classo

Leo

CONTENTS

CHAPTER

ONE

FUNCTIONS OF THE PACKAGE

1.1 Random data

CLasso.random_data (n, d, d_nonzero, k, sigma, zerosum=False, seed=False, classification=False)

Generation of random matrices as data such that y = X.sol + sigma. noise

The data X is generated as a normal matrix The vector sol is generated randomly with a random support of size d_nonzero, and componants are projected random intergers between -10 and 10 on the kernel of C restricted to the support The vector y is then generated with X.dot(sol)+sigma*noise, with noise a normal vector

Parameters

- n (int) Number of sample, dimension of y
- d (int) Number of variables, dimension of sol
- **d_nonzero** (*int*) Number of non null componant of sol
- **k** (*int*) Number of constraints, number of rows of C
- **sigma** (float) size of standard error
- zerosum (bool, optional) If True, then C is the all-one matrix with 1 row, independently of k
- **seed** (bool or int, optional) **Seed** for random values, for an equal seed, the result will be the same. If set to False: pseudo-random vectors
- classification (bool, optional) if True, then it returns sign(y) instead of y

Returns tuple of three ndarray that corresponds to the data : (X,C,y) ndarray : array corresponding to sol which is the real solution of the problem y = Xbeta + noise s.t. beta sparse and Cbeta = 0

Return type tuple

1.2 File converters

CLasso.csv to mat(file, begin=1, header=None)

Function to read a csv file and to create an ndarray with this

Parameters

- **file** (str) Name of csv file
- **begin** (int, optional) First colomn where it should read the matrix

• header (None or int, optional) - Same parameter as in the function pandas. read csv()

Returns matrix of the csv file

Return type ndarray

CLasso.mat_to_np(file)

Function to read a mat file and to create an ndarray with this

Parameters file (str) – Name of mat file

Returns matrix of the mat file

Return type ndarray

1.3 Matrices normalization

CLasso.rescale (matrices)

Function that rescale the matrix and returns its scale

Substract the mean of y, then divides by its norm. Also divide each colomn of X by its norm. This will change the solution, not only by scaling it, because then the L1 norm will affect every component equally (and not only the variables with big size)

Parameters matrices (tuple) – tuple of three ndarray matrices corresponding to (X,C,y)

Returns tuple of the three corresponding matrices after normalization tuple: tuple of the three information one need to recover the initial data: IX (list of initial colomn-norms of X), ly (initial norm of y), my (initial mean of y)

Return type tuple

CLasso.clr (array, coef=0.5)

Centered-Log-Ratio transformation

Set all negative or null entry to a constant coef. Then compute the log of each component. Then substract the mean of each colomn on each colomn.

Parameters

- array (ndarray) matrix nxd
- coef (float, optional) Value to replace the zero values

Returns clr transformed matrix nxd

Return type ndarray

1.4 Theoretical lambda

CLasso.theoretical_lam(n, d)

Theoretical lambda as a function of the dimension of the problem

This function returns (with $\phi = erf$):

$$4/\sqrt{n}\phi^{-1}(1-2x)$$
 such that $x=4/d(\phi^{-1}(1-2x)4+\phi^{-1}(1-2x)^2)$

Which is the same (thanks to formula : $norm^{-1}(1-t) = \sqrt{2}\phi^{-1}(1-2t)$) as :

$$\sqrt{2/n} * norm^{-1}(1-k/p)$$
 such that $k = norm^{-1}(1-k/p)^4 + 2norm^{-1}(1-k/p)^2$

Parameters

- **n** (*int*) number of sample
- **d**(*int*) number of variables

Returns theoretical lambda

Return type float

1.5 Numpy example

```
numpy.zeros (shape, dtype=float, order='C')
```

Return a new array of given shape and type, filled with zeros.

Parameters

- shape (int or tuple of ints) Shape of the new array, e.g., (2, 3) or 2.
- **dtype** (*data-type*, *optional*) The desired data-type for the array, e.g., *numpy.int8*. Default is *numpy.float64*.
- order ({'C', 'F'}, optional, default: 'C') Whether to store multi-dimensional data in row-major (C-style) or column-major (Fortran-style) order in memory.

Returns out – Array of zeros with the given shape, dtype, and order.

Return type ndarray

See also:

zeros_like() Return an array of zeros with shape and type of input.

empty () Return a new uninitialized array.

ones () Return a new array setting values to one.

full() Return a new array of given shape filled with value.

Examples

```
>>> np.zeros(5)
array([ 0.,  0.,  0.,  0.])
```

```
>>> np.zeros((5,), dtype=int)
array([0, 0, 0, 0, 0])
```

DESCRIPTION OF THE CLASS CLASSO PROBLEM

2.1 CLasso

2.2 Class classo_problem

 $\verb|classo.classo_problem| (X, y, C='zero-sum', labels=False)|$

Class that contains all the information about the problem

Parameters

- **X** (ndarray) Matrix representing the data of the problem
- **y** (ndarray) Vector representing the output of the problem
- **C**(str or ndarray, optional) Matrix of constraints to the problem. If it is 'zero-sum' then the corresponding attribute will be all-one matrix. Default value to 'zero-sum'
- rescale (bool, optional) if True, then the function rescale() will be applied to data when solving the problem. Default value is 'False'

label

list of the labels of each variable. If set to False then there is no label

Type list or bool

data

object containing the data of the problem.

Type classo_data

formulation

object containing the info about the formulation of the minimization problem we solve.

Type classo_formulation

model_selection

object giving the parameters we need to do variable selection.

Type classo_model_selection

solution

object giving caracteristics of the solution of the model_selection that is asked. Before using the method solve(), its componant are empty/null.

Type classo_solution

```
classo problem.solve()
```

Method that solve every model required in the attributes of the problem and update the attribute problem. solution with the characteristics of the solution.

2.3 Class classo data

class CLasso_data(X, y, C, rescale=False)

Class containing the data of the problem

Parameters

- **X** (ndarray) Matrix representing the data of the problem
- **y** (ndarray) Vector representing the output of the problem
- **C** (str or array, optional) Matrix of constraints to the problem. If it is 'zero-sum' then the corresponding attribute will be all-one matrix.
- **rescale** (bool, optional) if True, then the function rescale() will be applied to data when solving the problem

Х

Matrix representing the data of the problem

Type ndarray

У

Vector representing the output of the problem

Type ndarray

С

Matrix of constraints to the problem. If it is 'zero-sum' then the corresponding attribute will be all-one matrix.

Type str or array, optional

rescale

if True, then the function rescale () will be applied to data when solving the problem

Type bool, optional

2.4 Class classo formulation

class CLasso.solver.classo_formulation

Class containing the data of the problem

huber

True if the formulation of the problem should be robust Default value = False

Type bool

concomitant

True if the formulation of the problem should be with an M-estimation of sigma. Default value = True

Type bool

classification

True if the formulation of the problem should be classification (if yes, then it will not be concomitant) Default value = False

Type bool

rho

Value of rho for robust problem. Default value = 1.345

Type float

rho_classification

value of rho for huberized hinge loss function for classification (this parameter has to be negative). Default value = -1.

Type float

е

value of e in concomitant formulation. If 'n/2' then it becomes n/2 during the method solve(), same for 'n'. Default value: 'n' if huber formulation; 'n/2' else

Type float or string

2.5 Class classo_model_selection

class CLasso.solver.classo_model_selection

Class containing the data of the problem

PATH

True if path should be computed. Default Value = False

Type bool

PATHparameters

object parameters to compute the lasso-path.

Type PATHparameters

CV

True if Cross Validation should be computed. Default Value = False

Type bool

CVparameters

object parameters to compute the cross-validation.

Type CVparameters

StabSel

True if Stability Selection should be computed. Default Value = True

Type boolean

StabSelparameters

object parameters to compute the stability selection.

Type StabSelparameters

LAMfixed

True if solution for a fixed lambda should be computed. Default Value = False

Type boolean

LAMfixedparameters

object parameters to compute the lasso for a fixed lambda

Type LAMparameters

2.6 Classes used in classo_model_selection

class CLasso.solver.PATHparameters

object parameters to compute the lasso-path.

numerical method

name of the numerical method that is used, it can be: 'Path-Alg' (path algorithm), 'P-PDS' (Projected primal-dual splitting method), 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value: 'choose', which means that the function choose_numerical_method() will choose it accordingly to the formulation

Type str

n active

if it is an integer, then the algo stop computing the path when n_active variables are actives. then the solution does not change from this point. Dafault value: False

Type int or bool

lambdas

list of lambdas for computinf lasso-path for cross validation on lambda. Default value: np.array([10**(-delta*float(i)/nlam) for i in range(0,nlam)]) with delta=2. and nlam = 40

Type numpy.ndarray

plot_sigma

class CLasso.solver.CVparameters

object parameters to compute the cross-validation.

seed

Seed for random values, for an equal seed, the result will be the same. If set to False/None: pseudo-random vectors Default value: None

Type bool or int, optional

numerical method

name of the numerical method that is used, can be: 'Path-Alg' (path algorithm), 'P-PDS' (Projected primal-dual splitting method), 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value: 'choose', which means that the function choose_numerical_method() will choose it accordingly to the formulation

Type str

lambdas

list of lambdas for computinf lasso-path for cross validation on lambda. Default value : np.linspace(1., 1e-3, 500)

Type numpy.ndarray

oneSE

if set to True, the selected lambda if computed with method 'one-standard-error' Default value: True

Type bool

Nsubsets

number of subset in the cross validation method Dafault value: 5

Type int

class CLasso.solver.StabSelparameters

object parameters to compute the stability selection.

seed

Seed for random values, for an equal seed, the result will be the same. If set to False/None: pseudo-random vectors Default value: None

Type bool or int, optional

numerical_method

name of the numerical method that is used, can be: 'Path-Alg' (path algorithm), 'P-PDS' (Projected primal-dual splitting method), 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value: 'choose', which means that the function choose_numerical_method() will choose it accordingly to the formulation

Type str

lam

(only used if method = 'lam') lam for which the lasso should be computed. Default value: 'theoretical' which mean it will be equal to theoretical_lam once it is computed

Type float or str

true lam

(only used if method = `lam') True if the lambda given is the real lambda, False if it lambda/lambdamax which is between 0 and 1. If True and lam = 'theoretical', then it will takes the value n*theoretical_lam. Default value: True

Type bool

theoretical lam

(only used if method = 'lam') Theoretical lam. Default value : 0.0 (once it is not computed yet, it is computed thanks to the function theoretical_lam() used in classo_problem.solve())

Type float

method

'first', 'lam' or 'max' depending on the type of stability selection we do. Default value: 'first'

Type str

В

number of subsample considered. Default value: 50

Type int

q

number of selected variable per subsample. Default value: 10

Type int

percent nS

size of subsample relatively to the total amount of sample Default value: 0.5

Type float

lamin

lamin when computing the lasso-path for method 'max' Default value: 1e-2

Type float

hd

if set to True, then the 'max' will stop when it reaches n-k actives variables Default value: False

Type bool

threshold

threhold for stability selection Default value: 0.7

Type float

threshold label

threshold to know when the label should be plot on the graph. Default value: 0.4

Type float

class CLasso.solver.LAMfixedparameters

object parameters to compute the lasso for a fixed lambda

numerical_method

name of the numerical method that is used, can be: 'Path-Alg' (path algorithm), 'P-PDS' (Projected primal-dual splitting method), 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value: 'choose', which means that the function choose_numerical_method() will choose it accordingly to the formulation

Type str

lam

lam for which the lasso should be computed. Default value: 'theoretical' which mean it will be equal to theoretical_lam once it is computed

Type float or str

true_lam

True if the lambda given is the real lambda, False if it lambda/lambdamax which is between 0 and 1. If True and lam = 'theoretical', then it will takes the value n*theoretical_lam. Default value: True

Type bool

theoretical lam

Theoretical lam Default value: 0.0 (once it is not computed yet, it is computed thanks to the function theoretical_lam() used in classo_problem.solve())

Type float

2.7 Class classo solution

class CLasso.solver.classo_solution

Class giving characteristics of the solution of the model_selection that is asked. Before using the method solve(), its componant are empty/null.

PATH

Solution components of the model PATH

Type solution_PATH

CV

Solution components of the model CV

Type solution_CV

StabelSel

Solution components of the model StabSel

Type solution_StabSel

LAMfixed

Solution components of the model LAMfixed

Type solution_LAMfixed

2.8 Classes used in classo_solution

```
class CLasso.solver.solution_PATH (matrices, param, formulation)
     Class giving characteristics of the lasso-path computed, which also contains a method _repr_ that plot the
     graphic of this lasso-path
     BETAS
     SIGMAS
     LAMBDAS
     method
     save
     formulation
     time
class CLasso.solver.solution_CV (matrices, param, formulation)
     Class giving characteristics of the cross validation computed, which also contains a method _repr_() that plot
     the selected parameters and the solution of the not-sparse problem on the selected variables set It also contains
     a method gaphic(self, mse_max=1.,save=False) that computes the curve of validation error as a function of
     lambda
     beta
     sigma
     xGraph
     yGraph
     standard_error
     index_min
     index_1SE
     selected_param
     refit
     formulation
     time
class CLasso.solver.solution StabSel (matrices, param, formulation)
     Class giving characteristics of the stability selection computed, which also contains a method _repr_() that plot
     the selected parameters, the solution of the not-sparse problem on the selected variables set, the stability plot
     with the evolution of it with lambda if the used method is 'first'
     distribution
     lambdas_path
     selected_param
```

to_label
refit

time

formulation

```
class CLasso.solver.solution_LAMfixed (matrices, param, formulation)
    Class giving characteristics of the lasso computed which also contains a method _repr_() that plot this solution.
    beta
    sigma
    lambdamax
    selected_param
    refit
    formulation
    time
```

2.9 Example

CHAPTER

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