

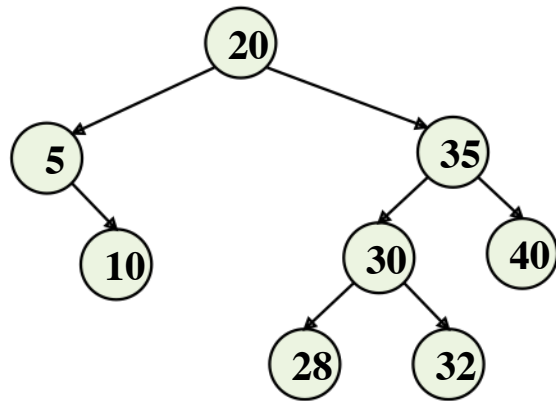
TL06

Live

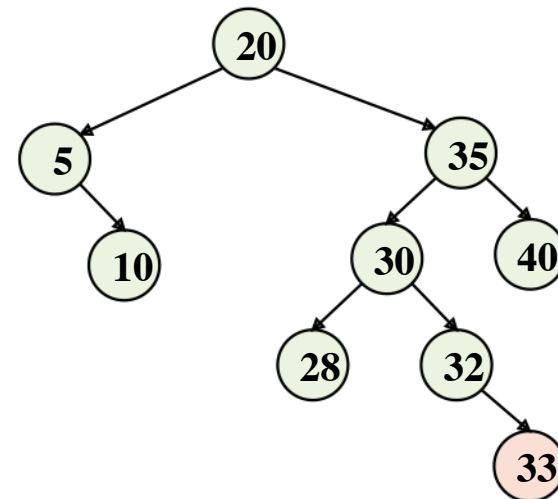
Q1

AVL Tree Insertion

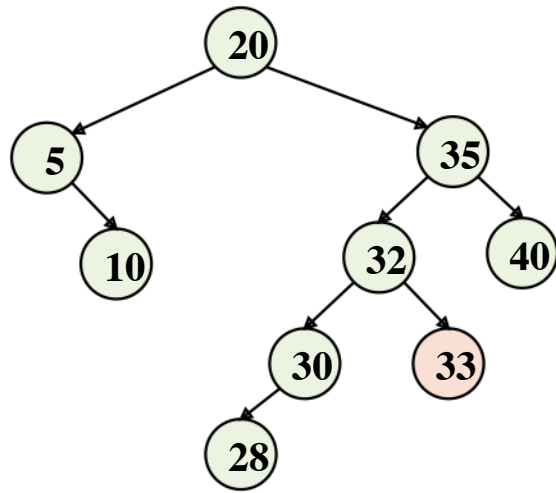
AVL – Insert 33



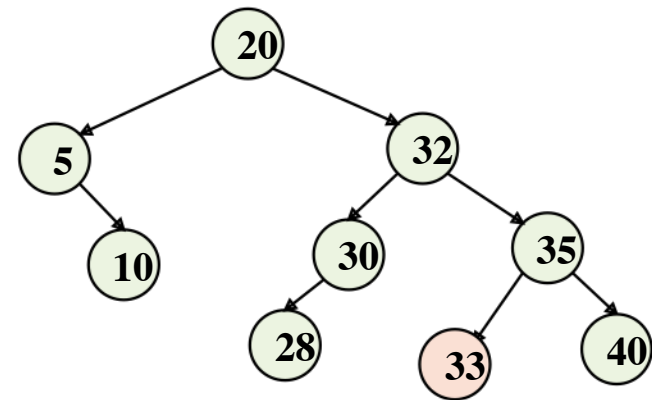
AVL – Insert 33



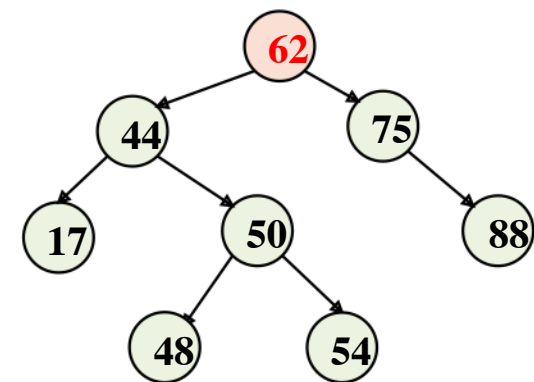
AVL – Insert 33



AVL – Insert 33



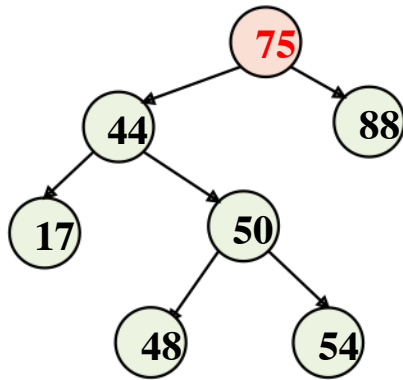
AVL – Delete 62



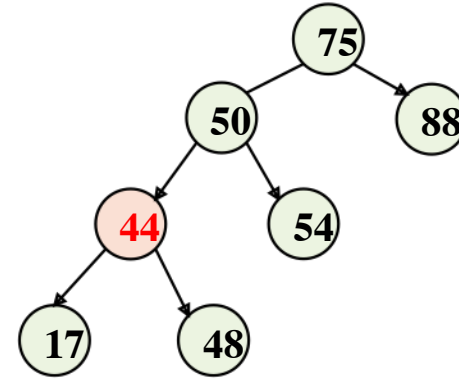
Q2

AVL Tree Deletion

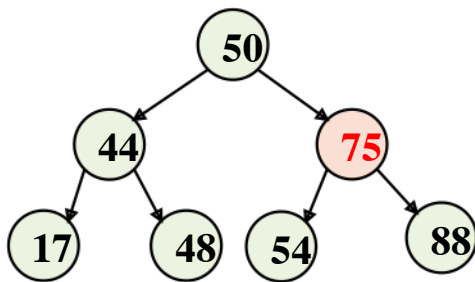
AVL – Delete 62



AVL – Delete 62



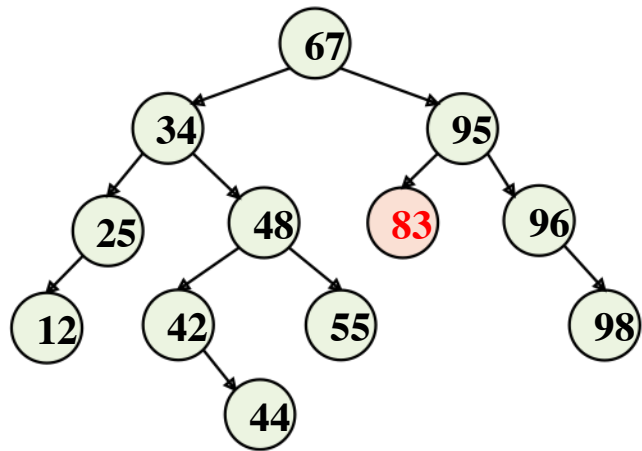
AVL – Delete 62



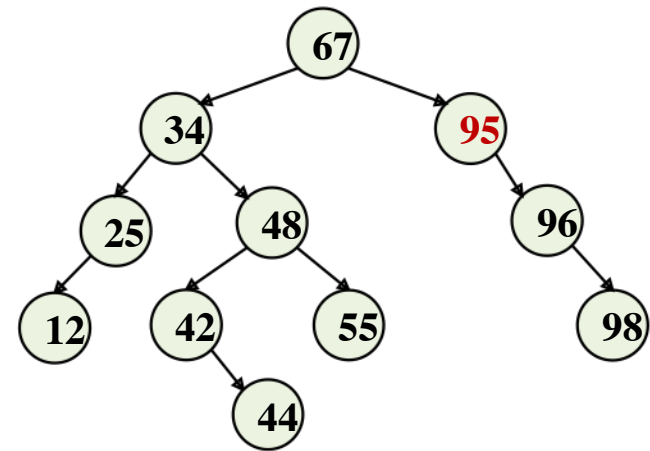
Q3

AVL Tree Deletion - General

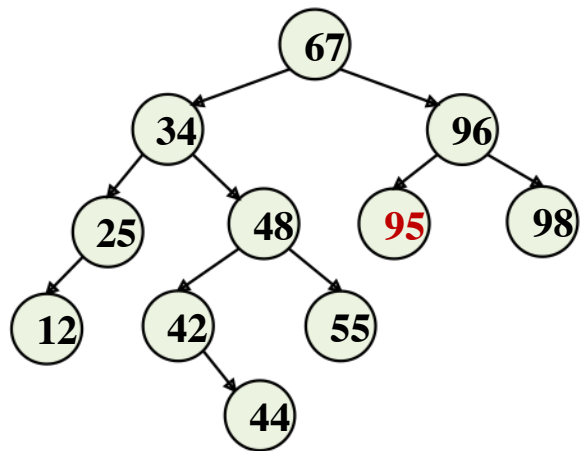
a. **Delete 83**



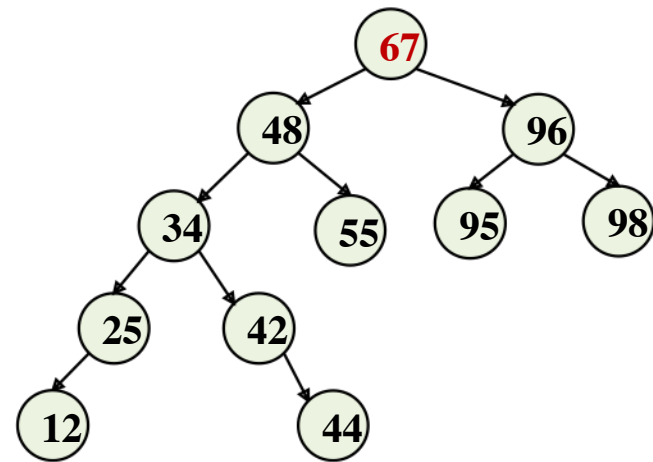
a. **Delete 83**



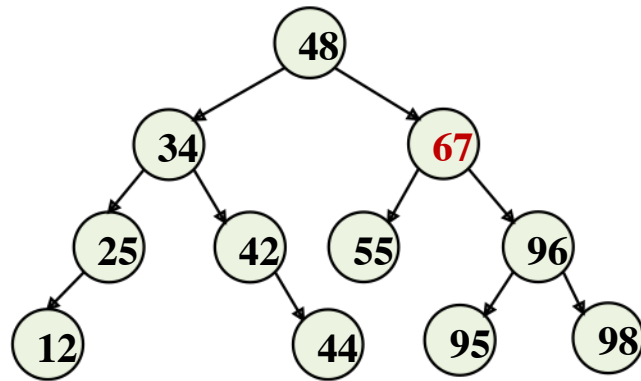
a. **Delete 83**



a. **Delete 83**

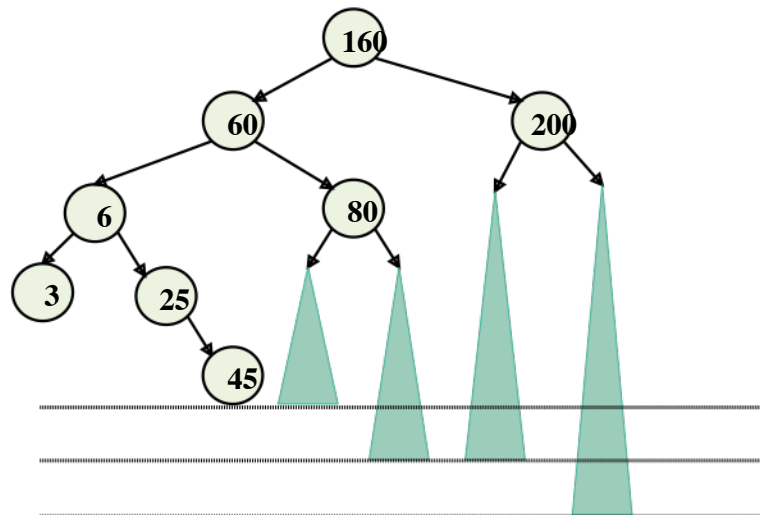


a. **Delete 83**



b. So, what's the **worst case**?

b. So, what's the **worst case**?



Q4

Hash Table – Collision Resolution

a. Separate Chaining

{ 10, 22, 31, 4, 15, 28, 17, 88, 59
}

$Hash(key) = key \% 11$

0	1	2	3	4	5	6	7	8	9	10

a. Separate Chaining

Delete(4),
Find(37)

$Hash(key) = key \% 11$

0	1	2	3	4	5	6	7	8	9	10
↓				↓		↓			↓	↓
88				59		17			31	10
↓				↓		↓				
22				15		28				
				↓						
				4						

b. Linear Probing

Insert(17), Insert(37), Insert(59),
Insert(70)

$Hash(key) = key \% 11$

0	1	2	3	4	5	6	7	8	9	10

b. Linear Probing

Find(60), Delete(59), Find(70),
Insert(16)

$Hash(key) = key \% 11$

0	1	2	3	4	5	6	7	8	9	10
				37	59	17	70			

c. Quadratic Probing

$Hash(key) = key \% 11$

Insert(20), Insert(82), Insert(28),
Insert(93)

0	1	2	3	4	5	6	7	8	9	10
					82	28			20	

c. Quadratic Probing

$Hash(key) = key \% 11$

Find(51), Delete(82), Find(93), Insert(24),
Insert(68)

0	1	2	3	4	5	6	7	8	9	10
			93		82	28			20	

d. Double Hashing

$Hash(key) = key \% 11$

Insert(32), Insert(49), Insert(65), Insert(26)

$Hash2(key) = 7 - key \% 7$

0	1	2	3	4	5	6	7	8	9	10

d. Double Hashing

$Hash(key) = key \% 11$

Find(37), Delete(26),
Insert(98)

$Hash2(key) = 7 - key \% 7$

0	1	2	3	4	5	6	7	8	9	10
				65	49	26				32

c. Key = even # in 0 to 1,000,000
Uniform?

$$\begin{aligned} \text{Hash}(\text{key}) \\ &= \text{key} \% 100 \end{aligned}$$

Q5

Hash Function Analysis

d. Key = 0 to 1,000,000
Uniform?

$$\begin{aligned} \text{Hash}(\text{key}) \\ &= \text{key} * 7 \% 49 \end{aligned}$$

e. Key = 1 to 10,000
Uniform?

Lab Q1

AVL Tree – Insertion

[Submission]

- Only need to work on `_balance(T)` function
- This function checks the BF of T:
 - If skewed:
 - What case?
 - What rotation?
 - Update height
 - Return
- Just return!

AVL Tree - Deletion

- With `_balance()`, this is literally a one line problem.....
- Hint: Look at how `insertion()` is updated from BST to AVL Tree.....

Lab Q2

Lab Q3

Hash Table?!!

Just the probe sequence

- i.e. simple calculation only!
 - If written in small steps = ~3-4 lines
 - If written in condense mode = 1 line 😊
-
- Note that ONLY part (c) needs to be **submitted!**