
classo

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FUNCTIONS OF THE PACKAGE

1.1 Random data

`CLasso.random_data` (*n*, *d*, *d_nonzero*, *k*, *sigma*, *zerosum=False*, *seed=False*, *classification=False*)

Generation of random matrices as data such that $y = X \cdot \text{sol} + \text{sigma} \cdot \text{noise}$

The data *X* is generated as a normal matrix The vector *sol* is generated randomly with a random support of size *d_nonzero*, and components are projected random integers between -10 and 10 on the kernel of *C* restricted to the support The vector *y* is then generated with $X \cdot \text{sol} + \text{sigma} \cdot \text{noise}$, with noise a normal vector

Parameters

- **n** (*int*) – Number of sample, dimension of *y*
- **d** (*int*) – Number of variables, dimension of *sol*
- **d_nonzero** (*int*) – Number of non null component of *sol*
- **k** (*int*) – Number of constraints, number of rows of *C*
- **sigma** (*float*) – size of standard error
- **zerosum** (*bool*, *optional*) – If True, then *C* is the all-one matrix with 1 row, independently of *k*
- **seed** (*bool* or *int*, *optional*) – Seed for random values, for an equal seed, the result will be the same. If set to False: pseudo-random vectors
- **classification** (*bool*, *optional*) – if True, then it returns $\text{sign}(y)$ instead of *y*

Returns tuple of three ndarray that corresponds to the data : (*X*,*C*,*y*) ndarray : array corresponding to *sol* which is the real solution of the problem $y = X \cdot \text{beta} + \text{noise}$ s.t. *beta* sparse and $C \cdot \text{beta} = 0$

Return type tuple

1.2 File converters

`CLasso.csv_to_mat` (*file*, *begin=1*, *header=None*)

Function to read a csv file and to create an ndarray with this

Parameters

- **file** (*str*) – Name of csv file
- **begin** (*int*, *optional*) – First column where it should read the matrix

- **header** (*None or int, optional*) – Same parameter as in the function `pandas.read_csv()`

Returns matrix of the csv file

Return type ndarray

`CLasso.mat_to_np(file)`

Function to read a mat file and to create an ndarray with this

Parameters **file** (*str*) – Name of mat file

Returns matrix of the mat file

Return type ndarray

1.3 Matrices normalization

`CLasso.rescale(matrices)`

Function that rescale the matrix and returns its scale

Subtract the mean of y, then divides by its norm. Also divide each column of X by its norm. This will change the solution, not only by scaling it, because then the L1 norm will affect every component equally (and not only the variables with big size)

Parameters **matrices** (*tuple*) – tuple of three ndarray matrices corresponding to (X,C,y)

Returns tuple of the three corresponding matrices after normalization tuple : tuple of the three information one need to recover the initial data : lX (list of initial column-norms of X), ly (initial norm of y), my (initial mean of y)

Return type tuple

`CLasso.clr(array, coef=0.5)`

Centered-Log-Ratio transformation

Set all negative or null entry to a constant coef. Then compute the log of each component. Then subtract the mean of each column on each column.

Parameters

- **array** (*ndarray*) – matrix nxd
- **coef** (*float, optional*) – Value to replace the zero values

Returns clr transformed matrix nxd

Return type ndarray

1.4 Theoretical lambda

`CLasso.theoretical_lam(n, d)`

Theoretical lambda as a function of the dimension of the problem

This function returns (with $\phi = \text{erf}$) :

$$4/\sqrt{n}\phi^{-1}(1-2x) \text{ such that } x = 4/d(\phi^{-1}(1-2x)4 + \phi^{-1}(1-2x)^2)$$

Which is the same (thanks to formula : $\text{norm}^{-1}(1-t) = \sqrt{2}\phi^{-1}(1-2t)$) as :

$$\sqrt{2/n} * \text{norm}^{-1}(1-k/p) \text{ such that } k = \text{norm}^{-1}(1-k/p)^4 + 2\text{norm}^{-1}(1-k/p)^2$$

Parameters

- **n** (*int*) – number of sample
- **d** (*int*) – number of variables

Returns theoretical lambda

Return type float

1.5 Numpy example

`numpy.zeros` (*shape, dtype=float, order='C'*)

Return a new array of given shape and type, filled with zeros.

Parameters

- **shape** (*int or tuple of ints*) – Shape of the new array, e.g., (2, 3) or 2.
- **dtype** (*data-type, optional*) – The desired data-type for the array, e.g., `numpy.int8`. Default is `numpy.float64`.
- **order** (*{'C', 'F'}, optional, default: 'C'*) – Whether to store multi-dimensional data in row-major (C-style) or column-major (Fortran-style) order in memory.

Returns out – Array of zeros with the given shape, dtype, and order.

Return type ndarray

See also:

zeros_like() Return an array of zeros with shape and type of input.

empty() Return a new uninitialized array.

ones() Return a new array setting values to one.

full() Return a new array of given shape filled with value.

Examples

```
>>> np.zeros(5)
array([ 0.,  0.,  0.,  0.,  0.]
```

```
>>> np.zeros((5,), dtype=int)
array([0, 0, 0, 0, 0])
```

```
>>> np.zeros((2, 1))
array([[ 0.],
       [ 0.]])
```

```
>>> s = (2,2)
>>> np.zeros(s)
array([[ 0.,  0.],
       [ 0.,  0.]])
```

```
>>> np.zeros((2,), dtype=[('x', 'i4'), ('y', 'i4')]) # custom dtype
array([(0, 0), (0, 0)],
      dtype=[('x', '<i4'), ('y', '<i4')])
```


DESCRIPTION OF THE CLASS CLASSO_PROBLEM

2.1 Classo

2.2 Class classo_problem

class `CLasso.classo_problem` ($X, y, C='zero-sum', labels=False$)

Class that contains all the information about the problem

Parameters

- \mathbf{X} (*ndarray*) – Matrix representing the data of the problem
- \mathbf{y} (*ndarray*) – Vector representing the output of the problem
- \mathbf{C} (*str or ndarray, optional*) – Matrix of constraints to the problem. If it is 'zero-sum' then the corresponding attribute will be all-one matrix. Default value to 'zero-sum'
- **rescale** (*bool, optional*) – if True, then the function `rescale()` will be applied to data when solving the problem. Default value is 'False'

label

list of the labels of each variable. If set to False then there is no label

Type list or bool

data

object containing the data of the problem.

Type *classo_data*

formulation

object containing the info about the formulation of the minimization problem we solve.

Type *classo_formulation*

model_selection

object giving the parameters we need to do variable selection.

Type *classo_model_selection*

solution

object giving characteristics of the solution of the model_selection that is asked. Before using the method `solve()`, its component are empty/null.

Type *classo_solution*

`classo_problem.solve()`

Method that solve every model required in the attributes of the problem and update the attribute `problem.solution` with the characteristics of the solution.

2.3 Class `classo_data`

class `CLasso.classo_data` (*X*, *y*, *C*, *rescale=False*)

Class containing the data of the problem

Parameters

- **X** (*ndarray*) – Matrix representing the data of the problem
- **y** (*ndarray*) – Vector representing the output of the problem
- **C** (*str or array, optional*) – Matrix of constraints to the problem. If it is ‘zero-sum’ then the corresponding attribute will be all-one matrix.
- **rescale** (*bool, optional*) – if True, then the function `rescale()` will be applied to data when solving the problem

X

Matrix representing the data of the problem

Type `ndarray`

y

Vector representing the output of the problem

Type `ndarray`

C

Matrix of constraints to the problem. If it is ‘zero-sum’ then the corresponding attribute will be all-one matrix.

Type `str or array, optional`

rescale

if True, then the function `rescale()` will be applied to data when solving the problem

Type `bool, optional`

2.4 Class `classo_formulation`

class `CLasso.solver.classo_formulation`

Class containing the data of the problem

huber

True if the formulation of the problem should be robust Default value = False

Type `bool`

concomitant

True if the formulation of the problem should be with an M-estimation of sigma. Default value = True

Type `bool`

classification

True if the formulation of the problem should be classification (if yes, then it will not be concomitant)
Default value = False

Type bool

rho

Value of rho for robust problem. Default value = 1.345

Type float

rho_classification

value of rho for huberized hinge loss function for classification (this parameter has to be negative). Default value = -1.

Type float

e

value of e in concomitant formulation. If 'n/2' then it becomes n/2 during the method solve(), same for 'n'. Default value : 'n' if huber formulation ; 'n/2' else

Type float or string

2.5 Class `classo_model_selection`

class `CLasso.solver.classo_model_selection`

Class containing the data of the problem

PATH

True if path should be computed. Default Value = False

Type bool

PATHparameters

object parameters to compute the lasso-path.

Type *PATHparameters*

CV

True if Cross Validation should be computed. Default Value = False

Type bool

CVparameters

object parameters to compute the cross-validation.

Type *CVparameters*

StabSel

True if Stability Selection should be computed. Default Value = True

Type boolean

StabSelparameters

object parameters to compute the stability selection.

Type *StabSelparameters*

LAMfixed

True if solution for a fixed lambda should be computed. Default Value = False

Type boolean

LAMfixedparameters

object parameters to compute the lasso for a fixed lambda

Type *LAMparameters*

2.6 Classes used in classo_model_selection

class `CLasso.solver.PATHparameters`

object parameters to compute the lasso-path.

numerical_method

name of the numerical method that is used, it can be : 'Path-Alg' (path algorithm) , 'P-PDS' (Projected primal-dual splitting method) , 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value : 'choose', which means that the function `choose_numerical_method()` will choose it accordingly to the formulation

Type str

n_active

if it is an integer, then the algo stop computing the path when `n_active` variables are actives. then the solution does not change from this point. Default value : False

Type int or bool

lambdas

list of lambdas for computing lasso-path for cross validation on lambda. Default value : `np.array([10**(-delta * float(i) / nlam) for i in range(0,nlam)])` with `delta=2.` and `nlam = 40`

Type numpy.ndarray

plot_sigma

class `CLasso.solver.CVparameters`

object parameters to compute the cross-validation.

seed

Seed for random values, for an equal seed, the result will be the same. If set to False/None: pseudo-random vectors Default value : None

Type bool or int, optional

numerical_method

name of the numerical method that is used, can be : 'Path-Alg' (path algorithm) , 'P-PDS' (Projected primal-dual splitting method) , 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value : 'choose', which means that the function `choose_numerical_method()` will choose it accordingly to the formulation

Type str

lambdas

list of lambdas for computing lasso-path for cross validation on lambda. Default value : `np.linspace(1., 1e-3, 500)`

Type numpy.ndarray

oneSE

if set to True, the selected lambda is computed with method 'one-standard-error' Default value : True

Type bool

Nsubsets

number of subset in the cross validation method Default value : 5

Type int

class `CLasso.solver.StabSelparameters`

object parameters to compute the stability selection.

seed

Seed for random values, for an equal seed, the result will be the same. If set to False/None: pseudo-random vectors Default value : None

Type bool or int, optional

numerical_method

name of the numerical method that is used, can be : 'Path-Alg' (path algorithm) , 'P-PDS' (Projected primal-dual splitting method) , 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value : 'choose', which means that the function `choose_numerical_method()` will choose it accordingly to the formulation

Type str

lam

(only used if `method = 'lam'`) lam for which the lasso should be computed. Default value : 'theoretical' which mean it will be equal to `theoretical_lam` once it is computed

Type float or str

true_lam

(only used if `method = 'lam'`) True if the lambda given is the real lambda, False if it lambda/lambda_max which is between 0 and 1. If True and lam = 'theoretical' , then it will takes the value `n*theoretical_lam`. Default value : True

Type bool

theoretical_lam

(only used if `method = 'lam'`) Theoretical lam. Default value : 0.0 (once it is not computed yet, it is computed thanks to the function `theoretical_lam()` used in `classo_problem.solve()`)

Type float

method

'first', 'lam' or 'max' depending on the type of stability selection we do. Default value : 'first'

Type str

B

number of subsample considered. Default value : 50

Type int

q

number of selected variable per subsample. Default value : 10

Type int

percent_nS

size of subsample relatively to the total amount of sample Default value : 0.5

Type float

lamin

lamin when computing the lasso-path for method 'max' Default value : 1e-2

Type float

hd

if set to True, then the 'max' will stop when it reaches n-k actives variables Default value : False

Type bool

threshold

threshold for stability selection Default value : 0.7

Type float

threshold_label

threshold to know when the label should be plot on the graph. Default value : 0.4

Type float

class CLasso.solver.LAMfixedparameters

object parameters to compute the lasso for a fixed lambda

numerical_method

name of the numerical method that is used, can be : 'Path-Alg' (path algorithm) , 'P-PDS' (Projected primal-dual splitting method) , 'PF-PDS' (Projection-free primal-dual splitting method) or 'DR' (Douglas-Rachford-type splitting method) Default value : 'choose', which means that the function `choose_numerical_method()` will choose it accordingly to the formulation

Type str

lam

lam for which the lasso should be computed. Default value : 'theoretical' which mean it will be equal to `theoretical_lam` once it is computed

Type float or str

true_lam

True if the lambda given is the real lambda, False if it lambda/lambda_max which is between 0 and 1. If True and lam = 'theoretical' , then it will takes the value n*theoretical_lam. Default value : True

Type bool

theoretical_lam

Theoretical lam Default value : 0.0 (once it is not computed yet, it is computed thanks to the function `theoretical_lam()` used in `classo_problem.solve()`)

Type float

2.7 Class classo_solution

class CLasso.solver.classo_solution

Class giving characteristics of the solution of the model_selection that is asked. Before using the method `solve()` , its component are empty/null.

PATH

Solution components of the model PATH

Type *solution_PATH*

CV

Solution components of the model CV

Type *solution_CV*

StabSel

Solution components of the model StabSel

Type *solution_StabSel*

LAMfixed

Solution components of the model LAMfixed

Type *solution_LAMfixed*

2.8 Classes used in classo_solution

class `CLasso.solver.solution_PATH` (*matrices, param, formulation*)

Class giving characteristics of the lasso-path computed, which also contains a method `_repr_` that plot the graphic of this lasso-path

BETAS

array of size `Npath x d` with the solution beta for each lambda on each row

Type `numpy.ndarray`

SIGMAS

array of size `Npath` with the solution sigma for each lambda when the formulation of the problem is R2 or R4

Type `numpy.ndarray`

LAMBDAS

array of size `Npath` with the lambdas (real lambdas, not divided by `lambda_max`) for which the solution is computed

Type `numpy.ndarray`

method

name of the numerical method that has been used. It can be 'Path-Alg', 'P-PDS', 'PF-PDS' or 'DR'

Type `str`

save

if it is a str, then it gives the name of the file where the graphics has been/will be saved (after using `print(solution)`)

Type `bool` or `str`

formulation

can be 'R1' ; 'R2' ; 'R3' ; 'R4' ; 'C1' ; 'C2'

Type `str`

time

running time of this action

Type `float`

class `CLasso.solver.solution_CV` (*matrices, param, formulation*)

Class giving characteristics of the cross validation computed, which also contains a method `_repr_()` that plot the selected parameters and the solution of the not-sparse problem on the selected variables set It also contains a method `gaphic(self, mse_max=1.,save=False)` that computes the curve of validation error as a function of lambda

xGraph

array of size `Nlambdas` of the lambdas / `lambda_max`

Type `numpy.ndarray`

yGraph

array of size `Nlambdas` of the average validation residual (over the `K` subsets)

Type `numpy.ndarray`

standard_error

array of size `Nlambdas` of the standard error of the validation residual (over the `K` subsets)

Type `numpy.ndarray`

index_min
 index on xGraph of the selected lambda without 1-standard-error method
Type int

index_1SE
 index on xGraph of the selected lambda with 1-standard-error method
Type int

lambda_min
 selected lambda without 1-standard-error method
Type float

lambda_oneSE
 selected lambda with 1-standard-error method
Type float

beta
 solution beta of classo at lambda_oneSE
Type numpy.ndarray

sigma
 solution sigma of classo at lambda_oneSE when formulation is 'R2' or 'R4'
Type float

selected_param
 boolean arrays of size d with True when the variable is selected
Type numpy.ndarray

refit
 solution beta after solving unsparse problem over the set of selected variables.
Type numpy.ndarray

formulation
 can be 'R1' ; 'R2' ; 'R3' ; 'R4' ; 'C1' ; 'C2'
Type str

time
 running time of this action
Type float

class CLasso.solver.solution_StabSel (*matrices, param, formulation*)

Class giving characteristics of the stability selection computed, which also contains a method `_repr_()` that plot the selected parameters, the solution of the not-sparse problem on the selected variables set, the stability plot with the evolution of it with lambda if the used method is 'first'

distribution
 d array of stability rations.
Type array

lambdas_path
 for 'first' method : N_lambdas array of the lambdas used. Other cases : 'not used'
Type array or string

distribution_path

for 'first' method : N_lambdas x d array with stability ratios as a function of lambda. Other cases : 'not computed'

Type array or string

threshold

threshold for StabSel, ie for a variable i, stability ratio that is needed to get selected

Type float

save1, save2, save3

if a string is given, the corresponding graph will be saved with the given name of the file (save1 is for stability plot ; save2 for path-stability plot; and save3 for refit beta-solution)

Type bool or string

selected_param

boolean arrays of size d with True when the variable is selected

Type numpy.ndarray

to_label

list that indicates the index of the True-components of selected_param (useful to find the right label in _repr_() method)

Type list of int

refit

solution beta after solving unsparse problem over the set of selected variables.

Type numpy.ndarray

formulation

can be 'R1' ; 'R2' ; 'R3' ; 'R4' ; 'C1' ; 'C2'

Type str

time

running time of this action

Type float

class CLasso.solver.solution_LAMfixed(*matrices, param, formulation*)

Class giving characteristics of the lasso computed which also contains a method _repr_() that plot this solution.

lambdamax

lambda maximum for which the solution is non-null

Type float

true_lam

if False, it means that the problem had been computed for lambda*lambdamax (so lambda should be between 0 and 1)

Type bool

lambda

lambda for which the problem is solved

Type float

beta

solution beta of classo

Type numpy.ndarray

sigma

solution sigma of classo when formulation is 'R2' or 'R4'

Type float

selected_param

boolean arrays of size d with True when the variable is selected (which is the case when the i-th component solution of the classo is non-null)

Type numpy.ndarray

refit

solution beta after solving unsparse problem over the set of selected variables.

Type numpy.ndarray

formulation

can be 'R1' ; 'R2' ; 'R3' ; 'R4' ; 'C1' ; 'C2'

Type str

time

running time of this action

Type float

2.9 Example

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