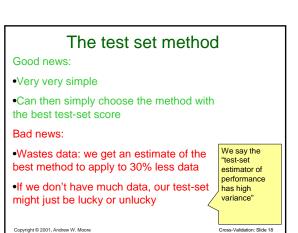
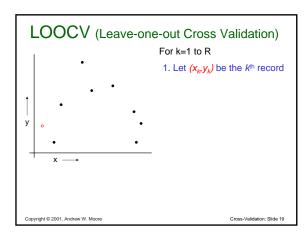
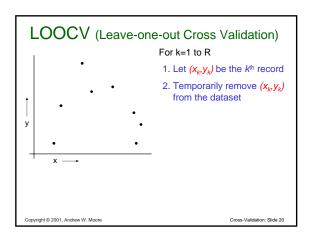
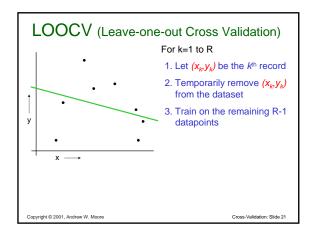


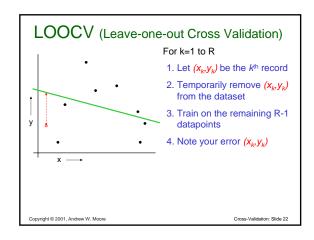
# The test set method Good news: •Very very simple •Can then simply choose the method with the best test-set score Bad news: •What's the downside? Copyright © 2001, Andrew W. Moore Cross-Validation: Slide 17

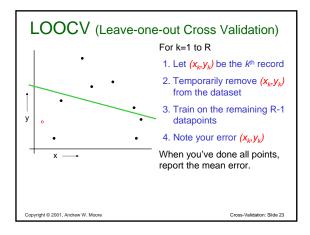


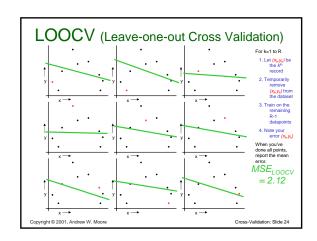


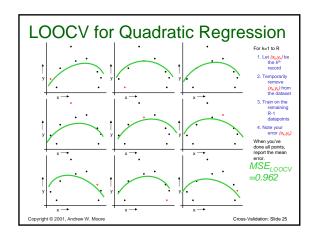


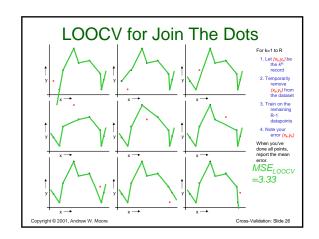


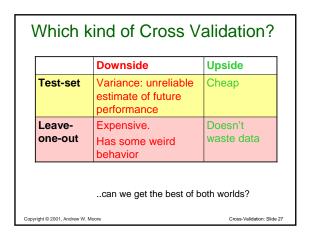


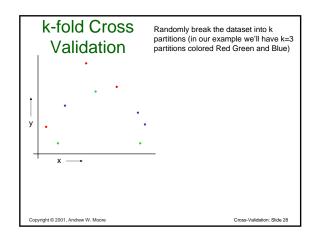


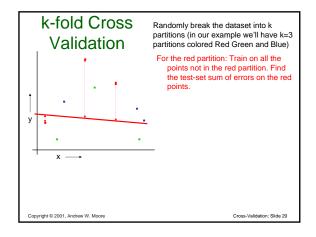


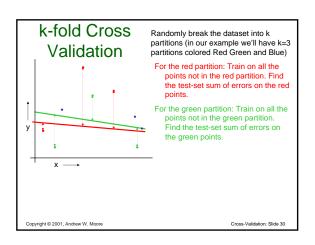


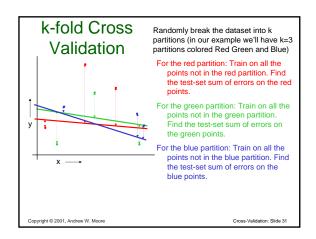


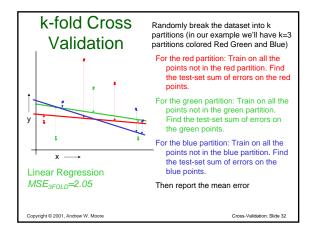


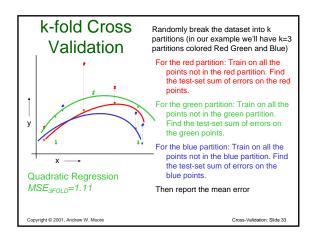


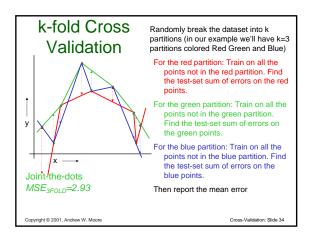












	Downside	Upside	
Test-set	st-set Variance: unreliable estimate of future performance Cheap		
Leave- one-out	Expensive. Has some weird behavior	Doesn't waste data	
10-fold	Wastes 10% of the data. 10 times more expensive than test set	Only wastes 10%. Only 10 times more expensive instead of R times.	
3-fold	Wastier than 10-fold. Expensivier than test set	Slightly better than test- set	
R-fold	Identical to Leave-one-out		

Which kind of Cross Validation?					
	Downside	Upside			
Test-set	Variance: unreliable estimate of future performance	Cheap			
Leave- one-out	Evnoncivo	But note: One of Andrew's joys in life is algorithmic tricks for			
10-fold	Wastes 10% of the data making these cheap 10 times more expensive than testset instead of R times.				
3-fold	Wastier than 10-fold. Expensivier than testset	Slightly better than test- set			
R-fold	Identical to Leave-one-ou	t			
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## CV-based Model Selection

- We're trying to decide which algorithm to use.
- · We train each machine and make a table...

i	$f_i$	TRAINERR	10-FOLD-CV-ERR	Choice
1	$f_1$			
2	$f_2$			
3	$f_3$			$\boxtimes$
4	f <sub>4</sub>			
5	$f_5$			
6	$f_6$	I		

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## Alternatives to CV-based model selection Model selection methods: 1. Cross-validation 2. AIC (Akaike Information Criterion) 3. BIC (Bayesian Information Criterion) 4. VC-dimension (Vapnik-Chervonenkis Dimension) Only directly applicable to choosing classifiers

Described in a future Andrew Lecture

### Which model selection method is best?

- 1. (CV) Cross-validation
- 2. AIC (Akaike Information Criterion)
- 3. BIC (Bayesian Information Criterion)
- 4. (SRMVC) Structural Risk Minimize with VC-dimension
- AIC, BIC and SRMVC advantage: you only need the training error.
- CV error might have more variance
- SRMVC is wildly conservative
- Asymptotically AIC and Leave-one-out CV should be the same
- Asymptotically BIC and carefully chosen k-fold should be same
   You want BIC you want the best structure instead of the best
- predictor (e.g. for clustering or Bayes Net structure finding)

   Many alternatives---including proper Bayesian approaches.
- It's an emotional issue.

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ss-Validation: S

### Other Cross-validation issues

- Can do "leave all pairs out" or "leave-allntuples-out" if feeling resourceful.
- Some folks do k-folds in which each fold is an independently-chosen subset of the data
- Do you know what AIC and BIC are?
   If so...
  - LOOCV behaves like AIC asymptotically.
  - k-fold behaves like BIC if you choose k carefully If not
  - Nyardely nyardely nyoo nyoo

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ross-Validation: Slide 40

### Cross-Validation for regression

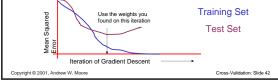
- Choosing the number of hidden units in a neural net
- Feature selection (see later)
- · Choosing a polynomial degree
- · Choosing which regressor to use

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Cross-Validation: Slide 41

### Supervising Gradient Descent

- This is a weird but common use of Test-set validation
- Suppose you have a neural net with too many hidden units. It will overfit.
- As gradient descent progresses, maintain a graph of MSE-testset-error vs. Iteration



# Supervising Gradient Descent This is a weird but common use of Test-set validation Suppose you have real net with too many hidder Relies on an intuition that a not-fully-minimized set of weights is somewhat like having fewer parameters. Works pretty well in practice, apparently Use the weights you found on this iteration Training Set Test Set

### Cross-validation for classification

 Instead of computing the sum squared errors on a test set, you should compute...

yright © 2001, Andrew W. Moore Cross-Validation:

### Cross-validation for classification

• Instead of computing the sum squared errors on a test set, you should compute...

The total number of misclassifications on a testset.

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### Cross-validation for classification

• Instead of computing the sum squared errors on a test set, you should compute...

The total number of misclassifications on a testset.

• But there's a more sensitive alternative:

Compute

log P(all test outputs|all test inputs, your model)

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Cross-Validation: Slide 46

### Cross-Validation for classification

- Choosing the pruning parameter for decision trees
- Feature selection (see later)
- What kind of Gaussian to use in a Gaussianbased Bayes Classifier
- · Choosing which classifier to use

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Cross-Validation: Slide 47

## Cross-Validation for density estimation

• Compute the sum of log-likelihoods of test points

### Example uses:

- Choosing what kind of Gaussian assumption to use
- Choose the density estimator
- NOT Feature selection (testset density will almost always look better with fewer features)

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Cross-Validation: Slide 48

### **Feature Selection**

- · Suppose you have a learning algorithm LA and a set of input attributes  $\{X_1, X_2 ... X_m\}$
- · You expect that LA will only find some subset of the attributes useful.
- · Question: How can we use cross-validation to find a useful subset?
- · Four ideas:
  - · Forward selection
  - Backward elimination

· Hill Climbing

• Stochastic search (Simulated Annealing or GAs)

Another fun area in which wild youth

Andrew has spent a lot of his

· What can be done about it?

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• How?

### Very serious warning

- Intensive use of cross validation can overfit.
- - Imagine a dataset with 50 records and 1000 attributes.
  - You try 1000 linear regression models, each one using one of the attributes.
- · What can be done about it?

### Very serious warning

Very serious warning
• Intensive use of cross validation can overfit.

- Intensive use of cross validation can overfit.
- - Imagine a dataset with 50 records and 1000 attributes.
  - You try 1000 linear regression models, each one using one of the attributes.
  - The best of those 1000 looks good!
- · What can be done about it?

### Very serious warning

- Intensive use of cross validation can overfit.
- How?
  - Imagine a dataset with 50 records and 1000 attributes.
  - You try 1000 linear regression models, each one using one of the attributes.
  - The best of those 1000 looks good!
  - But you realize it would have looked good even if the output had been purely random!
- · What can be done about it?
  - · Hold out an additional testset before doing any model selection. Check the best model performs well even on the additional testset.

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### What you should know

- Why you can't use "training-set-error" to estimate the quality of your learning algorithm on your data.
- Why you can't use "training set error" to choose the learning algorithm
- · Test-set cross-validation
- · Leave-one-out cross-validation
- · k-fold cross-validation
- Feature selection methods
- · CV for classification, regression & densities