm), blue, Arrow );
label( Label("Rotate", Rotate((4,2))),
      (0,0)--(4cm,2cm) );
```



这里坐标 (4, 2) 正是这条直线的绘制方向。

终于，使用了上面的全部功能，赵博士完成了全部的图形标注工作（图 1.7）：

```
settings.tex = "xelatex";
usepackage("xeCJK");
texpreamble("\setCJKmainfont{SimSun}");

import math;
add( scale(1cm) * grid(7, 7, gray) );
add( shift(0,3cm) * rotate(-aTan(3/4)) * scale(1cm) * grid(5, 5, gray) );

fill( box((3cm,3cm), (4cm,4cm)), opacity(0.5)+yellow );
filldraw( (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle
  ^^ (7cm,4cm) -- (4cm,4cm) -- (4cm,0) -- cycle
  ^^ (3cm,7cm) -- (3cm,4cm) -- (7cm,4cm) -- cycle
  ^^ (0,3cm) -- (3cm,3cm) -- (3cm,7cm) -- cycle,
  fillpen=opacity(0.1)+red, drawpen=red+0.5mm );
```

```

label("朱实", (2cm,4cm));
label("黄实", (3.5cm,3.5cm));
label("弦实", (5cm,4cm));
label( Label("勾三",Rotate(S)), (4cm,0)--(4cm,3cm), LeftSide );
label( Label("股四",Rotate(E)), (4cm,3cm)--(0,3cm), LeftSide );
label( Label("弦五",Rotate((4,-3))), (0,3cm)--(4cm,0), LeftSide );

```

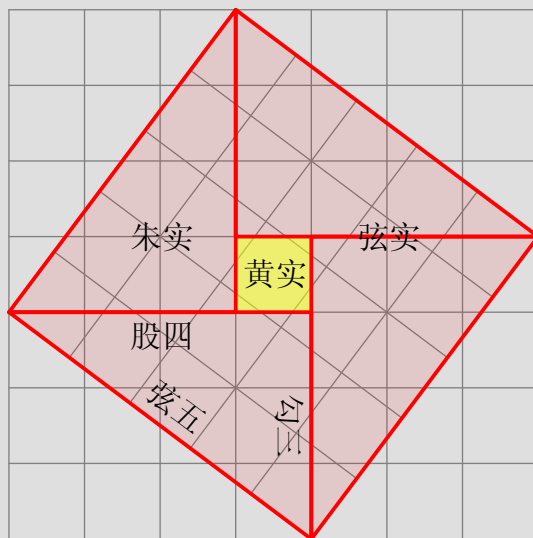


图 1.7: 带标注的完整弦图

## 习题

1. 查阅参考手册 [1], 看看都有哪些颜色可用。看看你的系统中安装了哪些中文字体。然后修改图 1.7, 使用另一种你喜欢的字体进行标注; 并且将“朱实”、“黄实”和“弦实”分别用红、黄、橙色标注。

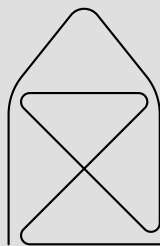
2. 查阅参考手册 [1], 看看 `draw`、`fill`、`label` 等命令都可以带哪些可选的参数, 并自己举例子试验一下效果。
3. 代码

```
path zhushi = (4cm,0) -- (4cm,3cm) -- (0,3cm) -- cycle;
```

可以把一个三角形的路径保存在变量 `zhushi` 中, 以后就可以使用 `draw(zhushi)` 这样的命令对此路径进行操作<sup>1</sup>。

考虑如何利用平移和旋转变换, 只定义一个三角形的路径, 就把弦图中的四个红色三角形都画出来。

4. 查阅手册 [1] 和 `Asymptote` 自带的例子, 研究模块 `roundedpath` 的用法。并利用它尝试画出下面的图形:



看看 `Asymptote` 中还有什么用法简单而又有趣的模块。

5. (较难) 研究在 `ETEX` 里中文直排的方法, 尽量精确地复现出赵博士理想中的弦图效果 (图 1.2)。

---

<sup>1</sup>关于变量定义和使用的详细内容, 参考后面的章节或手册 [1]。

## 第二章 André Deledicq 的铺砌插画

André 是一名兴趣广泛的法国数学教师，在他的新著《Le monde des pavages》(《铺砌世界》)中，打算画一幅有关羊的铺砌插画：

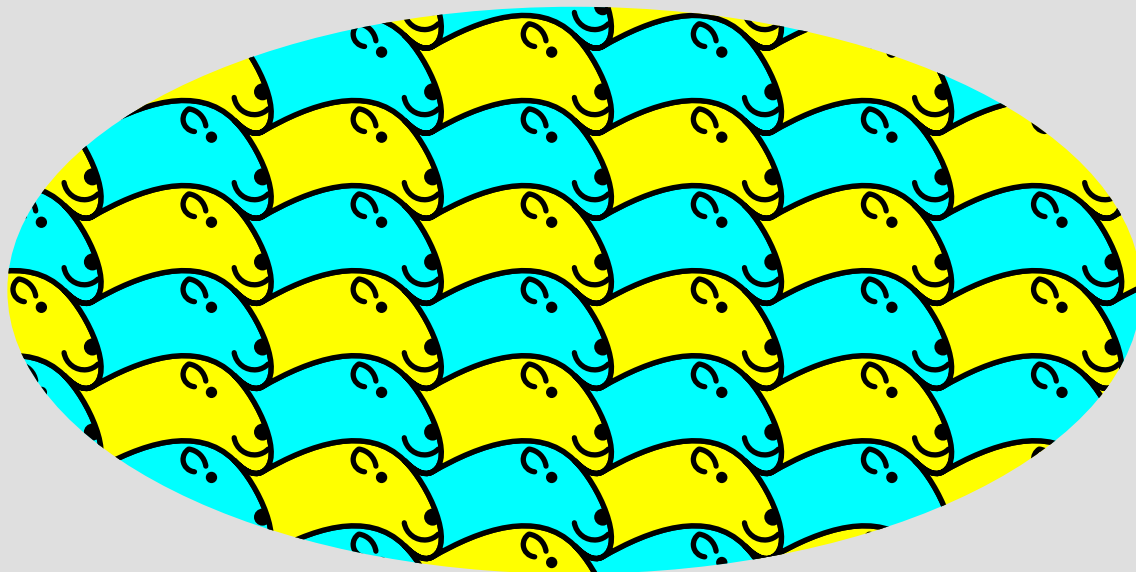


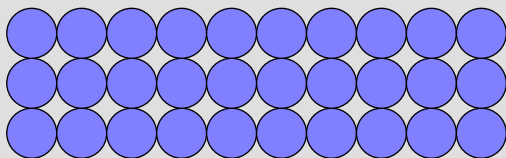
图 2.1: André 理想中的铺砌图



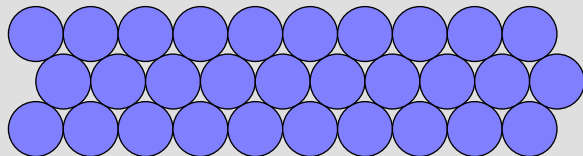
André 很清楚他要画的图形的数学理论，但 André 的朋友 Timothy 告诉他要画这样的图形多少是需要一些编程的知识的，对于他这样一位往日对计算机并不通晓的人来说可能会有困难。不过 André 并不以为意：这世上还有什么比数学更难的呢？于是他兴致勃勃的开始了。

## 2.1 从矩形到铺砌

铺砌图，顾名思义，就是像铺地板砖一样，把许多相同样式的图形平铺开。不过，并不是什么图形都可以平铺填满整个平面的——比如圆形就不行。把许多圆形一个挨一个排列起来，也只能得到



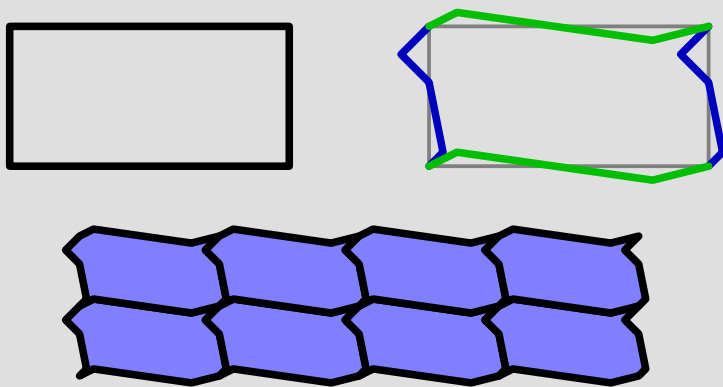
或者是



都会留下许多空隙。而矩形、平行四边形、六边形等等都可以不留空隙地把平面铺满。

但问题是，如何设计出 André 理想中的那种看起来形状不规则的铺砌图案呢？

身为数学教师的 André 当然有办法。其实不规则铺砌图案还是规则图案的变形。André 要画的羊形铺砌图，其实就是从矩形铺砌变化而来的。只要把一个矩形图案的上下两边、左右两边分别变形，使得变形后的上边与下边、左边与右边还对应重合，就依然可以完美地拼合起来。这正是铺砌图案最基本的构成方式：



有了这个方法，对复杂的铺砌图，也只要从一个基本形状（比如矩形、正六边形）开始变形，就等到铺砌所需要的一块“砖”。

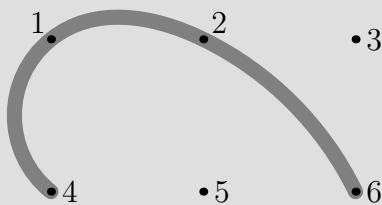
因此，要画出羊头形状铺砌图，只要把一个矩形按照上面的要求变形为一个羊头形状，在不同的位置重复画出就可以了。

## 2.2 变量与曲线

下面的问题就是，怎么画一个羊头呢？更具体地说，怎么画出羊头的曲线呢？

那么，首先要了解如何在 **Asymptote** 中描述曲线。1.2 节中提到 -- 连结一组坐标就成为直（折）线段；类似地，用 .. 连结坐标就得到经过这些坐标点的曲线：

```
size(5cm,0);
pair z1 = (0,1), z2 = (1,1), z3 = (2,1),
      z4 = (0,0), z5 = (1,0), z6 = (2,0);
path p = z4 .. z1 .. z2 .. z6;
draw(p, gray+2mm);
```



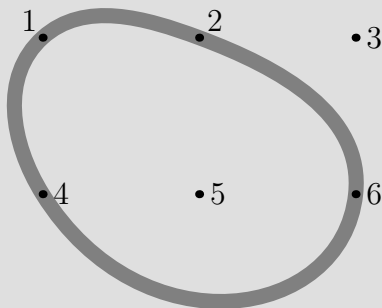
在这里，我们定义了一些变量以使代码清晰（这里略去了画点和标签的代码）。**pair** 类型的变量  $z1, \dots, z6$  保存六个坐标，**path** 类型的变量  $p$  保存一条曲线路径。因而上面 **size** 之后的绘图代码就相当于

```
draw( (0,0) .. (0,1) .. (1,1) .. (2,0), gray+2mm );
```

其中前面的一句 **size(5cm,0)** 表示代码中的坐标只是相对位置，最后将整个图形按比例放缩为 5cm 宽<sup>1</sup>。类似地，也可以使用 **size(0,4cm)** 把图形放缩到 4cm 高。

最重要的当然还是曲线的表示。以 **..** 连结的坐标会以一种尽量接近圆弧的方式连为经过这些点的光滑曲线。与画直线类似，**cycle** 可以作为一个特殊的坐标产生闭合曲线，即一条闭路径：

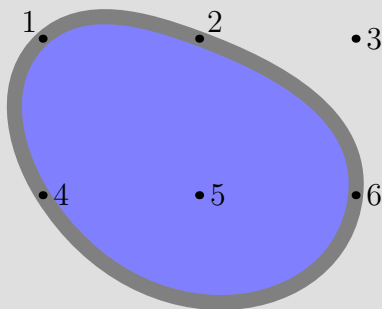
```
path q = z4 .. z1 .. z2 .. z6 .. cycle;
draw(q, gray+2mm);
```



变量不仅仅是给了坐标、路径等对象一个简洁的名字，它也使得对同一个对象重复使用并进行不同的操作变得十分方便：

<sup>1</sup>注意坐标、图形会被放缩，但画笔的宽度不会放缩。

```
fill(q, lightblue);
draw(q, gray+2mm);
```

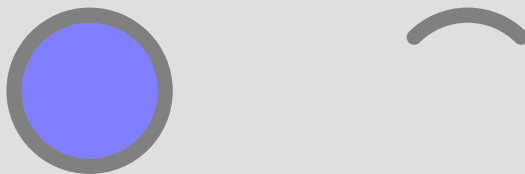


就像使用 `box` 可以直接得到矩形一样，最常用的曲线：圆、椭圆和圆弧，也可以使用现成的命令得到：

<b>circle</b> (c, r)	圆心 <code>c</code> ，半径 <code>r</code> 的圆，这是逆时针方向的闭曲线；
<b>ellipse</b> (c, a, b)	中心为 <code>c</code> ，长半轴 <code>a</code> ，短半轴 <code>b</code> 的椭圆，这也是逆时针方向的闭曲线；
<b>arc</b> (c, r, angle1, angle2)	圆心 <code>c</code> ，半径 <code>r</code> ，角度从 <code>angle1</code> 到 <code>angle2</code> 的圆弧。

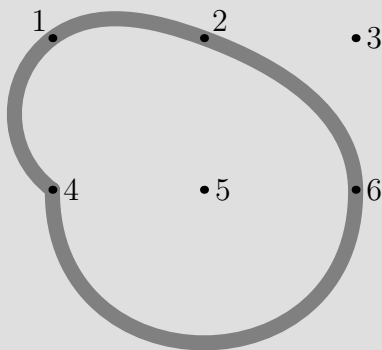
例如：

```
filldraw( circle((0,0), 1cm), lightblue, gray+2mm );
draw( arc((5cm,0), 1cm, 45, 135), gray+2mm );
```



一条用 **cycle** 产生的闭路径和简单地把首尾结点重合的路径是非常不同的。首先，只有闭路径可以填充颜色；其次，使用 **cycle** 连结的曲线在起点处是光滑连接的，而如果只是首尾结点重合则不会光滑连接。试将下面的曲线 q2 与上面的曲线 q 比较：

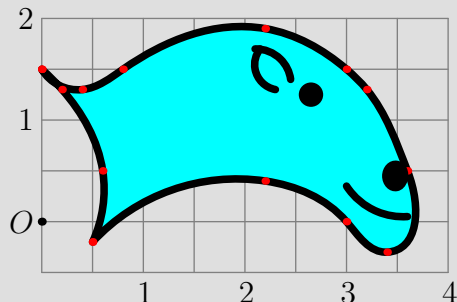
```
path q2 = z4 .. z1 .. z2 .. z6 .. z4;
draw(q2, gray+2mm);
```



现在有了绘制曲线的方法，画出一个羊头就只是把草稿上的坐标连接起来而已。André 有一个纸上的草图，于是在描出几个点以后，他很快得到这样的结果（这里给图形增加了辅助网格）：

```
size(0,4cm);
pen outline = black+1mm;
// 头
path head = (0.5,-0.2) .. (0.6,0.5) .. (0.2,1.3) .. (0,1.5) .. (0,1.5)
    .. (0.4,1.3) .. (0.8,1.5) .. (2.2,1.9) .. (3,1.5) .. (3.2,1.3)
    .. (3.6,0.5) .. (3.4,-0.3) .. (3,0) .. (2.2,0.4) .. (0.5,-0.2) .. cycle;
filldraw(head, cyan, outline);
dot(head, red+1mm); // 画出羊头路径上的结点
// 五官
fill( circle((2.65,1.25), 0.12), outline );
```

```
fill( (3.5,0.3) .. (3.35,0.45) .. (3.5,0.6) .. (3.6,0.4) .. cycle, outline );
draw( (3,0.35) .. (3.3,0.1) .. (3.6,0.05), outline );
draw( (2.3,1.3) .. (2.1, 1.5) .. (2.15,1.7), outline );
draw( (2.1,1.7) .. (2.35,1.6) .. (2.45,1.4), outline );
```



在一开始，André 使用

```
pen outline = black+1mm;
```

定义一个 **pen** 类型的变量 **outline** 表示用来画羊头轮廓的画笔，以备使用。

然后，André 直接用 `..` 连结一组坐标来定义羊的头部轮廓：

```
path head = (0.5,-0.2) .. (0.6,0.5) .. (0.2,1.3) .. (0,1.5) .. (0,1.5)
.. (0.4,1.3) .. (0.8,1.5) .. (2.2,1.9) .. (3,1.5) .. (3.2,1.3)
.. (3.6,0.5) .. (3.4,-0.3) .. (3,0) .. (2.2,0.4) .. (0.5,-0.2) .. cycle;
```

需要尖角的时候，就使用重复的相同点（如这里的起点）；曲线变化大的地方，取的点也比较密集。

最后五官的绘制。眼睛是填充的小黑圆，鼻子是黑色的卵形，耳朵和嘴都是简单的曲线。

于是，只要把这样一个图形一个挨一个地重复画许多遍，就可以得到 André 想要的铺砌效果了。设计羊头形状的工作无疑是最关键也最复杂的，因此 André 的任务现在就已经完成了一半。

不过继承了法国完美主义风气的 André 老师，很快挑出了毛病：这只羊头部的轮廓，并不完全是按照 2.1 节对矩形变形得到的——他的手稿基本上是这样设计的，但在使用 **Asymptote** 上绘图时则只是在手稿上相当随意地取了

一些结点连结得到曲线，这个轮廓想必也并不能严丝合缝地一个个拼起来。还有一件很令他恼火的事情则是：要画出羊头的轮廓，他要画的点太多了，一个尖角用两个结点表示，也太不符合他的简洁美学了。因此，这个看上去相当不错的羊头一号，就被 André 老师无情地否决掉了。他决定发扬数学教师严谨简洁的作风，再做出更完美的羊头二号来。

## 2.3 细致的曲线调整与曲线操作

### 2.4 子图和循环

### 2.5 路径剪裁

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```
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```

```
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```
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