# Universidad Autónoma de Chihuahua

## Facultad de Ingeniería

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# NOTEBOOK: Development of Topics Related to the Project

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Notes Before Start Working on the Thesis

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# BASIC RECAP

# DEFINITIONS

# 1. DIFFERENTIAL EQUATIONS

**DEFINITION 1.1.1 - Differential Equation**

An equation containing the derivatives of one or more unknown functions (or dependent variables), with respect to one or more independent variables, is said to be a **differential equation (DE)**.

## 1.1 Notation

- **Leibinz notation**:

$$\frac{dy}{dx},\ \frac{d^2y}{dx^2},\ \frac{d^3y}{dx^3},\ ...$$

- **Prime notation**:

$$y',\ y'',\ y''',\ y^{(4)},\ ...$$

In general, the $n$th derivative of y is written as $\frac{d^n y}{dx^n}$ or $y^{(n)}$.

- **Newton's dot notation**: used in physical science and engineering, to denote derivatives with respect to time $t$,

$$\frac{d^2s}{dt^2} = -32\ \rightarrow\ \text{becomes}\ \rightarrow\ \ddot{s} = -32.$$

- **Subscript notation**: often used in partial derivatives indicating the independent variables.

$$\frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial t^2} - 2\frac{\partial u}{\partial t}\ \rightarrow\ \text{becomes}\ \rightarrow\ u_{xx} = u_{tt} - 2u_t.$$

## 1.2 Classification By Type

If a differential equation contains only ordinary derivatives of one or more unknown functions with respect to a single independent variable, it is said to be an **ordinary differential equation (ODE)**. An equation involving partial derivatives of one or more unknown functions of two or more independent variables is called a **partial differential equation (PDE)**.

## 1.3 Classification By Order

The order of a differential equation (either ODE or PDE) is the order of the highest derivative in the equation. For example,

$$\frac{d^2y}{dx^2} + 5\left(\frac{dy}{dx}\right)^3 - 4y = e^x \,,$$

is a second-order differential equation.

# Part I

# MATHEMATICS OF PHYSICS

# 2. INFINITE SERIES, POWER SERIES

## 2.1   The Geometric Series

[1]

**Geometric Progression**, is a sequence of numbers where each term after the first is found by multiplying the previous term by a fixed, non-zero number called the common ratio. The **general form** of a geometric progression is:

$$a, \ ar, \ ar^2, \ ar^3, \ ... \tag{2.1}$$

where $a$ is the *first term* and $r$ is the *common ratio*. Geometric Progressions have some interesting properties:

- If $r > 1$, the terms will increase.

- If $0 < r < 1$, the terms will decrease.

- If $r = 1$ the sequence becomes constant (where each term is the same).

- If $r < 0$, the terms will alternate between positive and negative values.

i.e., Suppose a bouncing ball rises each time to $\frac{2}{3}$ of the height of the previous bounce. Then

$$1, \ \frac{2}{3}, \ \frac{4}{9}, \ \frac{8}{27}, \ \frac{16}{81}, \ ..., \tag{2.2}$$

# Part II

# NUMERICAL METHODS

# 3. INTRODUCTION

The term **Numerical Methods** refers to those techniques used to approximate the solution to a mathematical problem, these methods are used for mathematical processes such as integrals, differential equations, nonlinear equations in which the solution is close to the exact one and the error of that result can also be quantified by an approximation.

## 3.1   Steps for solving an Engineering Problem

- **Description**: present the problem exposing every single need related to it, write the background of it and the need for its solution.

- **Mathematical Model**: present an equation that best describes the situation when fitting the given data.

- **Solution of the Mathematical Model**: find the solution to the proposed equation.

- **Using the Solution**: propose a solution to the real problem based on the obtained result from the mathematical model.

# 4. MATHEMATICAL PROCESSES

### 4.1    Roots of Nonlinear Equations

### 4.2    Simultaneous Linear Equations

### 4.3    Curve Fitting by Interpolation

### 4.4    Differentiation

### 4.5    Curve Fitting by Regression

### 4.6    Numerical Integration

### 4.7    Ordinary Differential Equations

### 4.8    Partial Differential Equations

### 4.9    Optimization

### 4.10    Fast Fourier Transform

# 5. THESIS ACTUAL CONTENT

## 5.1    DATASETS

The dataset[2] was recorded by Anna Yang, it contains original data from European honeybee hives in California divided into 60-second segments and recorded approximately 23 to 24 samples per day, collected with a custom IoT device that combined an ESP32 Wi-Fi module, an INMP441

microphone module, and a BME280 temperature/humidity sensor. There are 7100 samples in total.

- First recording: 08 - June - 2022 at 14:52:28.

- Last recording: 15 - July - 2022 at 15:28:21.

- The "queen acceptance" values indicate whether the queen is accepted by the hive (0 - no queen present, 1 - not accepted/rejected, 2 - accepted).

- "queen status" is a combined value for "queen presence" and "queen acceptance" (0, queenright/original queen, 1 - not present, 2 - present and rejected, 3 - present and newly accepted).

- The "target" feature was another proposed way to combine "queen presence" and "queen acceptance", but the "queen status" feature was a better way to do it. "Time" is the time of day (24 hours) scaled to values between 0 and 1.

**Notes of the dataset creator**: *"queen status" would be the indicator of the queen situation. The sensor was placed in the telescoping cover of the hive, which is below the outer cover but above the frames. The telescoping cover was sealed with wire mesh so bees could not get to the sensors, which decreased bee interference with the microphone as well.*

*To confirm whether the queen was accepted or rejected, I conducted a daily hive inspection. I observed the bees' reaction towards the queen in the cage: Are they attempting to sting or ball (suffocate) her? Are they calm or excited? If there are 2+ layers of bees around the cage, it is an indication that they are aggressive and hostile towards the queen. In the 24-hour period that the queen's status changes from rejected to accepted (between hive inspections), there was ambiguity around the exact time that the queen became accepted. As a result, I discarded the data from this uncertain period.*

*I do not believe I ever noted that the dataset related to colony collapse disorder. However, I can describe how it could be indirectly related. Colony collapse disorder, a phenomenon that occurs when the majority of bees in a colony mysteriously disappear, has been on the decline in recent years. Initially, it was very concerning for scientists and beekeepers because bees were dying, seemingly without reason. Despite it being not as severe now, overall colony loss is still a major concern to beekeepers, and it has been reported that queen failure – when a colony is headed by a queen bee that is infertile or weak – has been consistently identified as one of the top four causes of colony mortality, annually, since 2009 (from the annual study conducted by the Canadian Association of Professional Apiculturists). This dataset records the difference in sound between queen states, addressing the widespread issue of queen failure.*

*I did not collect data on varroa mites or pesticide exposure for this dataset. In fact, pesticide exposure is quite difficult to track, especially since the data was mostly collected on suburban backyard beehives. It is near impossible to know whether nearby residences treat their gardens with chemical or organic pesticides, and even where the bees were visiting, since they can fly 3-4 miles just to collect pollen and nectar.*

# Bibliography

[1]  Mary L Boas. *Mathematical methods in the physical sciences.* John Wiley & Sons, 2006.

[2]  Anna Yang. *Smart Bee Colony Monitor: Clips of Beehive Sounds.* 2022. DOI: 10.34740/KAGGLE/DSV/4451415. URL: https://www.kaggle.com/dsv/4451415.