

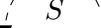
anyBSM - Model: SM (Amplitude: $h - h$)

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1 Overview

1.1 Topology: TwoPointA



$h \text{ --- } h$

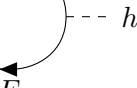
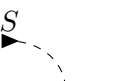
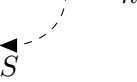

$\{S\} = \{G^+, \{G^0\}, \{h\}, \{G^-\}$

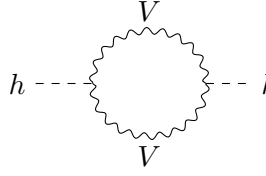


$h \text{ --- } h$

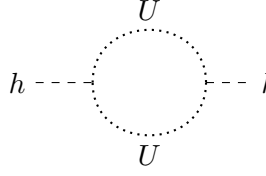
$\{V\} = \{Z\}, \{W^+\}, \{W^-\}$

1.2 Topology: TwoPointB

	$\{F, F\} =$	$\{d_1, d_1\}, \{d_2, d_2\}, \{d_3, d_3\}, \{u_1, u_1\}, \{u_2, u_2\}, \{u_3, u_3\},$ $\{e_1, e_1\}, \{e_2, e_2\}, \{e_3, e_3\}, \{\bar{d}_1, \bar{d}_1\}, \{\bar{d}_2, \bar{d}_2\}, \{\bar{d}_3, \bar{d}_3\}, \{\bar{u}_1, \bar{u}_1\},$ $\{\bar{u}_2, \bar{u}_2\}, \{\bar{u}_3, \bar{u}_3\}, \{\bar{e}_1, \bar{e}_1\}, \{\bar{e}_2, \bar{e}_2\}, \{\bar{e}_3, \bar{e}_3\}$
	$\{S, S\} =$	$\{G^+, G^+\}, \{G^0, G^0\}, \{h, h\}, \{G^-, G^-\}$
	$\{S, V\} =$	$\{G^+, W^+\}, \{G^0, Z\}, \{G^-, W^-\}$
	$\{V, S\} =$	$\{W^+, G^+\}, \{Z, G^0\}, \{W^-, G^-\}$

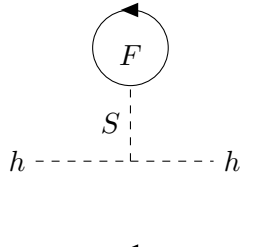


$$\{V, V\} = \{Z, Z\}, \{W^+, W^+\}, \{W^-, W^-\}$$

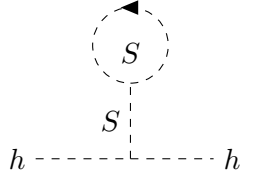


$$\{U, U\} = \{\eta_-^\gamma, \eta_-^Z\}, \{\eta_-^Z, \eta_-^Z\}, \{\eta^+, \eta^+\}, \{\eta^-, \eta^-\}, \{\eta_-^Z, \eta_-^\gamma\}, \{\eta_-^Z, \eta_-^Z\}, \{\eta^+, \eta^+\}, \{\eta^-, \eta^-\}$$

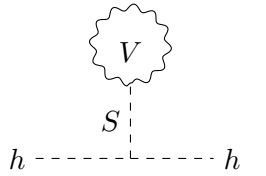
1.3 Topology: TwoPointTA



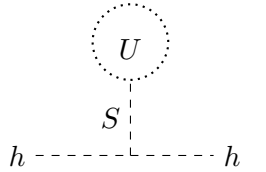
$$\{S, F\} = \{h, d_1\}, \{h, d_2\}, \{h, d_3\}, \{h, u_1\}, \{h, u_2\}, \{h, u_3\}, \{h, e_1\}, \{h, e_2\}, \{h, e_3\}, \{h, \bar{d}_1\}, \{h, \bar{d}_2\}, \{h, \bar{d}_3\}, \{h, \bar{u}_1\}, \{h, \bar{u}_2\}, \{h, \bar{u}_3\}, \{h, \bar{e}_1\}, \{h, \bar{e}_2\}, \{h, \bar{e}_3\}$$



$$\{S, S\} = \{h, G^+\}, \{h, G^0\}, \{h, h\}, \{h, G^-\}$$



$$\{S, V\} = \{h, Z\}, \{h, W^+\}, \{h, W^-\}$$



$$\{S, U\} = \{h, \eta^Z\}, \{h, \eta^+\}, \{h, \eta^-\}, \{h, \eta^{\bar{Z}}\}, \{h, \eta^{\bar{+}}\}, \{h, \eta^{\bar{-}}\}$$

2 Individual results

2.1 Topology: TwoPointA

2.1.1 S



$$64\pi^2 \times \quad \quad \quad = \quad \quad \quad -2\lambda A_0((M_{G^+})^2)$$

$$64\pi^2 \times \text{Diagram}(G^0) = -2\lambda A_0((M_{G^0})^2)$$

$$64\pi^2 \times \text{Diagram}(h) = -6\lambda A_0(M_h^2)$$

$$64\pi^2 \times \text{Diagram}(G^-) = -2\lambda A_0((M_{G^+})^2)$$

2.1.2 V

$$64\pi^2 \times \text{Diagram}(Z) = -4 \left(-\frac{M_Z^2}{2} + A_0(M_Z^2) \right) (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^2$$

$$64\pi^2 \times \text{Diagram}(W^+) = -4g_2^2 \left(-\frac{(M_{W^+})^2}{2} + A_0((M_{W^+})^2) \right)$$

$$64\pi^2 \times \text{Diagram}(W^-) = -4g_2^2 \left(-\frac{(M_{W^-})^2}{2} + A_0((M_{W^-})^2) \right)$$

2.2 Topology: TwoPointB

2.2.1 FF

$$64\pi^2 \times \text{Diagram}(d_1) = 12M_{d_1}^2 \left(Y_{11}^d \right)^2 B_0(p_1^2, M_{d_1}^2, M_{d_1}^2) - 6 \left(Y_{11}^d \right)^2 ((-2M_{d_1}^2 + p_1^2) B_0(p_1^2, M_{d_1}^2, M_{d_1}^2) -$$

$$\begin{aligned}
64\pi^2 \times \text{Diagram}_1 &= 12M_{d_2}^2 (Y_{22}^d)^2 B_0(p_1^2, M_{d_2}^2, M_{d_2}^2) - 6(Y_{22}^d)^2 ((-2M_{d_2}^2 + p_1^2) B_0(p_1^2, M_{d_2}^2, M_{d_2}^2) - \\
64\pi^2 \times \text{Diagram}_2 &= 12M_{d_3}^2 (Y_{33}^d)^2 B_0(p_1^2, M_{d_3}^2, M_{d_3}^2) - 6(Y_{33}^d)^2 ((-2M_{d_3}^2 + p_1^2) B_0(p_1^2, M_{d_3}^2, M_{d_3}^2) - \\
64\pi^2 \times \text{Diagram}_3 &= 12M_{u_1}^2 (Y_{11}^u)^2 B_0(p_1^2, M_{u_1}^2, M_{u_1}^2) - 6(Y_{11}^u)^2 ((-2M_{u_1}^2 + p_1^2) B_0(p_1^2, M_{u_1}^2, M_{u_1}^2) - \\
64\pi^2 \times \text{Diagram}_4 &= 12M_{u_2}^2 (Y_{22}^u)^2 B_0(p_1^2, M_{u_2}^2, M_{u_2}^2) - 6(Y_{22}^u)^2 ((-2M_{u_2}^2 + p_1^2) B_0(p_1^2, M_{u_2}^2, M_{u_2}^2) - \\
64\pi^2 \times \text{Diagram}_5 &= 12M_{u_3}^2 (Y_{33}^u)^2 B_0(p_1^2, M_{u_3}^2, M_{u_3}^2) - 6(Y_{33}^u)^2 ((-2M_{u_3}^2 + p_1^2) B_0(p_1^2, M_{u_3}^2, M_{u_3}^2) - \\
64\pi^2 \times \text{Diagram}_6 &= 4M_{e_1}^2 (Y_{11}^e)^2 B_0(p_1^2, M_{e_1}^2, M_{e_1}^2) - 2(Y_{11}^e)^2 ((-2M_{e_1}^2 + p_1^2) B_0(p_1^2, M_{e_1}^2, M_{e_1}^2) - 2 \\
64\pi^2 \times \text{Diagram}_7 &= 4M_{e_2}^2 (Y_{22}^e)^2 B_0(p_1^2, M_{e_2}^2, M_{e_2}^2) - 2(Y_{22}^e)^2 ((-2M_{e_2}^2 + p_1^2) B_0(p_1^2, M_{e_2}^2, M_{e_2}^2) - 2 \\
64\pi^2 \times \text{Diagram}_8 &= 4M_{e_3}^2 (Y_{33}^e)^2 B_0(p_1^2, M_{e_3}^2, M_{e_3}^2) - 2(Y_{33}^e)^2 ((-2M_{e_3}^2 + p_1^2) B_0(p_1^2, M_{e_3}^2, M_{e_3}^2) - 2 \\
64\pi^2 \times \text{Diagram}_9 &= 12M_{d_1}^2 (Y_{11}^d)^2 B_0(p_1^2, M_{d_1}^2, M_{d_1}^2) - 6(Y_{11}^d)^2 ((-2M_{d_1}^2 + p_1^2) B_0(p_1^2, M_{d_1}^2, M_{d_1}^2) -
\end{aligned}$$

$$\begin{aligned}
64\pi^2 \times \text{Diagram}_1 &= 12M_{d_2}^2 (Y_{22}^d)^2 B_0(p_1^2, M_{d_2}^2, M_{d_2}^2) - 6(Y_{22}^d)^2 ((-2M_{d_2}^2 + p_1^2) B_0(p_1^2, M_{d_2}^2, M_{d_2}^2) - \\
64\pi^2 \times \text{Diagram}_2 &= 12M_{d_3}^2 (Y_{33}^d)^2 B_0(p_1^2, M_{d_3}^2, M_{d_3}^2) - 6(Y_{33}^d)^2 ((-2M_{d_3}^2 + p_1^2) B_0(p_1^2, M_{d_3}^2, M_{d_3}^2) - \\
64\pi^2 \times \text{Diagram}_3 &= 12M_{u_1}^2 (Y_{11}^u)^2 B_0(p_1^2, M_{u_1}^2, M_{u_1}^2) - 6(Y_{11}^u)^2 ((-2M_{u_1}^2 + p_1^2) B_0(p_1^2, M_{u_1}^2, M_{u_1}^2) - \\
64\pi^2 \times \text{Diagram}_4 &= 12M_{u_2}^2 (Y_{22}^u)^2 B_0(p_1^2, M_{u_2}^2, M_{u_2}^2) - 6(Y_{22}^u)^2 ((-2M_{u_2}^2 + p_1^2) B_0(p_1^2, M_{u_2}^2, M_{u_2}^2) - \\
64\pi^2 \times \text{Diagram}_5 &= 12M_{u_3}^2 (Y_{33}^u)^2 B_0(p_1^2, M_{u_3}^2, M_{u_3}^2) - 6(Y_{33}^u)^2 ((-2M_{u_3}^2 + p_1^2) B_0(p_1^2, M_{u_3}^2, M_{u_3}^2) - \\
64\pi^2 \times \text{Diagram}_6 &= 4M_{e_1}^2 (Y_{11}^e)^2 B_0(p_1^2, M_{e_1}^2, M_{e_1}^2) - 2(Y_{11}^e)^2 ((-2M_{e_1}^2 + p_1^2) B_0(p_1^2, M_{e_1}^2, M_{e_1}^2) - 2 \\
64\pi^2 \times \text{Diagram}_7 &= 4M_{e_2}^2 (Y_{22}^e)^2 B_0(p_1^2, M_{e_2}^2, M_{e_2}^2) - 2(Y_{22}^e)^2 ((-2M_{e_2}^2 + p_1^2) B_0(p_1^2, M_{e_2}^2, M_{e_2}^2) - 2 \\
64\pi^2 \times \text{Diagram}_8 &= 4M_{e_3}^2 (Y_{33}^e)^2 B_0(p_1^2, M_{e_3}^2, M_{e_3}^2) - 2(Y_{33}^e)^2 ((-2M_{e_3}^2 + p_1^2) B_0(p_1^2, M_{e_3}^2, M_{e_3}^2) - 2
\end{aligned}$$

2.2.2 SS

$$\begin{aligned}
64\pi^2 \times \quad & \begin{array}{c} W^+ \\ \text{---} h \text{ ---} \text{---} h \\ G^+ \end{array} = 0 \\
64\pi^2 \times \quad & \begin{array}{c} Z \\ \text{---} h \text{ ---} \text{---} h \\ G^0 \end{array} = 0 \\
64\pi^2 \times \quad & \begin{array}{c} W^- \\ \text{---} h \text{ ---} \text{---} h \\ G^- \end{array} = 0
\end{aligned}$$

2.2.5 VV

$$\begin{aligned}
64\pi^2 \times \quad & \begin{array}{c} Z \\ \text{---} h \text{ ---} \text{---} h \\ Z \end{array} = -2v^2 (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^4 \left(B_0(p_1^2, M_Z^2, M_Z^2) - \frac{1}{2} \right) \\
64\pi^2 \times \quad & \begin{array}{c} W^+ \\ \text{---} h \text{ ---} \text{---} h \\ W^+ \end{array} = -2g_2^4 v^2 \left(B_0(p_1^2, (M_{W^+})^2, (M_{W^+})^2) - \frac{1}{2} \right) \\
64\pi^2 \times \quad & \begin{array}{c} W^- \\ \text{---} h \text{ ---} \text{---} h \\ W^- \end{array} = -2g_2^4 v^2 \left(B_0(p_1^2, (M_{W^+})^2, (M_{W^+})^2) - \frac{1}{2} \right)
\end{aligned}$$

2.2.6 UU

$$64\pi^2 \times \quad \begin{array}{c} \eta^\gamma \\ \text{---} h \text{ ---} \text{---} h \\ \eta^Z \end{array} = \frac{\xi_Z^2 v^2 (2g_1 g_2 \cos(2\theta_w) + (g_1^2 - g_2^2) \sin(2\theta_w))^2 B_0(p_1^2, 0^2, (M_{\eta^Z})^2)}{32}$$

$64\pi^2 \times \begin{array}{c} \eta^Z \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^Z \end{array} =$	$\frac{\xi_Z^2 v^2 (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^4 B_0(p_1^2, (M_{\eta^Z})^2, (M_{\eta^Z})^2)}{8}$
$64\pi^2 \times \begin{array}{c} \eta^+ \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^+ \end{array} =$	$\frac{(\xi_{W^+})^2 g_2^4 v^2 B_0(p_1^2, (M_{\eta^+})^2, (M_{\eta^+})^2)}{8}$
$64\pi^2 \times \begin{array}{c} \eta^- \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^- \end{array} =$	$\frac{(\xi_{W^+})^2 g_2^4 v^2 B_0(p_1^2, (M_{\eta^-})^2, (M_{\eta^-})^2)}{8}$
$64\pi^2 \times \begin{array}{c} \eta^- \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^{\bar{Z}} \end{array} =$	$\frac{\xi_Z^2 v^2 (2g_1 g_2 \cos(2\theta_w) + (g_1^2 - g_2^2) \sin(2\theta_w))^2 B_0(p_1^2, (M_{\eta^Z})^2, 0^2)}{32}$
$64\pi^2 \times \begin{array}{c} \eta^{\bar{Z}} \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^{\bar{Z}} \end{array} =$	$\frac{\xi_Z^2 v^2 (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^4 B_0(p_1^2, (M_{\eta^Z})^2, (M_{\eta^Z})^2)}{8}$
$64\pi^2 \times \begin{array}{c} \eta^+ \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^{\bar{+}} \end{array} =$	$\frac{(\xi_{W^+})^2 g_2^4 v^2 B_0(p_1^2, (M_{\eta^+})^2, (M_{\eta^+})^2)}{8}$
$64\pi^2 \times \begin{array}{c} \eta^- \\ \text{---} h \text{ ---} \text{---} h \text{ ---} \\ \eta^{\bar{-}} \end{array} =$	$\frac{(\xi_{W^+})^2 g_2^4 v^2 B_0(p_1^2, (M_{\eta^-})^2, (M_{\eta^-})^2)}{8}$

$$64\pi^2 \times \quad h \text{-----} \overset{16}{\underset{\text{16}}{\text{L}}} \text{-----} h =$$

$$64\pi^2 \times h \text{-----} \overset{|}{\perp} \text{-----} h =$$

$$64\pi^2 \times h \text{-----} \overset{\text{no}}{\underset{|}{\perp}} \text{-----} h =$$

$$64\pi^2 \times \quad h \text{-----} \overset{|}{\perp} \text{-----} h =$$

$$64\pi^2 \times h \text{-----} \perp \text{-----} h =$$

$$64\pi^2 \times h \text{-----} \overset{\text{tree}}{\underset{\text{loop}}{\text{L}}} \text{-----} h =$$

$$64\pi^2 \times h \text{-----} \perp \text{-----} h =$$

$$64\pi^2 \times \text{Diagram} = -\frac{12\sqrt{2}\lambda M_{e_2} Y_{22}^e v A_0(M_{e_2}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{12\sqrt{2}\lambda M_{e_3} Y_{33}^e v A_0(M_{e_3}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{36\sqrt{2}\lambda M_{d_1} Y_{11}^d v A_0(M_{d_1}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{36\sqrt{2}\lambda M_{d_2} Y_{22}^d v A_0(M_{d_2}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{36\sqrt{2}\lambda M_{d_3} Y_{33}^d v A_0(M_{d_3}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{36\sqrt{2}\lambda M_{u_1} Y_{11}^u v A_0(M_{u_1}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{36\sqrt{2}\lambda M_{u_2} Y_{22}^u v A_0(M_{u_2}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = -\frac{12\sqrt{2}\lambda M_{e_3} Y_{33}^e v A_0(M_{e_3}^2)}{M_h^2}$$

$$64\pi^2 \times \text{Diagram} = \frac{18\lambda^2 v^2 A_0(M_h^2)}{M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} h \text{---} \end{array} \begin{array}{c} \text{---} G^- \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$\frac{6\lambda^2 v^2 A_0 ((M_{G^+})^2)}{M_h^2}$$

2.3.3 SV

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} Z \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$-\frac{6\lambda v^2 (M_Z^2 - 2A_0(M_Z^2)) (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^2}{M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} W^+ \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$-\frac{6\lambda g_2^2 v^2 ((M_{W^+})^2 - 2A_0((M_{W^+})^2))}{M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} W^- \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$-\frac{6\lambda g_2^2 v^2 ((M_{W^+})^2 - 2A_0((M_{W^+})^2))}{M_h^2}$$

2.3.4 SU

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} \eta^Z \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$-\frac{3\lambda \xi_Z v^2 (g_1 \sin(\theta_w) + g_2 \cos(\theta_w))^2 A_0((M_{\eta^Z})^2)}{2M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} \eta^+ \text{---} \\ | \\ \text{---} h \text{---} \end{array} =$$

$$-\frac{3\lambda \xi_{W^+} g_2^2 v^2 A_0((M_{\eta^+})^2)}{2M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} h \text{---} \end{array} \begin{array}{c} \circlearrowleft \eta^- \end{array} = - \frac{3\lambda\xi_{W^+}g_2^2v^2A_0((M_{\eta^-})^2)}{2M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} h \text{---} \end{array} \begin{array}{c} \circlearrowleft \eta^Z \end{array} = - \frac{3\lambda\xi_Zv^2(g_1\sin(\theta_w) + g_2\cos(\theta_w))^2A_0((M_{\eta^Z})^2)}{2M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} h \text{---} \end{array} \begin{array}{c} \circlearrowleft \eta^+ \end{array} = - \frac{3\lambda\xi_{W^+}g_2^2v^2A_0((M_{\eta^+})^2)}{2M_h^2}$$

$$64\pi^2 \times \begin{array}{c} \text{---} h \text{---} \\ | \\ \text{---} h \text{---} \end{array} \begin{array}{c} \circlearrowleft \eta^- \end{array} = - \frac{3\lambda\xi_{W^+}g_2^2v^2A_0((M_{\eta^-})^2)}{2M_h^2}$$

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