STAT2005 Programming Languages for Statistics Exercise for Chapter 2

- 1. Mary is living in an integer-valued one-dimensional space. She is initially at the origin at x = 0. She can either move to the left or right by 1 or 2 units in each second with equal probabilities. E.g. If Mary is at 0, she can move to -2, -1, 1, 2, in a second with equal probabilities.
- (a) Using a random seed 2005, write R codes to simulate Mary's movements during the first 120 seconds. Draw the path over time.
- (b) Plot two red dashed horizontal lines at the maximum and minimum of the path.
- 2. (a) Using a random seed 2005, generate 1,000 pseudorandom numbers from $X \sim N(3,4)$, store them in a vector named x.
- (b) Generate 2,000 pseudorandom numbers from $Y \sim N(1,4)$, store them in a vector named y. Assume that the population mean and standard deviations of X and Y are unknown to us, but we know that their standard deviations are the same. Write R codes to find the pooled standard deviation of x and y and store it into a variable named PooledSD. The formula of pooled standard deviation is

$$s_p = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}},$$

where n_1 , n_2 are the sample size of x and y, s_1^2 and s_2^2 are the sample variance of x and y.

(c) We are interested to perform a two-sample t-test for x and y.

$$H_0$$
: $\mu_1 = \mu_2$ vs. H_1 : $\mu_1 \neq \mu_2$,

where μ_1 , μ_2 are the unknown population means of X and Y/Write R codes to find the following t-statistics and compute the corresponding critical value at 95% significance level. The t-statistics is given by

$$t = \frac{(\overline{x} - \overline{y})}{s_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}} \sim t_{n_1 + n_2 - 2},$$

where t_{df} denotes the t-distribution with df degrees of freedom.

3. The file $ex2_q3$. dat stores the data of the GDP (Gross Domestic Product) for 26 countries (from "A" to "Z") in the first and second year. The variables are

Country: Country label from "A" to "Z";

gdp1: GDP of the first year;

gdp2: GDP of the second year;

Region: Each country belongs to one of the four regions "East", "South", "West" or "North".

- (a) Write R codes to read gdp.dat as a data.frame object named data. Display the first 6 data.
- (b) Write R codes to find the mean of gdp1 in each region.

1. (a).

- (c) Using the by () function, compute the sum of values in column gdp1 and gdp2.
- (d) Draw a scatter plot of gdp1 and gdp2 to show the relationship between GDP in the first and second year. Do you find any linear relation between the two?

```
set, seed (2025)
 moves < sample ( c(-2,-111,2), size = 100, replace = T, prob = c(0.25,0.7,0.7,0.8))
 pos - cumsum (c(o, moves))
 pos ← as.ts ( pos)
 plot (pos)
 (b)
  max-pos - max (pos)
  min_ pos - min (pos)
   abline (h = max - pos, col = "red", Ity = "dashed")
   abline ( n = min - pos, col = "red", Ity = "dashed")
2(1)
 Set. seed (2023)
  x< morm(1000, 3,4)
 (h)
  y < rnorm (2000, ()*)
   n1 ← length (x)
   n2 < longth (y)
   $1_2 \leftarrow \text{Var}(x)
    S_{2-2} \leftarrow var(y)
    Pooled SD \leftarrow Sqrt((n1-1) \times S1-2+(n2-1) \times S2-2) / (n1+n2-2))
(c)
   X_mean & mean (X)
   y-meane-mean cy)
   t \leftarrow (x_{mean} - y_{mean}) / (Pooled SD * Sqrt (1/n1 + 1/n2))
   (abs(t) >qt(0.975, n1+n2-2))
3. (a)
  data < read. consuc " gdp.det", header = T)
  head (idata)
  By (dota & golp 1, data & Kegion, mean)
     for vector, use tapply Region //, use by is also OK
 (C)
   by cdata [,cc 2,3)], data Svegion, colSum)
  rd). Plot ( data & gdp1, data & gdp2)
```