

Tarefas Básicas - Aula 5

1.

$$\text{geratriz} = 20 \text{ cm}$$

$$20^2 = 10^2 + h^2$$

$$400 = 100 + h^2$$

$$h^2 = 300$$

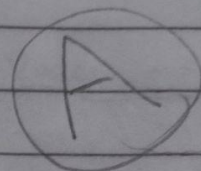
$$h = \sqrt{300}$$

$$h = 10\sqrt{3} \text{ cm}$$

$$\frac{\pi(20)^2}{2} = \pi r \cdot 20$$

$$200 = 20r$$

$$r = 10$$



2.

$$V = \frac{\pi r^2 h}{3}$$

$$64\pi = \frac{\pi r^2 \cdot 12}{3}$$

$$64 = r^2 \cdot 4$$

$$r^2 = 64/4$$

$$r = \sqrt{16} = 4 \text{ cm}$$

$$g^2 = h^2 + r^2$$

$$g^2 = 12^2 + 4^2$$

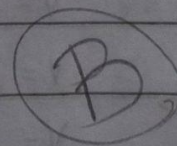
$$g^2 = 144 + 16$$

$$g = \sqrt{160}$$

$$g = \sqrt{2^2 \cdot 2^2 \cdot 2 \cdot 5}$$

$$g = 4\sqrt{10}$$

$$\begin{array}{r|l} 160 & 27 \cdot 2^2 \\ 80 & 2 \\ 40 & 27 \cdot 2^2 \\ 20 & 2 \\ 10 & 27 \cdot 2 \cdot 5 \\ 5 & 5 \\ 1 & \end{array}$$



3.

$$r = h = 6 \text{ cm}$$

$$S_b = 36\pi \text{ cm}^2$$

$$V = ?$$

$$S_b = \pi r^2$$

$$36\pi = \pi r^2$$

$$36 = r^2$$

$$r = \sqrt{36}$$

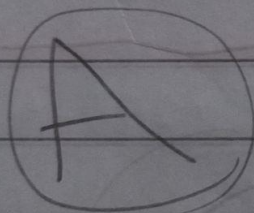
$$r = 6 \text{ cm} = h$$

$$V = \frac{\pi r^2 h}{3}$$

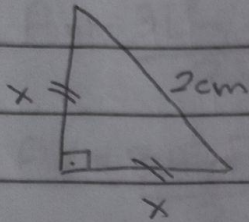
$$V = \frac{\pi 36 \cdot 6}{3}$$

$$V = \pi 36 \cdot 2$$

$$V = 72\pi$$



4.

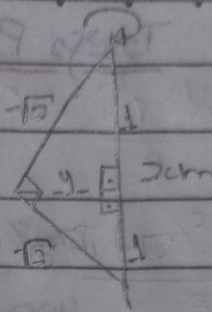


$$2^2 = x^2 + x^2$$

$$4 = 2x^2$$

$$x^2 = 2$$

$$x = \sqrt{2}$$

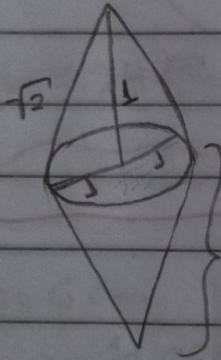


$$2^2 = y^2 + 1^2$$

$$2 = y^2 + 1$$

$$y = \sqrt{1}$$

$$y = 1$$

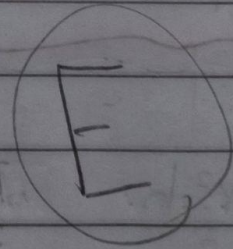


$$V = \frac{\pi \cdot 1^2 \cdot 1}{3}$$

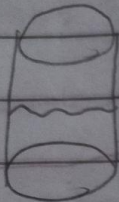
$$V = \frac{\pi \cdot 1}{3}$$

$$V = \frac{\pi \cdot 1}{3} \cdot 2 \Rightarrow \frac{2\pi}{3}$$

$$\frac{2\pi}{3}$$



5.



$$V = \pi \cdot 3^2 \cdot 10$$

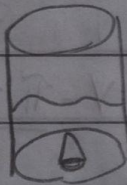
$$V = \pi \cdot 90 (\div 2)$$

$$V = 45\pi$$

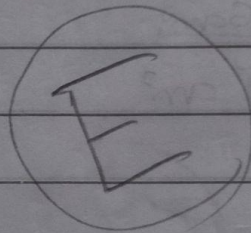
$$V = \pi \cdot 3^2 \cdot 3$$

$$A \rightarrow$$

$$V = \pi$$



$$\rightarrow (45\pi) - \pi = \frac{44\pi}{1}$$



6.

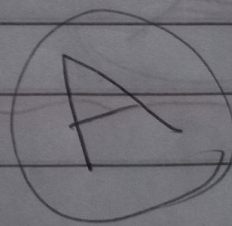
$$V_p = \frac{b \cdot h^2}{3}$$

$$V_c = \frac{b \cdot h}{3}$$

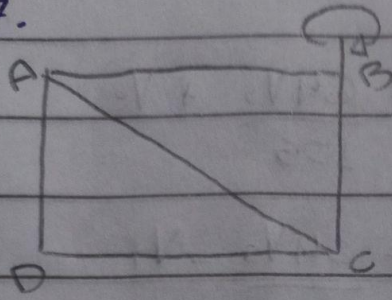
$$\frac{b \cdot h^2}{3}$$

$$\frac{b \cdot h}{3}$$

$$= \frac{2}{1} = 2$$



7.



Simulando valores:

$$\overline{AB} = 2$$

$$\overline{AD} = 1$$

$$V_{ABC} = \frac{\pi \cdot 2^2 \cdot 1}{3} = \boxed{\frac{4\pi}{3}}$$

$$V_{ADC} = (\pi \cdot 2^2 \cdot 1) - V_{ABC}$$

$$V_{ADC} = \frac{4\pi}{1} - \frac{4\pi}{3}$$

Razão:

$$\frac{V_{ABC}}{V_{ADC}}$$

$$\frac{4\pi}{3}$$

$$\frac{4\pi}{3}$$

$$= \frac{4}{8}$$

$$\frac{8\pi}{3}$$

2

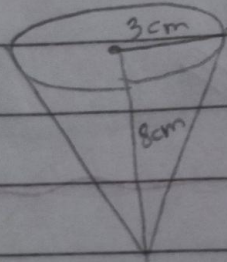
E

$$V_{ADC} = \frac{12\pi - 4\pi}{3}$$

$$V_{ADC} = \frac{8\pi}{3}$$

$$\boxed{\frac{1}{2}}$$

1.



$$V_t = \frac{\pi 3^2 \cdot 8}{3}$$

$$V_{pl/liquido} = \frac{24\pi}{2} = 12\pi \text{ cm}^3$$

$$V_t = \pi 3 \cdot 8$$

$$V_t = 24\pi \text{ cm}^3 \rightarrow$$

$$\frac{V_t}{V} = \frac{h^3}{h^3}$$

$$24\pi = 8^3$$

$$12\pi = h^3$$

$$2 = \frac{8^3}{h^3}$$

$$2h^3 = 8^3$$

$$h^3 = \frac{512}{2}$$

$$h = \sqrt[3]{256}$$

$$h = \sqrt[3]{2^3 \cdot 2^5 \cdot 2^3}$$

$$h = 4\sqrt[3]{4} \text{ cm}$$

$$\begin{array}{r|l} 256 & 2 \\ \hline 128 & 2 \\ 64 & 2 \\ 32 & 2 \\ 16 & 2 \\ 8 & 2 \\ 4 & 2 \\ 2 & 2 \\ 1 & \end{array}$$

(C)

2.

$V_t = \text{Total}$

$V_s = \text{Sorvete}$

$V_e = \text{Espuma}$

$$\frac{V_s}{V_t} = \left(\frac{16}{20}\right)^3$$

$$\frac{V_s}{V_t} = \frac{4^3}{5^3}$$

$$V_t = \frac{64V_s}{125} + V_e$$

$$V_e = \frac{64V_s}{125} - V_t$$

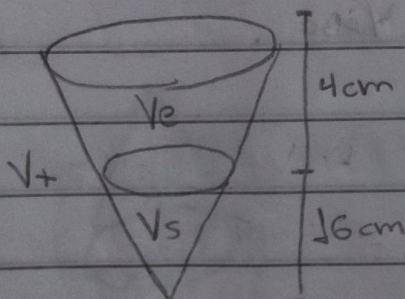
$$\frac{V_s}{V_t} = \frac{64}{125}$$

$$V_s = \frac{64V_t}{125}$$

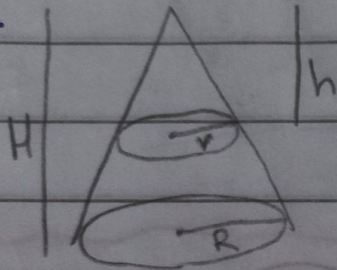
$$V_e = \frac{64V_s}{125}$$

$$V_e = 0,488V_s$$

$$V_e \approx 50\%$$



3.



$$\frac{1}{2} = \left(\frac{h}{H}\right)^3$$

$$h = \frac{\sqrt[3]{H^3}}{\sqrt[3]{2}}$$

$$\frac{1}{2} = \frac{h^3}{H^3}$$

$$h = \frac{H}{\sqrt[3]{2}} \cdot \frac{\sqrt[3]{2^3}}{\sqrt[3]{2^3}}$$

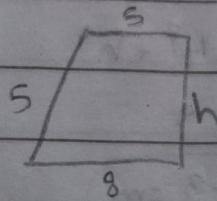
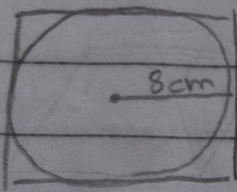
$$\frac{V_2}{V_1} = \frac{1}{2}$$

$$H^3 = 2h^3$$

$$h = \frac{H \sqrt[3]{4}}{2}$$

$$h^3 = \frac{H^3}{2}$$

4.



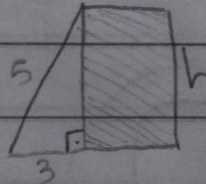
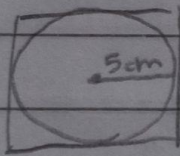
$$5^2 = h^2 + 3^2$$

$$25 = h^2 + 9$$

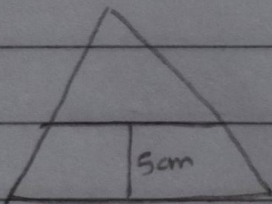
$$h^2 = 16$$

$$h = \sqrt{16}$$

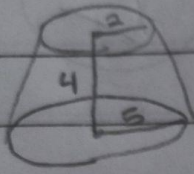
$$h = 4 \text{ cm}$$



4 cm



5.



$$V = \frac{\pi \cdot 4}{3} (5^2 + 10 + 2^2)$$

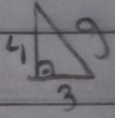
$$A_1 = \pi \cdot 5 (2 + 5)$$

$$A_1 = 35\pi$$

$$V = \frac{4\pi}{3} (25 + 10 + 4)$$

$$A_2 = \pi \cdot 5^2 = 25\pi$$

$$A_3 = \pi \cdot 2^2 = 4\pi$$



$$g^2 = 4^2 + 3^2$$

$$g^2 = 16 + 9$$

$$g = \sqrt{25}$$

$$g = 5 \text{ m}$$

$$V = \frac{4\pi \cdot 39}{3}$$

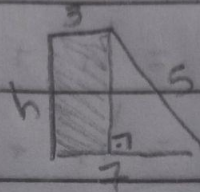
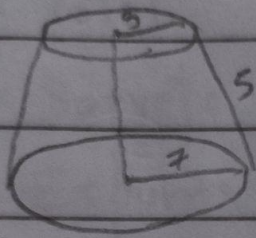
$$V = \frac{156\pi}{3}$$

$$V = 52\pi$$

$$A = 35\pi + 25\pi + 4\pi$$

$$A = 64\pi$$

6.



$$5^2 = 4^2 + h^2$$

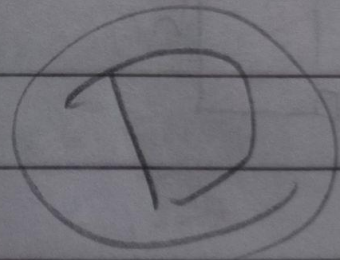
$$h^2 = 9$$

$$h = 3 \text{ cm}$$

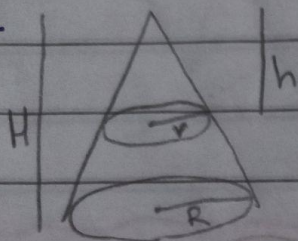
$$V = \frac{\pi \cdot 3}{3} (7^2 + 21 + 3^2)$$

$$V = \pi \cdot 49 + 21 + 9$$

$$V = 79\pi$$



7.



$$\frac{1}{2} = \left(\frac{h}{H}\right)^3$$

$$\frac{1}{2} \neq \frac{h^3}{H^3}$$

$$h = \frac{\sqrt[3]{H^3}}{\sqrt[3]{2}}$$

$$h = H \cdot \frac{\sqrt[3]{2^3}}{\sqrt[3]{2^3}}$$

$$\frac{V_2}{V_1} = \frac{1}{2}$$

$$H^3 = 2h^3$$

$$h^3 = \frac{H^3}{2}$$

$$h = \frac{H \sqrt[3]{4}}{2}$$

