


Putting it all together

$$P(\text{E} \text{ } \text{ } \text{ } \text{ } | \text{ }) = \frac{P(\text{ } | \text{E} \text{ } \text{ } \text{ }) P(\text{E} | \text{ }) P(\text{ }) P(\text{ }) P(\text{ })}{P(\text{ })}$$


Alignment


Chronogram


Branching model
(can be an epi model)

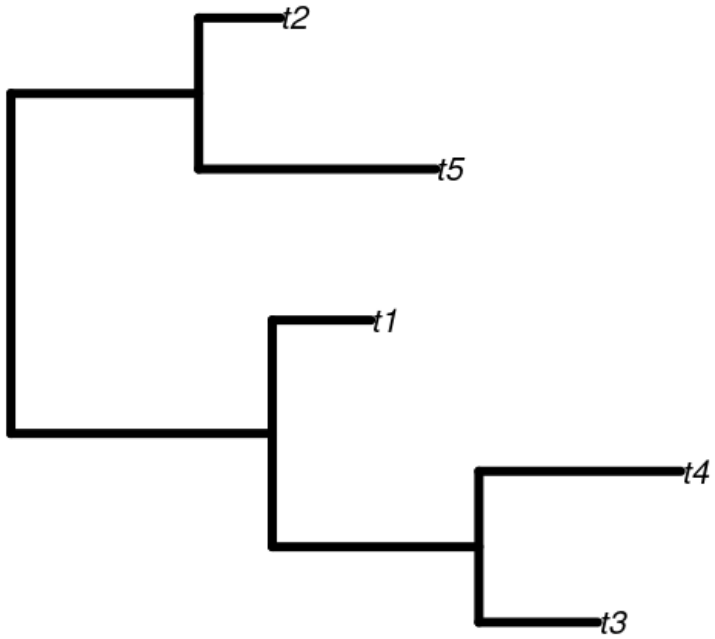

Substitution
model


Clock
model

- HKY+G: 2 parameters (kappa, shape)
- Coalescent exponential: 2 parameters (growthRate, ePopSize)
- UCLN clock model: 2 parameters (ucldMean, ucldStdev)*

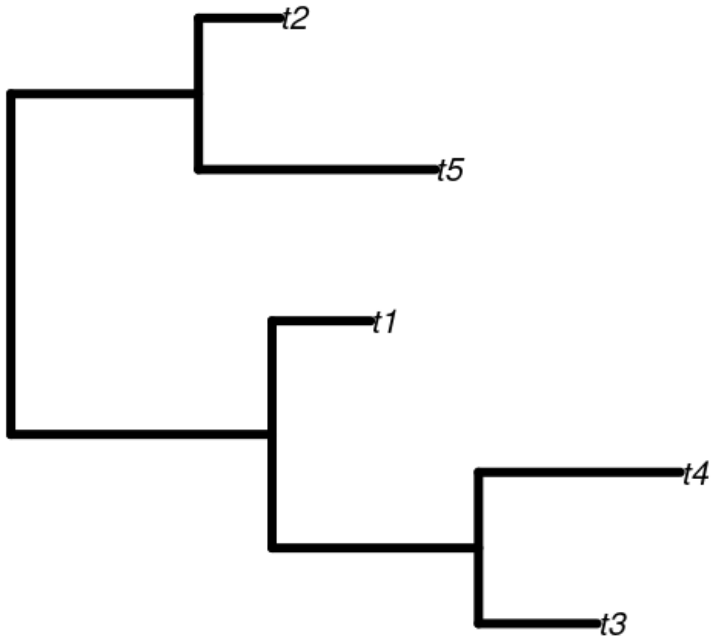
* arguably the branch lengths are also parameters, but they are much less tractable.

Exp. Coalescent:
growthRate, ePopSize



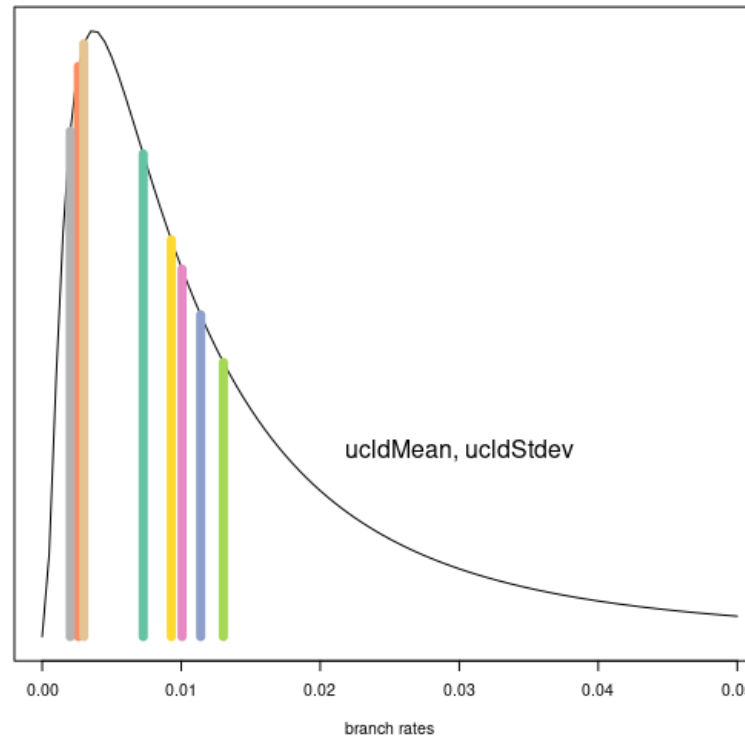
Chronogram or time tree

Exp. Coalescent:
growthRate, ePopSize



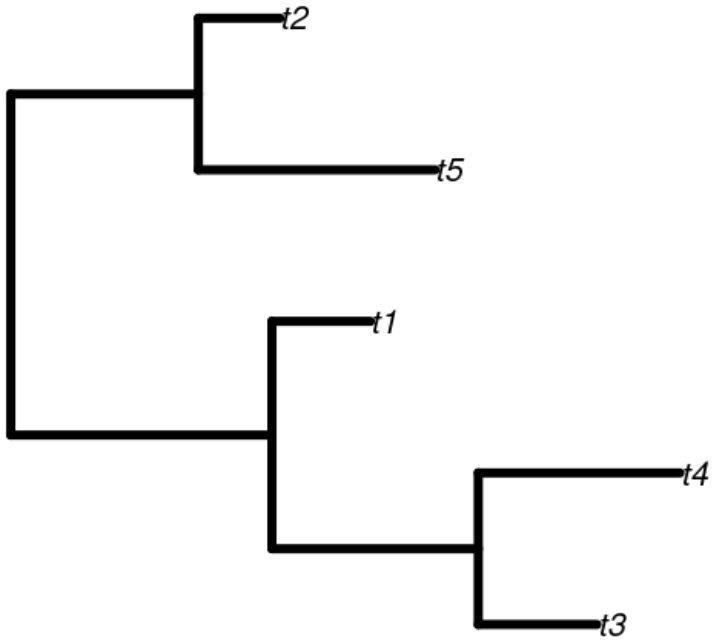
Chronogram or time tree

UCLN clock model:
uclMean, uclStdev



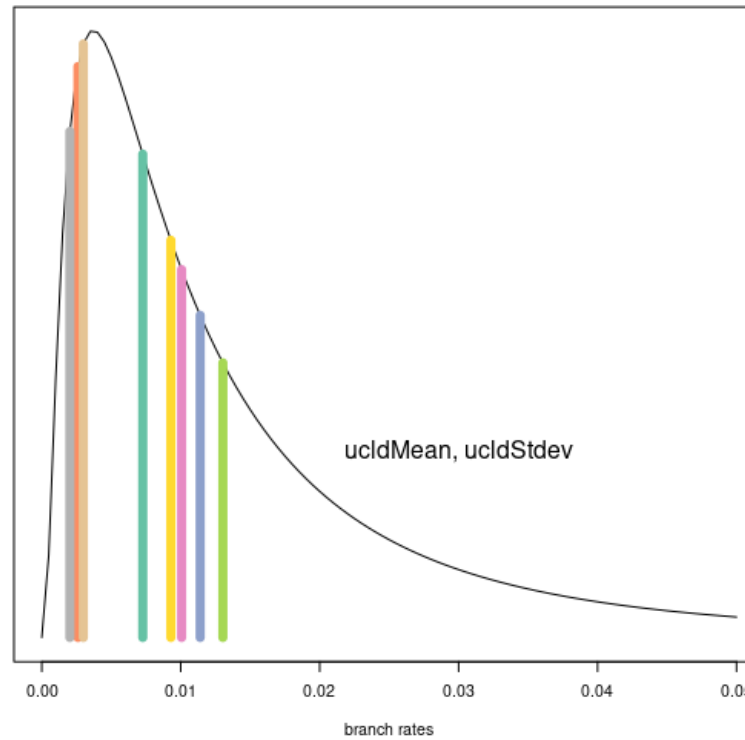
Branch rates

Exp. Coalescent:
growthRate, ePopSize



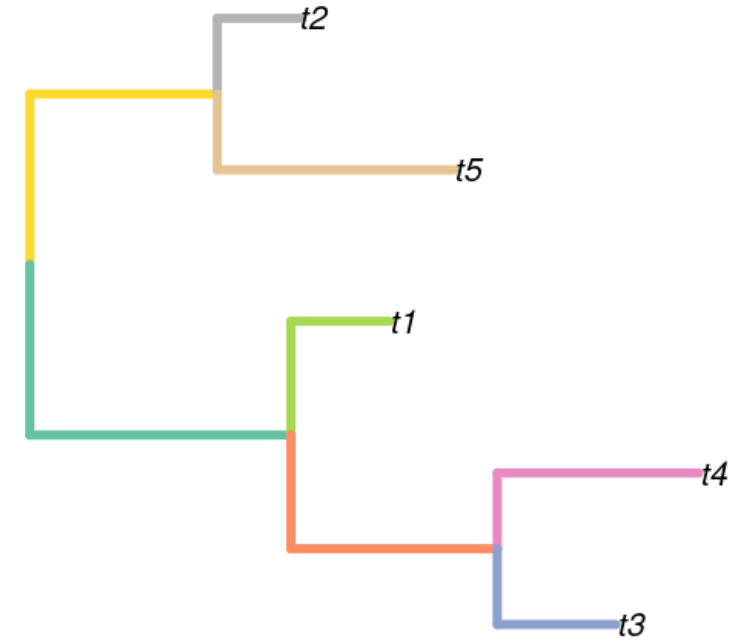
Chronogram or time tree

UCLN clock model:
uclMean, uclStdev



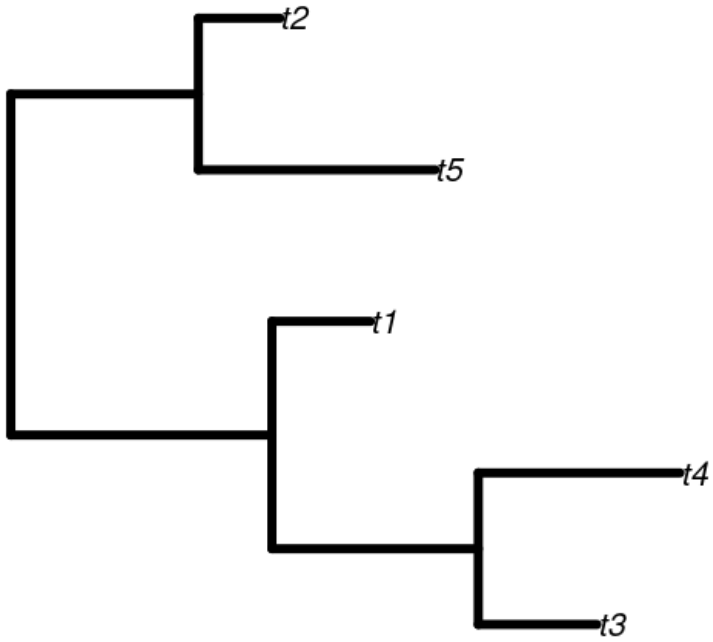
Branch rates

Branch rates * times



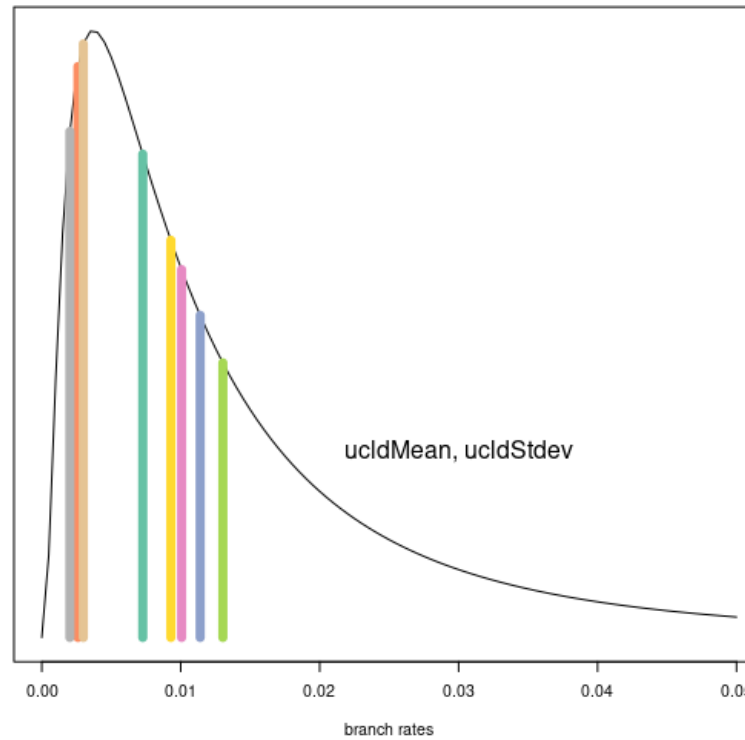
Phylogram

Exp. Coalescent:
growthRate, ePopSize



Chronogram or time tree

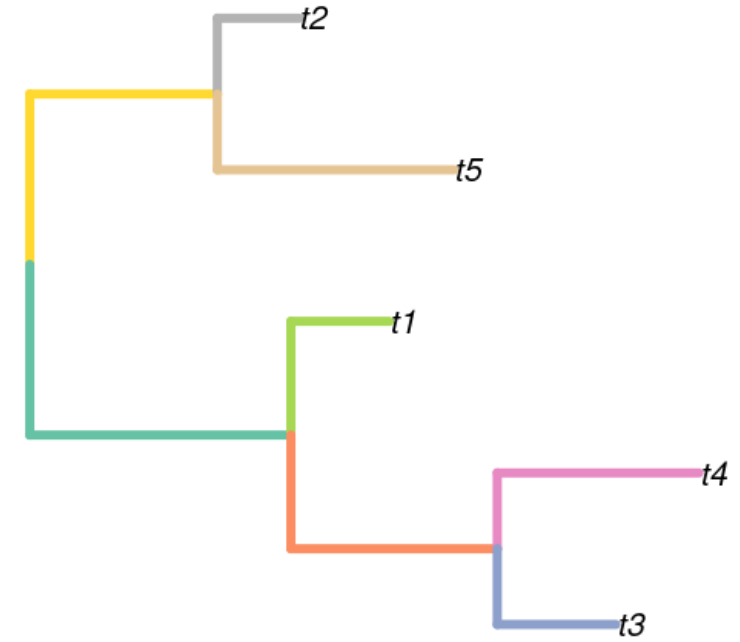
UCLN clock model:
uclMean, uclStdev



Branch rates

Kappa, gammaShape

Branch rates * times



Phylogram

treeLikelihood or likelihood:

$$P(\text{alignment} \mid \text{kappa}, \text{gammaShape},$$

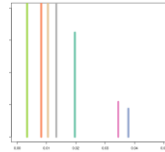


coalescentExponential:

$$P(\text{tree} \mid \text{growthRate}, \text{ePopSize})$$

Density of branch rates:

$$P(\text{branch rates} \mid \text{ucldMean}, \text{ucldStdev})$$



Prior on subst model:
parameters

$$P(\text{kappa}) * P(\text{gammaShape})$$

(hyper)prior on clock model:
parameters

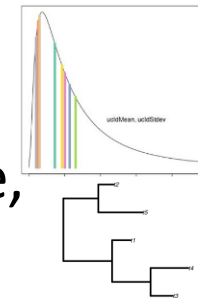
$$P(\text{ucldMean}) * P(\text{ucldStdev})$$

(hyper)prior on tree prior:
parameters

$$P(\text{growthRate}) * P(\text{ePopSize})$$

We do not typically log
these prior probabilities
individually, but we can
inspect the individual
parameters

treeLikelihood or likelihood: $P(\text{alignment} \mid \text{kappa}, \text{gammaShape}, \text{ucldMean}, \text{ucldStdev})$



coalescentExponential:

$P(\text{tree} \mid \text{growthRate}, \text{ePopSize})$

Prior on clock parameters:

$P(\text{ucldMean}) * P(\text{ucldStdev})$

Prior on subst model:
parameters

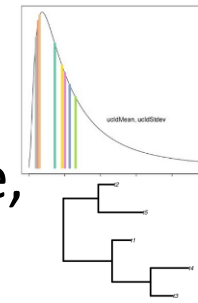
$P(\text{kappa}) * P(\text{gammaShape})$

(hyper)prior on tree prior:
parameters

$P(\text{growthRate}) * P(\text{ePopSize})$

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coalescentExponential:

$P(\text{tree} \mid \text{growthRate}, \text{ePopSize})$

Prior on clock parameters:

$P(\text{ucldMean}) * P(\text{ucldStdev})$

Prior on subst model:
parameters

$P(\text{kappa}) * P(\text{gammaShape})$

(hyper)prior on tree prior:
parameters

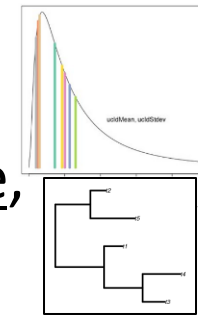
$P(\text{growthRate}) * P(\text{ePopSize})$

Prior densities

This is the 'prior'

This is the 'posterior' or
joint

treeLikelihood or likelihood: $P(\text{alignment} \mid \text{kappa}, \text{gammaShape}, \text{ucldMean}, \text{ucldStdev})$



coalescentExponential:

$$P(\text{tree} \mid \text{growthRate}, \text{ePopSize})$$

Prior on clock parameters:

$$P(\text{ucldMean}) * P(\text{ucldStdev})$$

Prior on subst model:
parameters

$$P(\text{kappa}) * P(\text{gammaShape})$$

(hyper)prior on tree prior:
parameters

$$P(\text{growthRate}) * P(\text{ePopSize})$$

Prior densities

This is the 'prior'

Parameters we can estimate: $\text{kappa}, \text{gammaShape}, \text{ucldMean}, \text{ucldStdev},$
 $\text{growthRate}, \text{PopSize},$



This is the 'posterior' or
joint

Concept summary

- The 'likelihood model' is that which includes the data directly.
- The prior model has an impact on the likelihood model, via the tree, but its parameters are not in the likelihood function.
- We can estimate parameters in the model formulation.